

**1.22 Theorem.** If a natural number is divisible by 3, then, when expressed in base 10, the sum of its digits is divisible by 3.

**Proof.** Let  $n \in \mathbb{N}$  be given such that  $n$  is divisible by 3. Since  $3 \mid n$ ,  $n \equiv 0 \pmod{3}$ . By Thm 1.21,  $n \equiv m \pmod{3}$  where  $m =$  (sum of  $n$ 's digits). By Thm 1.10,  $m \equiv n \pmod{3}$ . Since  $n \equiv 0 \pmod{3}$ ,  $m \equiv 0 \pmod{3}$  by Thm 1.11. Thus, the sum of its digits is divisible by 3.  $\square$