

$$(1) \cdot \omega_c = \frac{2}{T} \tan\left(\frac{\omega_c T}{2}\right) = 2 \tan\left(\frac{\pi}{6}\right)$$

$$(2) \quad H(z) = H(s) \Big|_{s = \frac{2}{T} \left(\frac{z-1}{z+1}\right)}$$

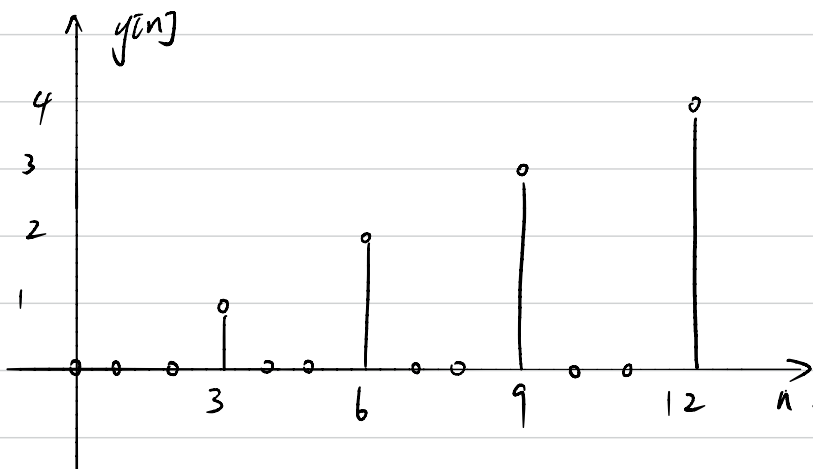
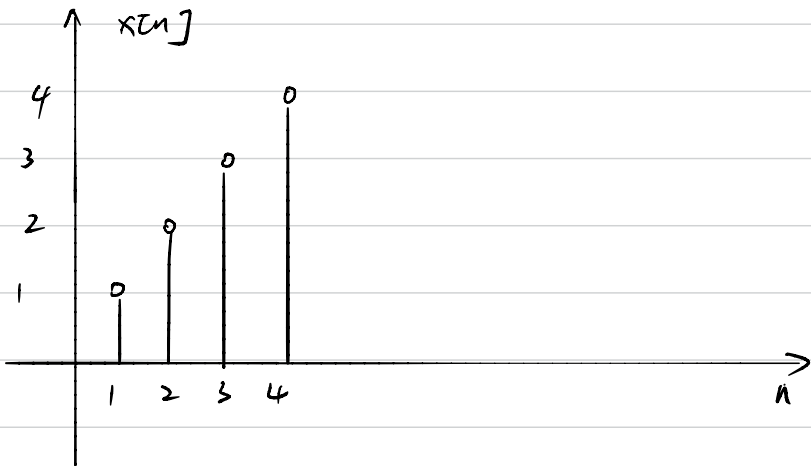
$$H(z) = \frac{2 \cdot \left(\frac{z-1}{z+1}\right)}{2 \left(\frac{z-1}{z+1}\right) + 2} = \frac{z-1}{2z}$$

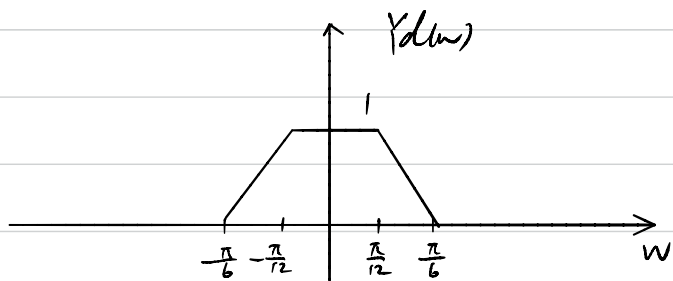
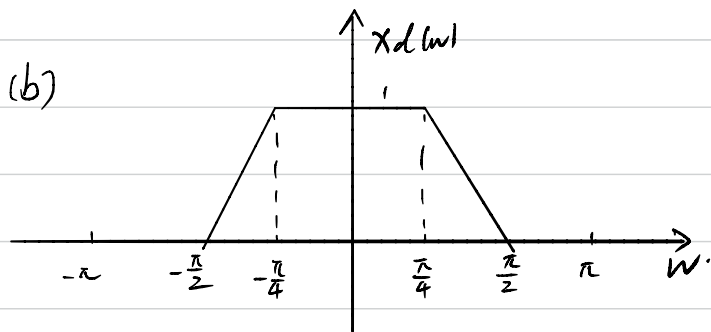
$$(3) \quad \omega_c - \omega_s = \frac{\pi}{10}$$

$$\omega_c = \frac{3}{5}\pi - \frac{1}{10}\pi = \frac{5}{10}\pi = \frac{1}{2}\pi$$

$$\omega_c = \frac{2}{T} \tan \frac{\omega}{2} = 2 \tan \frac{\pi}{2 \times 10} = 0.3167 \text{ Hz}$$

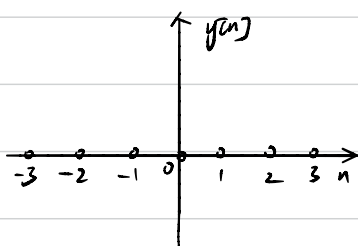
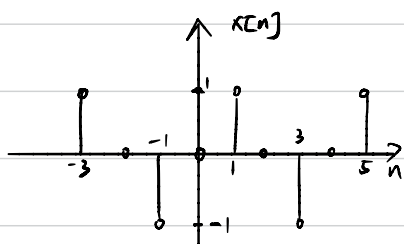
$$(4) \quad (a) \quad y[n] = \begin{cases} x[n/3] & n \text{ is multiple of } 3 \\ 0 & \text{else} \end{cases}$$





(5). a)  $x[n] = \sin(n\frac{\pi}{2})$

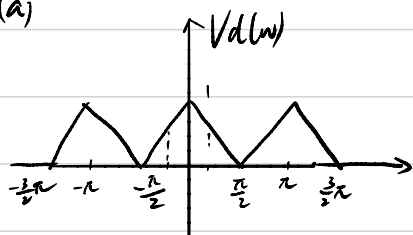
$$y[n] = \begin{cases} \sin(n\pi) \\ 0 \end{cases}$$



(b)  $X_d(w) = \frac{1}{1 - \frac{1}{2}e^{-jw}} = \frac{1}{1 - \frac{1}{2}z^{-1}} = \frac{z}{z - \frac{1}{2}} = (\frac{1}{2}z)^n \cdot u[n]$

$$y[n] = x[2n] = (\frac{1}{2})^{2n} \cdot u[2n] = (\frac{1}{4})^n \cdot u[n] = (\frac{1}{4})^n \cdot u[n] \Rightarrow \frac{z}{z - \frac{1}{4}} = \frac{1}{1 - \frac{1}{4}z^{-1}} = \frac{1}{1 - \frac{1}{4}e^{-jw}}$$

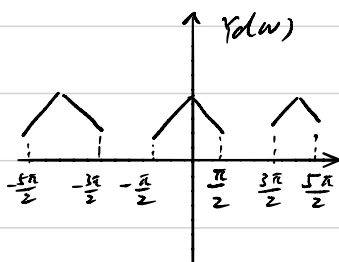
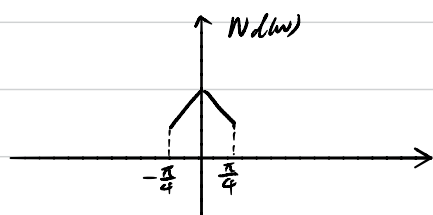
6. (a)



$$\frac{4}{\pi}$$

(b)  $\text{rect}(\frac{2w}{\pi}) = H(w)$

(c)  $\text{IIR LSI}$



(c)