Introduction to PuMaS

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March 3, 2019

1 Introduction

This is an introduction to PuMaS, a software for pharmacometric modeling and simulation. The basic workflow of PuMaS is:

- 1. Build a model.
- 2. Define subjects or populations to simulate or estimate.
- 3. Analyze the results with post-processing and plots.

We will show how to build a multiple-response PK/PD model via the <code>@model</code> macro, define a subject with multiple doses, and analyze the results of the simulation. This tutorial is made to be a broad overview of the workflow and more in-depth treatment of each section can be found in the subsequent tutorials and documentation.

1.1 Installation

Because PuMaS is still unregistered, you will need to give the Git repository in order to add the package. To do this, use the command <code>ladd https://github.com/UMCTM/PuMaS.jl.</code> Doing it this way, PuMaS and its dependencies will install automatically. If one cannot authenticate for this command (since the repository is currently private!), then first clone the repository how you please, use <code>ldev path/to/package</code>, then then do <code>lbuild PuMaS</code>. Using the build command will download and install the dependencies.

1.2 Getting Started

To load the package, use

using PuMaS

1.3 Using the Model Macro

Now let's define a model. A model is defined in an Qmodel block. Inside of this block we have a few subsections. The first of which is Qparam. In here we define what kind of parameters we have. For this model we will define a vector parameter θ of size 12:

```
\begin{array}{l} {\tt @param \ begin} \\ \theta \ \in \ {\tt VectorDomain(12)} \\ {\tt end} \end{array}
```

Next we define our random effects. The random effects are defined by a distribution from Distributions.jl. For more information on defining distributions, please see the Distributions.jl documentation. For this tutorial, we wish to have a multivariate normal of 11 uncorrelated random effects, so we utilize the syntax:

Notice that here we imported I from LinearAlgebra and and said that our Normal distribution's covariance is said I, the identity matrix.

Now we define our pre-processing step in **@pre**. This is where we choose how the parameters, random effects, and the covariates collate. We define the values and give them a name as follows:

```
@pre begin
     Ka1
                  = \theta[1]
     CL
                  = \theta[2] * \exp(\eta[1])
      Vс
                  = \theta[3] * \exp(\eta[2])
                   = \theta[4] * \exp(\eta[3])
      ۷p
                  = \theta[5] * \exp(\eta[4])
                  = \theta[6] * \exp(\eta[5])
     Kin
     Kout
                  = \theta[7] * \exp(\eta[6])
      IC50
                  = \theta[8] * \exp(\eta[7])
      XAMI
                  = \theta[9] * \exp(\eta[8])
                  = \theta[10] * \exp(\eta[9])
      {\tt Vmax}
                  = \theta[11] * \exp(\eta[10])
                  = \theta[12] * \exp(\eta[11])
      Km
end
```

Next we define the @init block which gives the inital values for our differential equations. Any variable not mentioned in this block is assumed to have a zero for its starting value. We wish to only set the starting value for Resp, and thus we use:

```
@init begin
Resp = \theta[6]/\theta[7]
end
```

Now we define our dynamics. We do this via the **@dynamics** block. Differential variables are declared by having a line defining their derivative. For our model, we use:

Lastly we utilize the **@derived** macro to define our post-processing. We can output values using the following:

```
 \begin{array}{lll} \textbf{@derived begin} \\ & \textbf{ev1} & = \textbf{Ev1} \\ & \textbf{cp} & = \textbf{Cent} \ / \ \theta \textbf{[3]} \\ & \textbf{periph} & = \textbf{Periph} \\ & \textbf{resp} & = \textbf{Resp} \\ \\ \textbf{end} \end{array}
```

The Cmodel block is all of these together, giving us the following model:

```
using LinearAlgebra
model = @model begin
    @param begin
       \theta \in \texttt{VectorDomain}(12)
    @random begin
       \eta \sim MvNormal(Matrix{Float64}(I, 11, 11))
    @pre begin
         Ka1
                 = \theta[1]
         CL
                  = \theta[2] * \exp(\eta[1])
         Vс
                  = \theta[3] * \exp(\eta[2])
         Q
                  = \theta[4] * \exp(\eta[3])
               = \theta[5] * \exp(\eta[4])
         Vр
         Kin = \theta[6] * exp(\eta[5])
         Kout = \theta[7]*exp(\eta[6])
         IC50 = \theta[8] * exp(\eta[7])
                = \theta[9] * \exp(\eta[8])
         IMAX
                  = \theta[10] * \exp(\eta[9])
         Vmax = \theta[11]*exp(\eta[10])
                  = \theta[12] * \exp(\eta[11])
         Km
    end
    @init begin
         Resp = \theta[6]/\theta[7]
    end
    @dynamics begin
         Ev1'
                 = -Ka1*Ev1
         Cent' = Ka1*Ev1 - (CL+Vmax/(Km+(Cent/Vc))+Q)*(Cent/Vc) + Q*(Periph/Vp)
         Periph' = Q*(Cent/Vc) - Q*(Periph/Vp)
                 = Kin*(1-(IMAX*(Cent/Vc)^{\gamma}/(IC50^{\gamma}+(Cent/Vc)^{\gamma}))) - Kout*Resp
         Resp'
    end
```

```
@derived begin
    ev1 = Ev1
    cp = Cent / θ[3]
    periph = Periph
    resp = Resp
    end
end

PKPDModel
    Parameters: θ
    Random effects: η
    Covariates:
    Dynamical variables: Ev1, Cent, Periph, Resp
    Derived: ev1, cp, periph, resp
```

1.4 Building a Subject

Now let's build a subject to simulate the model with. A subject defines three components:

- 1. The dosage regimen
- 2. The covariates of the indvidual
- 3. Observations associated with the individual.

Our model did not make use of covariates so we will ignore (2) for now, and (3) is only necessary for fitting parameters to data which will not be covered in this tutorial. Thus our subject will be defined simply by its dosage regimen.

To do this, we use the DosageRegimen constructor. It uses terms from the NMTRAN format to specify its dose schedule. The first value is always the dosing amount. Then there are optional arguments, the most important of which is time which specifies the time that the dosing occurs. For example,

```
DosageRegimen(15, time=0)
```

```
PuMas.DosageRegimen(1 \times 8 DataFrames.DataFrame
Row time
               cmt
                                evid ii
                                                addl
                                                        rate
                                                                 SS
      Float64 Int64 Float64 Int8 Float64
                                                Int64
                                                       Float64
                                                                 Int8
      0.0
                       15.0
                                       0.0
                                                        0.0
                                                                 0
1
               1
                                1
```

is a dosage regimen which simply does a single dose at time t=0 of amount 15. If we use arrays, then the dosage regimen will be the grouping of the values. For example, let's define a dose of amount 15 at times t=0,4,8, and 12:

```
regimen = DosageRegimen([15,15,15,15], time=[0,4,8,12])
```

PuMaS.DosageRegimen(4×8 DataFrames.DataFrame												
Row	time	cmt	amt	evid	ii	addl	rate	SS				
	Float64	Int64	Float64	Int8	Float64	Int64	Float64	Int8				
1	0.0	1	15.0	1	0.0	0	0.0	0				
2	4.0	1	15.0	1	0.0	0	0.0	0				
3	8.0	1	15.0	1	0.0	0	0.0	0				
4	12.0	1	15.0	1	0.0	0	0.0	0				

Let's define our subject to have id=1 and this multiple dosing regimen:

```
subject = Subject(id=1,evs=regimen)
Subject
  ID: 1
  Events: 4
  Observations: 0
```

1.5 Running a Simulation

The main function for running a simulation is simobs. simobs on a population simulates all of the population (in parallel), while simobs on a subject simulates just that subject. If we wish to change the parameters from the initialized values, then we pass them in. Let's simulate subject 1 with a set of chosen parameters:

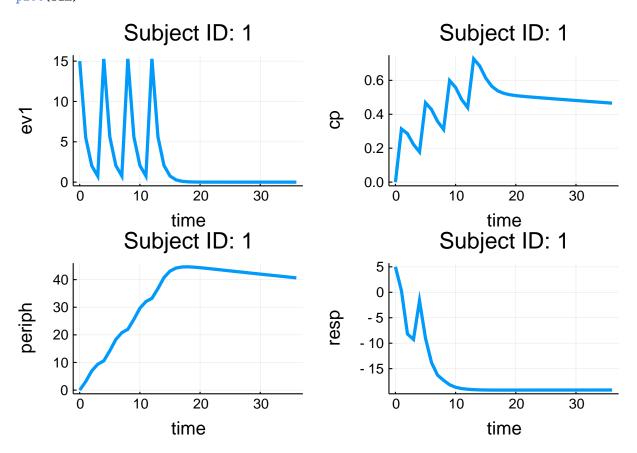
PuMas.SimulatedObservations{PuMas.Subject{StructArrays.StructArray{NamedTuple{(),Tuple{}},1,NamedTuple{(),Tuple{}}},Nothing,Array{PuMas.Event{Float64,Float64,Float64,Float64,Float64},1},Int64},StepRangeLen{Float64,Base.TwicePrecision{Float64},Base.TwicePrecision{Float64}},NamedTuple{(:ev1, :cp, :periph, :resp),NTuple{4,Array{Float64,1}}}}(Subject

ID: 1
Events: 4
Observations: 0

, 0.0:1.0:36.0, (ev1 = [15.0, 5.51819, 2.03002, 0.746802, 15.2747, 5.61917, 2.06716, 0.760493, 15.2798, 5.62125 ... 4.69095e-6, 1.74671e-6, 6.22187e-7, 2.50809e-7, 7.7347e-8, 4.51083e-8, 7.05561e-9, 3.11017e-9, 1.00973e-8, 3. 72031e-9], cp = [0.0, 0.313464, 0.285825, 0.221941, 0.178076, 0.467523, 0.4 27793, 0.35796, 0.311068, 0.598755 ... 0.489206, 0.486533, 0.483875, 0.4812 32, 0.478603, 0.47599, 0.47339, 0.470805, 0.468233, 0.465676], periph = [0.0, 3.0874, 6.94691, 9.35919, 10.5922, 14.2369, 18.3156, 20.7888, 22.0121, 2 5.6174 ... 42.6949, 42.4618, 42.2299, 41.9993, 41.7699, 41.5418, 41.3149, 4 1.0892, 40.8648, 40.6417], resp = [5.0, 0.305137, -8.18658, -9.25497, -1.65 224, -9.05399, -13.8201, -16.2742, -17.2906, -18.1647 ... -19.2056, -19.2046, -19.2036, -19.2026, -19.2015, -19.2003, -19.1991, -19.1978, -19.1965, -1 9.1951]))

We can then plot the simulated observations by using the plot command:

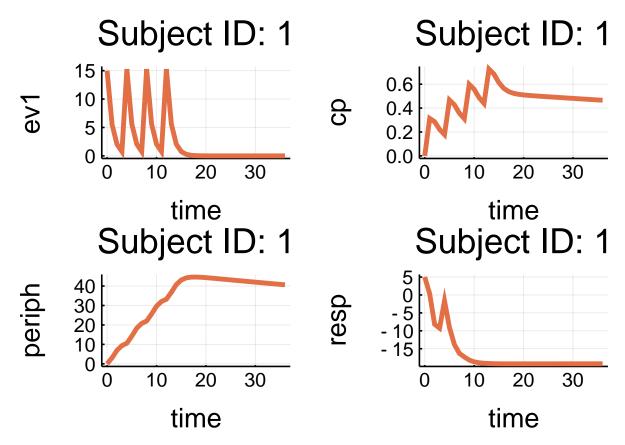
using Plots
plot(sim)



Note that we can use the attributes from Plots. jl to further modify the plot. For example,

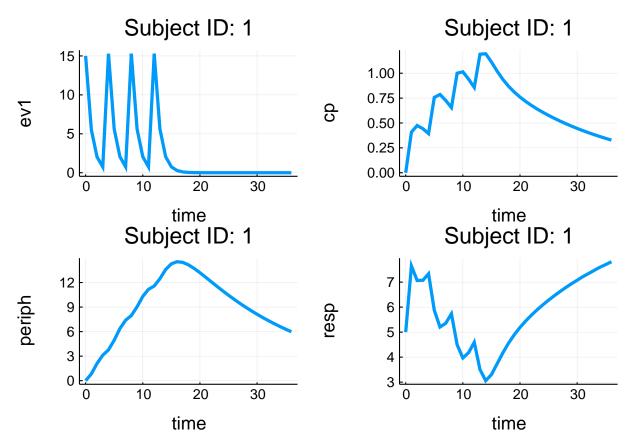
plot(sim,

color=2,thickness_scaling=1.5,
legend=false, lw=2)



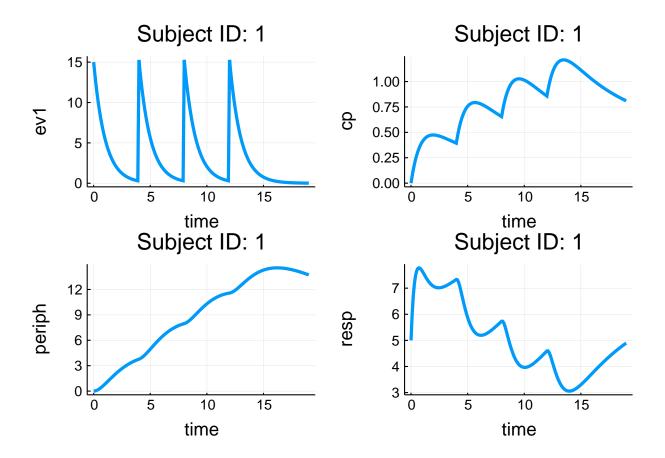
Notice that in our model we said that there was a single parameter θ so our input parameter is a named tuple with just the name θ . When we only give the parameters, the random effects are automatically sampled from their distributions. If we wish to prescribe a value for the random effects, we pass initial values similarly:

```
rfx = (η = rand(11),)
sim = simobs(model, subject, p, rfx)
plot(sim)
```



The points which are saved are by default at once every hour until one day after the last event. If you wish to change the saving time points, pass the keyword argument obstimes. For example, let's save at every 0.1 hours and run the simulation for 19 hours:

```
sim = simobs(model, subject, p, rfx, obstimes = 0:0.1:19)
plot(sim)
```



1.6 Handling the SimulatedObservations

The resulting SimulatedObservations type has two fields. sim.times is an array of time points for which the data was saved. sim.derived is the result of the derived variables. From there, the derived variables are accessed by name. For example,

```
sim[:cp]
```

```
191-element Array{Float64,1}:
0.07037765328279763
0.13215868350050847
0.18624251804965614
0.23343926699001613
0.2744783807378028
0.31001638347313165
0.34064428045570283
0.366893504097005
0.38924201107460493
0.856426960974048
0.8503466663376876
0.8443673919896246
0.8384863609601216
0.8327008553011449
0.8270082160863638
```

0.8214058005240823

- 0.815890856398964
- 0.8104607748418997

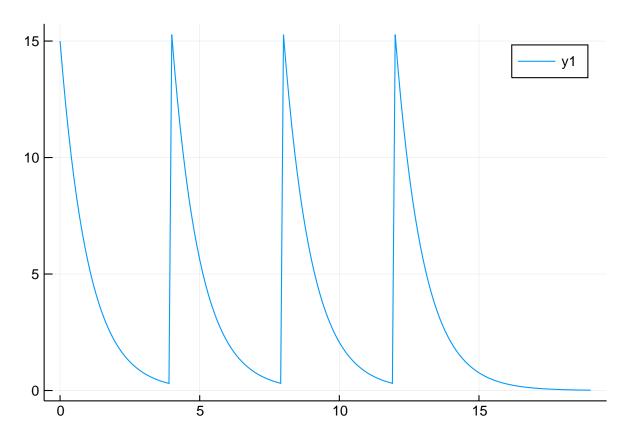
is the array of cp values at the associated time points. We can turn this into a DataFrame via using the DataFrame command:

DataFrame(sim)

	time	ev1	cp	periph	resp
	Float64	Float64	Float64	Float64	Float64
1	0.0	15.0	0.0	0.0	5.0
2	0.1	13.5726	0.0703777	0.0128867	6.00151
3	0.2	12.281	0.132159	0.0490161	6.70518
4	0.3	11.1123	0.186243	0.104911	7.18054
5	0.4	10.0548	0.233439	0.177485	7.48518
6	0.5	9.09796	0.274478	0.264	7.6644
7	0.6	8.23217	0.310016	0.362037	7.75319
8	0.7	7.44878	0.340644	0.469454	7.77827
9	0.8	6.73993	0.366894	0.584364	7.75985
10	0.9	6.09855	0.389242	0.705109	7.71295
11	1.0	5.51819	0.40812	0.830227	7.64894
12	1.1	4.99307	0.423913	0.958445	7.57581
13	1.2	4.51791	0.436967	1.08865	7.49949
14	1.3	4.08797	0.447596	1.21986	7.4243
15	1.4	3.69895	0.456077	1.35125	7.35285
16	1.5	3.34695	0.462661	1.4821	7.28698
17	1.6	3.02845	0.467574	1.61176	7.228
18	1.7	2.74024	0.471016	1.73972	7.17647
19	1.8	2.47948	0.473167	1.86553	7.13243
20	1.9	2.24353	0.474188	1.98881	7.09585
21	2.0	2.03003	0.474224	2.10923	7.06662
22	2.1	1.83683	0.473405	2.22654	7.04437
23	2.2	1.66203	0.471843	2.34055	7.02853
24	2.3	1.50388	0.469641	2.45107	7.01855

From there, any Julia tools can be used to analyze these arrays and DataFrames. For example, if we wish the plot the result of ev1 over time, we'd use the following:

plot(sim.times,sim[:ev1])



Using these commands, a Julia program can be written to post-process the program however you like!

1.7 Conclusion

This tutorial covered basic workflow for how to build a model and simulate results from it. The subsequent models will go into more detail in the components, such as:

- 1. More detailed treatment of specifying populations, dosage regimens, and covariates.
- 2. Reading in dosage regimens and observations from NMTRAN data.

```
using PuMaSTutorials
PuMaSTutorials.tutorial_footer(WEAVE_ARGS[:folder],WEAVE_ARGS[:file])
```

1.8 Appendix

These tutorials are part of the PuMaSTutorials.jl repository, found at: https://github.com/JuliaDiffEq/D To locally run this tutorial, do the following commands:

```
using PuMaSTutorials
PuMaSTutorials.weave_file("introduction","introduction.jmd")
```

Computer Information:

```
Julia Version 1.1.0
Commit 80516ca202 (2019-01-21 21:24 UTC)
Platform Info:
    OS: Windows (x86_64-w64-mingw32)
    CPU: Intel(R) Core(TM) i7-8700 CPU @ 3.20GHz
    WORD_SIZE: 64
    LIBM: libopenlibm
    LLVM: libLLVM-6.0.1 (ORCJIT, skylake)
Environment:
    JULIA_EDITOR = "C:\Users\accou\AppData\Local\atom\app-1.34.0\atom.exe" -a
    JULIA_NUM_THREADS = 6
```

Package Information:

```
Status `C:\Users\accou\.julia\environments\v1.1\Project.toml`
[7e558dbc-694d-5a72-987c-6f4ebed21442] ArbNumerics 0.3.6
[c52e3926-4ff0-5f6e-af25-54175e0327b1] Atom 0.7.14
[6e4b80f9-dd63-53aa-95a3-0cdb28fa8baf] BenchmarkTools 0.4.2
[336ed68f-0bac-5ca0-87d4-7b16caf5d00b] CSV 0.4.3
[3895d2a7-ec45-59b8-82bb-cfc6a382f9b3] CUDAapi 0.6.0
[be33ccc6-a3ff-5ff2-a52e-74243cff1e17] CUDAnative 1.0.1
[3a865a2d-5b23-5a0f-bc46-62713ec82fae] CuArrays 0.9.1
[a93c6f00-e57d-5684-b7b6-d8193f3e46c0] DataFrames 0.17.1
[55939f99-70c6-5e9b-8bb0-5071ed7d61fd] DecFP 0.4.8
[abce61dc-4473-55a0-ba07-351d65e31d42] Decimals 0.4.0
[bcd4f6db-9728-5f36-b5f7-82caef46ccdb] DelayDiffEq 5.2.0+
[39dd38d3-220a-591b-8e3c-4c3a8c710a94] Dierckx 0.4.1
[2b5f629d-d688-5b77-993f-72d75c75574e] DiffEqBase 5.4.1+
[bb2cbb15-79fc-5d1e-9bf1-8ae49c7c1650] DiffEqBenchmarks 0.0.0
[459566f4-90b8-5000-8ac3-15dfb0a30def] DiffEqCallbacks 2.5.2
[f3b72e0c-5b89-59e1-b016-84e28bfd966d] DiffEqDevTools 2.7.0
[aae7a2af-3d4f-5e19-a356-7da93b79d9d0] DiffEqFlux 0.2.0
[c894b116-72e5-5b58-be3c-e6d8d4ac2b12] DiffEqJump 6.1.0+
[1130ab10-4a5a-5621-a13d-e4788d82bd4c] DiffEqParamEstim 1.6.0+
[055956cb-9e8b-5191-98cc-73ae4a59e68a] DiffEqPhysics 3.1.0
[a077e3f3-b75c-5d7f-a0c6-6bc4c8ec64a9] DiffEqProblemLibrary 4.1.0
[225cb15b-72e6-54e6-9a40-306d353791de] DiffEqTutorials 0.1.0
[Oc46a032-eb83-5123-abaf-570d42b7fbaa] DifferentialEquations 6.3.0
[497a8b3b-efae-58df-a0af-a86822472b78] DoubleFloats 0.7.5
[587475ba-b771-5e3f-ad9e-33799f191a9c] Flux 0.7.3
[f6369f11-7733-5829-9624-2563aa707210] ForwardDiff 0.10.3+
[28b8d3ca-fb5f-59d9-8090-bfdbd6d07a71] GR 0.38.1
[7073ff75-c697-5162-941a-fcdaad2a7d2a] IJulia 1.17.0
[c601a237-2ae4-5e1e-952c-7a85b0c7eef1] Interact 0.9.1
[b6b21f68-93f8-5de0-b562-5493be1d77c9] Ipopt 0.5.4
[4076af6c-e467-56ae-b986-b466b2749572] JuMP 0.19.0
[e5e0dc1b-0480-54bc-9374-aad01c23163d] Juno 0.5.4
[7f56f5a3-f504-529b-bc02-0b1fe5e64312] LSODA 0.4.0
```

```
[eff96d63-e80a-5855-80a2-b1b0885c5ab7] Measurements 2.0.0
[76087f3c-5699-56af-9a33-bf431cd00edd] NLopt 0.5.1
[c030b06c-0b6d-57c2-b091-7029874bd033] ODE 2.4.0
[54ca160b-1b9f-5127-a996-1867f4bc2a2c] ODEInterface 0.4.5+
[47be7bcc-f1a6-5447-8b36-7eeeff7534fd] ORCA 0.2.1
[429524aa-4258-5aef-a3af-852621145aeb] Optim 0.17.2
[1dea7af3-3e70-54e6-95c3-0bf5283fa5ed] OrdinaryDiffEq 5.3.0+
[65888b18-ceab-5e60-b2b9-181511a3b968] ParameterizedFunctions 4.1.1
[f0f68f2c-4968-5e81-91da-67840de0976a] PlotlyJS 0.12.3
[91a5bcdd-55d7-5caf-9e0b-520d859cae80] Plots 0.23.1
[71ad9d73-34c4-5ce9-b7b1-f7bd31ac38ba] PuMaS 0.0.0
[02bcfc65-177a-5a82-813b-f02a21c9b35a] PuMaSTutorials 0.0.0
[d330b81b-6aea-500a-939a-2ce795aea3ee] PyPlot 2.8.0
[731186ca-8d62-57ce-b412-fbd966d074cd] RecursiveArrayTools 0.20.0
[90137ffa-7385-5640-81b9-e52037218182] StaticArrays 0.10.3
[789caeaf-c7a9-5a7d-9973-96adeb23e2a0] StochasticDiffEq 6.1.1+
[c3572dad-4567-51f8-b174-8c6c989267f4] Sundials 3.1.0+
[1986cc42-f94f-5a68-af5c-568840ba703d] Unitful 0.14.0
[2a06ce6d-1589-592b-9c33-f37faeaed826] UnitfulPlots 0.0.0
[44d3d7a6-8a23-5bf8-98c5-b353f8df5ec9] Weave 0.7.2
```