1 Bioequivalence

Bioequivalence.jl is a package for performing bioequivalence analysis part of the Pumas (PharmaceUtical Modeling And Simulation) ecosystem for developing, simulating, fitting, and analyzing pharmaceutical models.

This document provides a how-to and technical details for performing bioequivalence analysis using the software.

1.1 How to obtain Bioequivalence.jl?

Bioequivalence.jl is covered under the Julia Computing EULA and distributed through via JuliaPro from Julia Computing Inc.

Using JuliaPro, one can install the Bioequivalence.jl package using the Julia package manager.

```
using Pkg;
Pkg.add("Bioequivalence")
```

1.2 Getting Started

To load the package, use using Bioequivalence

The Bioequivalence package provides two functions: read be and generate design.

read_be is an alias for BioequivalenceStudy which takes a table with data from a bioequivalence study and other optional arguments and returns the output of the analysis. This function tries to be quite smart and flexible. For most cases, it should work how you want it to work, but allows for users to overwrite default behavior.

The other function provided by Bioequivalence.jl is generate_design which allows to generate data according to some bioequivalence study design.

1.2.1 Setting up the environment

There are a few packages that can be helpful when using Bioequivalence.jl.

- CSV.jl is a package for importing text files (e.g., comma-separated values or CSV)
- DataFrames.jl is a package that provides a table representation for data
- StatsBase.jl is a package that provides a common way to query statistical models

In order to install any of these packages, one can use the package manager.

For example to install CSV.il,

```
julia> using Pkg;
julia> Pkg.add("CSV")
```

We can load the packages through,

```
using CSV, DataFrames, StatsBase, Bioequivalence
```

We always recommend using a local environment for each application which allows for reproducibility. For learning more about environments, we recommend checking out the Julia documentation.

1.3 Designs

For each design, we well use the syntax read_be(data, endpoint, kwargs...) where the kewyword arguments allows to change some default behavior.

For example, every data, should be a DataFrame with the following variables:

- id: the subject ID
- sequence: the sequence of formulations (e.g., "RT" for reference and test)
- period: integers referring to the periods starting with the first period being 1
- endpoint: the values for the endpoint (e.g., AUC)

If the dataset has the endpoint under the variable auc, the syntax would be

```
output = read be(data, :auc)
```

If the id variable is named subject id then the syntax would follow as

```
output = read be(data, :auc, id = :subject id)
```

Other arguments will be explained through the examples.

The result may be queried in the following manner,

```
output.data
output.design
output.model
output.result
```

The final section on additional information provides a complete summary.

This section will cover the most common arguments for each of the supported designs:

- Parallel (e.g., R|T, A|B|C)
- 2x2 (e.g., RT|TR)

- Balaam (e.g., RR|RT|TR|TT)
- Dual (e.g., RTT|TRR)
- 2S4P1 (e.g., RTTR|TRRT)
- 2S4P2 (e.g., RTRT|TRTR)
- WD3F (e.g., ABC|ACB|BAC|BCA|CAB|CBA)
- WD4F (e.g., ABCD|CADB|DCBA|BDAC)

1.3.1 Nonparametric

Nonparametric designs are included for analysis of endpoints such as Tmax.

We can load data from a bioequivalence study by using the CSV.read function and giving itt the path to a file.

In this case, we will use some example/validation datasets included with Bioequivalence.jl.

This dataset is available from Patterson and Jones (2006).

	id	sequence	period	Tmax
	Int64	String	Int64	Float64
1	1	RT	1	0.5
2	1	RT	2	0.5
3	2	TR	1	1.0
4	2	TR	2	1.0
5	3	TR	1	0.5
6	3	TR	2	0.5

We have now assigned the data to the variable PJ31.

The average bioequivalence analysis can be requested through read_be.

```
Tmax = read_be(PJ31, :Tmax)
```

Design: RT|TR

Sequences: RT|TR (2) Periods: 1:2 (2)

Subjects per Sequence: (RT = 17, TR = 15)

Average Bioequivalence

lnLB lnUB LB UI

T - R -0.202733 0.346574 0.816497 1.41421

The first argument is the data and the second argument is which variable should be used as the endpoint.

Variable names in DataFrames are symbols.

When the name of the endpoint matches some form of Tmax (case insensitive) it defaults to nonparametric.

Otherwise, it will attempt a parametric design. This can be overwriten through the nonparametric argument.

Nonparametric analysis uses the Wilcoxon signed rank test.

Tmax.model

1-element Array{HypothesisTests.ApproximateSignedRankTest{Float64},1}: Approximate Wilcoxon signed rank test

Population details:

parameter of interest: Location parameter (pseudomedian)

value under h_0: point estimate: 0.0

95% confidence interval: (-0.2027, 0.3466)

Test summary:

outcome with 95% confidence: fail to reject h_0

two-sided p-value: 0.8774

Details:

number of observations: Wilcoxon rank-sum statistic: 182.0

rank sums: [182.0, 169.0] adjustment for ties: 1848.0

normal approximation (μ , σ): (6.5, 38.88122940443113)

Other endpoints can potentially be analyzed through a nonparametric method as well

PJ46 = CSV.read(string(dirname(pathof(Bioequivalence)),

"/../data/Williams/PJ2006_4_6.tsv"))

first(PJ46, 6)

	id	sequence	period	AUC	Cmax
	Int64	String	Int64	Float64	Float64
1	1	DCAB	1	2942.0	563.6
2	1	DCAB	2	2525.0	658.1
3	1	DCAB	3	278.0	55.6
4	1	DCAB	4	359.0	73.0
5	2	ADBC	1	484.0	108.4
6	2	ADBC	2	4190.0	818.0

NP = read_be(PJ46, nonparametric = true)

Design: ADBC|BACD|CBDA|DCAB

Sequences: ADBC|BACD|CBDA|DCAB (4)

Periods: 1:4 (4)

Subjects per Sequence: (ADBC = 7, BACD = 7, CBDA = 7, DCAB = 7)

Average Bioequivalence

lnLB lnUB LB IJB D - A 2.03582 2.11813 7.65856 8.31556 B - A -0.0734472 0.0543133 0.929185 1.05582 7.7751 8.57292 C - A 2.05093 2.14861

1.3.2 Parallel

Consider a parallel design dataset with balance between treatment groups such as Clayton and Leslie (1981).

first(ClaytonandLeslie1981, 6)

	id	sequence	period	AUC
	Int64	String	Int64	Float64
1	1	Τ	1	2.52
2	2	${ m T}$	1	8.87
3	3	${ m T}$	1	0.79
4	4	${ m T}$	1	1.68
5	5	${ m T}$	1	6.95
6	6	${ m T}$	1	1.05

The bioequivalence analysis can be requested through BioequivalenceStudy or its alias read_be.

```
# notice it defaults to the AUC endpoint
Parallel = read_be(ClaytonandLeslie1981) # Same as read_be(ClaytonandLeslie1981, :AUC)
```

Design: R|T

Sequences: R|T (2) Periods: 1:1 (1)

Subjects per Sequence: (R = 9, T = 9)

Average Bioequivalence

```
PE SE 1nLB 1nUB GMR LB UB
T - R -0.721906 0.333328 -1.31755 -0.126258 0.485825 0.267789 0.881387
```

The output shows the design, statistical model, and result.

One can access the statistical model directly through

Parallel.model

```
1-element Array{HypothesisTests.UnequalVarianceTTest,1}:
   Two sample t-test (unequal variance)
```

Population details:

parameter of interest: Mean difference

value under h_0: 0

point estimate: -0.7219063401460275 95% confidence interval: (-1.4507, 0.0069)

Test summary:

outcome with 95% confidence: fail to reject h_0

two-sided p-value: 0.0519

Details:

number of observations: [9,9]

t-statistic: -2.1657564404915037 degrees of freedom: 11.633717042877814 empirical standard error: 0.3333275739825092 The results can be accessed through

Parallel.result

	Parameter	PE	SE	lnLB	lnUB	GMR	LB	UB
	String	Float64	Float64	Float64	Float64	Float64	Float64	Float64
1	T - R	-0.721906	0.333328	-1.31755	-0.126258	0.485825	0.267789	0.881387

or calling coeftable on the object

coeftable(Parallel)

```
PE SE lnLB lnUB GMR LB UB
T - R -0.721906 0.333328 -1.31755 -0.126258 0.485825 0.267789 0.881387
```

Notice that the results are validated with those reported in Fuglsang, Schütz, and Labes (2015). The Geometric Means Ratio (GMR) has a point estimate of (48.58) and a 90% confidence interval of (26.78, 88.14). These are the values reported in the study obtained with various statistical packages with the Welch correction.

1.3.3 Crossover

The most common bioequivalence design is perhaps the 2x2 crossover (RT|TR). Consider a dataset from Schütz, Labes, and Fuglsang (2014) which has been simulated with an extreme range in raw data, outliers, and imbalance between sequences and a large number of subjects.

	id	period	sequence	AUC
	Int64	Int64	String	Float64
1	1	1	TR	168.407
2	1	2	TR	210.919
3	2	1	TR	131.031
4	2	2	TR	67.4314
5	3	1	TR	151.737
6	3	2	TR	85.1296

The bioequivalence analysis can be requested through BioequivalenceStudy

```
# notice it defaults to the AUC endpoint
Crossover = read_be(SLF2014)
```

Design: RT|TR

Sequences: RT|TR (2) Periods: 1:2 (2)

Subjects per Sequence: (RT = 288, TR = 429)

Average Bioequivalence

PE SE 1nLB 1nUB GMR LB UB
T - R -0.0680309 0.044609 -0.141501 0.00543947 0.934232 0.868054 1.00545

As with other designs one can access the specific elements of the models use in the analysis.

loglikelihood(Crossover.model.model)

-1265.3503174162302

The results are obtained through,

Crossover.result

	Parameter	PE	SE	lnLB	lnUB	GMR	LB	UB
	String	Float64	Float64	Float64	Float64	Float64	Float64	Float64
1	T - R	-0.0680309	0.044609	-0.141501	0.00543947	0.934232	0.868054	1.00545

Crossover 2x2 designs are validated with Schütz, Labes, and Fuglsang (2014) and Patterson and Jones (2006). In this example, the estimate for the GMR is (93.42) with a 90% confidence interval of (86.81, 100.55).

1.3.4 Balaam

The Balaam design (RR|RT|TR|TT) is explored with a dataset from Chow and Liu (2009).

	id	sequence	period	AUC
	Int64	String	Int64	Int64
1	1	TT	1	280
2	1	TT	2	482
3	2	TT	1	219
4	2	TT	2	161
5	3	TT	1	230
6	3	TT	2	99

The data has the same specification as other crossover studies.

The analysis follows similarly as well.

```
# notice it defaults to the AUC endpoint
Balaam = read_be(ChowandLiu2009)
```

Design: RR|RT|TR|TT

Sequences: RR|RT|TR|TT (4)

Periods: 1:2 (2)

Subjects per Sequence: (RR = 6, RT = 6, TR = 6, TT = 6) Regulatory constant for reference-scaled estimates: 0.10Auxiliary parameter for reference-scaled estimates: 1.11

Average Bioequivalence

```
PE SE 1nLB 1nUB GMR LB UB scLB scUB Varratio VarLB VarUB

T - R -0.129419 0.0936591 -0.290245 0.0314075 0.878606 0.74808 1.03191 0.75401 1.32624 6.49813 3.871 10.9082
```

We can also obtain the results for the intra-subject variabilities through

 ${\tt Balaam.model.}\sigma$

0.2294170516947747

Designs with repeated measures include rescaled parameter estimates and variance analysis.

The rescaled parameter estimates are especially of interest when the reference drug is a highly variable drug (HVD) or a narrow therapeutic index (NTI) drug (Haidar et al. 2008).

The default values are:

- regulatory constant for reference-scaled estimates: 0.1
- auxiliary parameter for reference-scaled estimates: 1.11

These maybe be overwriten by passing the keyword arguments (see the docstring of read_be for more details).

1.3.5 Dual

Consider the example 4.1 in Patterson and Jones (2006)

	id	sequence	period	AUC	Cmax
	Int64	String	Int64	Float64	Float64
1	101	TRR	1	12.26	0.511
2	101	TRR	2	16.19	0.688
3	101	TRR	3	11.34	0.533
4	102	TRR	1	397.98	13.27
5	102	TRR	2	267.63	7.933
6	102	TRR	3	487.55	12.952

Dual = read_be(PJ41, :Cmax)

Design: RTT|TRR

Sequences: RTT|TRR (2)

Periods: 1:3 (3)

Subjects per Sequence: (RTT = 47, TRR = 48)

Regulatory constant for reference-scaled estimates: 0.10 Auxiliary parameter for reference-scaled estimates: 1.11

Average Bioequivalence

```
PE SE lnLB lnUB GMR LB UB scLB scUB Varratio VarLB VarUB
```

T - R -0.0565121 0.0685313 -0.169803 0.0567792 0.945055 0.843831 1.05842 0.57774 1.73088 1.23391 1.03853 1.46604

1.3.6 2S4P Designs

For 2S4P designs both RRTT|TTRR and RTRT|TRTR are supported

	id	sequence	period	AUC	Cmax
	Int64	String	Int64	Int64	Int64
1	1	RTTR	1	10671	817
2	1	RTTR	2	12772	1439
3	1	RTTR	3	13151	1310
4	1	RTTR	4	11206	1502
5	2	TRRT	1	6518	1393
6	2	TRRT	2	6068	1372

Inner = read_be(PJ43)

Design: RTTR|TRRT

Sequences: RTTR|TRRT (2)

Periods: 1:4 (4)

Subjects per Sequence: (RTTR = 8, TRRT = 9)

Regulatory constant for reference-scaled estimates: 0.10 Auxiliary parameter for reference-scaled estimates: 1.11

Average Bioequivalence

PE SE lnLB lnUB GMR LB UB scLB scUB Varratio VarLB VarUB

T - R 0.0356935 0.0226361 -0.00230475 0.0736918 1.03634 0.997698 1.07647 0.908307 1.10095 1.29984 0.962939 1.7546

	id	sequence	period	AUC	Cmax
	Int64	String	Int64	Float64	Float64
1	1	RTRT	1	812.6	99.85
2	1	RTRT	2	1173.7	204.09
3	1	RTRT	3	889.1	170.94
4	1	RTRT	4	620.1	112.78
5	2	TRTR	1	216.3	29.06
6	2	TRTR	2	338.0	50.48

Outer = read_be(PJ44, :Cmax)

Design: RTRT|TRTR

Sequences: RTRT|TRTR (2)

Periods: 1:4 (4)

Subjects per Sequence: (RTRT = 27, TRTR = 27)

Regulatory constant for reference-scaled estimates: 0.10 Auxiliary parameter for reference-scaled estimates: 1.11

Average Bioequivalence

```
PE SE lnLB lnUB GMR LB UB scLB scUB Varratio VarLB VarUB
```

T - R 0.413998 0.0745634 0.29061 0.537386 1.51285 1.33724 1.71153 0.566073 1.76656 0.937014 0.79558 1.10359

1.3.7 Williams

Consider a 3 formulations Williams design

first(PJ45, 6)

	id	sequence	period	AUC	Cmax
	Int64	String	Int64	Int64	Int64
1	1	SRT	1	7260	1633
2	1	SRT	2	6463	1366
3	1	SRT	3	8759	2141
4	2	RTS	1	3457	776
5	2	RTS	2	6556	2387
6	2	RTS	3	4081	1355

 $W3F = read_be(PJ45)$

Design: RST|RTS|SRT|STR|TRS|TSR

Sequences: RST|RTS|SRT|STR|TRS|TSR (6)

Periods: 1:3 (3)

Subjects per Sequence: (RST = 9, RTS = 11, SRT = 11, STR = 10, TRS = 11, TSR = 10)

Average Bioequivalence

```
PE SE 1nLB 1nUB GMR LB UB

S - R 0.341072 0.0378374 0.278325 0.403819 1.40645 1.32092 1.49753

T - R 0.149693 0.0378182 0.086978 0.212408 1.16148 1.09087 1.23665
```

Imagine for a moment that the reference formulation is actually S instead of R. One can pass such a parameter as following.

```
W3F = read_be(PJ45, reference = 'S')
```

Design: RST|RTS|SRT|STR|TRS|TSR

Sequences: RST|RTS|SRT|STR|TRS|TSR (6)

Periods: 1:3 (3)

Subjects per Sequence: (RST = 9, RTS = 11, SRT = 11, STR = 10, TRS = 11, TSR = 10)

Average Bioequivalence

```
PE SE 1nLB 1nUB GMR LB UB

R - S -0.341072 0.0378374 -0.403819 -0.278325 0.711008 0.667765 0.757051

T - S -0.191379 0.0380271 -0.254441 -0.128318 0.825819 0.77535 0.879574
```

Williams designs for four formulations are available as well

```
PJ46 = CSV.read(string(dirname(pathof(Bioequivalence)),
                       "/../data/Williams/PJ2006_4_6.tsv"))
```

first(PJ46, 6)

	id	sequence	period	AUC	Cmax
	Int64	String	Int64	Float64	Float64
1	1	DCAB	1	2942.0	563.6
2	1	DCAB	2	2525.0	658.1
3	1	DCAB	3	278.0	55.6
4	1	DCAB	4	359.0	73.0
5	2	ADBC	1	484.0	108.4
6	2	ADBC	2	4190.0	818.0

 $W4F = read_be(PJ46)$

Design: ADBC|BACD|CBDA|DCAB

Sequences: ADBC|BACD|CBDA|DCAB (4)

Periods: 1:4 (4)

Subjects per Sequence: (ADBC = 7, BACD = 7, CBDA = 7, DCAB = 7)

Average Bioequivalence

	PE	SE	lnLB	lnUB	GMR	LB	UB
D - A	0.00468645	0.0342341	-0.0523004	0.0616733	1.0047	0.949044	1.06361
B - A	2.09353	0.0342341	2.03654	2.15052	8.11351	7.66407	8.5893
C - A	2.05738	0.0342341	2.0004	2.11437	7.82546	7.39198	8.28436

1.3.8 Additional documentation

@doc BioequivalenceStudy

```
BioequivalenceStudy(data::AbstractDataFrame,
                    endpoint::Union{Integer, Symbol} = :AUC,
                    w::Real = 0.1,
                    ::Real = 1.11;
                    id::Union{Integer, Symbol} = :id,
                    sequence::Union{Integer, Symbol} = :sequence,
                    period::Union{Integer, Symbol} = :period,
                    reference::Union{Nothing, Char} = nothing,
                    nonparametric::Bool = occursin(r"(?i)tmax", string(endpoint))),
                    reml::Bool = false)
```

Return a bioequivalence study

Arguments

• data: must have id, sequence, period, and an endpoint.

- id: which variable is the subject id?
- sequence: which variable is the sequence?
- period: which variable is the period?
- endpoint: which variable is the endpoint?
- w: regulatory constant for reference-scaled estimates
- : auxiliary parameter for reference-scaled estimates
- reference: which formulation is the reference?

For example, in a design with RTTR|TRRT one can specify 'R' to be the reference. By default, the reference is taken to be the first character (alphabetically).

- nonparametric: use nonparametric method for analysis of the endpoint?
- reml: if the design uses a linear mixed model should it optimize REML instead of ML?

Each bioequivalence study has the following fields:

- data: data used for the study
- design: number of subjects in each sequence
- model: statistical models used for the analysis
- result: result based on previous components

Current designs include:

- Parallel (e.g., R|T, A|B|C)
- 2x2 (e.g., RT|TR)
- Balaam (e.g., RR|RT|TR|TT)
- Dual (e.g., RTT|TRR)
- 2S4P1 (e.g., RTTR|TRRT)
- 2S4P2 (e.g., RTRT|TRTR)
- WD3F (e.g., ABC|ACB|BAC|BCA|CAB|CBA)
- WD4F (e.g., ABCD|CADB|DCBA|BDAC)

Examples,

```
julia> read_be(data) # read_be is an alias for BioequivalenceStudy, same as `BioequivalenceStudy, same as `Bioequivalence
```

@doc generate_design

Returns a DataFrame with id, sequence, period, formulation, amt, evid, cmt, and time. It can be used to quickly set up data for PuMaS, NCA, and Bioequivalence. In order to add covariates, use join to join the result of this function with another DataFrame with covariates.

The following designs are available:

- "Parallel" => 'A':'A' + num formulations 1
- "2x2" => ["RT", "TR"]
- "Balaam" => ["RR", "RT", "TR", "TT"]
- "Dual" => ["RTT", "TRR"]
- "2S4P1" => ["RTTR", "TRRT"]
- "2S4P2" => ["RTRT", "TRTR"]
- "WD3F" => ["ABC", "ACB", "BAC", "BCA", "CAB", "CBA"]
- "WD4F" => ["ABCD", "CADB", "DCBA", "BDAC"]

Examples

```
julia> skeleton = generate_design("Parallel", 100, ["tablet", "soft", "hard"], 10)
```

1.4 References

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Haidar, Sam H., Fairouz Makhlouf, Donald J. Schuirmann, Terry Hyslop, Barbara Davit, Dale Conner, and Lawrence X. Yu. 2008. "Evaluation of a Scaling Approach for the Bioequivalence of Highly Variable Drugs." The AAPS Journal 10 (3): 450-54. DOI:10.1208/s12248-008-9053-4.

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