

Pumas.jl Workshop Solutions

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1 Problem 1: Simulate a first-order absorption model with linear elimination after a 100 mg oral dose in 24 subjects

Parameters are: $K_a = 1 \text{ hr}^{-1}$, $CL = 1 \text{ L/hr}$, $V = 20 \text{ L/hr}$.

1.1 Part 1: Setup the population

```
using Pumas, Plots, CSV, Random
Random.seed!(0)
```

```
MersenneTwister(UInt32[0x00000000], Random.DSFMT.DSFMT_state{Int32}[74839879
7, 1073523691, -1738140313, 1073664641, -1492392947, 1073490074, -162528183
9, 1073254801, 1875112882, 1073717145 ... 943540191, 1073626624, 1091647724
, 1073372234, -1273625233, -823628301, 835224507, 991807863, 382, 0]), [0.0
, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0 ... 0.0, 0.0, 0.0, 0.0, 0.0,
0.0, 0.0, 0.0, 0.0, 0.0], UInt128[0x00000000000000000000000000000000, 0x000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x00000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000
00000000000000000000000000000000 ... 0x00000000000000000000000000000000, 0x0000000000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000000000
00000000000000000000000000000000, 0x00000000000000000000000000000000, 0x0000000000000000
00000000, 0x00000000000000000000000000000000, 0x00000000000000000000000000000000
00000], 1002, 0)
```

```
single_dose_regimen = DosageRegimen(100, time=0)
first(single_dose_regimen.data)
```

	time	cmt	amt	evid	ii	addl	rate	duration	ss
	Float64	Int64	Float64	Int8	Float64	Int64	Float64	Float64	Int8
1	0.0	1	100.0	1	0.0	0	0.0	0.0	0

to build a single subject

```
s1 = Subject(id=1, events=single_dose_regimen, covariates=(Wt=70,))
```

```
Subject
  ID: 1
  Events: 1
  Covariates: Wt
```

let's first define a function to choose body weight randomly

```
choose_covariates() = (Wt = rand(55:80),)
```

```
choose_covariates (generic function with 1 method)
```

Then, we use it to generate a population of subjects with a random weight generated from the covariate function above

```
pop = Population(map(i -> Subject(id = i, events=single_dose_regimen,
covariates=choose_covariates()),1:24))
```

```
Population
  Subjects: 24
  Covariates: Wt
```

You can view the generated population using by calling a random subject by index and look at the subject's

- covariates
- events
- id numbers
- observations
- time

Let us us peek at the first subject's covariates

```
pop[1].covariates
```

```
Pumas.ConstantCovar{NamedTuple{(:Wt,),Tuple{Int64}}}(Wt = 74,)
```

1.2 Part 2: Write the model

```
mymodel = @model begin
  @param begin
    tvcl ∈ RealDomain(lower=0, init = 1.0)
    tvv ∈ RealDomain(lower=0, init = 20)
    tvka ∈ RealDomain(lower = 0, init= 1)
    Ω ∈ PDiagDomain(init=[0.09,0.09, 0.09])
    σ_prop ∈ RealDomain(lower=0,init=0.04)
  end

  @random begin
    η ~ MvNormal(Ω)
  end

  @pre begin
    CL = tvcl * (Wt/70)^0.75 * exp(η[1])
    Vc = tvv * (Wt/70) * exp(η[2])
```

```

    Ka = tvka * exp( $\eta$ [3])
end
@covariates Wt

@analytics Depots1Central1
  #@analytics begin
  #   Depot' = -Ka*Depot
  #   Central' = Ka*Depot - (CL/V)*Central
  #end

@derived begin
  cp = @. 1000*(Central / Vc)
  dv ~ @. Normal(cp, sqrt(cp^2* $\sigma$ _prop))
end
end

PumasModel
  Parameters: tvcl, tvv, tvka,  $\Omega$ ,  $\sigma$ _prop
  Random effects:  $\eta$ 
  Covariates: Wt
  Dynamical variables: Depot, Central
  Derived: cp, dv
  Observed: cp, dv

```

Note that above, we are using the analytical solution in `@analytics`. You can switch to using the differential equation system if you prefer.

1.3 Part 3: Simulate

Let's first extract the model parameters

```

param = init_param(mymodel)

(tvcl = 1.0, tvv = 20, tvka = 1,  $\Omega$  = PDMats.PDiagMat{Float64,Array{Float64,1}}(3, [0.09, 0.09, 0.09], [11.111111111111111, 11.111111111111111, 11.111111111111111]),  $\sigma$ _prop = 0.04)

```

Then using the `simobs` function, carry out the simulation and visualize the simulation output

```

obs = simobs(mymodel, pop, param, obstimes=0:1:72)
plot(obs)

```

where

- `mymodel` is the model setup in the Part 2,
- `pop` is the population of subjects that was setup in Part 1
- `param` is the specified set of model parameters
- `obstimes` specifies the simulation time period.

2 Problem 2: Perform Non-compartmental analysis

We will start by generating a dataframe of the results from the simulation step

```
simdf = DataFrame(obs)
first(simdf, 6)
```

	id	time	cp	dv	amt	evid	cmt	rate	Wt
	String	Float64	Float64?	Float64?	Float64	Int8	Int64?	Float64	Int64
1	1	0.0	<i>missing</i>	<i>missing</i>	100.0	1	1	0.0	74
2	1	0.0	0.0	0.0	0.0	0	<i>missing</i>	0.0	74
3	1	1.0	2136.14	1928.23	0.0	0	<i>missing</i>	0.0	74
4	1	2.0	2803.41	3018.93	0.0	0	<i>missing</i>	0.0	74
5	1	3.0	2977.33	3186.01	0.0	0	<i>missing</i>	0.0	74
6	1	4.0	2986.35	2872.35	0.0	0	<i>missing</i>	0.0	74

For the purpose of NCA, let us use the `cp` (output without residual error) as our observed value

To prepare the dataset for NCA analysis, let us use the `read_nca` function. The NCA datasets in Pumas requires a `route` specification which can either be `iv` or `ev`. Since this is an oral drug administration, lets add that to the `simdf`.

```
simdf[:, :route] .= "ev"
```

```
1776-element Array{String,1}:
```

```
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
⋮
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
"ev"
```

Next we can define time, concentration and dose units so the report includes the units for the pharmacokinetic parameters. The general syntax for units are `u` followed by the unit in quotes `"`.

```
timeu = u"hr"
concu = u"mg/L"
amtu = u"mg"
```

```
mg
```

```
nca_df = read_nca(simdf, id=:id, time=:time, conc=:cp, amt=:amt,
  route=:route, timeu=timeu, concu=concu, amtu=amtu, lloq=0.4concu)
```

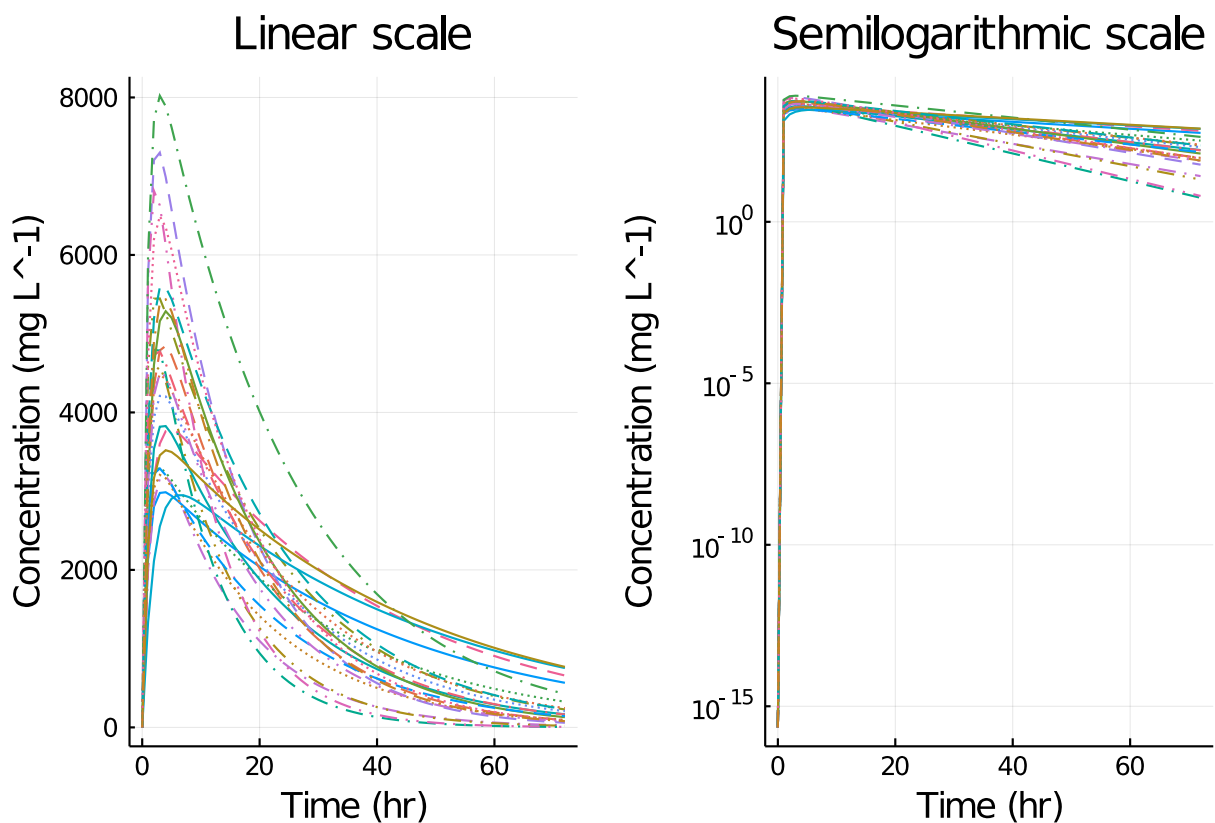
```
NCAPopulation (24 subjects):
```

```
ID: ["1", "2", "3", "4", "5", "6", "7", "8", "9", "10", "11", "12", "13",
```

```
"14", "15", "16", "17", "18", "19", "20", "21", "22", "23", "24"]
concentration: mg L-1
time:         hr
auc:          mg hr L-1
aumc:         mg hr2 L-1
λz:           hr-1
dose:         mg
```

You can view the concentration-time plots by doing

```
plot(ncadf)
```



You can then generate `cmax` and `auc` for each subject

```
auc = NCA.auc(ncadf)
```

	id	auc
	String	Quantit...
1	1	132198.0 mg hr L ⁻¹
2	2	102079.0 mg hr L ⁻¹
3	3	106989.0 mg hr L ⁻¹
4	4	57458.7 mg hr L ⁻¹
5	5	71282.8 mg hr L ⁻¹
6	6	96739.3 mg hr L ⁻¹
7	7	161621.0 mg hr L ⁻¹
8	8	72576.2 mg hr L ⁻¹
9	9	61923.5 mg hr L ⁻¹
10	10	132283.0 mg hr L ⁻¹
11	11	157841.0 mg hr L ⁻¹
12	12	124295.0 mg hr L ⁻¹
13	13	109570.0 mg hr L ⁻¹
14	14	110130.0 mg hr L ⁻¹
15	15	83332.2 mg hr L ⁻¹
16	16	118001.0 mg hr L ⁻¹
17	17	81171.9 mg hr L ⁻¹
18	18	119144.0 mg hr L ⁻¹
19	19	210948.0 mg hr L ⁻¹
20	20	90731.3 mg hr L ⁻¹
21	21	169402.0 mg hr L ⁻¹
22	22	139547.0 mg hr L ⁻¹
23	23	124435.0 mg hr L ⁻¹
24	24	108008.0 mg hr L ⁻¹

`cmax` = `NCA.cmax(ncadf)`

	id	cmax
	String	Quantit...
1	1	2986.35 mg L ⁻¹
2	2	4845.71 mg L ⁻¹
3	3	3300.26 mg L ⁻¹
4	4	3188.57 mg L ⁻¹
5	5	4587.95 mg L ⁻¹
6	6	3826.88 mg L ⁻¹
7	7	3786.89 mg L ⁻¹
8	8	3206.47 mg L ⁻¹
9	9	4795.85 mg L ⁻¹
10	10	5447.36 mg L ⁻¹
11	11	2948.35 mg L ⁻¹
12	12	7299.77 mg L ⁻¹
13	13	4210.48 mg L ⁻¹
14	14	4776.76 mg L ⁻¹
15	15	6813.03 mg L ⁻¹
16	16	5285.48 mg L ⁻¹
17	17	3288.68 mg L ⁻¹
18	18	4481.94 mg L ⁻¹
19	19	8022.22 mg L ⁻¹
20	20	4503.52 mg L ⁻¹
21	21	3520.06 mg L ⁻¹
22	22	5590.86 mg L ⁻¹
23	23	6493.77 mg L ⁻¹
24	24	5435.34 mg L ⁻¹

Or generate the entire NCA report using

```
report = NCAReport(ncadf)
first(report,6)
```

	id	doseamt	tlag	tmax	cmax	tlast	clast	clast_
	String	Quantit...	Quantit...	Quantit...	Quantit...	Quantit...	Quantit...	Quan
1	1	100.0 mg	0.0 hr	4.0 hr	2986.35 mg L ⁻¹	72.0 hr	566.15 mg L ⁻¹	566.267 r
2	2	100.0 mg	0.0 hr	4.0 hr	4845.71 mg L ⁻¹	72.0 hr	93.876 mg L ⁻¹	94.0492 r
3	3	100.0 mg	0.0 hr	3.0 hr	3300.26 mg L ⁻¹	72.0 hr	326.361 mg L ⁻¹	326.425 r
4	4	100.0 mg	0.0 hr	4.0 hr	3188.57 mg L ⁻¹	72.0 hr	26.0065 mg L ⁻¹	26.0723 r
5	5	100.0 mg	0.0 hr	3.0 hr	4587.95 mg L ⁻¹	72.0 hr	20.3659 mg L ⁻¹	20.3848 r
6	6	100.0 mg	0.0 hr	4.0 hr	3826.88 mg L ⁻¹	72.0 hr	166.316 mg L ⁻¹	166.438 r

3 Problem 3: Estimate using Non-linear mixed effects

We can use the simulated dataset in the Problem 1 for our estimation. We need a couple of data manipulation steps

1. missing `cmt` should be converted to 2 to reflect central compartment
2. data rows where `time` = 0, and `cp`=0 should be removed

```
simdf.cmt = ifelse(ismissing(simdf.cmt), 2, simdf.cmt)
est_df = simdf[!((simdf.dv == 0.0) & (simdf.cmt == 2)),:]
first(est_df, 6)
```

	id	time	cp	dv	amt	evid	cmt	rate	Wt	route
	String	Float64	Float64?	Float64?	Float64	Int8	Int64	Float64	Int64	String
1	1	0.0	<i>missing</i>	<i>missing</i>	100.0	1	1	0.0	74	ev
2	1	1.0	2136.14	1928.23	0.0	0	2	0.0	74	ev
3	1	2.0	2803.41	3018.93	0.0	0	2	0.0	74	ev
4	1	3.0	2977.33	3186.01	0.0	0	2	0.0	74	ev
5	1	4.0	2986.35	2872.35	0.0	0	2	0.0	74	ev
6	1	5.0	2941.06	2521.28	0.0	0	2	0.0	74	ev

3.1 Part 1: Read datasets for NLME estimation

We can use the `read_pumas` function to prepare the dataset for NLME estimation

```
data = read_pumas(est_df, covariates=[Wt], observations=[dv])
```

```
Population
Subjects: 24
Covariates: Wt
Observables: dv
```

where

- `covariates` is a symbol that maps to the columns of covariates
- `observations` is a symbol that maps to the columns of dependent variables
- since the dataframe has `time` as the variable, the function does not need a specific input

3.2 Part 2: Perform a model fit

We now use the

- `mymodel` model that we wrote earlier
- the set of parameters specified in `param` as initial estimates
- `data` that was read in using the `read_pumas` function

to fit the model.

```
res = fit(mymodel, data, param, Pumas.FOCEI())
```

```
Iter      Function value      Gradient norm
  0      1.134964e+04      1.928833e+01
* time: 4.100799560546875e-5
  1      1.134928e+04      3.577934e+01
* time: 0.13331985473632812
  2      1.134867e+04      2.016275e+01
```



```

* time: 0.22821497917175293
  3      1.134846e+04      1.467966e+01
* time: 0.3383779525756836
  4      1.134813e+04      2.651939e+00
* time: 0.40964698791503906
  5      1.134812e+04      2.339406e+00
* time: 0.48030900955200195
  6      1.134809e+04      1.934372e+00
* time: 0.5583829879760742
  7      1.134805e+04      3.034282e-01
* time: 0.6122348308563232
  8      1.134805e+04      2.558618e-01
* time: 0.661628007888794
  9      1.134804e+04      8.600182e-02
* time: 0.7146708965301514
 10      1.134804e+04      2.772043e-02
* time: 0.7851088047027588
 11      1.134804e+04      9.824259e-03
* time: 0.8478918075561523
 12      1.134804e+04      4.457464e-03
* time: 0.9215497970581055
 13      1.134804e+04      1.025930e-03
* time: 0.9732668399810791
 14      1.134804e+04      8.285445e-05
* time: 1.0309419631958008
FittedPumasModel

```

```
Successful minimization: true
```

```

Likelihood approximation: Pumas.FOCEI
Log-likelihood value: -11348.038
Number of subjects: 24
Number of parameters: Fixed Optimized
                      0      5
Observation records: Active Missing
dv: 1728 0
Total: 1728 0

```

```

-----
              Estimate
-----
tvcl      0.96606
tvv       20.124
tvka      0.89507
 $\Omega_{1,1}$  0.10253
 $\Omega_{2,2}$  0.077902
 $\Omega_{3,3}$  0.074778
 $\sigma_{prop}$  0.038981
-----

```

3.3 Part 3: Infer the results

infer provides the model inference

```
infer(res)
```

```

Calculating: variance-covariance matrix. Done.
Asymptotic inference results

```

```

Successful minimization:                true

Likelihood approximation:                Pumas.FOCEI
Log-likelihood value:                   -11348.038
Number of subjects:                     24
Number of parameters:                   Fixed    Optimized
                                         0        5
Observation records:                    Active    Missing
dv:                                     1728      0
Total:                                  1728      0

```

	Estimate	SE	95.0% C.I.
tvcl	0.96606	0.063144	[0.8423 ; 1.0898]
tvv	20.124	1.1628	[17.845 ; 22.403]
tvka	0.89507	0.066005	[0.7657 ; 1.0244]
$\Omega_{1,1}$	0.10253	0.026178	[0.05122 ; 0.15384]
$\Omega_{2,2}$	0.077902	0.020065	[0.038576 ; 0.11723]
$\Omega_{3,3}$	0.074778	0.04165	[-0.0068549; 0.15641]
σ_{prop}	0.038981	0.0015704	[0.035903 ; 0.042059]

3.4 Part 4: Inspect the results

inspect gives you the

- model predictions
- residuals
- Empirical Bayes estimates

```

preds = DataFrame(predict(res))
first(preds, 6)

```

	id	time	evid	dv	dv_pred	dv_ipred	Wt
	String	Float64	Int64	Float64	Float64	Float64	Int64
1	1	1.0	0	1928.23	2705.81	1956.5	74
2	1	2.0	0	3018.93	3686.23	2724.75	74
3	1	3.0	0	3186.01	3967.48	2997.53	74
4	1	4.0	0	2872.35	3968.57	3064.41	74
5	1	5.0	0	2521.28	3860.47	3046.41	74
6	1	6.0	0	3474.89	3712.77	2994.1	74

```

resids = DataFrame(wresiduals(res))
first(resids, 6)

```

	id	time	dv_wres	dv_iwres	wres_approx	Wt
	String	Float64	Float64	Float64	FOCEI...	Int64
1	1	1.0	-0.411365	-0.073188	FOCEI()	74
2	1	2.0	0.187917	0.546827	FOCEI()	74
3	1	3.0	-0.0281296	0.318467	FOCEI()	74
4	1	4.0	-0.642131	-0.317451	FOCEI()	74
5	1	5.0	-1.17404	-0.87309	FOCEI()	74
6	1	6.0	0.535575	0.813335	FOCEI()	74

```
ebes = DataFrame(empirical_bayes(res))
first(ebes, 6)
```

	Array...
1	[-0.290432, 0.320516, -0.0259105]
2	[0.151995, 0.00669468, -0.0850562]
3	[0.0315156, 0.407506, -0.0865642]
4	[0.688058, 0.303218, -0.362252]
5	[0.334693, -0.183283, 0.16122]
6	[0.0829534, 0.123602, -0.17294]

There is an `inspect` function that provides all the results at once

Note that this function below fails to convert into a dataframe due to a bug. Will be fixed soon

```
resout = DataFrame(inspect(res))
first(resout, 6)
```