Chapter 1

Introduction

1.1 RNA Secondary Structure Prediction

In the nucleus of a cell, RNA is constantly being synthesized by transcribing sections of DNA onto a portable chain. These RNAs serve several functions inside of the cell, including acting as:

mRNA: 'messanger RNA', which travel to ribosomes to serve as blueprints for proteins,

tRNA: 'transfer RNA', which bond to and transport amino acids to the ribosome to be formed into proteins,

rRNA: 'ribosomal RNA', which make up ribosomes,

ncRNAs 'non-coding RNAs', which are not involved in the manufacturing of proteins, instead being used as tools of the cell for tasks including the regulation of gene expression.

The last group, ncRNAs, comprises the majority of RNAs synthesized and have mostly unknown functions. It is unlikely that they just float around the cell uselessly,

rather they are the tools the cell uses to build and run itself. It is also widely believed that the function of a strand of RNA is directly related to its structure. While DNA is composed of 2 seperate strands woven together in a double helix, RNA is most often found as a single strand that folds back onto itself. There are considered to be 3 main levels of structure of RNA. The first, the primary structure, is the sequence of nucleic acids that make up the strand of RNA i.e. 'GACCUUGGGGCCCC...'. The second, the secondary structure, is how these bases fold back on each other and form base pairs, most often of the Watson and Crick variety ('G-C', 'A-U', although sometimes 'G-U' is possible as well). The third, the tertiary structure, is how the structure bends on a larger scale as the stems and loops formed by the secondary structure interact with each other.

Primary structure can be readily observed by modern sequencing technology, however it is the secondary structure that determines the shape of the molecule, which is the most important when considering interactions with other biological molecules. The full specification of a secondary structure includes a list of every pair that is made by 2 of the nucleic bases in the primary structure making a bond. Finding the secondary structure of an RNA molecule is a different task than finding the primary structure of RNA because there is no single solution for one chemical chain. For an individual RNA molecule there are many valid pairings, in fact for a sequence of length n there are $O(1.8^n)$ secondary structures [TODO: cite].

To find which of these structures the molecule is likely to assume in nature, we turn to statistical mechanics. We approximate the RNA molecule as an isolated system in contact with a thermal resevoir that is the cell, with each secondary structure as a state of that system. In such a system the probability of any state s is its boltzmann factor divided by the partition function:

$$P(s) = \frac{1}{Z} e^{-\beta E(s)}, \tag{1.1}$$

where $\beta = \frac{1}{RT}$, R is the gas constant, T is the temperature, and

$$Z = \sum_{s} e^{-\beta E(s)}. \tag{1.2}$$

Initially researchers were satisfied with presenting the MFE (minimum free energy) state as the state the molecule assumes in nature, after all this state is the most probable. However it has become clear that this analysis is unsufficient, as MFE structures still are not very probable. Statistical procedures, sampling the Boltzmann distribution, are a more modern tool for predicting the secondary structure found in nature.

1.2 The Energy Model of RNA

Computing the partition function and probabilities is impossible without an energy model for RNA, $E(s)$. Setting the energy of the single-stranded (no pair) state as $E = 0$, the energy model must accurately estimate an energy for a folded secondary structure. In chemical experiments, this can be measured by using a strand with an known secondary structure and finding it's ΔG by deducing it from the relative concentrations of single-stranded states to double-stranded states in solution (see UV melting section).

The first energy models developed by researchers awarded energy bonuses to pairs formed. One of the first papers by Nussinov and Jacobson (1980) awarded the same amount of points to A-U and G-C pairs and found the MFE state, so the algorithm reduced to finding the legal folding with the most base pairs. After, it was discovered exprimentally that G-C pairs are more stable than A-U pairs. Because of this, in further iterations the energy would be determined by counting hydrogen bonds of cannonically paired bases, assigning each -1 kcal/mol of free energy. This would mean that GC pairs are given -3 kcals/mol, AU and GU pairs are both given -2.

The algorithm developed for this model minimized the free energy. Both this algorithm and the previous one had elementary dynamic programming solutions. They were useful models to use as a baseline, however, even the second iteration was not very accurate, on average only 20.5% of known base pairs are correctly predicted. Later energy models would use it as a control for the hypothesis that they increased secondary structure prediction accuracy (Mathews et al 1999).

Indeed, much improvement was made over the hydrogen bond model by expanding it to include what is now called the Nearest Neighbor model. Experiments made it clear that energy of an RNA folding is not linearly dependent on the bonds that are made. There are significant interaction effects between nearby bases and bonds, this is called 'sequence dependence', and there are polymer physics based energy terms that scale logarithmically with the length of a loop (this can be thought of as the energy it takes to bend the strand). To handle these interaction effects in a model, we approximate that they are contained within loop regions. We divide our structure into its loops and compute the energy of each loop, with a seperate energy model for each.

1.2.1 UV Melting Experiments

The individual loop regions are given energies as parameters to linear regression models of free energy change in predictably folding strands. For example, the strand 'GGGAAACCC' folds predictably into a structure with all the G's paired to the C's and a 3-A hairpin turn (because G's pair very strongly to C's and A's tend to resist pairing). Large amounts of identical strands are synthesized and put into solution and heated. As the solution heats, there is enough ambient energy to put all the strands in the unfolded, no-bonds state. RNA is an organic, aromatic molecule that absobes light in the UV spectrum in different amounts depending on whether it is in a folded state or unfolded state, so the UV absobtion is fit to a curve that then

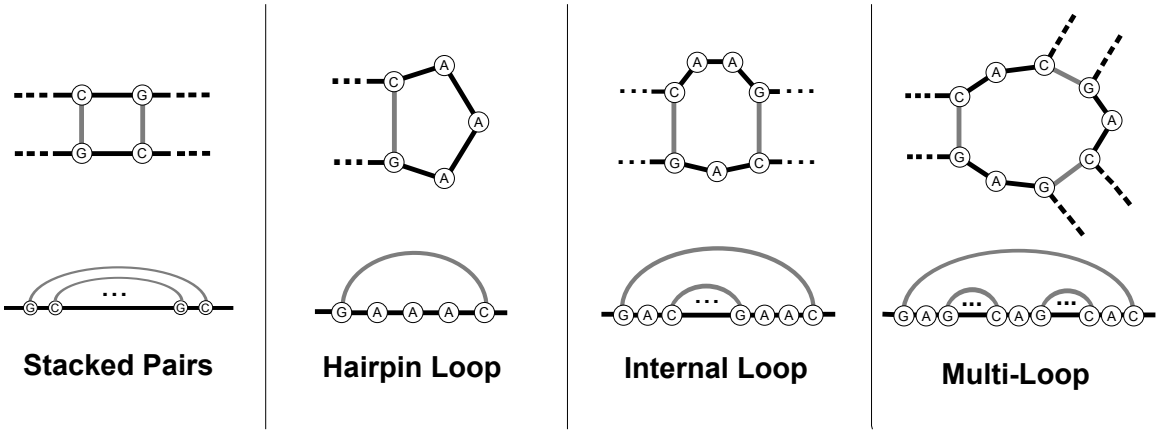

Figure 1-1: The 4 types of loops, black connections are bonds in the RNA backbone, grey connections are hydrogen bonds between bases. The types are: *Stacked Pairs*, adjacent pairs of bonded bases, *Hairpin Loops*, one bonding pair closing off a turn in the RNA backbone, *Internal Loops*, which can range from bulges to long loops, connecting to pairs with 2 chains of unpaired bases, and *Multi-Loops*, which connect 3 or more pairs.

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tells us about the relative concentrations of the single-stranded vs. double-stranded state, which in turn tells us about the free energy change between the two at a given temperature. This free energy change is extracted and treated as a function of the loop variables, which are then fitted to a linear model over experiments on many different such strands.

To continue with the example, we are creating a model:

[TODO: example energy figure]

$$\Delta G(GGGAAACCCC) = \Delta G_s \begin{pmatrix} 3'CC5' \\ 5'GG3' \end{pmatrix} + \Delta G_S \begin{pmatrix} 3'CC5' \\ 5'GG3' \end{pmatrix} + \Delta G_H(GAAAC) \tag{1.3}$$

Where ΔG_S is an individual parameter for the stack loop energy term and ΔG_H contains the terms for the hairpin energy term.

Briefly, the loop types are:

Stacked Pairs Two pairs right next to each other. The energies for each possible

legal pairing has been determined by linear regression on experimental data (see UV Melting Experiments). Finding an energy amounts to a table look-up of these regression coefficients.

$$\Delta G \begin{pmatrix} 5'GC3' \\ 3'CG5' \end{pmatrix} = -3.42 \text{ (from Xia et al 1998)} \tag{1.4}$$

Hairpin Loops One pair enclosing an empty loop region. The energy of this loop contains a term dependent on the length n, the sequence of the closing stack, and several bonus terms for special loops experimentally determined to be stable or unstable.

$$\begin{aligned} \Delta G_{Hairpin}(n > 3) = & \Delta G_{init}(n) + \Delta G(\text{closing stack}) \\ & + \Delta G_{bonus}(\text{UU or GA first mismatch, but not AG}) \\ & + \Delta G_{bonus}(\text{special GU closure}) \\ & + \Delta G_{penalty}(\text{oligo-C loops}) \\ & (\text{from Mathews et al 1999}) \end{aligned} \tag{1.5}$$

For example (with $\bar{A}$ meaning base A is unpaired):

$$\Delta G \begin{pmatrix} 5'G\bar{A}\bar{A}3' \\ 3'C\bar{A}\bar{A}5' \end{pmatrix} = \Delta \tag{1.6}$$

Internal Loops Two pairs connected by a loop. [TODO: add example]

Multi Loops Mutiple pairs, each with their own stems. This has a linear energy model, with an energy penalty for starting the loop, an energy term for each base pair, and one for each unpaired base.

1.3 UV Melting Experiments

The thermodynamic behavior of an RNA strand can be determined by subjecting it to melting curve analysis. When a folded RNA strand denatures, or unfolds because it is heated, its absorbtion of UV radiation changes. A physical model of this melting process can be developed to interpret these curves.

$$\Delta G = \Delta H + T\Delta S \tag{1.7}$$

$$T_M^{-1} = \frac{R}{\Delta H} \log\left(C_T/a\right) + \frac{\Delta S}{R} \tag{1.8}$$

The free energy of a loop structure, or rather its ΔG relative to the unfolded state,

Stacked Pairs The energy parameters for stacked pair loops were computed in a series of optical melting experiments (estimating parameters by UV absorbtion) by Xia et al (1998). For each combination of 2 sets of 2 paired bases, the change in energy at 37 Kelven was computed by fitting ΔH and ΔS to the data. [Todo: decide whether to have an in depth discussion of this]

For GU, a non-cannonical base pair that happens nontheless, the free energy is calculated by subtracting the free energy of a CGUACG strand from the free energy of a CGUUGACG strand, both of whose free energies are determined by optical melting experiments.

Dangling ends and terminal mismatches [TODO: read serra & turner 1995]

bases adjacent to GU pairs are treated the same as bases adjacent to AU pairs

Hairpin loops The energy function for a hairpin loop is a similar table lookup.

[TODO: finish this]

- Tetraloop bonus

Bulge loops

Internal loops - 2x2 tandem mismatches - 2x1 internal loops - 1x1 (single mismatch