

CSCI 5521: Machine Learning Fundamentals (Spring 2022)

Quiz 1 (Thursday, Feb 10)

Due on Gradescope at 02:00 PM, Friday, Feb 11

Instructions:

- This quiz has 3 questions, 30 points, on 1 page.
 - Please write your name & ID on your submission pages.
1. (6 points) Supervised learning has a wide range of applications. For example, one can define a robot (vs non-robot) based on a number of traits. Please model the question as a two-class classification task and answer the following questions.

- (a) Name two relevant features to this two-class classification task. (Any reasonable features are acceptable).
- (b) What are the labels in this two-class classification task?

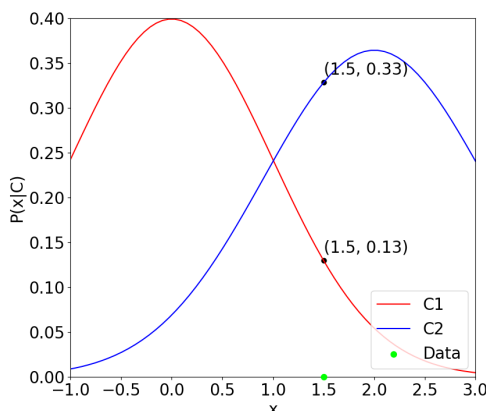
a) $x = \begin{bmatrix} \text{instructions received} \\ \text{actions performed in real world} \end{bmatrix}$ b) $r = \begin{cases} 1, & \text{if } x \text{ is positive (is robot)} \\ 0, & \text{if } x \text{ is negative (not robot)} \end{cases}$

2. (10 points) What could we do to reduce overfitting in a polynomial regression model? Select all the option(s) that apply.

- (a) Decrease polynomial degree. *100%*
- (b) Change to a more complex model (e.g., a model with more parameters). *overfitting?*
- (c) Add new training data and keep test data the same. *underfitting*
- (d) Add new test data and keep training data the same. *wouldn't it result in the same thing?*
- (e) Sample half of the original training data as new training data. *same generalization*

3. (14 points) The conditional probability density functions of two classes C_1 and C_2 are shown in the figure below, with $P(x|C_1) \sim \mathcal{N}(0, 1)$ and $P(x|C_2) \sim \mathcal{N}(2, 1.2)$.

- (a) Assuming the priors are equal, predict which class (C_1 or C_2) the data point $x = 1.5$ (illustrated with the green dot) belongs to. Briefly explain why.
- (b) What if the priors are $P(C_1) = 0.9$ and $P(C_2) = 0.1$, respectively? (Note: High-level explanation is good, but you can use formulations if it helps explain).



$$a) P(C_1) = 0.5, P(C_2) = 0.5, x = 1.5$$

$$P(x|C_1) = 0.13, P(x|C_2) = 0.33$$

$$P(C_1|x) = \frac{0.5 * 0.13}{0.5 * 0.13 + 0.5 * 0.33} = 0.283$$

$$P(C_2|x) = \frac{0.5 * 0.33}{0.5 * 0.13 + 0.5 * 0.33} = 0.717$$

$\therefore x = 1.5$ would most likely belong to C_2 .