Subject: ACS 597 - Module 1 Assignement

Date: January 31, 2025 (Submitted)

Problem 1 - Cut-on Frequencies in Ducts and Pipes

Problem 1a

The lowest cut-on frequency for a rectangular duct with air flow is given by equation,

$$f_{\text{cut-on}} = 0.5 \cdot \frac{c}{L} \tag{1}$$

where c is the speed of sound in air, 343 $\frac{m}{s}$, and L is the largest side of the rectangular cross-section.

With cross-sectional dimensions of $L_x=12~\mathrm{cm}$ and $L_y=20~\mathrm{cm}$, the lowest cut-on frequency for this rectangular duct is,

$$f_{
m cut-on} = 0.5 \cdot rac{343 \ rac{m}{s}}{0.20 \ m} =$$
857.5 Hz

Problem 1b

The lowest cut-on frequency for a circular duct with air flow with the same cross-sectional area as the rectangular duct in part (a.) can be calculated using equation,

$$f_{\text{cut-on}} = 0.568 \cdot \frac{c}{d} \tag{2}$$

where c is the speed of sound in air, 343 $\frac{m}{s}$, and d is diameter of the circular duct.

The cross-sectional area of the rectangular duct is,

Area
$$_{\text{rectangular duct}} = 0.12 \text{ m} \cdot 0.20 \text{ m} = 0.024 \text{ m}$$

The corresponding diameter for this area is,

diameter =
$$\sqrt{\frac{0.24 \text{ m}^2}{\pi}} \cdot 2 = 0.17 \text{ m}$$

Using Eq. 2, the lowest cut-on frequency for this circular duct with air flow is,

$$f_{\text{cut-on}} = 0.568 \cdot \frac{1,500 \frac{\text{m}}{\text{s}}}{0.17 \text{ m}} = 1,114.5 \text{ Hz}$$

Problem 1c

The lowest cut-on frequency for this circular duct with water flow can be calculated using Eq. 2,

$$f_{\rm cut-on} = 0.568 \cdot \frac{1,500 \frac{m}{s}}{0.17 \text{ m}} = 4,873.9 \text{ Hz}$$

The lowest cut-on frequency for water is considerable larger than it is for air flow.

Problem 1d

The speed of sound in air is calculated by,

$$c = \sqrt{\gamma \cdot R \cdot T_K} \tag{3}$$

where $\gamma=1.4$ is the ratio of specific heats, $R=287~\frac{J}{kg\cdot K}$ is the gas constant, and T_K is the absolute temperature in Kelvin.

Figure 1 illustrates how the lowest cut-on frequency changes as the air heats from 0° to 500° Celsius.

The square-root relationship between temperature and the speed of sound in air is apparent and governs the behaviour of the cut-on frequency.

Lowest Cut-on Frequency for a Circular Pipe with Air Flow Versus Air Temperature

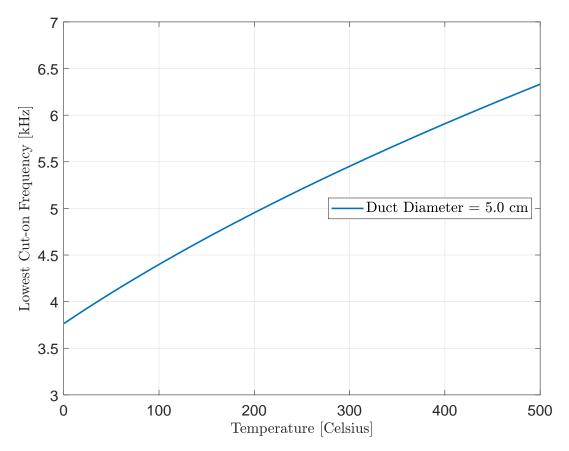


Figure 1: Lowest cut-on frequency for a circular 5 cm diameter duct versus air temperature.

Problem 1e

Question: Are cut-on frequencies higher for a circular or rectangular duct for a given cross-sectional area?

The lowest cut-on frequency is higher for a circular duct than for a rectangular duct for a given cross-sectional area.

For the dimensions given in class, the rectangular duct is not square. This produces a larger dimension and thus a smaller, lowest cut-on frequency. If the rectangular duct is square dimensions on the order of the circular duct diameter with the same cross-sectional area, the cut-on frequencies are approximately equal.

Question: What about in air versus water?

The lowest cut-on frequency is larger for water than for air. The cut-on frequency is proportional to the speed of sound and the speed of sound in water is greater than the speed of sound in air.

Question: What about cold versus hot air?

The lowest cut-on frequency is higher for warm air than it is for cold air.

Problem 2 - Muffler Design Comparison

$\label{eq:Assumptions:equation:assumptions:} Assumptions:$

No resistive terms (i.e., R_{A} is zero). No flow.

There is no damping in the system; resonances will be artificially high.

Problem 2a

Problem 2b

Problem 2c

Problem 3 - Bugle Recorder

Problem 3a

Problem 3b

Problem 4 - Intake Duct

Problem 4a

Problem 4b

Problem 4c

Problem 4d

Problem 5 - Intake Duct Silencer

Problem 5a
Problem 5b
Problem 5c
Problem 5d
Problem 5e

Appendix A: Matlab Code - Problem 1

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%% Synopsis
% Homework Set 1- Cut—on Frequencies in Ducts and Pipes
% Note: Send draft of report before submission for comments.
% Dimensions are annontated in the class notes.
% To Do
% Focus on interpretation.
% Environment
close all; clear; clc;
% restoredefaultpath;
% set( 0, 'DefaultFigurePosition', [ 400 400 900 400 ] ); % [ left bottom width
   height ]
set( 0, 'DefaultFigurePaperPositionMode', 'manual' );
set( 0, 'DefaultFigureWindowStyle', 'normal' );
set( 0, 'DefaultLineLineWidth', 1.5 );
set( 0, 'DefaultTextInterpreter', 'Latex' );
format ShortG;
pause(1);
PRINT_FIGURES = 0;
%% Define Values and Functions
c_{air} = 343; % The speed of sound in air in meters per second.
c_{water} = 1500; % The speed of sound in water in meters per second.
gamma = 1.4; % The ratio of specific heats [unitless].
R = 287; % The gas constant [Joules per ( kilogram * Kelvin)].
h_f_cut_on_rectangular_duct = @( c, L ) 0.5 .* c ./ L;
% c - The speed of sound.
% L - The largest cross—section dimension of the rectangular duct.
h_f_cut_on_circular_duct = @(c, d) 0.568 * c ./ d;
```

```
%
% c - The speec of sound.
% L - The diameter of the circular duct.
h_speed_of_sound_in_air = @( gamma, R, temperature_Kelvin) sqrt( gamma .* R .*
   temperature_Kelvin );
%% Problem 1a
% The cross—sectional dimensions for the rectangular duct are: Lx = 12 cm and Ly = 20
% The largest dimension is Ly = 20 cm or 0.2 m.
% The cut—on frequency is,
h_f_cut_on_rectangular_duct( c_air, 0.2 ); % 857.5 Hz (shown in class 858 Hz)
    fprintf( 1, '\n Problem 1a: The lowest cut—on frequency for the rectangular pipe
   with air is %3.1f Hz.\n', h_f_cut_on_rectangular_duct( c_air, 0.2 ) );
%% Problem 1b
% The cross—sectional dimensions for the rectangular duct are: Lx = 12 cm and Ly = 20
% The cross—sectional area of the rectangular duct is 12 cm * 20 cm = 240 cm^2 or 0.024
rectangular_duct_cross_sectional_area = 0.12 * 0.20; % 0.024 m^2
% The diameter of the circulat pipe is,
circular_duct_diameter = sqrt( 0.024 / pi ) * 2; % 0.17481 meters
% Check:
    % pi * ( circular_duct_diameter / 2 )^2 CHECKED
% The cut—on frequency for the circular duct is,
h_f_cut_on_circular_duct( c_air, circular_duct_diameter ); % 1,114.5 Hz
    fprintf( 1, '\n Problem 1b: The lowest cut—on frequency for the circular pipe (of
   equal area) with air is %3.1f Hz.\n', h_f_cut_on_circular_duct( c_air,
   circular_duct_diameter ) );
%% Problem 1c
% The cut—on frequency for the circular duct with water is,
h_f_cut_on_circular_duct( c_water, circular_duct_diameter ); % 4,873.9 Hz
    fprintf( 1, '\n Problem 1c: The lowest cut—on frequency for the circular pipe (of
   equal area) with water is %3.1f Hz.\n', h_f_cut_on_circular_duct( c_water,
```

```
% The cut—on frequency should be higher because it is proportional to the
% speed of sound in a given medium.
%% Problem 1d
fprintf( 1, '\n Problem 1d: See the figure.\n' );
temperature_range_celsius = 0:0.1:500; % Celsius
    temperature_range_kelvin = temperature_range_celsius + 273.15; % Kelvin
FONT_SIZE = 14:
figure(); ...
    plot( temperature_range_celsius, h_f_cut_on_circular_duct( h_speed_of_sound_in_air(
   gamma, R, temperature_range_kelvin ), 0.05 ) ./ le3 ); grid on;
        legend( 'Duct Diameter = 5.0 cm', 'Location', 'East', 'FontSize', FONT_SIZE, '
   Interpreter', 'Latex' );
        set( gca, 'FontSize', FONT_SIZE );
   xlabel( 'Temperature [Celsius]', 'FontSize', FONT_SIZE );
       % xl = get( gca, 'xlabel' ); pxl = get( xl, 'position' ); pxl( 2 ) = 1.1 *
   pxl(2);
             set( xl, 'position', pxl );
    ylabel( 'Lowest Cut—on Frequency [kHz]', 'FontSize', FONT_SIZE );
       % yl = get(gca, 'ylabel'); pyl = get(yl, 'position'); pyl(1) = 1.2 * pyl
   (1);
             set( yl, 'position', pyl );
    caption = sprintf( 'Lowest Cut—on Frequency for a Circular Pipe with Air Flow Versus
    Air Temperature\n' );
       title( caption, 'FontSize', FONT_SIZE );
   ylim([3 7]);
% if ( PRINT_FIGURES == 1 )
     saveas( gcf, 'Cut—on Frequency Versus Temperature — Sunday, January 19, 2025.pdf'
   );
% end
```

%% Problem 1e

circular_duct_diameter));

fprintf(1, '\n Problem 1e: See Section Problem 1e of the Matlab script for the answers
 .\n\n');

```
% Clean-up

if ( ~isempty( findobj( 'Type', 'figure' ) ) )
    monitors = get( 0, 'MonitorPositions' );
    if ( size( monitors, 1 ) == 1 )
        autoArrangeFigures( 2, 2, 1 );
    elseif ( 1 < size( monitors, 1 ) )
        autoArrangeFigures( 2, 2, 1 );
    end

end

if ( PRINT_FIGURES == 1 )
    saveas( gcf, 'Cut—on Frequency Versus Temperature — Sunday, January 19, 2025.pdf' );
end

fprintf( 1, '\n\n\n*** Processing Complete ***\n\n\n' );</pre>
```

% Reference(s)