

Predicting Abalone Age Through Ridge Regression

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Revised: December 2015

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Introduction

There are a number of packages in R, Python, and other languages that can perform linear regression analysis (LRA) on a given dataset. While the use of these packages saves a data scientist or analysis quite a bit of time, it is important to do these from scratch every now and then to reenforce the concepts behind this most fundamental of machine learning algorithms. By doing so, we deepen our intuitions that allow us to make better use of the available tools.

In this project, an LRA was performed on a dataset of characteristics (features) related to the number of abalone rings which was treated as the independent or response variable. This analysis was performed in two ways. First, it was done “from scratch” using nothing but base R language constructs such as matrix operations. Second, the analysis is duplicate used the caret package.

The analysis starts with a quick exploratory data analysis (EDA) which begins with standardizing the independent variables (features) before constructing a matrix of scatter plots in order to gain a high level

understanding of the relationships between feature pairs. The features analyzed were: Sex (Male, Female, or Infant), Length, Diameter, Height, Whole weight, Shucked weight, Viscera weight, and Shell weight.

Following the pairs plot, the construction of the linear model was initiated by randomly partitioning the data into training and test sets. Following the data partitioning, the coefficients for the linear model were calculated for various ridge regression parameters (λ) on the training set. The λ which minimized the root mean square error (RMSE) was determined and then used in the model to make some predictions.

The parameters for the optimized linear model was as follows: [put table output here]

The optimized ridge regression parameter λ was found to be 0.8. The mean and the std dev columns above were used in the standardization which will be explained in detail later.

Background Information

What are Abalone?

Abalone are marine snails. Abalone shells have a low and open spiral structure, and are characterized by several respiratory holes in a row near the shell's outer edge. The innermost layer of the shell is composed of nacre or mother-of-pearl, which in many species is highly iridescent, giving rise to a range of strong and changeable colors which make them attractive to humans as decorative objects [1].

The abalone of the Northwest's Puget Sound are a delicacy in Asia, prized for their meat and beautiful shell. As a result they were poached nearly to extinction in the early 1990s, but with a little help from scientists, the wild abalone is slowly recovering [2].

Why Model Rings

Rings in abalone correspond to their age, similar to rings in trees. The age of abalone would be of interest to marine biologists as well as abalone farmers for a variety of reasons. Although other methods exist [3], the method described on the data repository page for determining the age of abalone involves cutting the shell through the cone, staining it, and counting the number of rings through a microscope which is a destructive and time-consuming task [4].

In order to make the task of predicting age faster and easier, other measurements, which are easier to obtain, were investigated to predict the age [4].

Data Preparation

Reading the Data

The data was first obtained from the UCI repository[4] and then read into R by running:

```
abalone <- read.table("abalone.data", sep=',')
```

When running this command, one must make sure that the working directory is set to the same directory where the data file resides.

Converting Catagorical Data

The first column of the original data [4] was labeled **Sex** and was populated with the categorical values **M**, **F**, and **I** corresponding to males, females and infants respectively. In facilitate inclusion of the **Sex** variable in the model, these categorical values were converted to numerical values. This was doneby replacing the original colun with two new columns. The first new column was labeled **M** for male and the second was labeled **F** for female. Males were deignated by putting a 1 in the **M** column and a 0 in the **F** column. Females were designated by putting a 0 in the **M** column and a 1 in teh **F** column. Infants were designated by a 0 in both the **M** and **F** columns.

The following code was used to convert the **Sex** (V1) column:

```
convertSex <- function(data.df = abalone) {  
  library(dplyr)  
  male <- (data.df[, 1] == 'M') * 1  
  female <- (data.df[, 1] == 'F') * 1  
  converted <- cbind(male, female, data.df[, 2:length(data.df)])  
  
  return(converted)  
}
```

Data Partitioning

As is standard practice, the model was constructed using randomly selected portions of the dataset. The portion used to create the model is referred to as the *training set* while the remaining portion which is used to test and validate predictions is referred to as the *testing set*.

During the analysis, many iterations based on different randomly selected training and test sets had to be constructed. The following two R functions were frequently called to accomplish this task:

```
# Returns a randomly selected subset of rows from the original input dataframe.  
# orig - original (complete) dataset (dataframe), assumed that samples  
#       are stored in rows of a 2-D table  
# fraction - fraction of the original dataset used for training  
# randomSeed - integer used to set the seed for the random number generator  
trainSetRows <- function(orig, fraction, randomSeed) {  
  set.seed(randomSeed)  
  randorder <- sample(nrow(orig)) # create set of randomly selected rows  
  nTrain <- round(nrow(orig)*fraction) # calc # of rows in training set  
  trainRows <- randorder[1:nTrain] # 1st nTrain rows in rand order  
  trainRows  
}  
  
# Returns a vector of integers corresponding to row numbers of the test set  
# allRows - a vector containing all the row numbers in the data table  
# trainRows - the vector of training rows returned from the trainSetRows function  
testSetRows <- function(allRows, trainRows) {  
  testRows <- setdiff(allRows, trainRows) # take away train rows leaves test rows  
  testRows  
}
```

Regressions Analysis

The Linear Model

Definition of the Linear Model

The model used to describe the data is as follows:

$$(1) R = w_0 + \sum_{i=1}^9 w_i x_i$$

In equation (1), R is the number of rings the abalone has, the w 's are the weights (our fitted parameters) and the x_i 's are the independent variables. The independent variables can be described as: $x_1 = M$, $x_2 = F$, $x_3 = \text{Length}$, $x_4 = \text{Diameter}$, $x_5 = \text{Height}$, $x_6 = \text{Whole weight}$, $x_7 = \text{Shucked weight}$, $x_8 = \text{Viscera weight}$, and $x_9 = \text{Shell weight}$.

λ Parameterization

The goal was to fit the w vector described in (1), in such a way as to minimize the residual sum of squares (RSS) parameterized by the ridge regression factor λ . Since minimizing a constant times RSS is the same as minimizing RSS, the error which we want to minimize can be written in matrix form as:

$$(2) \frac{1}{2} RSS = \frac{1}{2} \sum_{i=1}^9 (t_n - \mathbf{w}^T \mathbf{x}_i)^2 + \frac{1}{2} \lambda \mathbf{w}^T \mathbf{w}$$

where t_n are known target values and the constant $\frac{1}{2}$ has been multiplied by both sides to make the result of differentiation cleaner. Taking the gradient of (2), setting it equal to zero, and solving for the vector \mathbf{w} , yields the following solution in matrix notation:

$$(3) \mathbf{w} = (\lambda + \mathbf{X}_T^T \mathbf{X})^{-1} \mathbf{X}_T^T \mathbf{T}$$

The matrices \mathbf{X} and \mathbf{T} are the independent and dependent (target) variables respectively.

Experiments

Results

A Personal Curiosity: Bias and Training Partition

Discussion

References

- [1] Wikipedia - <https://en.wikipedia.org/wiki/Abalone>
- [2] Living On Earth - <http://loe.org/shows/segments.html?programID=15-P13-00031&segmentID=3>
- [3] Stable oxygen method - http://www.researchgate.net/profile/Craig_Mundy/publication/201169638_Determining_age_and_growth_of_abalone_using_stable_oxygen_isotopes_a_tool_for_fisheries_management
- [4] UCI data repository (data source) - <https://archive.ics.uci.edu/ml/datasets/Abalone>
- [9] Rings not annual - <http://www.publish.csiro.au/?paper=MF9921215>