ADEPT fast automatic differentiation library for C++: User guide

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1 Introduction

Adept (Automatic Differentiation using Expression Templates) is a software library that enables algorithms written in C and C++ to be automatically differentiated. It uses an operator overloading approach, so very little code modification is required. Differentiation can be performed in forward mode (the "tangent-linear" computation), reverse mode (the "adjoint" computation), or the full Jacobian matrix can be computed. This behaviour is common to several other libraries, namely ADOL-C (Griewank et al., 1996), CppAD (Bell, 2007) and Sacado (Gay, 2005), but the use of expression templates, an efficient way to store the differential information and several other optimizations mean that reverse-mode differentiation tends to be significantly faster and use less memory. In fact, *Adept* is also usually only a little slower than an adjoint code you might write by hand, but immeasurably faster in terms of user time; adjoint coding is very time consuming and error-prone. For technical details of how it works and benchmark results, see Hogan (2013).

This user guide describes how to apply the *Adept* software library to your code, and many of the examples map on to those in the test directory of the *Adept* software package. Section 2 describes the functionality that the library provides. Section 3 outlines how to install it on your system and how to compile your own code to use it. Section 4 describes how to prepare your code for automatic differentiation, and section 5 describes how to perform forward- and reverse-mode automatic differentiation on this code. Section 6 describes how to compute Jacobian

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matrices. Section 7 provides a detailed description of how to interface an algorithm implemented using *Adept* with a third-party minimization library. Section 8 describes how to call a function both with and without automatic differentiation from within the same program. Section 9 describes how to interface to software modules that compute their own Jacobians. Section 10 provides some tips for getting the best performance from *Adept*. Section 11 describes the user-oriented member functions of the Stack class that contains the differential information and section 12 describes the member functions of the "active" double-precision type adouble. Section 13 describes the exceptions that can be thrown by some *Adept* functions. Section 14 describes how to configure the behaviour of *Adept* by defining certain preprocessor variables. Finally, section 16 describes the license terms.

2 What functionality does *Adept* provide?

Adept provides the following functionality:

Full Jacobian matrix Given the non-linear function $\mathbf{y} = f(\mathbf{x})$ relating vector \mathbf{y} to vector \mathbf{x} coded in C or C++, after a little code modification Adept can compute the Jacobian matrix $\mathbf{H} = \partial \mathbf{y}/\mathbf{x}$, where the element at row i and column j of \mathbf{H} is $H_{i,j} = \partial y_i/\partial x_j$. This matrix will be computed much more rapidly and accurately than if you simply recompute the function multiple times, each time perturbing a different element of \mathbf{x} by a small amount. The Jacobian matrix is used in the Gauss-Newton and Levenberg-Marquardt minimization algorithms.

Reverse-mode differentiation This is a key component in optimization problems where a non-linear function needs to be minimized but the state vector \mathbf{x} is too large for it to make sense to compute the full Jacobian matrix. Atmospheric data assimilation is the canonical example in the field of meteorology. Given a nonlinear function $J(\mathbf{x})$ relating the scalar to be minimized J to vector \mathbf{x} , Adept will compute the vector of adjoints $\partial J/\partial \mathbf{x}$. Moreover, for a component of the code that may be expressed as a multi-dimensional non-linear function $\mathbf{y} = f(\mathbf{x})$, Adept can compute $\partial J/\partial \mathbf{x}$ if it is provided with the vector of input adjoints $\partial J/\partial \mathbf{y}$. In this case, $\partial J/\partial \mathbf{x}$ is equal to the matrix-vector product $\mathbf{H}^T \partial J/\partial \mathbf{y}$, but it is computed here without computing the full Jacobian matrix \mathbf{H} . The vector $\partial J/\partial \mathbf{x}$ may then be used in a quasi-Newton minimization scheme (e.g., Liu and Nocedal, 1989).

Forward-mode differentiation Given the non-linear function $\mathbf{y} = f(\mathbf{x})$ and a vector of perturbations $\delta \mathbf{x}$, Adept will compute the corresponding vector $\delta \mathbf{y}$ arising from a linearization of the function f. Formally, $\delta \mathbf{y}$ is equal to the matrix-vector product $\mathbf{H}\delta \mathbf{x}$, but it is computed here without computing the full Jacobian matrix \mathbf{H} . Note that Adept is designed for the reverse case, so might not be as fast or economical in memory in the forward mode as libraries written especially for that purpose (although Hogan, 2013, showed that it was competitive).

Adept can currently automatically differentiate the standard mathematical operators +, -, * and /, as well as their assignment versions +=, -=, *= and /=. It supports the mathematical functions sqrt, exp, log, log10, sin, cos, tan, asin, acos, atan, sinh, cosh, tanh, abs and pow. The "active" variables can take part in comparison operations ==, !=, >, <, >= and <=, as well as the diagnostic functions isfinite, isinf and isnan.

Note that at present *Adept* is missing some functionality that you may require:

- Differentiation is first-order only: it cannot directly compute higher-order derivatives such as the Hessian matrix.
- It has limited support for complex numbers; no support for mathematical functions of complex numbers, and expressions involving operations (addition, subtraction, multiplication and division) on complex numbers are not optimized.
- All code to be differentiated in a single program must use the same precision. By default this is double precision, although the library may be recompiled to use single precision or quadruple precision (the latter only if supported by your compiler).
- Your code should operate on variables individually: they can be stored in C-style arrays or std::vector types, but if you use containers that allow operations on entire arrays, such as the std::valarray type, then

some array-wise functionality (such as mathematical functions applied to the whole array and multiplying an array of active variables by an ordinary non-active scalar) will not work.

• It can be applied to C and C++ only; *Adept* could not be written in Fortran since the language provides no template capability.

It is hoped that future versions will remedy these limitations (and it is hoped that a future version of Fortran will support templates).

3 Installing Adept and compiling your own code to use it

The code has been tested on Linux with the GNU C++ compiler, but should compile on any Unix-like system with a C++98 compliant compiler. On a Unix-like system, do the following:

- 1. Unpack the package (tar xvfz adept-1.x.tar.gz on Linux) and cd to the directory adept-1.x (where x is the number of the most recent subversion).
- 2. Compile the code by typing make. You may need to configure a few things first, such as the compiler, by editing the Makefile_include file first. See also section 14 for ways to configure the behaviour of *Adept*.
- 3. This will create the static library lib/libadept.a. To copy this and the include file include/adept.h into/usr/local, use su to log-in as the superuser and type make install. To first specify another install directory, edit the PREFIX variable in Makefile.

To compile source files that use the *Adept* library, you need to make sure that adept.h is in your include path. If this file is located in a directory that is not in the default include path, add something like <code>-I/home/fred/include</code> to the compiler command line. At the linking stage, add <code>-ladept</code> to the command line to tell the linker to look for the <code>libadept.a</code> static library. If this file is in a non-standard location, also add something like <code>-L/home/fred/lib</code> before the <code>-ladept</code> argument to specify its location. Section 8.2 provdes an example Makefile for compiling code that uses the *Adept* library.

4 Code preparation

If you have used ADOL-C, CppAD or Sacado then you will already be familiar with what is involved in applying an operator-overloading automatic differentiation package to your code. The user interface to *Adept* differs from these only in the detail. It is assumed that you have an algorithm written in C or C++ that you wish to differentiate. This section deals with the modifications needed to your code, while section 5 describes the small additional amount of code you need to write to differentiate it.

In all source files containing code to be differentiated, you need to include the adept.h header file and import the adouble type from the adept namespace. Assuming your code uses double precision, you then search and replace double with the "active" equivalent adouble, but doing this only for those variables whose values depend on the independent input variables. If you wish to use a different precision, or to enable your code to be easily recompiled to use different precisions, then you may alternatively use the generic Real type from the adept namespace with its active equivalent aReal. Section 14 describes how to configure these types to represent single, double or quadruple precision, but be aware that accumulation of round-off error can make the accuracy of derivatives computed using single precision insufficient for minimization algorithms. For now we consider only double precision.

Consider the following contrived algorithm from Hogan (2013) that takes two inputs and returns one output:

```
double algorithm(const double x[2]) {
  double y = 4.0;
  double s = 2.0*x[0] + 3.0*x[1]*x[1];
  y *= sin(s);
  return y;
}
```

The modified code would look like this:

```
#include "adept.h"
using adept::adouble;

adouble algorithm(const adouble x[2]) {
   adouble y = 4.0;
   adouble s = 2.0*x[0] + 3.0*x[1]*x[1];
   y *= sin(s);
   return y;
}
```

Changes like this need to be done in all source files that form part of an algorithm to be differentiated.

If you need to access the real number underlying an adouble variable a, for example in order to use it as an argument to the fprintf function, then use a.value() or adept::value(a). Any mathematical operations performed on this real number will not be differentiated.

You may use adouble as the template argument of a Standard Template Library (STL) vector type (i.e. std::vector<adouble>), or indeed any container where you access individual elements one by one. For types allowing mathematical operations on the whole object, such as the STL complex and valarray types, you will find that although you can multiply one std::complex<adouble> or std::valarray<adouble> object by another, mathematical functions (exp, sin etc.) will not work when applied to whole objects, and neither will some simple operations such as multiplying these types by an ordinary (non-active) double variable. Moreover, the performance is not great because expressions cannot be fully optimized when in these containers. It is expected that a future version of *Adept* will include its own complex and vector types that overcome these limitations.

5 Applying reverse-mode differentiation

Suppose you wanted to create a version of algorithm that returned not only the result but also the gradient of the result with respect to its inputs, you would do this:

```
#include "adept.h"
double algorithm and gradient(
                 const double x_val[2], // Input values
                 double dy_dx[2]) {      // Output gradients
 adept::Stack stack,
                                     // Where the derivative information is stored
 using adept::adouble;
                                     // Import adouble from adept
 stack.new_recording();
                                     // Start recording
                                     // Call version overloaded for adouble args
 adouble y = algorithm(x);
 y.set_gradient(1.0);
                                     // Defines y as the objective function
 stack.compute_adjoint();
                                     // Run the adjoint algorithm
 dy_dx[0] = x[0].get_gradient();
                                     // Store the first gradient
 dy_dx[1] = x[1].get_gradient();
                                     // Store the second gradient
 return y.value();
                                      // Return the result of the simple computation
```

The component parts of this function are in a specific order, and if this order is violated then the code will not run correctly.

5.1 Set-up stack to record derivative information

```
adept::Stack stack;
```

The Stack object is where the differential version of the algorithm will be stored. When initialized, it makes itself accessible to subsequent statements via a global variable, but using thread-local storage to ensure thread safety. It must be initialized before the first adouble object is instantiated, because such an instantiation registers the adouble object with the currently active stack. Otherwise the code will crash with a segmentation fault.

In the example here, the Stack object is local to the scope of the function. If another Stack object had been initialized by the calling function and so was active at the point of entry to the function, then the local Stack object would throw an adept::stack_already_active exception (see Test 3 described at test/README in the *Adept* package if you want to use multiple Stack objects in the same program). A disadvantage of local Stack

objects is that the memory it uses must be reallocated each time the function is called. This can be overcome in several ways:

- Declare the Stack object to be static, which means that it will persist between function calls. This has the disadvantage that you won't be able to use other Stack objects in the program without deactivating this one first (see Test 3 in the *Adept* package, referred to above, for how to do this).
- Initialize Stack in the main body of the program and pass a reference to it to the algorithm_and_gradient function, so that it does not go out of scope between calls.
- Put it in a class so that it is accessible to member functions; this approach is demonstrated in section 7.

5.2 Initialize independent variables and start recording

```
adouble x[2] = {x_val[0], x_val[1]};
stack.new_recording();
```

The first line here simply copies the input values to the algorithm into adouble variables. These are the *inde*pendent variables, but note that there is no obligation for these to be stored as one array (as in CppAD), and for forward- and reverse-mode automatic differentiation you do not need to tell *Adept* explicitly via a function call which variables are the independent ones. The next line clears all differential statements from the stack so that it is ready for a new recording of differential information.

Note that the first line here actually stores two differential statements, $\delta x[0]=0$ and $\delta x[1]=0$, which are immediately cleared by the new_recording function call. To avoid the small overhead of storing redundant information on the stack, we could replace the first line with

```
x[0].set_value(x_val[0]);
x[1].set_value(x_val[1]);
or
adept::set_values(x, 2, x_val);
```

which have the effect of setting the values of x without storing the equivalent differential statements.

Users of *Adept* version 0.9 should note that the new_recording function replaces the start function call, which had to be put *before* the independent variables were initialized. The problem with this was that the independent variables had to be initialized with the set_value or set_values functions, otherwise the gradients coming out of the automatic differentiation would all be zero. Since it was easy to forget this, new_recording was introduced to allow the independent variables to be assigned in the normal way using the assignment operator (=). But don't just replace start in your version-0.9-compatible code with new_recording; the latter must appear *after* the independent variables have been initialized.

5.3 Perform calculations to be differentiated

```
adouble y = algorithm(x);
```

The algorithm is called, and behind the scenes the equivalent differential statement for every mathematical statement is stored in the stack. The result of the forward calculation is stored in y, known as a dependent variable. This example has one dependent variable, but any number is allowed, and they could be returned in another way, e.g. by passing a non-constant array to algorithm that is filled with the final values when the function returns.

5.4 Perform reverse-mode differentiation

```
y.set_gradient(1.0);
stack.compute_adjoint();
```

The first line sets the initial gradient (or adjoint) of y. In this example, we want the output gradients to be the derivatives of y with respect to each of the independent variables; to achieve this, the initial gradient of y must be unity.

More generally, if y was only an intermediate value in the computation of objective function J, then for the outputs of the function to be the derivatives of J with respect to each of the independent variables, we would need to set the gradient of y to $\partial J/\partial y$. In the case of multiple intermediate values, a separate call to set_gradient is needed for each intermediate value. If y was an array of length n then the gradient of each element could be set to the values in a double array y_ad using

```
adept::set_gradients(y, n, y_ad);
```

The compute_adjoint() member function of stack performs the adjoint calculation, sweeping in reverse through the differential statements stored on the stack. Note that this must be preceded by at least one set_gradient or set_gradients call, since the first such call initializes the list of gradients for compute_adjoint() to act on. Otherwise, compute_adjoint() will throw a gradients_not_initialized exception.

5.5 Extract the final gradients

```
dy_dx[0] = x[0].get_gradient();
dy_dx[1] = x[1].get_gradient();
```

These lines simply extract the gradients of the objective function with respect to the two independent variables. Alternatively we could have extracted them simultaneously using

```
adept::get_gradients(x, 2, dy_dx);
```

To do forward-mode differentiation in this example would involve setting the initial gradients of x instead of y, calling the member function compute_tangent_linear() instead of compute_adjoint(), and extracting the final gradients from y instead of x.

6 Computing Jacobian matrices

Until now we have considered a function with two inputs and one output. Consider the following more general function whose declaration is

```
void algorithm2(int n, const adouble* x, int m, adouble* y);
```

where x points to the n independent (input) variables and y points to the m dependent (output) variables. The following function would return the full Jacobian matrix:

```
#include <vector>
#include "adept.h"
void algorithm2_jacobian(
                  // Number of output values
                  int m,
                  double* y_val,
                                      // Output values
                  double* jac) {
                                      // Output Jacobian matrix
                                      // Import Stack and adouble from adept
 using adept::adouble;
                                      // Where the derivative information is stored
 adept::Stack stack;
                                      // Vector of active input variables
 std::vector<adouble> x(n);
 adept::set_values(&x[0], n, x_val);
                                       // Initialize adouble inputs
                                       // Start recording
 adept.new recording();
 std::vector<adouble> y(m);
                                       // Create vector of active output variables
 algorithm2(n, &x[0], m, &y[0]);
                                      // Run algorithm
 stack.independent(&x[0], n);
                                       // Identify independent variables
 stack.dependent(&y[0], m);
                                       // Identify dependent variables
 stack.jacobian(jac);
                                       // Compute & store Jacobian in jac
```

Note that:

• The independent member function of stack is used to identify the independent variables, i.e. the variables that the derivatives in the Jacobian matrix will be with respect to. In this example there are n independent variables located together in memory and so can be identified all at once. Multiple calls are possible to identify further independent variables. To identify a single independent variable, call independent with just one argument, the independent variable (not as a pointer).

- The dependent member function of stack identifies the dependent variables, and its usage is identical to independent.
- The memory provided to store the Jacobian matrix (pointed to by jac) must be a one-dimensional array of size m×n, where m is the number of dependent variables and n is the number of independent variables.
- The resulting matrix is stored in the sense of the index representing the dependent variables varying fastest (column-major order). To get row-major order, call the jacobian function with a second argument of true (see section 11).
- Internally, the Jacobian calculation is performed by multiple forward or reverse passes, whichever would be faster (dependent on the numbers of independent and dependent variables).
- The use of std::vector<adouble> rather than new adouble[n] ensures no memory leaks in the case of an exception being thrown, since the memory associated with x and y will be automatically deallocated when they go out of scope.

7 Real-world usage: interfacing Adept to a minimization library

Suppose we want to find the vector \mathbf{x} that minimizes a cost function $J(\mathbf{x})$ that consists of a large algorithm coded using the Adept library and encapsulated within a C++ class. In this section we illustrate how it may be interfaced to a third-party minimization algorithm with a C-style interface, specifically the free one in the GNU Scientific Library. The full working version of this example, using the N-dimensional Rosenbrock banana function as the function to be minimized, is "Test 4" in the test directory of the Adept software package. The interface to the algorithm is as follows:

```
#include <vector>
#include "adept.h"
using adept::adouble;
class State {
 public:
   // Construct a state with n state variables
   State(int n) { active_x_.resize(n); x_.resize(n); }
   // Minimize the function, returning true if minimization successful, false otherwise
   bool minimize();
   // Get copy of state variables after minimization
   void x(std::vector<double>& x_out) const;
   // For input state variables x, compute the function J(x) and return it
   double calc_function_value(const double* x);
   // For input state variables x, compute function and put its gradient in dJ_dx
   double calc_function_value_and_gradient(const double* x, double* dJ_dx);
   // Return the size of the state vector
   unsigned int nx() const { return active_x_.size(); }
 protected:
   // Active version: the algorithm is contained in the definition of this function
   adouble calc_function_value(const adouble* x);
   // DATA
   adept::Stack stack ;
                                    // Adept stack object
   std::vector<adouble> active_x_; // Active state variables
};
```

The algorithm itself is contained in the definition of calc_function_value(const adouble*), which is implemented using adouble variables (following the rules in section 4). However, the public interface to the class uses only standard double types, so the use of *Adept* is hidden to users of the class. Of course, a complicated algorithm may be implemented in terms of multiple classes that do exchange data via adouble objects. We will be using a quasi-Newton minimization algorithm that calls the algorithm many times with trial vectors \mathbf{x} , and for each call may request not only the value of the function, but also its gradient with respect to \mathbf{x} . Thus the public interface provides calc_function_value(const double*) and calc_function_value_and_gradient, which could be implemented as follows:

```
double State::calc_function_value(const double* x) {
  for (unsigned int i = 0; i < nx(); ++i) active_x_[i] = x[i];
  stack_.new_recording();
  return value(calc_function_value(&active_x_[0]));
}

double State::calc_function_value_and_gradient(const double* x, double* dJ_dx) {
  for (unsigned int i = 0; i < nx(); ++i) active_x_[i] = x[i];
  stack_.new_recording();
  adouble J = calc_function_value(&active_x_[0]);
  J.set_gradient(1.0);
  stack_.compute_adjoint();
  adept::get_gradients(&active_x_[0], nx(), dJ_dx);
  return value(J);
}</pre>
```

The first function simply copies the double inputs into an adouble vector and runs the version of calc_function_value for adouble arguments. Obviously there is an inefficiency here in that gradients are recorded that are then not used, and this function would be typically 2.5–3 times slower than an implementation of the algorithm that did not store gradients. Section 8 describes two ways to overcome this problem. The second function above implements reverse-mode automatic differentiation as described in section 5.

The minimize member function could be implemented using GSL as follows:

```
#include <iostream>
#include <gsl/gsl_multimin.h>
bool State::minimize() {
  // Minimizer settings
  const double initial_step_size = 0.01;
  const double line_search_tolerance = 1.0e-4;
  const double converged_gradient_norm = 1.0e-3;
  // Use the "limited-memory BFGS" quasi-Newton minimizer
  const gsl_multimin_fdfminimizer_type* minimizer_type
    = gsl_multimin_fdfminimizer_vector_bfgs2;
  // Declare and populate structure containing function pointers
  gsl_multimin_function_fdf my_function;
  my_function.n = nx();
  my_function.f = my_function_value;
  my_function.df = my_function_gradient;
  my_function.fdf = my_function_value_and_gradient;
  my_function.params = reinterpret_cast<void*>(this);
  // Set initial state variables using GSL's vector type
  gsl_vector *x;
  x = gsl_vector_alloc(nx());
  for (unsigned int i = 0; i < nx(); ++i) gsl_vector_set(x, i, 1.0);</pre>
  // Configure the minimizer
  gsl_multimin_fdfminimizer* minimizer
    = gsl_multimin_fdfminimizer_alloc(minimizer_type, nx());
  gsl_multimin_fdfminimizer_set(minimizer, &my_function, x,
                                initial_step_size, line_search_tolerance);
  // Begin loop
  size_t iter = 0;
  int status;
  do {
    ++iter;
    // Perform one iteration
    status = gsl_multimin_fdfminimizer_iterate(minimizer);
    // Quit loop if iteration failed
    if (status != GSL_SUCCESS) break;
    // Test for convergence
```

The GSL interface requires three functions to be defined, each of which takes a vector of state variables \mathbf{x} as input: my_function_value, which returns the value of the function; my_function_gradient, which returns the gradient of the function with respect to \mathbf{x} ; and my_function_value_and_gradient, which returns the value and the gradient of the function. These functions are provided to GSL as function pointers (see above), but since GSL is a C library, we need to use the 'extern "C"' specifier in their definition. Thus the function definitions would be:

When the gsl_multimin_fdfminimizer_iterate function is called, it chooses a search direction and performs several calls of these functions to approximately minimize the function along this search direction. The this pointer (i.e. the pointer to the State object), which was provided to the my_function structure in the definition of the minimize function above, is provided as the second argument to each of the three functions above. Unlike in C, in C++ this pointer needs to be cast back to a pointer to a State type, hence the use of reinterpret_cast.

That's it! A call to minimize should successfully minimize well behaved differentiable multi-dimensional functions. It should be straightforward to adapt the above to work with other minimization libraries.

8 Calling an algorithm with and without automatic differentiation from the same program

The calc_function_value(const double*) member function defined in section 7 is sub-optimal in that it simply calls the calc_function_value(const adouble*) member function, which not only computes the value of the function, it also records the derivative information of all the operations involved. This information is then ignored. This overhead makes the function typically 2.5–3 times slower than it needs to be, although

sometimes (specifically for loops containing no trancendental functions) the difference between an algorithm coded in terms of doubles and the same algorithm coded in terms of adoubles can exceed a factor of 10 (Hogan, 2013). The impact on the computational speed of the entire minimization process depends on how many requests are made for the function value only as opposed to the gradient of the function, and can be significant. We require a way to avoid the overhead of *Adept* computing the derivative information for calls to calc_function_value(const double*), without having to maintain two versions of the algorithm, one coded in terms of doubles and the other in terms of adoubles. The two ways to achieve this are now described.

8.1 Pausable recording

The first method involves compiling the entire code with the ADEPT_RECORDING_PAUSABLE preprocessor variable defined, which can be done by adding an argument -DADEPT_RECORDING_PAUSABLE to the compler command line. This modifies the behaviour of mathematical operations performed on adouble variables: instead of performing the operation and then storing the derivative information, it performs the operation and then only stores the derivative information if the *Adept* stack is not in the "paused" state. We then use the following member function definition instead of the one in section 7:

```
double State::calc_function_value(const double* x) {
   stack_.pause_recording();
   for (unsigned int i = 0; i < nx(); ++i) active_x_[i] = x[i];
   double J = value(calc_function_value(&active_x_[0]));
   stack_.continue_recording();
   return J;
}</pre>
```

By pausing the recording for all operations on adouble objects, most of the overhead of storing derivative information is removed. The extra run-time check to see whether the stack is in the paused state, which is carried out by mathematical operations involving adouble objects, generally adds a small overhead. However, in algorithms where most of the number crunching occurs in loops containing no trancendental functions, even if the stack is in the paused state, the presence of the check can prevent the compiler from agressively optimizing the loop. In that instance the second method may be preferable.

8.2 Multiple object files per source file

The second method involves compiling each source file containing functions with adouble arguments twice. The first time, the code is compiled normally to produce an object file containing compiled functions including automatic differentiation. The second time, the code is compiled with the <code>-DADEPT_NO_AUTOMATIC_DIFFERENTIATION</code> flag on the compiler command line. This instructs the <code>adept.h</code> header file to turn off automatic differentiation by defining the <code>adouble</code> type to be an alias of the <code>double</code> type. This way, a second set of object files are created containing overloaded versions of the same functions as the first set but this time without automatic differentiation. These object files can be compiled together to form one executable. In the example presented in section 7, the <code>calc_function_value(const adouble*)</code> version and the other to provide the <code>calc_function_value(const adouble*)</code> version and the other to provide the <code>calc_function_value(const double*)</code> version. Note that any functions that do not include <code>adouble</code> arguments must be compiled only once, because otherwise the linker will complain about multiple versions of the same function.

The following shows a Makefile from a hypothetical project that compiles two source files (algorithm1.cpp and algorithm2.cpp) twice and a third (main.cpp) once:

```
# Specify compiler and flags
CPP = g++
CPPFLAGS = -Wall -O3 -g
# Normal object files to be created
OBJECTS = algorithm1.o algorithm2.o main.o
# Object files created with no automatic differentiation
NO_AD_OBJECTS = algorithm1_noad.o algorithm2_noad.o
# Program name
```

There is a further modification required with this approach, which arises because if a header file declares both the double and adouble versions of a function, then when compiled with -DADEPT_NO_AUTOMATIC_DIFFERENTIATION it appears to the compiler that the same function is declared twice, leading to a compile-time error. This can be overcome by using the preprocessor to hide the adouble version if the code is compiled with this flag, as follows (using the example from section 7):

```
#include "adept.h"
class State {
  public:
    ...
    double calc_function_value(const double* x);
  protected:
#ifndef ADEPT_NO_AUTOMATIC_DIFFERENTIATION
    adouble calc_function_value(const adouble* x);
#endif
    ...
}
```

A final nuance is that if the code contains an adouble object x, then x.value() will work fine in the compilation when x is indeed of type adouble, but in the compilation when it is set to a simple double variable, the value() member function will not be found. Hence it is better to use adept::value(x), which returns a double regardless of the type of x, and works regardless of whether the code was compiled with or without the -DADEPT_NO_AUTOMATIC_DIFFERENTIATION flag.

9 Interfacing with software containing hand-coded Jacobians

Often a complicated algorithm will include multiple components. Components of the code written in C or C++ for which the source is available are straightforward to convert to using *Adept*, following the rules in section 4. For components written in Fortran, this is not possible, but if such components have their own hand-coded Jacobian then it is possible to interface *Adept* to them. More generally, in certain situations automatic differentiation is much slower than hand-coding (see the Lax-Wendroff example in Hogan, 2013) and we may wish to hand-code certain critical parts. In general the Jacobian matrix is quite expensive to compute, so this interfacing strategy makes most sense if the component of the algorithm has a small number of inputs or a small number of outputs. A full working version of the following example is given as "Test 3" in the test directory of the *Adept* package.

Consider the example of a radiative transfer model for simulating satellite microwave radiances at two wavelengths, I and J, which takes as input the surface temperature T_s and the vertical profile of atmospheric temperature T from a numerical weather forecast model. Such a model would be used in a data assimilation system to assimilate the temperature information from the satellite observations into the weather forecast model. In addition to returning the radiances, the model returns the gradient $\partial I/\partial T_s$ and the gradients $\partial I/\partial T_i$ for all height layers i between 1 and n, and likewise for radiance J. The interface to the radiative transfer model is the following:

```
const double* temperature,
// Output variables:
double radiance[2],
// Output Jacobians:
double dradiance_dsurface_temperature[2],
double* dradiance_dtemperature);
```

The calling function needs to allocate 2*n elements for the temperature Jacobian dradiance_dtemperature to be stored, and the stored Jacobian will be oriented such that the radiance index varies fastest.

Adept needs to be told how to relate the radiance perturbations δI and δJ , to perturbations in the input variables, δT_s and δT_i (for all layers i). Mathematically, we wish the following relationship to be stored within the *Adept* stack:

$$\delta I = \frac{\partial I}{\partial T_s} \delta T_s + \sum_{i=1}^n \frac{\partial I}{\partial T_i} \delta T_i. \tag{1}$$

This is achieved with the following wrapper function, which has adouble inputs and outputs and therefore can be called from within other parts of the algorithm that are coded in terms of adouble objects:

```
void simulate_radiances_wrapper(int n,
                                const adouble& surface temperature,
                                const adouble* temperature,
                                adouble radiance[2]) {
  // Create inactive (double) versions of the active (adouble) inputs
  double st = value(surface_temperature);
  std::vector<double> t(n);
  for (int i = 0; i < n; ++i) t[i] = value(temperature[i]);</pre>
  // Declare variables to hold the inactive outputs and their Jacobians
  double r[2];
  double dr dst[2];
  std::vector<double> dr_dt(2*n);
  // Call the non-Adept function
  simulate_radiances(n, st, &t[0], &r[0], dr_dst, &dr_dt[0]);
  // Copy the results into the active variables, but use set_value in order
  // not to write any equivalent differential statement to the Adept stack
  radiance[0].set_value(r[0]);
  radiance[1].set_value(r[1]);
  // Loop over the two radiances and add the differential statements to the Adept stack
  for (int i = 0; i < 2; ++i) {
    // Add the first term on the right-hand-side of Equation 1 in the text
   radiance[i].add_derivative_dependence(surface_temperature, dr_dst[i]);
    // Now append the second term on the right-hand-side of Equation 1. The third argument
    // "n" of the following function says that there are n terms to be summed, and the fourth
    // argument "2" says to take only every second element of the Jacobian dr\_dt, since the
    // derivatives with respect to the two radiances have been interlaced. If the fourth
    // argument is omitted then relevant Jacobian elements will be assumed to be contiguous
    // in memory.
   radiance[i].append_derivative_dependence(temperature, &dr_dt[i], n, 2);
  }
```

In this example, the form of add_derivative_dependence for one variable on the right-hand-side of the derivative expression has been used, and the form of append_derivative_dependence for an array of variables on the right-hand-side has been used. As described in section 12, both functions have forms that take single variables and arrays as arguments. Note also that the use of std::vector<double> rather than new double[n] ensures that if simulate_radiances throws an exception, the memory allocated to hold dr_dt will be freed correctly.

10 Tips for the best performance

- If you are working with single-threaded code, or in a multi-threaded program but with only one thread using a Stack object, then you can get slightly faster code by compiling all of your code with -DADEPT_STACK_THREAD_UNSAFE. This uses a standard (i.e. non-thread-local) global variable to point to the currently active stack object, which is slightly faster to access.
- If you compile with the -g option to store debugging symbols, your object files and executable will be much larger because every mathematical statement in the file will have the name of its associated templated type stored in the file, and these names can be long. Once you have debugged your code, you may wish to omit debugging symbols from production versions of the executable. There appears to be no performance penalty associated with the debugging symbols, at least with the GNU C++ compiler.
- A high compiler optimization setting is recommended to inline the function calls associated with mathematical expressions. On the GNU C++ compiler, the -o3 setting is recommended.
- By default the Jacobian functions are compiled to process a strip of rows or columns of the Jacobian matrix at once. The optimum width of the strip depends on your platform, and you may wish to change it. To make the Jacobian functions process *n* rows or columns at once, recompile the *Adept* library with -DADEPT_MULTIPASS_SIZE=n.
- If you suspect memory usage is a problem, you may investigate the memory used by *Adept* by simply sending your Stack object to a stream, e.g. "std::cout << stack". You may also use the memory() member function, which returns the total number of bytes used. Further details of similar functions is given in section 11.

11 Member functions of the Stack class

This section describes the user-oriented member functions of the Stack class. Some functions have arguments with default values; if these arguments are omitted then the default values will be used (for example, if only one argument is supplied to the jacobian function below, then it will be executed as if called with a second argument false). Some of these functions throw *Adept* exceptions, defined in section 13.

- Stack(bool activate_immediately = true) The constructor for the Stack class. Normally Stack objects are constructed with no arguments, which means that the object will attempt to make itself the currently active stack by placing a pointer to itself into a global variable. If another Stack object is currently active, then the present one will be fully constructed, left in the unactivated state, and an stack_already_active exception will be thrown. If a Stack object is constructed with an argument "false", it will be started in an unactivated state, and a subsequent call to its member function activate will be needed to use it.
- void new_recording() Clears all the information on the stack in order that a new recording can be started. Specifically this function clears all the differential statements, the list of independent and dependent variables (used in computing Jacobian matrices) and the list of gradients used by the compute_tangent_linear and compute_adjoint functions. Note that this function leaves the memory allocated to reduce the overhead of reallocation in the new recordings.
- bool pause_recording() Stops recording differential information every time an adouble statement is executed. This is useful if within a single program an algorithm needs to be run both with and without automatic differentiation. This option is only effective within compilation units compiled with ADEPT_RECORDING_PAUSABLE defined; if it is, the function returns true, otherwise it returns false. Further information on using this and the following function are provided in section 8.1.
- bool continue_recording() Instruct a stack that may have previously been put in a paused state to now continue recording differential information as normal. This option is only effective within compilation units compiled with ADEPT_RECORDING_PAUSABLE defined; if it is, the function returns true, otherwise it returns false.

- **bool** is_recording() Returns false if recording has been paused with pause_recording() and the code has been compiled with ADEPT_RECORDING_PAUSABLE defined. Otherwise returns true.
- void compute_tangent_linear() Perform a tangent-linear calculation (forward-mode differentiation) using
 the stored differential statements. Before calling this function you need call the adouble::set_gradient
 or set_gradients function (see section 12) on the independent variables to set the initial gradients, otherwise the function will throw a gradients_not_initialized exception. This function is synonymous
 with forward().
- void compute_adjoint() Perform an adjoint calculation (reverse-mode differentiation) using the stored
 differential statements. Before calling this function you need call the adouble::set_gradient or
 set_gradients function on the dependent variables to set the initial gradients, otherwise the function
 will throw a gradients_not_initialized exception. This function is synonymous with reverse().
- void independent(const adouble& x) Before computing Jacobian matrices, you need to identify the independent and dependent variables, which correspond to the columns and rows of he Jacobian, respectively. This function adds x to the list of independent variables. If it is the nth variable identified in this way, the nth column of the Jacobian will correspond to derivatives with respect to x.
- void dependent (const adouble y) Add y to the list of dependent variables. If it is the mth variable identified in this way, the mth row of the Jacobian will correspond to derivatives of y with respect to each of the independent variables.
- void independent(const adouble* x_ptr, size_t n) Add n independent variables to the list, which
 must be stored consecutively in memory starting at the memory pointed to by x_ptr.
- void dependent(const adouble* y_ptr, size_t n) Add n dependent variables to the list, which must
 be stored consecutively in memory starting at the memory pointed to by y_ptr.
- void jacobian(double* jacobian_out) Compute the Jacobian matrix, i.e., the gradient of the m dependent variables (identified with the dependent(...) function) with respect to the n independent variables (identified with independent(...). The result is returned in the memory pointed to by jacobian_out, which must have been allocated to hold $m \times n$ values. The result is stored in column-major order, i.e., the m diemension of the matrix varies fastest. If no dependents or independents have been identified, then the function will throw a dependents_or_independents_not_identified exception. In practice, this function calls jacobian_forward if $n \le m$ and jacobian_reverse if n > m.
- void jacobian_forward(double* jacobian_out) Compute the Jacobian matrix by executing n forward passes through the stored list of differential statements; this is typically faster than jacobian_reverse for $n \le m$.
- void jacobian_reverse(double* jacobian_out) Compute the Jacobian matrix by executing m reverse passes through the stored list of differential statements; this is typically faster than jacobian_forward for n > m.
- void clear_gradients() Clear the gradients set with the set_gradient member function of the adouble class. This enables multiple adjoint and/or tangent-linear calculations to be performed with the same recording.
- void clear_independents() Clear the list of independent variables, enabling a new Jacobian matrix to be computed from the same recording but for a different set of independent variables.
- **void clear_dependents()** Clear the list of dependent variables, enabling a new Jacobian matrix to be computed from the same recording but for a different set of dependent variables.
- size_t n_independents() Return the number of independent variables that have been identified.
- ${\tt size_t}$ ${\tt n_dependents}()$ Return the number of dependent variables that have been identified.

- size_t n_statements() Return the number of differential statements in the recording.
- size_t n_operations() Return the total number of operations in the recording, i.e the total number of terms on the right-hand-side of all the differential statements.
- **size_t max_gradients()** Return the number of working gradients that need to be stored in order to perform a forward or reverse pass.
- std::size_t memory() Return the number of bytes currently used to store the differential statements and the working gradients. Note that this does not include memory allocated but not currently used.
- size_t n_gradients_registered() Each time an adouble object is created, it is allocated a unique index that is used to identify its gradient in the recorded differential statements. When the object is destructed, its index is freed for reuse. This function returns the number of gradients currently registered, equal to the number of adouble objects currently created.
- void print_status(std::ostream& os = std::cout) Print the current status of the Stack object, such
 as number of statements and operations stored and allocated, to the stream specified by os, or standard
 output if this function is called with no arguments. Sending the stack object to the stream using the "<<"
 operator results in the same behaviour.</pre>
- void print_statements(std::ostream& os = std::cout) Print the list of differential statements to the
 specified stream (or standard output if not specified). Each line corresponds to a separate statement, for
 example "d[3] = 1.2*d[1] + 3.4*d[2]".
- bool print_gradients(std::ostream& os = std::cout) Print the vector of gradients to the specified stream (or standard output if not specified). This function returns false if no set_gradient function has been called to set the first gradient and initialize the vector, and true otherwise. To diagnose what compute_tangent_linear and compute_adjoint are doing, it can be useful to call print_gradients immediately before and after.
- void activate() Activate the Stack object by copying its this pointer to a global variable that will be
 accessed by subsequent operations involving adouble objects. If another Stack is already active, a
 stack_already_active exception will be thrown. To check whether this is the case before calling
 activate(), check that the active_stack() function (described below) returns 0.
- void deactivate() Deactivate the Stack object by checking whether the global variable holding the pointer
 to the currently active Stack is equal to this, and if it is, setting it to 0.
- bool is_active() Returns true if the Stack object is the currently active one, false otherwise.
- void start() This function was present in version 0.9 to activate a Stack object, since in that version they were not constructed in an activated state. This function has now been deprecated and will always throw a feature_not_available exception.

The following non-member functions are provided in the adept namespace:

- adept::Stack* active_stack() Returns a pointer to the currently active Stack object, or 0 if there is none.
- bool is_thread_unsafe() Returns true if your code has been compiled with ADEPT_STACK_THREAD_UNSAFE, false otherwise.

12 Member functions of the adouble object

This section describes the user-oriented member functions of the adouble class. Some functions have arguments with default values; if these arguments are omitted then the default values will be used. Some of these functions throw *Adept* exceptions, defined in section 13.

- double value() Return the underlying double value.
- void set_value(double x) Set the value of the adouble object to x, without storing the equivalent differential statement in the currently active stack.
- void set_gradient(const double& gradient) Set the gradient corresponding to this adouble variable. The first call of this function (for any adouble variable) after a new recording is made also initializes the vector of working gradients. This function should be called for one or more adouble objects after a recording has been made but before a call to Stack::compute_tangent_linear() or Stack::compute_adjoint().
- void get_gradient(double& gradient) Set gradient to the value of the gradient corresponding to this adouble object. This function is used to extract the result after a call to Stack::compute_tangent_linear() or Stack::compute_adjoint(). If the set_gradient function was not called since the last recording was made, this function will throw a gradients_not_initialized exception. The function can also throw a gradient_out_of_range exception if new adouble objects were created since the first set_gradient function was called.
- void add_derivative_dependence(const adouble& r, const adouble& g) Add a differential statement to the currently active stack of the form $\delta 1 = g \times \delta r$, where 1 is the adouble object from which this function is called. This function is needed to interface to software containing hand-coded Jacobians, as described in section 9; in this case g is the gradient $\partial 1/\partial r$ obtained from such software.
- void append_derivative_dependence(const adouble& r, const adouble& g) Assuming that the same adouble object has just had its add_derivative_dependence member function called, this function appends $+ g \times \delta r$ to the most recent differential statement on the stack. If the calling adouble object is different, then a wrong_gradient exception will be thrown. Note that multiple append derivative dependence calls can be made in succession.
- void add_derivative_dependence(const adouble* r, const double* g,

size_t n = 1, size_t m_stride = 1) Add a differential statement to the currently active stack of the form $\delta \mathbf{1} = \sum_{i=0}^{\mathbf{n}-1} \mathbf{m}[i] \times \delta \mathbf{r}[i]$, where 1 is the adouble object from which this function is called. If the g_stride argument is provided, then the index to the g array will be $i \times g$ _stride rather than i. This is useful if the Jacobian provided is oriented such that the relevant gradients for 1 are not spaced consecutively.

void append_derivative_dependence(const adouble* rhs, const double* g,

size_t n = 1, size_t g_stride = 1)
Assuming that the same adouble object has just called the add_derivative_dependence function, this function appends $+\sum_{i=0}^{\mathbf{n}-1}\mathbf{m}[i]\times\delta\mathbf{r}[i]$ to the most recent differential statement on the stack. If the calling adouble object is different, then a wrong_gradient exception will be thrown. The g_stride argument behaves the same way as in the previous function described.

The following non-member functions are provided in the adept namespace:

- double value (const adouble& x) Returns the underlying value of x as a double. This is useful to enable x to be used in fprintf function calls. It is generally better to use adept::value(x) rather than x.value(), because the former also works if you compile the code with the ADEPT_NO_AUTOMATIC_DIFFERENTIATION flag set, as discussed in section 8.2.
- void set_values(adouble* x, size_t n, const double* x_val) Set the value of the n adouble objects starting at x to the values in x_val, without storing the equivalent differential statement in the currently active stack.
- void set_gradients(adouble* x, size_t n, const double* gradients) Set the gradients corresponding to the n adouble objects starting at x to the n doubles starting at gradients. This has the same effect as calling the set_gradient member function of each adouble object in turn, but is more concise.

void get_gradients(const adouble* y, size_t n, double* gradients) Copy the gradient of the n adouble objects starting at y into the n doubles starting at gradients. This has the same effect as calling the get_gradient member function of each adouble object in turn, but is more concise. This function can throw a gradient_out_of_range exception if new adouble objects were created since the first set_gradients function or set_gradient member function was called.

13 Exceptions thrown by the *Adept* library

Some functions in the *Adept* library can throw exceptions, and all of the exceptions that can be thrown are derived from adept::autodiff_exception, which is itself derived from std::exception. All these exceptions indicate an error in the users code, usually associated with calling *Adept* functions in the wrong order.

An exception-catching implementation that takes different actions depending on whether a specific Adept exception, a general *Adept* exception, or a non-*Adept* exception is thrown might have the following form:

```
try {
   adept::Stack stack;
   // ... Code using the Adept library goes here ...
}
catch (adept::stack_already_active& e) {
   // Catch a specific Adept exception
   std::cerr << "Error: " << e.what() << std::endl;
   // ... any further actions go here ...
}
catch (adept::autodiff_exception& e) {
   // Catch any Adept exception not yet caught
   std::cerr << "Error: " << e.what() << std::endl;
   // ... any further actions go here ...
}
catch (...) {
   // Catch any exceptions not yet caught
   std::cerr << "An error occurred" << std::endl;
   // ... any further actions go here ...
}</pre>
```

All exceptions implement the what () member function, which returns a const char* containing an error message. The following exceptions can be thrown, and all are in the adept namespace:

gradient_out_of_range This exception can be thrown by the adouble::get_gradient member function if
the index to its gradient is larger than the number of gradients stored. This can happen if the adouble object
was created after the first adouble::set_gradient call since the last Stack::new_recording call. The
first adouble::set_gradient call signals to the Adept stack that the main algorithm has completed and
so memory can be allocated to store the gradients ready for a forward or reverse pass through the differential
statements. If further adouble objects are created then they may have a gradient index that is out of range
of the memory allocated.

gradients_not_initialized This exception can be thrown by functions that require the list of working gradients to have been initialized (particularly the functions Stack::compute_tangent_linear and Stack::compute_adjoint). This initialization occurs when adouble::set_gradient is called.

stack_already_active This exception is thrown when an attempt is made to make a particular Stack object
 "active", but there already is an active stack in this thread. This can be thrown by the Stack constructor or
 the Stack::activate member function.

dependents_or_independents_not_identified This exception is thrown when an attempt is made to compute a Jacobian but the independents and/or dependents have not been identified.

wrong_gradient This exception is thrown by the adouble::append_derivative_dependence if the adouble object that it is called from is not the same as that of the most recent adouble::add_derivative_dependence.

non_finite_gradient This exception is thrown if the users code is compiled with the preprocessor variable ADEPT_TRACK_NON_FINITE_GRADIENTS defined, and a mathematical operation is carried out for which the derivative is not finite. This is useful to locate the source of non-finite derivatives coming out of an algorithm.

feature_not_available This exception is thrown by deprecated functions, such as Stack::start().

14 Configuring the behaviour of *Adept*

The behaviour of the *Adept* library can be changed by defining one or more of the *Adept* preprocessor variables. This can be done either by editing the adept.h file and uncommenting the relevant #define lines in sections 1 or 2 of the file, or by compiling your code with -Dxxx compiler options (replacing xxx by the relevant preprocessor variable. There are two types of preprocessor variable: the first types only apply to the compilation of user code, while the second types require the *Adept* library to be recompiled.

The preprocessor variables that apply only to user code and do not require the *Adept* library to be recompiled are as follows:

- ADEPT_STACK_THREAD_UNSAFE If this variable is defined, the currently active stack is stored as a global variable but is not defined to be "thread-local". This is slightly faster, but means that you cannot use multi-threaded code with separate threads holding their own active Stack object. Note that although defining this variable does not require a library recompile, all source files that make up a single executable must be compiled with this option (or all not be).
- ADEPT_RECORDING_PAUSABLE This option enables an algorithm to be run both with and without automatic differentiation from within the same program via the functions Stack::pause_recording() and Stack::continue_recording(). Note that although defining this variable does not require a library recompile, all source files that make up a single executable must be compiled with this option (or all not be). Further details on this option are provided in section 8.1.
- **ADEPT_NO_AUTOMATIC_DIFFERENTIATION** This option turns off automatic differentiation by treating adouble objects as double. It is useful if you want to compile one source file twice to produce versions with and without automatic differentiation. Further details on this option are provided in section 8.2.
- **ADEPT_TRACK_NON_FINITE_GRADIENTS** Often when an algorithm is first converted to use an operator-overloading automatic differentiation library, the gradients come out as Not-a-Number or Infinity. The reason is often that the algorithm contains operations for which the derivative is not finite (e.g. \sqrt{a} for a=0), or constructions where a non-finite value is produced but subsequently made finite (e.g. $\exp(-1.0/a)$ for a=0). Usually the algorithm can be recoded to avoid these problems, if the location of the problematic operations can be identified. By defining this preprocessor variable, a non_finite_gradient exception will be thrown if any operation results in a non-finite derivative. Running the program within a debugger (and ensuring that the exception is not caught within the program) enables the offending line to be identified.
- **ADEPT_INITIAL_STACK_LENGTH** This preprocessor variable is set to an integer, and is used as the default initial amount of memory allocated for the recording, in terms of the number of statements and operations.
- **ADEPT_REMOVE_NULL_STATEMENTS** If many variables in your code are likely to be zero then redundant operations will be added to the list of differential statements. For example, the assignment $a = b \times c$ with active variables b and c both being zero results in the differential statement $\delta a = 0 \times \delta b + 0 \times \delta c$. This preprocessor variable checks for zeros and removes terms on the right-hand-side of differential statements if it finds them. In this case it would put $\delta a = 0$ on the stack instead. This option slows down the recording stage, but speeds up the subsequent use of the recorded stack for adjoint and Jacobian calculations. The speed up of the latter is only likely to exceed the slow down of the former if your code contains many zeros. For most codes, this option causes a net slow down.
- **ADEPT_COPY_CONSTRUCTOR_ONLY_ON_RETURN_FROM_FUNCTION** If copy constructors for adouble objects are only used in the return values for functions, then defining this preprocessor variable will lead to slightly

faster code, because it will be assumed that when a copy constructor is called, the index to its gradient can simply be copied because the object being copied will shortly be destructed (otherwise communication with the Stack object is required to unregister one and immediately register the other). You need to be sure that the code being compiled with this option does not invoke the copy constructor in any other circumstances. Specifically, it must not include either of these constructions: "adouble x = yi" or "adouble x(y)i", where y is an adouble object. If it does, then strange errors will occur.

The preprocessor variables that require the *Adept* library to be recompiled are as follows. Note that if these variables are used they must be the same when compiling both the library and the user code. This is safest to implement by editing the adept.h header file.

- **ADEPT_FLOATING_POINT_TYPE** If you want to compile *Adept* to use a precision other than double, define this preprocessor variable to be the floating-point type required, e.g. float or long double. To use from the compiler command-line, use the argument -DADEPT_FLOATING_POINT_TYPE=float or -DADEPT_FLOATING_POINT_TYPE="long double".
- **ADEPT_STACK_STORAGE_STL** Use the C++ standard template library vector or valarray classes for storing the recording and the list of gradients, rather than dynamically allocated arrays. In practice, this tends to slow down the code.
- **ADEPT_MULTIPASS_SIZE** This is set to an integer, invariably a power of two, specifying the number of rows or columns of a Jacobian that are calculated at once. The optimum value depends on the platform and the capability of the compiler to optimize loops whose length is known at compile time.
- ADEPT_MULTIPASS_SIZE_ZERO_CHECK This is also set to an integer; if it is greater than ADEPT_MULTIPASS_SIZE, then the Stack::jacobian_reverse function checks gradients are non-zero before using them in a multiplication.

15 Frequently asked questions

Why are all the gradients coming out of the automatic differentiation zero? You have almost certainly omitted or misplaced the call of the adept::Stack member function "new_recording()". It should be placed after the independent variables in the algorithm have been initialized, but before any subsequent calculations are performed on these variables. If it is omitted or placed before the point where the independent variables are initialized, the differential statements corresponding to this initialization (which are all of the form $\delta x = 0$), will be placed in the list of differential statements and will unhelpfully set to zero all your gradients right at the start of a forward pass (resulting from a call to forward()) or set them to zero right at the end of a reverse pass (resulting from a call to reverse()).

Can Adept reuse a stored tape for multiple runs of the same algorithm but with different inputs? No.

Adept does not store the full algorithm in its stack (as ADOL-C does in its tapes, for example), only the derivative information. So from the stack alone you cannot rerun the function with different inputs. However, rerunning the algorithm including recomputing the derivative information is fast using Adept, and is still faster than libraries that store enough information in their tapes to enable a tape to be reused with different inputs. It should be stressed that for any algorithm that includes different paths of execution ("if" statements) based on the values of the inputs, such a tape would need to be rerecorded anyway. This includes any algorithm containing a look-up table.

Why does my code crash with a segmentation fault? This means it is trying to access a memory address not belonging to your program, and the first thing to do is to run your program in a debugger to find out at what point in your code this occurs. If it is in the adept::aReal constructor (note that aReal is synonymous with adouble), then it is very likely that you have tried to initiate an adept::adouble object before initiating an adept::Stack object. As described in section 5.1, there are good reasons why you need to initialize the adept::Stack object first.

16. License

16 License

The *Adept* library is released under the GNU General Public License (GPL) version 3, which is available at http://www.gnu.org/licenses/gpl.html. This license permits you to use and modify the library for any purpose, but if you distribute a software package that incorporates the library or a modified version of it, you must release the source code for the entire software package under the conditions of the GNU GPL.

If you would like to use *Adept* under other licensing terms, for example in commercial software, please contact Robin Hogan (r.j.hogan@reading.ac.uk).

In addition to the legally binding terms of the license, it is *requested* that you cite Hogan (2013) in publications describing algorithms and software that make use of the *Adept* library. This is not a condition of the license, but is good honest practice in science and engineering.

References

- Bell, B., 2007: CppAD: A package for C++ algorithmic differentiation. http://www.coin-or.org/CppAD
- Liu, D. C., and Nocedal, J., 1989: On the limited memory method for large scale optimization. *Math. Programming B*, **45**, 503–528.
- Gay, D. M., 2005: Semiautomatic differentiation for efficient gradient computations. In *Automatic Differentiation: Applications, Theory, and Implementations*, H. M. Bücker, G. F. Corliss, P. Hovland, U. Naumann and B. Norris (eds.), Springer, 147–158.
- Griewank, A., Juedes, D., and Utke, J., 1996: Algorithm 755: ADOL-C: a package for the automatic differentiation of algorithms written in C/C++. *ACM Trans. Math. Softw.*, **22**, 131–167.
- Hogan, R. J., 2013: Fast reverse-mode automatic differentiation using expression templates in C++. *Submitted to ACM Trans. Math. Softw.*