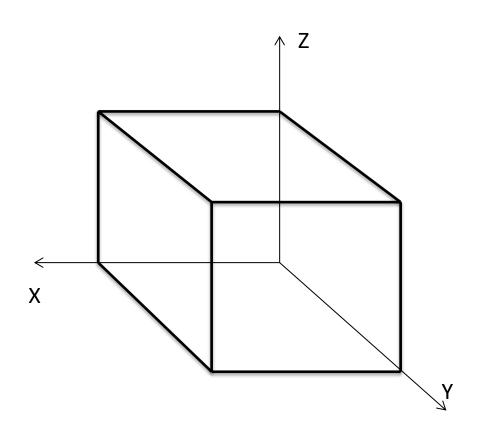
АКСОНОМЕТРИЯ

АНАЛИТИЧНО ЗАДАВАНЕ ВИДОВЕ АКСОНОМЕТРИИ

КАВАЛИЕРНА ПЕРСПЕКТИВА



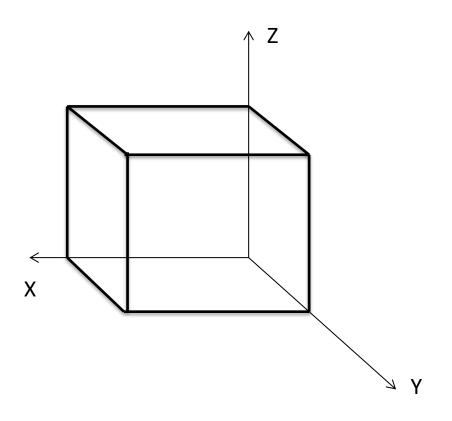
Изометрия: p = q = r

$$\angle (Ox, Oz) = 90^{\circ};$$

 $\angle (Ox, Oy) = 135^{\circ}$
 $\angle (Oy, Oz) = 135^{\circ}$

$$C = \begin{pmatrix} 1 & -\frac{\sqrt{2}}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2}}{2} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

КАБИНЕТНА ПРОЕКЦИЯ



Диметрия: p = 2q = r

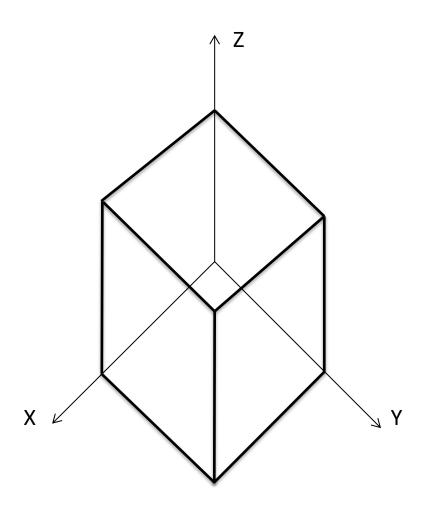
$$\angle(Ox, Oz) = 90^{\circ};$$

$$\sphericalangle(Ox, Oy) = 135^{\circ}$$

 $\sphericalangle(Oy, Oz) = 135^{\circ}$

$$C = \begin{pmatrix} 1 & -\frac{\sqrt{2}}{4} & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & -\frac{\sqrt{2}}{4} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

ВОЕННА ПЕРСПЕКТИВА



Изометрия: p = q = r

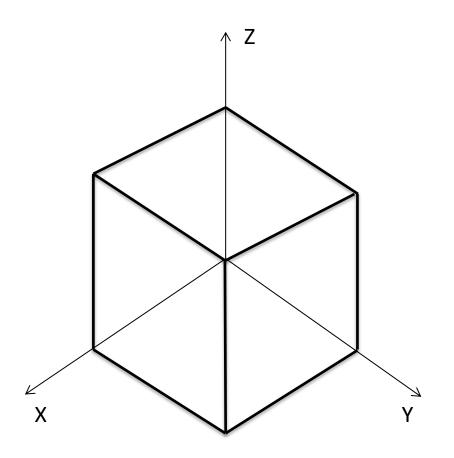
$$\angle(Ox, Oy) = 90^{\circ};$$

$$\sphericalangle(0x,0z) = 135^{\circ}$$

$$\sphericalangle(0y,0z) = 135^{\circ}$$

$$C = \begin{pmatrix} 1 & 0 & -\frac{\sqrt{2}}{2} & 0 \\ 0 & 1 & -\frac{\sqrt{2}}{2} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

ПРАВОЪГЪЛНА ИЗОМЕТРИЯ



Изометрия: p = q = r

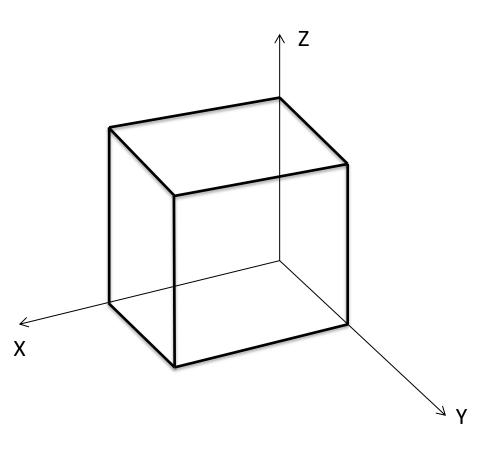
$$\triangleleft (Ox, Oy) = 120^{\circ}$$

$$\sphericalangle(Ox, Oz) = 120^{\circ}$$

$$\sphericalangle(Oy, Oz) = 120^{\circ}$$

$$C = \begin{pmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} & 0 & 0 \\ -\frac{\sqrt{6}}{6} & -\frac{\sqrt{6}}{6} & \frac{\sqrt{6}}{3} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

ПРАВОЪГЪЛНА ДИМЕТРИЯ



Изометрия: p = 2q = r

$$\sphericalangle(Ox,Oy) = 131^{\circ}25'$$

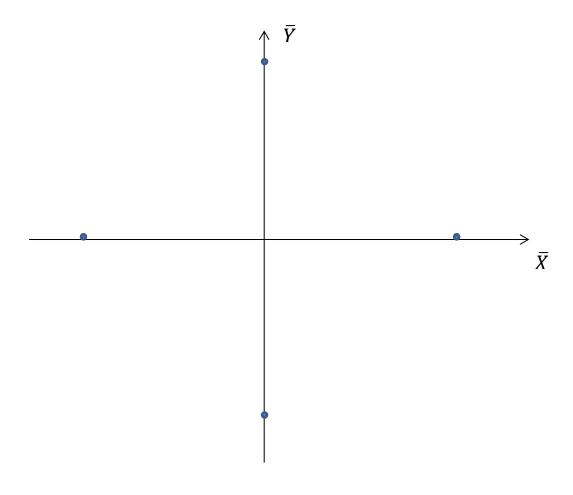
$$\sphericalangle(0x, 0z) = 97^{\circ}10'$$

$$<(0y, 0z) = 131^{\circ}25'$$

$$C = \begin{pmatrix} -\frac{\sqrt{14}}{4} & \frac{\sqrt{2}}{4} & 0 & 0 \\ -\frac{\sqrt{2}}{12} & -\frac{\sqrt{14}}{12} & \frac{\sqrt{8}}{3} & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$C = \begin{pmatrix} -0.93 & 0.35 & 0 & 0 \\ -0.12 & -0.31 & 0.94 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 \\ 0 \\ 1 \\ 1 \end{pmatrix}$$

$$ar{A}(0,0,0,1)
ightharpoonup A(0,0,0,1)
ightharpoonup A(0,0)$$
 $ar{B}(0,1,0,1)
ightharpoonup B(0.35,-0.31,0,1)
ightharpoonup B(0.35,-0.31)$
 $ar{C}(1,1,0,1)
ightharpoonup C(-0.58,-0.43,0,1)
ightharpoonup C(-0.58,-0.43)$
 $ar{D}(1,0,0,1)
ightharpoonup D(-0.93,-0.12,0,1)
ightharpoonup D(-0.93,-0.12)$
 $ar{A}_1(0,0,1,1)
ightharpoonup A_1(0,0.94,0,1)
ightharpoonup A_1(0,0.94)$
 $ar{B}_1(0,1,1,1)
ightharpoonup B_1(0.35,0.63,0,1)
ightharpoonup B_1(0.35,0.63)$
 $ar{C}_1(1,1,1,1)
ightharpoonup C_1(-0.58,0.51,0,1)
ightharpoonup C_1(-0.58,0.51)$
 $ar{D}_1(1,0,1,1)
ightharpoonup D_1(-0.93,0.82,0,1)
ightharpoonup D_1(-0.93,0.82)$



ПЕРСПЕКТИВА

АНАЛИТИЧНО ЗАДАВАНЕ ВИДОВЕ ОБРАЗИ

$$\pi \equiv Oxy, \qquad S\left(\frac{1}{2}, \frac{1}{2}, -2, 1\right)$$

$$B\left(\begin{array}{c} \frac{1}{2}, -\frac{1}{2}, 0, \\ C\left(\begin{array}{c} \frac{1}{2}, \frac{1}{2}, 0, \\ D\left(-\frac{1}{2}, \frac{1}{2}, 0, \right), \end{array}\right)$$

 χ

$$A\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \quad A_1\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right)$$

$$B\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \quad B_1\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right)$$

$$C\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \quad C_1\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right)$$

$$D\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \quad D_1\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right)$$

$$\pi \equiv Oxy, \qquad S\left(\frac{1}{2}, 1, -2, 1\right)$$

$$A\left(-\frac{1}{2}, -1, 0, 2\right) \quad A_1\left(-\frac{1}{2}, -1, 0, 3\right)$$

$$B\left(-\frac{1}{2}, -1, 0, 2\right) \quad B_1\left(-\frac{1}{2}, -1, 0, 3\right)$$

$$C\left(-\frac{1}{2}, 0, 0, 2\right) \quad C_1\left(-\frac{1}{2}, 0, 0, 3\right)$$

$$D\left(-\frac{1}{2}, 0, 0, 2\right) \quad D_1\left(-\frac{1}{2}, 0, 0, 3\right)$$

$$\pi \equiv Oxy, \qquad S(0,0,-2,1)$$

$$A(0,0,0,2)$$
 $A_1(0,0,0,3)$
 $B(1,0,0,2)$ $B_1(1,0,0,3)$
 $C(1,1,0,2)$ $C_1(1,1,0,3)$
 $D(0,1,0,2)$ $D_1(0,1,0,3)$

y

 χ

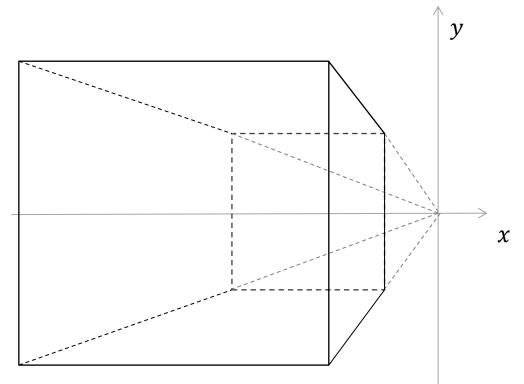
$$\pi \equiv Oxy, \qquad S\left(\frac{3}{2}, \frac{1}{2}, -2, 1\right)$$

$$A\left(-\frac{3}{2}, -\frac{1}{2}, 0, 2\right) \quad A_1\left(-\frac{3}{2}, -\frac{1}{2}, 0, 3\right)$$

$$B\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \quad B_1\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right)$$

$$C\left(-\frac{1}{2}, \frac{1}{2}, 0, 2\right) \quad C_1\left(-\frac{1}{2}, \frac{1}{2}, 0, 3\right)$$

$$D\left(-\frac{3}{2}, \frac{1}{2}, 0, 2\right) \quad D_1\left(-\frac{3}{2}, \frac{1}{2}, 0, 3\right)$$



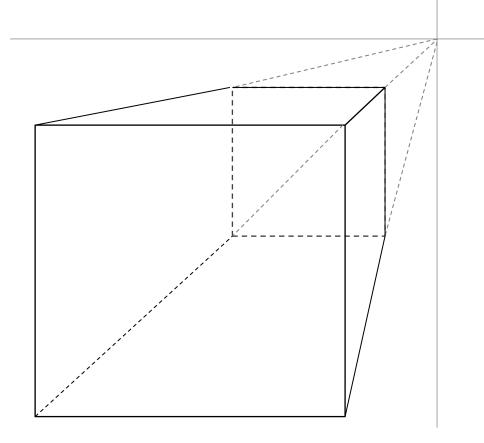
$$\pi \equiv Oxy, \qquad S\left(\frac{3}{2}, \frac{3}{2}, -2, 1\right)$$

$$A\left(-\frac{3}{2}, -\frac{3}{2}, 0, 2\right) \quad A_1\left(-\frac{3}{2}, -\frac{3}{2}, 0, 3\right)$$

$$B\left(-\frac{1}{2}, -\frac{3}{2}, 0, 2\right) \quad B_1\left(-\frac{1}{2}, -\frac{3}{2}, 0, 3\right)$$

$$C\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \quad C_1\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right)$$

$$D\left(-\frac{3}{2}, -\frac{1}{2}, 0, 2\right) \quad D_1\left(-\frac{3}{2}, -\frac{1}{2}, 0, 3\right)$$



 $\boldsymbol{\chi}$

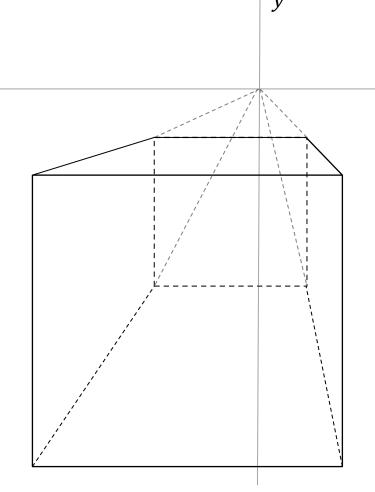
$$\pi \equiv Oxy, \qquad S\left(\frac{3}{4}, \frac{5}{4}, -2, 1\right)$$

$$A\left(-\frac{3}{4}, -\frac{5}{4}, 0, 2\right) \quad A_1\left(-\frac{3}{4}, -\frac{5}{4}, 0, 3\right)$$

$$B\left(-\frac{1}{4}, -\frac{5}{4}, 0, 2\right) \quad B_1\left(-\frac{1}{4}, -\frac{5}{4}, 0, 3\right)$$

$$C\left(-\frac{1}{4}, -\frac{1}{4}, 0, 2\right) \quad C_1\left(-\frac{1}{4}, -\frac{1}{4}, 0, 3\right)$$

$$D\left(-\frac{3}{4}, -\frac{1}{4}, 0, 2\right) \quad D_1\left(-\frac{3}{4}, -\frac{1}{4}, 0, 3\right)$$



АНАЛИТИЧНО ЗАДАВАНЕ НА ПЕРСПЕКТИВА

Пространствената координатна система е $\,\overline{K}=\bar{O}\bar{x}\bar{y}\bar{z}$. Спрямо тази к.с.

$$\pi \parallel \bar{O}\bar{x}\bar{y}, \qquad \pi[0,0,1,1], \qquad \pi{:}\,z+1=0$$

$$\Sigma \parallel \bar{O}\bar{x}\bar{z}, \qquad \Sigma[0, 1, 0, n]$$

$$\rho = A. a + B. b + C. c + D. 1 = c + 1$$

Координатната система K = Oxyz, спрямо която нанасяме образа, е избрана по следния начин:

$$\pi \equiv Oxy$$

 $O \equiv S_0$ – главната точка на картината

$$0x \equiv h$$
 – хоризонта

Така за матрицата, с която действа перспективата, получаваме:

$$C = \begin{pmatrix} 1 & 0 & 0 & -a \\ 0 & 1 & 0 & -b \\ 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{-1}{c+1} & \frac{c}{c+1} \end{pmatrix}$$

$$C = \begin{pmatrix} 1 & 0 & 0 & -\frac{3}{2} \\ 0 & 1 & 0 & -\frac{1}{2} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \end{pmatrix} \qquad S\left(\frac{3}{2}, \frac{1}{2}, -2, 1\right)$$

$$\bar{A}(0,0,0,1) \to A\left(-\frac{3}{2}, -\frac{1}{2}, 0, 2\right) \to A\left(-\frac{3}{4}, -\frac{1}{4}\right)
\bar{B}(0,1,0,1) \to B\left(-\frac{1}{2}, -\frac{1}{2}, 0, 2\right) \to B\left(-\frac{1}{4}, -\frac{1}{4}\right)
\bar{C}(1,1,0,1) \to C\left(-\frac{1}{2}, \frac{1}{2}, 0, 2\right) \to C\left(-\frac{1}{4}, \frac{1}{4}\right)
\bar{D}(1,0,0,1) \to D\left(-\frac{3}{2}, \frac{1}{2}, 0, 2\right) \to D\left(-\frac{3}{4}, \frac{1}{4}\right)$$

$$\bar{A}_{1}(0,0,1,1) \to A_{1}\left(-\frac{3}{2}, -\frac{1}{2}, 0, 3\right) \to A_{1}\left(-\frac{3}{6}, -\frac{1}{6}\right)
\bar{B}_{1}(0,1,1,1) \to B_{1}\left(-\frac{1}{2}, -\frac{1}{2}, 0, 3\right) \to B_{1}\left(-\frac{1}{6}, -\frac{1}{6}\right)
\bar{C}_{1}(1,1,1,1) \to C_{1}\left(-\frac{1}{2}, \frac{1}{2}, 0, 3\right) \to C_{1}\left(-\frac{1}{6}, \frac{1}{6}\right)
\bar{D}_{1}(1,0,1,1) \to D_{1}\left(-\frac{3}{2}, \frac{1}{2}, 0, 3\right) \to D_{1}\left(-\frac{3}{6}, \frac{1}{6}\right)$$