Outline

- Introduction
- Background
- Distributed Database Design
 - → Fragmentation
 - → Data distribution
- Database Integration
- Semantic Data Control
- Distributed Query Processing
- Multidatabase Query Processing
- Distributed Transaction Management
- Data Replication
- Parallel Database Systems
- Distributed Object DBMS
- Peer-to-Peer Data Management
- Web Data Management
- Current Issues

Design Problem

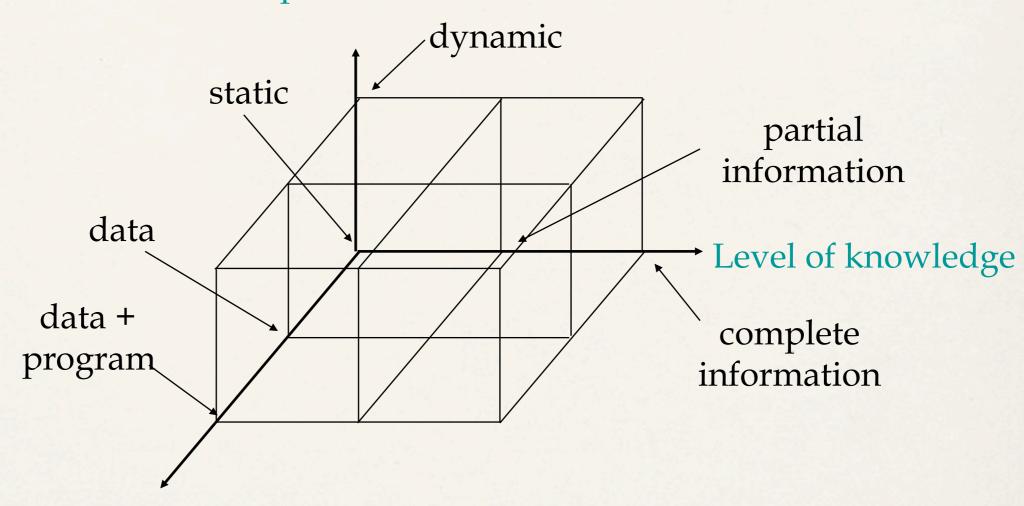
• In the general setting :

Making decisions about the placement of data and programs across the sites of a computer network as well as possibly designing the network itself.

- In Distributed DBMS, the placement of applications entails
 - placement of the distributed DBMS software; and
 - placement of the applications that run on the database

Dimensions of the Problem

Access pattern behavior

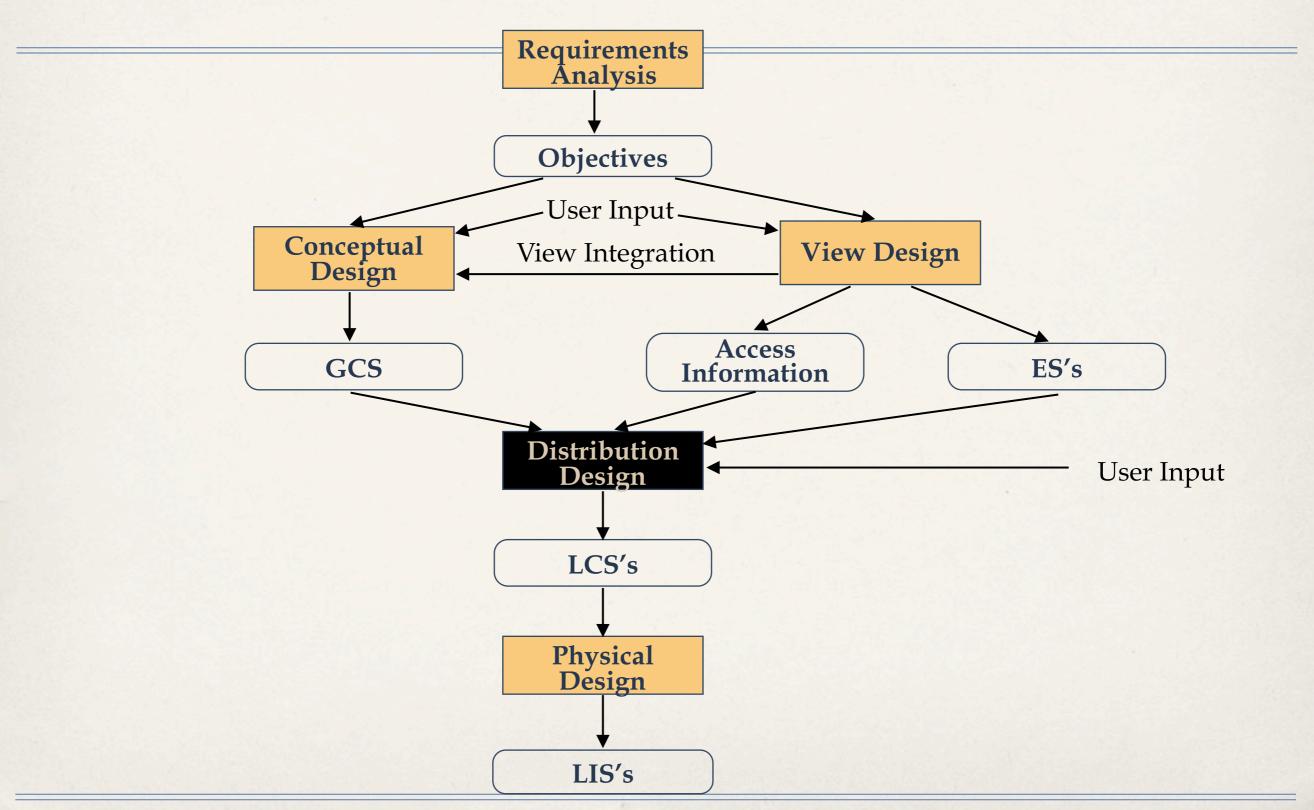


Level of sharing

Distribution Design

- Top-down
 - mostly in designing systems from scratch
 - mostly in homogeneous systems
- Bottom-up
 - when the databases already exist at a number of sites

Top-Down Design



Distribution Design Issues

- Why fragment at all?
- 2 How to fragment?
- 3 How much to fragment?
- 4 How to test correctness?
- **5** How to allocate?
- **6** Information requirements?

Fragmentation

- Can't we just distribute relations?
- What is a reasonable unit of distribution?
 - → relation
 - → views are subsets of relations → locality
 - extra communication
 - fragments of relations (sub-relations)
 - concurrent execution of a number of transactions that access different portions of a relation
 - views that cannot be defined on a single fragment will require extra processing
 - semantic data control (especially integrity enforcement) more difficult

Fragmentation Alternatives – Horizontal

PROJ₁: projects with budgets less than

\$200,000

PROJ₂: projects with budgets greater

than or equal to \$200,000

PROJ

| PNO | PNAME | BUDGET | LOC |
|----------------|---|--|---|
| P2 P3 P4 | Instrumentation Database Develop. CAD/CAM Maintenance CAD/CAM | 150000 135000 250000 310000 500000 | Montreal New York New York Paris Boston |

$PROJ_1$

| PNO | PNAME | BUDGET | LOC |
|-----|-------------------|--------|----------|
| P1 | Instrumentation | 150000 | Montreal |
| P2 | Database Develop. | 135000 | New York |

PROJ₂

| 7 | PNO | PNAME | BUDGET | LOC |
|---|-----|-------------|--------|----------|
| | P3 | CAD/CAM | 250000 | New York |
| | P4 | Maintenance | 310000 | Paris |
| | P5 | CAD/CAM | 500000 | Boston |

Fragmentation Alternatives – Vertical

PROJ₁: information about project

budgets

PROJ₂: information about project

names and locations

PROJ

| PNO | PNAME | BUDGET | LOC |
|----------------------------|---|--|---|
| P1 P2 P3 P4 P5 | Instrumentation Database Develop. CAD/CAM Maintenance CAD/CAM | 150000 135000 250000 310000 500000 | Montreal New York New York Paris Boston |

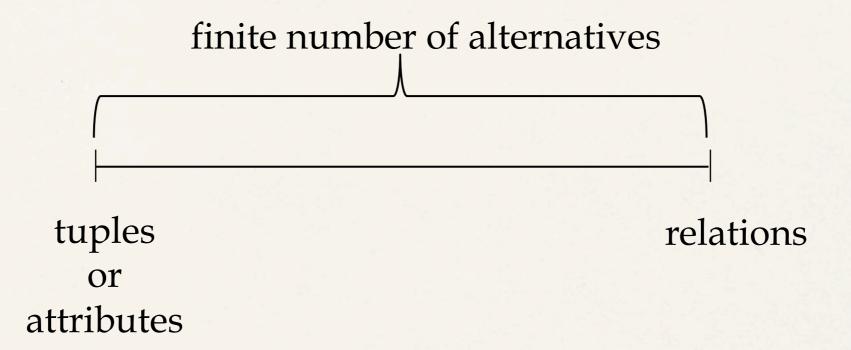
 $PROJ_1$

| PNO | BUDGET |
|-----|--------|
| P1 | 150000 |
| P2 | 135000 |
| P3 | 250000 |
| P4 | 310000 |
| P5 | 500000 |

PROJ₂

| PNO | PNAME | LOC |
|----------------------------|---|---|
| P1 P2 P3 P4 P5 | Instrumentation Database Develop. CAD/CAM Maintenance CAD/CAM | Montreal New York New York Paris Boston |

Degree of Fragmentation



Finding the suitable level of partitioning within this range

Correctness of Fragmentation

Completeness

→ Decomposition of relation R into fragments R_1 , R_2 , ..., R_n is complete if and only if each data item in R can also be found in some R_i

Reconstruction

▶ If relation R is decomposed into fragments R_1 , R_2 , ..., R_n , then there should exist some relational operator ∇ such that

$$R = \nabla_{1 \le i \le n} R_i$$

Disjointness

■ If relation R is decomposed into fragments R_1 , R_2 , ..., R_n , and data item d_i is in R_j , then d_i should not be in any other fragment R_k ($k \neq j$).

Allocation Alternatives

- Non-replicated
 - partitioned : each fragment resides at only one site
- Replicated
 - fully replicated : each fragment at each site
 - partially replicated : each fragment at some of the sites
- Rule of thumb:

If $\frac{\text{read-only queries}}{\text{update queries}}$ << 1, replication is advantageous, otherwise replication may cause problems

Comparison of Replication Alternatives

| | Full-replication | Partial-replication | Partitioning |
|-------------------------|-------------------------|---------------------|----------------------|
| QUERY PROCESSING | Easy | ✓ Same Di | fficulty |
| DIRECTORY MANAGEMENT | Easy or Non-existant | → Same Di | fficulty |
| CONCURRENCY CONTROL | Moderate | Difficult | Easy |
| RELIABILITY | Very high | High | Low |
| REALITY | Possible application | Realistic | Possible application |

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Information Requirements

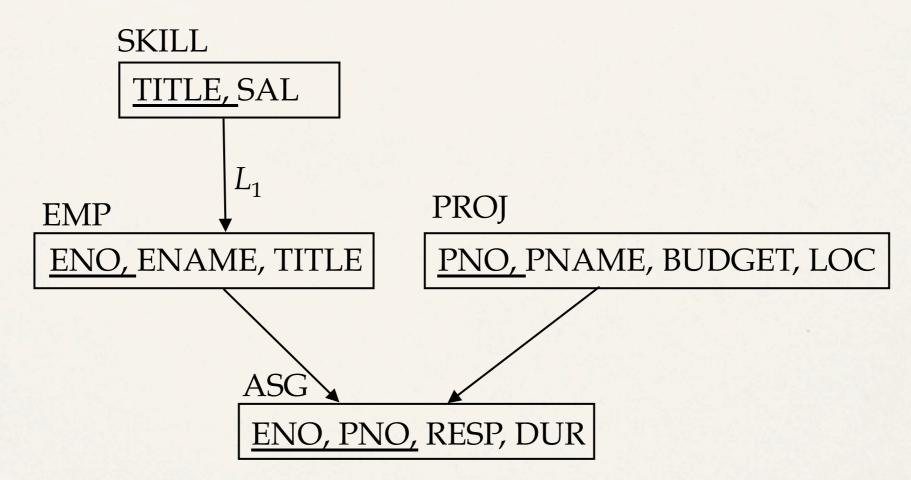
- Four categories:
 - Database information
 - Application information
 - Communication network information
 - Computer system information

Fragmentation

- Horizontal Fragmentation (HF)
 - Primary Horizontal Fragmentation (PHF)
 - Derived Horizontal Fragmentation (DHF)
- Vertical Fragmentation (VF)
- Hybrid Fragmentation (HF)

PHF - Information Requirements

- Database Information
 - relationship



 \rightarrow cardinality of each relation: card(R)

PHF - Information Requirements

- Application Information
 - → **simple predicates** : Given $R[A_1, A_2, ..., A_n]$, a simple predicate p_j is

$$p_i: A_i \ \theta \ Value$$

where $\theta \in \{=,<,\leq,>,\neq\}$, $Value \in D_i$ and D_i is the domain of A_i .

For relation *R* we define $Pr = \{p_1, p_2, ..., p_m\}$

Example:

PNAME = "Maintenance"

BUDGET ≤ 200000

→ minterm predicates : Given R and $Pr = \{p_1, p_2, ..., p_m\}$

define
$$M = \{m_1, m_2, ..., m_r\}$$
 as

$$M = \{ m_i \mid m_i = \Lambda_{p_j \in Pr} p_j^* \}, 1 \le j \le m, 1 \le i \le z$$

where $p_j^* = p_j$ or $p_j^* = \neg(p_j)$.

PHF – Information Requirements

Example

*m*₁: PNAME="Maintenance" ∧ BUDGET≤200000

*m*₂: **NOT**(PNAME="Maintenance") ∧ BUDGET≤200000

*m*₃: PNAME= "Maintenance" ∧ **NOT**(BUDGET≤200000)

*m*₄: **NOT**(PNAME="Maintenance") ∧ **NOT**(BUDGET≤200000)

PHF – Information Requirements

- Application Information
 - \rightarrow minterm selectivities: $sel(m_i)$
 - ♦ The number of tuples of the relation that would be accessed by a user query which is specified according to a given minterm predicate m_i .
 - \rightarrow access frequencies: $acc(q_i)$
 - \bullet The frequency with which a user application qi accesses data.
 - ◆ Access frequency for a minterm predicate can also be defined.

Primary Horizontal Fragmentation

Definition:

$$R_j = \sigma_{F_j}(R), \ 1 \le j \le w$$

where F_j is a selection formula, which is (preferably) a minterm predicate.

Therefore,

A horizontal fragment R_i of relation R consists of all the tuples of R which satisfy a minterm predicate m_i .



Given a set of minterm predicates M, there are as many horizontal fragments of relation R as there are minterm predicates.

Set of horizontal fragments also referred to as minterm fragments.

PHF – Algorithm

Given: A relation R, the set of simple predicates Pr

Output: The set of fragments of $R = \{R_1, R_2, ..., R_w\}$ which obey the

fragmentation rules.

Preliminaries:

- → *Pr* should be *complete*
- → *Pr* should be *minimal*

Completeness of Simple Predicates

• A set of simple predicates *Pr* is said to be *complete* if and only if the accesses to the tuples of the minterm fragments defined on *Pr* requires that two tuples of the same minterm fragment have the same probability of being accessed by any application.

Example :

 Assume PROJ[PNO,PNAME,BUDGET,LOC] has two applications defined on it.

→ Find the budgets of projects at each location. (1)

→ Find projects with budgets less than \$200000. (2)

Completeness of Simple Predicates

```
According to (1),

Pr={LOC="Montreal",LOC="New York",LOC="Paris"}

which is not complete with respect to (2).

Modify

Pr ={LOC="Montreal",LOC="New York",LOC="Paris",
BUDGET≤200000,BUDGET>200000}

which is complete.
```

Minimality of Simple Predicates

- If a predicate influences how fragmentation is performed, (i.e., causes a fragment f to be further fragmented into, say, f_i and f_j) then there should be at least one application that accesses f_i and f_j differently.
- In other words, the simple predicate should be *relevant* in determining a fragmentation.
- If all the predicates of a set Pr are relevant, then Pr is minimal.

$$\frac{acc(m_i)}{card(f_i)}! = \frac{acc(m_j)}{card(f_i)}$$

Minimality of Simple Predicates

Example:

```
Pr ={LOC="Montreal",LOC="New York", LOC="Paris", BUDGET≤200000,BUDGET>200000}
```

is minimal (in addition to being complete). However, if we add

PNAME = "Instrumentation"

then Pr is not minimal.

COM_MIN Algorithm

Given: a relation R and a set of simple predicates Pr

Output: a complete and minimal set of simple predicates Pr' for Pr

Rule 1: a relation or fragment is partitioned into at least two parts which are accessed differently by at least one application.

COM_MIN Algorithm

• Initialization:

- ⇒ find a p_i ∈ Pr such that p_i partitions R according to Rule 1
- ightharpoonup set $Pr' = p_i$; $Pr \leftarrow Pr \{p_i\}$; $F \leftarrow \{f_i\}$
- 2 Iteratively add predicates to Pr' until it is complete
 - ⇒ find a p_j ∈ Pr such that p_j partitions some f_k defined according to minterm predicate over Pr' according to $Rule\ 1$
 - ightharpoonup set $Pr' = Pr' \cup \{p_i\}$; $Pr \leftarrow Pr \{p_i\}$; $F \leftarrow F \cup \{f_i\}$
 - \rightarrow if $\exists p_k \in Pr'$ which is nonrelevant then

$$Pr' \leftarrow Pr - \{p_k\}$$

$$F \leftarrow F - \{f_k\}$$

PHORIZONTAL Algorithm

Makes use of COM_MIN to perform fragmentation.

Input: a relation R and a set of simple predicates Pr

Output: a set of minterm predicates M according to which relation R is to

be fragmented

- $Pr' \leftarrow COM_MIN(R,Pr)$
- 2 determine the set *M* of minterm predicates
- 3 determine the set I of implications among $p_i \in Pr$
- 4 eliminate the contradictory minterms from *M*

- Two candidate relations : PAY and PROJ.
- Fragmentation of relation PAY
 - Application: Check the salary info and determine raise.
 - → Employee records kept at two sites ⇒ application run at two sites
 - Simple predicates

 $p_1: SAL \le 30000$

 p_2 : SAL > 30000

 $Pr = \{p_1, p_2\}$ which is complete and minimal Pr' = Pr

Minterm predicates

 $m_1 : (SAL \le 30000)$

 m_2 : **NOT**(SAL \leq 30000) = (SAL > 30000)

PAY_1

| TITLE | SAL |
|------------|-------|
| Mech. Eng. | 27000 |
| Programmer | 24000 |

PAY_2

| TITLE | SAL |
|-------------|-------|
| Elect. Eng. | 40000 |
| Syst. Anal. | 34000 |

- Fragmentation of relation PROJ
 - Applications:
 - ◆ Find the name and budget of projects given their no.
 - ✓ Issued at three sites
 - Access project information according to budget
 - ✓ one site accesses ≤200000 other accesses >200000
 - Simple predicates
 - For application (1)

```
p_1: LOC = "Montreal"
```

$$p_2$$
: LOC = "New York"

$$p_3$$
: LOC = "Paris"

→ For application (2)

 p_4 : BUDGET \leq 200000

 p_5 : BUDGET > 200000

 $ightharpoonup Pr = Pr' = \{p_1, p_2, p_3, p_4, p_5\}$

- Fragmentation of relation PROJ continued
 - Minterm fragments left after elimination

```
m_1: (LOC = "Montreal") \land (BUDGET \leq 200000)
```

$$m_2$$
: (LOC = "Montreal") \land (BUDGET > 200000)

$$m_3$$
: (LOC = "New York") \land (BUDGET \leq 200000)

$$m_4$$
: (LOC = "New York") \land (BUDGET > 200000)

$$m_5$$
: (LOC = "Paris") \land (BUDGET \leq 200000)

$$m_6$$
: (LOC = "Paris") \land (BUDGET > 200000)

$PROJ_1$

PNO PNAME BUDGET LOC P1 Instrumentation 150000 Montreal

$PROJ_2$

| PNO | PNAME | BUDGET | LOC |
|-----|----------------------|--------|----------|
| P2 | Database Develop. | 135000 | New York |

$PROJ_4$

| PNO | PNAME | BUDGET | LOC |
|-----|---------|--------|----------|
| P3 | CAD/CAM | 250000 | New York |

$PROJ_6$

| PNO | PNAME | BUDGET | LOC |
|-----|-------------|--------|-------|
| P4 | Maintenance | 310000 | Paris |

PHF - Correctness

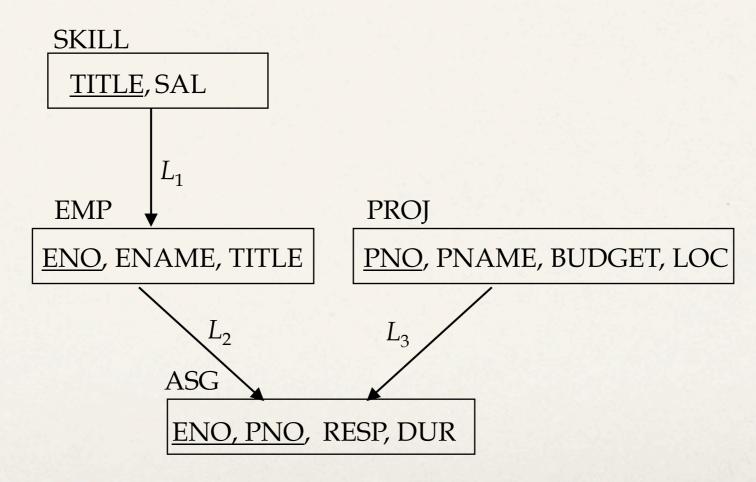
- Completeness
 - \Rightarrow Since Pr' is complete and minimal, the selection predicates are complete
- Reconstruction
 - → If relation *R* is fragmented into $F_R = \{R_1, R_2, ..., R_r\}$

$$R = \bigcup_{\forall R_i \in FR} R_i$$

- Disjointness
 - → Minterm predicates that form the basis of fragmentation should be mutually exclusive.

Derived Horizontal Fragmentation

- Defined on a member relation of a link according to a selection operation specified on its owner.
 - Each link is an equijoin.
 - Equijoin can be implemented by means of semijoins.



DHF – Definition

Given a link L where owner(L)=S and member(L)=R, the derived horizontal fragments of R are defined as

$$R_i = R \ltimes_F S_i$$
, $1 \le i \le w$

where w is the maximum number of fragments that will be defined on R and

$$S_i = \sigma_{F_i}(S)$$

where F_i is the formula according to which the primary horizontal fragment S_i is defined.

DHF – Example

Given link L_1 where owner(L_1)=SKILL and member(L_1)=EMP

 $EMP_1 = EMP \ltimes SKILL_1$

 $EMP_2 = EMP \ltimes SKILL_2$

where

 $SKILL_1 = \sigma_{SAL \leq 30000}(SKILL)$

 $SKILL_2 = \sigma_{SAL>30000}(SKILL)$

EMP_1

| ENO | ENAME | TITLE |
|-----|-----------|------------|
| ЕЗ | A. Lee | Mech. Eng. |
| E4 | J. Miller | Programmer |
| E7 | R. Davis | Mech. Eng. |

EMP_2

| ENO | ENAME | TITLE |
|-----|----------|-------------|
| E1 | J. Doe | Elect. Eng. |
| E2 | M. Smith | Syst. Anal. |
| E5 | B. Casey | Syst. Anal. |
| E6 | L. Chu | Elect. Eng. |
| E8 | J. Jones | Syst. Anal. |

DHF - Correctness

- Completeness
 - Referential integrity
 - Let R be the member relation of a link whose owner is relation S which is fragmented as $F_S = \{S_1, S_2, ..., S_n\}$. Furthermore, let A be the join attribute between R and S. Then, for each tuple t of R, there should be a tuple t' of S such that

$$t[A] = t'[A]$$

- Reconstruction
 - Same as primary horizontal fragmentation.
- Disjointness
 - Simple join graphs between the owner and the member fragments.

Vertical Fragmentation

- Has been studied within the centralized context
 - design methodology
 - physical clustering
- More difficult than horizontal, because more alternatives exist.

Two approaches:

- grouping
 - attributes to fragments
- ⇒ splitting
 - relation to fragments

Vertical Fragmentation

- Overlapping fragments
 - grouping
- Non-overlapping fragments
 - splitting

We do not consider the replicated key attributes to be overlapping.

Advantage:

Easier to enforce functional dependencies (for integrity checking etc.)

VF – Information Requirements

- Application Information
 - Attribute affinities
 - a measure that indicates how closely related the attributes are
 - ◆ This is obtained from more primitive usage data
 - → Attribute usage values
 - ♦ Given a set of queries $Q = \{q_1, q_2, ..., q_q\}$ that will run on the relation $R[A_1, A_2, ..., A_n]$,

$$use(q_{i}, A_{j}) = \begin{cases} 1 \text{ if attribute } A_{j} \text{ is referenced by query } q_{i} \\ 0 \text{ otherwise} \end{cases}$$

 $use(q_i, \bullet)$ can be defined accordingly

VF – Definition of $use(q_i, A_i)$

Consider the following 4 queries for relation PROJ

q₁:SELECT

BUDGET

q₂: **SELECT** PNAME,BUDGET

FROM

PROJ

FROM

PROJ

WHERE

PNO=Value

 q_3 :SELECT

PNAME

 q_4 : **SELECT SUM**(BUDGET)

FROM

PROJ

FROM

PROJ

WHERE LOC=Value

WHERE

LOC=Value

Let A_1 = PNO, A_2 = PNAME, A_3 = BUDGET, A_4 = LOC

VF – Affinity Measure $aff(A_i, A_j)$

The attribute affinity measure between two attributes A_i and A_j of a relation $R[A_1, A_2, ..., A_n]$ with respect to the set of applications $Q = (q_1, q_2, ..., q_q)$ is defined as follows:

$$aff(A_i, A_j) = \sum_{\text{all queries that access } A_i \text{ and } A_j}$$

query access =
$$\sum_{\text{all sites}}$$
 access frequency of a query * $\frac{\text{access}}{\text{execution}}$

VF – Calculation of $aff(A_i, A_j)$

Assume each query in the previous example accesses the attributes once

during each execution.

 S_2

Then

$$aff(A_1, A_3)$$
 = 15*1 + 20*1+10*1
= 45

and the attribute affinity matrix AA is

$$A_1$$
 A_2 A_3 A_4
 A_1 A_5 0 45 0
 A_2 0 80 5 75
 A_3 45 5 53 3
 A_4 0 75 3 78

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VF – Clustering Algorithm

- Take the attribute affinity matrix *AA* and reorganize the attribute orders to form clusters where the attributes in each cluster demonstrate high affinity to one another.
- Bond Energy Algorithm (BEA) has been used for clustering of entities.
 BEA finds an ordering of entities (in our case attributes) such that the global affinity measure is maximized.

$$AM = \sum_{i} \sum_{j}$$
 (affinity of A_i and A_j with their neighbors)

Bond Energy Algorithm

Input: The AA matrix

Output: The clustered affinity matrix *CA* which is a perturbation of *AA*

- Initialization: Place and fix one of the columns of AA in CA.
- 2 *Iteration*: Place the remaining *n-i* columns in the remaining *i*+1 positions in the *CA* matrix. For each column, choose the placement that makes the most contribution to the global affinity measure.
- 3 Row order: Order the rows according to the column ordering.

Bond Energy Algorithm

"Best" placement? Define contribution of a placement:

$$cont(A_i, A_k, A_j) = 2bond(A_i, A_k) + 2bond(A_k, A_l) - 2bond(A_i, A_j)$$

where

$$bond(A_x, A_y) = \sum_{z=1}^{n} aff(A_z, A_x) aff(A_z, A_y)$$

BEA – Example

Consider the following AA matrix and the corresponding CA matrix where A_1 and A_2 have been placed. Place A_3 :

$$AA = \begin{bmatrix} A_1 & A_2 & A_3 & A_4 \\ A_1 & 45 & 0 & 5 & 0 \\ A_2 & A_3 & 45 & 5 & 53 & 3 \\ A_4 & 0 & 75 & 3 & 78 \end{bmatrix} \quad CA = \begin{bmatrix} A_1 & A_2 \\ 45 & 0 \\ 0 & 80 \\ 45 & 5 \\ 0 & 75 \end{bmatrix}$$

Ordering (0-3-1):

$$cont(A_0, A_3, A_1)$$
 = $2bond(A_0, A_3) + 2bond(A_3, A_1) - 2bond(A_0, A_1)$
= $2*0 + 2*4410 - 2*0 = 8820$

Ordering (1-3-2):

$$cont(A_1, A_3, A_2)$$
 = $2bond(A_1, A_3) + 2bond(A_3, A_2) - 2bond(A_1, A_2)$
= $2*4410 + 2*890 - 2*225 = 10150$

Ordering (2-3-4):

$$cont(A_2, A_3, A_4) = 1780$$

BEA – Example

• Therefore, the CA matrix has the form

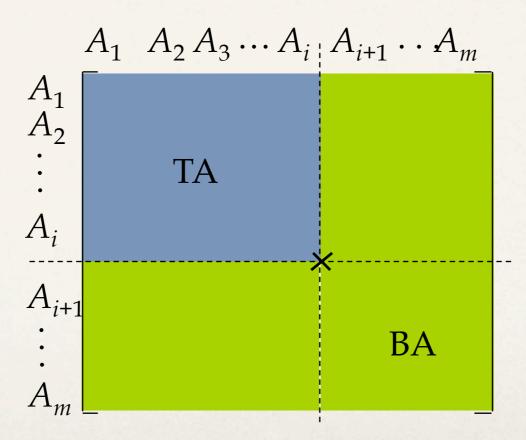
$$A_1$$
 A_3 A_2

• When A_4 is placed, the final form of the CA matrix (after row organization) is A_1 A_3 A_2 A_4

$$A_1$$
 $\begin{bmatrix} 45 & 45 & 0 & 0 \\ A_3 & 45 & 53 & 5 & 3 \\ A_2 & 0 & 5 & 80 & 75 \\ A_4 & 0 & 3 & 75 & 78 \end{bmatrix}$

VF – Algorithm

How can you divide a set of clustered attributes $\{A_1, A_2, ..., A_n\}$ into two (or more) sets $\{A_1, A_2, ..., A_i\}$ and $\{A_i, ..., A_n\}$ such that there are no (or minimal) applications that access both (or more than one) of the sets.



VF – ALgorithm

Define

TQ = set of applications that access only TA

BQ = set of applications that access only BA

OQ = set of applications that access both TA and BA

and

CTQ = total number of accesses to attributes by applications that access only TA

CBQ = total number of accesses to attributes by applications that access only BA

COQ = total number of accesses to attributes by applications that access both TA and BA

Then find the point along the diagonal that maximizes

 $CTQ^*CBQ-COQ^2$

VF – Algorithm

Two problems:

- Cluster forming in the middle of the CA matrix
 - → Shift a row up and a column left and apply the algorithm to find the "best" partitioning point
 - Do this for all possible shifts
 - \rightarrow Cost $O(m^2)$
- 2 More than two clusters
 - → m-way partitioning
 - → try 1, 2, ..., *m*–1 split points along diagonal and try to find the best point for each of these
 - \rightarrow Cost $O(2^m)$

VF - Correctness

A relation R, defined over attribute set A and key K, generates the vertical partitioning $F_R = \{R_1, R_2, ..., R_r\}$.

- Completeness
 - → The following should be true for *A*:

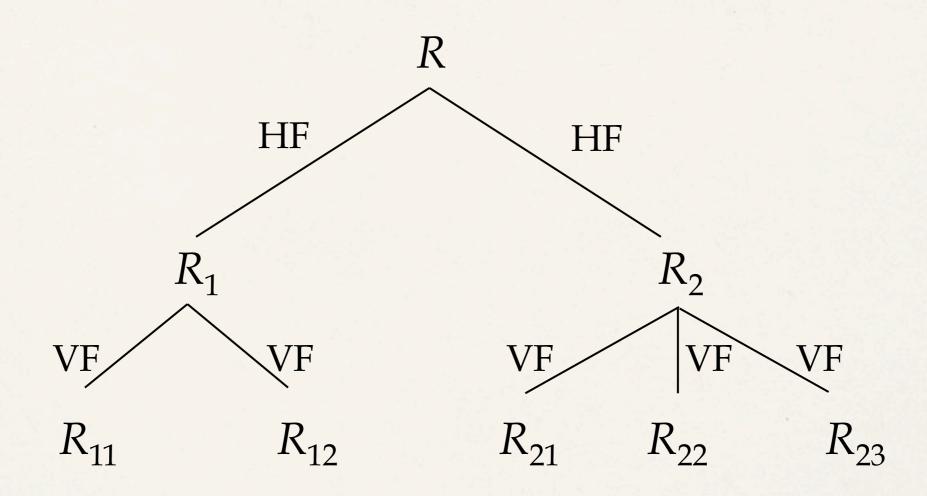
$$A = \bigcup A_{R_i}$$

- Reconstruction
 - Reconstruction can be achieved by

$$R = \bowtie K R_i, \forall R_i \in F_R$$

- Disjointness
 - ➡ TID's are not considered to be overlapping since they are maintained by the system
 - Duplicated keys are not considered to be overlapping

Hybrid Fragmentation



Fragment Allocation

Problem Statement

Given

$$F = \{F_1, F_2, ..., F_n\}$$
 fragments
 $S = \{S_1, S_2, ..., S_m\}$ network sites
 $Q = \{q_1, q_2, ..., q_q\}$ applications

Find the "optimal" distribution of *F* to *S*.

- Optimality
 - → Minimal cost
 - ◆ Communication + storage + processing (read & update)
 - Cost in terms of time (usually)
 - → PerformanceResponse time and/or throughput
 - Constraints
 - Per site constraints (storage & processing)

Information Requirements

- Database information
 - selectivity of fragments
 - ⇒ size of a fragment
- Application information
 - access types and numbers
 - access localities
- Communication network information
 - unit cost of storing data at a site
 - unit cost of processing at a site
- Computer system information
 - → bandwidth
 - → latency
 - communication overhead

Allocation

File Allocation (FAP) vs Database Allocation (DAP):

- Fragments are not individual files
 - relationships have to be maintained
- Access to databases is more complicated
 - remote file access model not applicable
 - relationship between allocation and query processing
- Cost of integrity enforcement should be considered
- Cost of concurrency control should be considered

Allocation – Information Requirements

- Database Information
 - selectivity of fragments
 - size of a fragment
- Application Information
 - number of read accesses of a query to a fragment
 - number of update accesses of query to a fragment
 - A matrix indicating which queries updates which fragments
 - → A similar matrix for retrievals
 - originating site of each query
- Site Information
 - unit cost of storing data at a site
 - unit cost of processing at a site
- Network Information
 - communication cost/frame between two sites
 - → frame size

General Form

```
min(Total Cost)
subject to
response time constraint
storage constraint
```

processing constraint

Decision Variable

$$x_{ij} = \begin{cases} 1 \text{ if fragment } F_i \text{ is stored at site } S_j \\ 0 \text{ otherwise} \end{cases}$$

Total Cost

all queries

\(\sum_{\text{all sites}} \) \(\sum_{\text{all fragments}} \) cost of storing a fragment at a site all sites

- Storage Cost (of fragment F_j at S_k)

 (unit storage cost at S_k) * (size of F_j) * x_{jk}
- Query Processing Cost (for one query)
 processing component + transmission component

• Query Processing Cost

Processing component

access cost + integrity enforcement cost + concurrency control cost

→ Access cost

 $\sum_{\text{all sites}} \sum_{\text{all fragments}} \text{(no. of update accesses+ no. of read accesses)*}$

- Integrity enforcement and concurrency control costs
 - Can be similarly calculated

• Query Processing Cost

Transmission component

cost of processing updates + cost of processing retrievals

Cost of updates

→ Retrieval Cost

min_{all sites} (cost of retrieval command + all fragments cost of sending back the result)

- Constraints
 - Response Time
 execution time of query ≤ max. allowable response time for that query
 - Storage Constraint (for a site)

storage requirement of a fragment at that site ≤ storage capacity at that site

Processing constraint (for a site)

processing load of a query at that site ≤
all queries processing capacity of that site

- Solution Methods
 - → FAP is NP-complete
 - DAP also NP-complete
- Heuristics based on
 - ⇒ single commodity warehouse location (for FAP)
 - knapsack problem
 - branch and bound techniques
 - network flow

- Attempts to reduce the solution space
 - assume all candidate partitionings known; select the "best" partitioning
 - ignore replication at first
 - sliding window on fragments