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FACULTY OF ELECTRICAL ENGINEERING
DEPARTMENT OF CYBERNETICS
MULTI-ROBOT SYSTEMS



Development of a Safe Flocking Algorithm for UAVs Using 3D Lidar and Collaborative Multi-Robot Coordination

Bachelor's Thesis

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Study programme: Electrical Engineering and Information Technology
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Bachelor's thesis title in English:

Development of a Safe Flocking Algorithm for UAVs Using 3D Lidar and Collaborative Multi-Robot Coordination

Bachelor's thesis title in Czech:

Vývoj bezpečného algoritmu pro koordinaci UAV pomocí 3D lidar a koordinace více robotů

Guidelines:

- (1) Develop a safe flocking algorithm for UAVs in C++ within the MRS system framework. The algorithm must ensure collision-free and efficient movement of UAV.
- (2) Compare your solution to some of the most promising algorithms in the literature within the MRS simulator, in particular [1],[2],[3].
- (3) The novel contributions of the thesis will include
 - i) Extend existing multi-robot algorithm from 2d to 3d.
 - ii) Use 3d lidar to localize, sense, process, and react to environments such as a forest.
 - iii) Research on possible enhancements of the algorithm for example using neural networks or learning-based techniques.
- (4) Conduct an experimental campaign to validate the theoretical findings. Include different real-world scenarios, such as navigating through forests or crowded spaces.

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Abstract

The study of autonomous Unmanned Aerial Vehicles (UAVs) has become a prominent sub-field of mobile robotics.

Keywords TODOUnmanned Aerial Vehicles, Automatic Control

Abbreviations

LiDAR Light Detection and Ranging

UAV Unmanned Aerial Vehicle

UGV Unmanned Ground Vehicle

ToF Time-of-Flight

PCL Point Cloud Library

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■ 1 Introduction

TODO

■ 1.1 Related works

TODO

■ 1.2 Contributions

TODO

■ 1.3 Mathematical notation

TODO

\mathcal{N}_i	set of neighboring agents for the i -th agent
$\mathbf{x}, \boldsymbol{\alpha}$	vector, pseudo-vector, or tuple
$\hat{\mathbf{x}}, \hat{\boldsymbol{\omega}}$	unit vector or unit pseudo-vector
$\hat{\mathbf{e}}_1, \hat{\mathbf{e}}_2, \hat{\mathbf{e}}_3$	elements of the <i>standard basis</i>
$\mathbf{X}, \boldsymbol{\Omega}$	matrix
\mathbf{I}	identity matrix
$x = \mathbf{a}^\top \mathbf{b}$	inner product of $\mathbf{a}, \mathbf{b} \in \mathbb{R}^3$
$\mathbf{x} = \mathbf{a} \times \mathbf{b}$	cross product of $\mathbf{a}, \mathbf{b} \in \mathbb{R}^3$
$\mathbf{x} = \mathbf{a} \circ \mathbf{b}$	element-wise product of $\mathbf{a}, \mathbf{b} \in \mathbb{R}^3$
$\mathbf{x}_{(n)} = \mathbf{x}^\top \hat{\mathbf{e}}_n$	n^{th} vector element (row), $\mathbf{x}, \mathbf{e} \in \mathbb{R}^3$
$\mathbf{X}_{(a,b)}$	matrix element, (row, column)
x_d	x_d is <i>desired</i> , a reference
$\dot{x}, \ddot{x}, \dot{\ddot{x}}, \ddot{\ddot{x}}$	1 st , 2 nd , 3 rd , and 4 th time derivative of x
$x_{[n]}$	x at the sample n
$\mathbf{A}, \mathbf{B}, \mathbf{x}$	LTI system matrix, input matrix and input vector
$SO(3)$	3D special orthogonal group of rotations
$SE(3)$	$SO(3) \times \mathbb{R}^3$, special Euclidean group

Table 1.1: Mathematical notation, nomenclature and notable symbols.

■ 2 Extension of the Rule-Based Lloyd Algorithm to 3D

■ 2.1 Introduction

TODO

■ Motivation

Motivation in using RBL algo instead of some other algorithm

■ Problem Statement

Problems in the transition from 2d to 3d - algo needs to be fast

■ Objectives

Extend the algorithm to 3D, do some experiments that are succesfull - show that algo works also for 3d tasks

■ Chapter Overview

Summary of what this chapter covers

■ 2.2 Overview of RBL - TODO rename

■ Overview

The algorithm is a communication-less approach designed to navigate agents from point A to point B. It relies on global positioning data, such as GPS or alternative methods for obtaining global coordinates, combined with sensor inputs that provide information about the agent's environment. These sensors can include LiDAR, depth cameras, or standard cameras with estimation techniques, allowing the agent to detect and avoid obstacles or other agents. The algorithm enables autonomous navigation without requiring direct communication between agents, making it suitable for scalable and decentralized applications.

■ Applications and Limitations in 2D

Modern robotics relies on the capability to navigate from point A to point B. Navigation plays a crucial role in various robotic applications, such as Unmanned Ground Vehicle (UGV)s, which are commonly used in manufacturing and logistics. UGVs typically follow predefined 2D trajectories guided by visual [6], magnetic [9], or LiDAR-based navigation [8]. Additionally, 2D navigation is widely employed in robotic vacuum cleaners, enabling them to systematically cover an area while avoiding obstacles.

An obvious limitation for algorithms in 2D is scalability. As the number of agents in a system increases, the complexity of managing their movements and coordination also grows significantly. Obstacle avoidance in 2D can also be less efficient compared to 3D environments,

as agents have fewer options for evading obstacles. In 3D, agents can change their altitude in addition to their horizontal trajectory, giving them more freedom to maneuver around obstacles.

■ Key principles

RBL, as presented in the original paper [1], ensures convergence to the goal and provides sufficient conditions for achieving it. The problem involves individual control of N agents from their initial position $\mathbf{p}_i(0)$ toward a goal region, represented as circle. This goal region is denoted as $G(\mathbf{g}_i, r_g)$, where \mathbf{g}_i is center and r_g is radius of goal region. The agent is progressing towards its designated destination, \mathbf{d}_i . Each agent knows its current position \mathbf{p}_i , encumbrance δ_i , which determines safe space around agent. Additionally, each agent also knows the positions and encumbrances of its neighboring agents \mathcal{N}_i , agent $j \in \mathcal{N}_i$ if $\|\mathbf{p}_i - \mathbf{p}_j\| \leq 2r_{s,i}$, where $r_{s,i}$ is denoted as half of the sensing radius of the i -th agent. For simplicity $r_{s,i}$ is considered to be same for all agents, therefore $r_{s,i} = r_s$.

The core objective of the algorithm is to minimize the coverage cost function, which accounts for the distribution of agents and obstacles over the environment. This function is expressed as:

$$J_{cov}(\mathbf{p}) = \sum_{i=1}^N \int_{\mathcal{V}_i} \|\mathbf{q} - \mathbf{p}_i\|^2 \varphi_i(\mathbf{q}) d\mathbf{q}, \quad (2.1)$$

where \mathbf{p}_i is the position of agent i , \mathcal{V}_i is the Voronoi cell of the i -th robot, $\|\mathbf{q} - \mathbf{p}_i\|^2$ is squared Euclidian distance between point in the mission space $\mathbf{q} \in \mathcal{Q}$ and agent's position \mathbf{p}_i , and $\varphi_i(\mathbf{q})$ is the weighting function.

Voronoi cell is defined as:

$$\mathcal{V}_i = \{\mathbf{q} \in \mathcal{Q} \mid \|\mathbf{q} - \mathbf{p}_i\| \leq \|\mathbf{q} - \mathbf{p}_j\|, \forall j \neq i\} \quad (2.2)$$

For visual representation see Fig. 2.1a. However, this standard definition of Voronoi cells does not take into account the physical space occupied by the agents, or their encumbrances. To address this, a Modified Voronoi cell is introduced, which takes into account the encumbrances of agents. This modified version adjusts the boundaries of each Voronoi cell to account for the encumbrances of neighboring agents. The modified Voronoi cell definition is as follows:

$$\tilde{\mathcal{V}}_i = \begin{cases} \{\mathbf{q} \in \mathcal{Q} \mid \|\mathbf{q} - \mathbf{p}_i\| \leq \|\mathbf{q} - \mathbf{p}_j\|\}, & \text{if } \Delta_{ij} \leq \frac{\|\mathbf{p}_i - \mathbf{p}_j\|}{2} \\ \{\mathbf{q} \in \mathcal{Q} \mid \|\mathbf{q} - \mathbf{p}_i\| \leq \|\mathbf{q} - \tilde{\mathbf{p}}_j\|\}, & \text{otherwise,} \end{cases} \quad (2.3)$$

$\forall j \in \mathcal{N}_i$, where $\Delta_{ij} = \delta_i + \delta_j$ and $\tilde{\mathbf{p}}_j = \mathbf{p}_j + 2(\Delta_{ij} - \frac{\|\mathbf{p}_i - \mathbf{p}_j\|}{2}) \frac{\mathbf{p}_i - \mathbf{p}_j}{\|\mathbf{p}_i - \mathbf{p}_j\|}$. Together with cell \mathcal{S}_i defined as:

$$\mathcal{S}_i = \{\mathbf{q} \in \mathcal{Q} \mid \|\mathbf{q} - \mathbf{p}_i\| \leq r_{s,i}\} \quad (2.4)$$

the cell \mathcal{A}_i is obtained as $\mathcal{A}_i = \tilde{\mathcal{V}}_i \cap \mathcal{S}_i$.

Convergence to goal region $G(\mathbf{g}_i, r_g)$ depends on the choice of weighting function that assigns weights to points \mathbf{q} in the mission space \mathcal{Q} . The weighting function $\varphi_i(\mathbf{q})$ is defined as follows:

$$\varphi_i(\mathbf{q}) = \exp\left(-\frac{\|\mathbf{q} - \mathbf{d}_i\|}{\beta_i}\right), \quad (2.5)$$

where β_i is the weighting factor for points \mathbf{q} , and \mathbf{d}_i represents the current destination of the agent. The destination is computed as follows:

$$\mathbf{d}_i = \mathbf{p}_i + R(\theta)(\mathbf{g}_i - \mathbf{p}_i) \quad (2.6)$$

where R is the azimuthal rotation. Rules:

■ **Weighting rule**

$$\dot{\beta}_i(A_i) = \begin{cases} -k & \text{if } \beta_i > \beta_{min} \wedge \|\mathbf{c}_{A_i} - \mathbf{p}_i\| < d_1 \wedge \|\mathbf{c}_{A_i} - \mathbf{c}_{S_i}\| > d_2 \\ 0 & \text{if } \beta_i > \beta_{min} \wedge \|\mathbf{c}_{A_i} - \mathbf{p}_i\| < d_1 \wedge \|\mathbf{c}_{A_i} - \mathbf{c}_{S_i}\| > d_2 \\ -(\beta_i - \beta_i^D) & \text{otherwise} \end{cases} \quad (2.7)$$

where the first case decreases β_i over time, the second case ensures that β_i does not decrease below its minimum threshold β_{min} (saturation) and the third case provides a general update rule when the previous conditions are not met.

■ **Azimuth rule**

$$\dot{\theta}_i = \begin{cases} k & \text{if } \theta < \frac{\pi}{2} \wedge \|\mathbf{c}_{A_i} - \mathbf{c}_{S_i}\| > d_4 \wedge \|\mathbf{p}_i - \mathbf{c}_{A_i}\| > d_3 \\ -k & \text{if } \theta > 0 \wedge \neg(\|\mathbf{c}_{A_i} - \mathbf{c}_{S_i}\| > d_4 \wedge \|\mathbf{p}_i - \mathbf{c}_{A_i}\| > d_3) \\ 0 & \text{otherwise} \end{cases} \quad (2.8)$$

where the first case increases θ_i over time, the second case ensures that θ_i converges back when the distance constraints are not satisfied, and the third case keeps θ_i unchanged.

■ **Azimuth reset rule**

$$\theta = 0 \text{ if } \theta = \frac{\pi}{2} \wedge \|\mathbf{p}_i - \bar{\mathbf{c}}_{A_i}\| \quad (2.9)$$

where $\bar{\mathbf{c}}_{A_i}$ represents the centroid computed from the cell A_i , which is weighted using the unrotated destination, meaning $\mathbf{d}_i = \mathbf{g}_i$.

Weighted centroid is computed as follows:

$$\mathbf{c}_{A_i} = \frac{\int_{A_i} \mathbf{q} \varphi_i(\mathbf{q}) d\mathbf{q}}{\int_{A_i} \varphi_i(\mathbf{q}) d\mathbf{q}}, \quad (2.10)$$

where \mathbf{q} represents the point in mission space, and $\varphi_i(\mathbf{q})$ is a weighting function.

By applying the previously defined rules and computations, the RBL algorithm successfully guides agents movement toward the goal. However, these rules focus solely on rotating the centroid A_i in the azimuthal plane. To enhance performance in a fully three-dimensional space, additional rules are required to account for elevation adjustments.

■ **Agressivity of RBL alog TODO rename**

modification of cell A so it can move closer to objects - cwvd parameters

■ **2.3 Extension of the RBL algorithm to 3D**

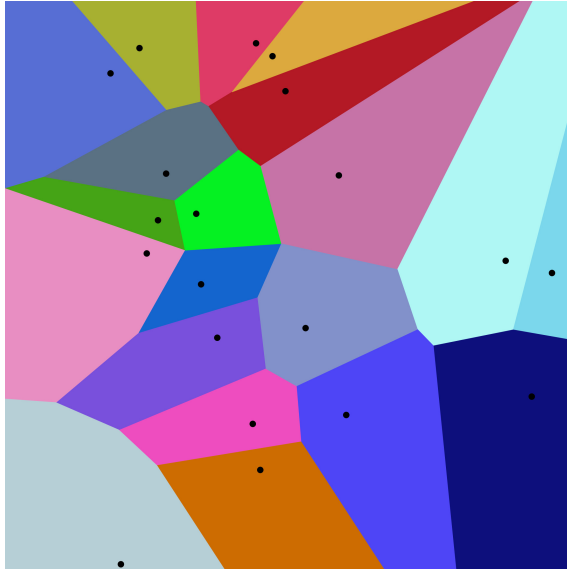
■ **Motivation for 3D Extension**

In many practical applications, agents must operate in three-dimensional spaces, considering not only horizontal movement but also vertical positioning. A 3D extension is necessary

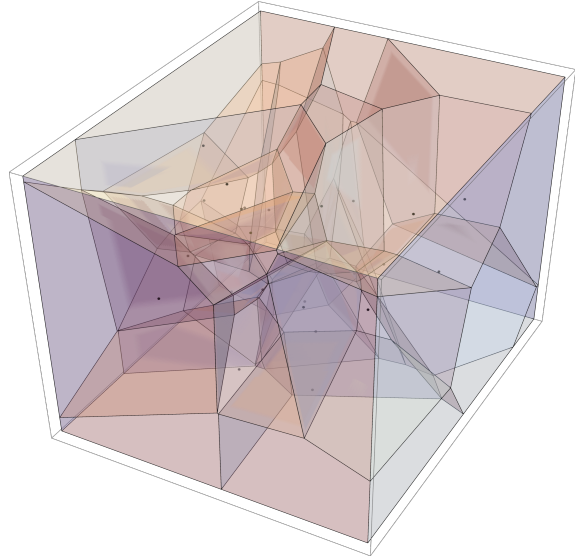
to navigate complex environments that feature obstacles in all directions. In 2D, agents are restricted to a flat plane, which simplifies navigation but limits the ability to interact with objects and environments that exist in the third dimension. The ability to utilize vertical space can enhance energy efficiency, as agents can optimize their paths by ascending or descending to avoid obstacles or to find more favorable environmental conditions, such as discovering more open space. The transition from 2D to 3D also opens up possibilities for more advanced movement strategies, such as navigating through multi-level environments or optimizing trajectories by utilizing vertical space. Moreover, the use of 3D models allows for more accurate representations of real-world scenarios, where elevation plays a crucial role in decision-making and task execution.

■ Differences between 2D and 3D

The primary distinction in the 3D extension is that each goal region is now represented as a sphere rather than a circle. Similarly, the sensing cell \mathcal{S}_i is also modeled as a sphere instead of a circle, allowing for a more accurate representation of the Unmanned Aerial Vehicle (UAV)'s perception in three-dimensional space. This change introduces a key modification when defining \tilde{V}_i : in the 2D case, a line was sufficient to slice the sensing region, whereas in 3D, a plane must be computed to properly segment the spherical sensing cell.



(a) Euclidean Voronoi Diagram in 2D



(b) Euclidean Voronoi Diagram in 3D

Figure 2.1: (a) an example of 20 Voronoi cells in 2D [4] (b) 25 Voronoi cells in 3D [5]

■ Additional Constraints and Modifications

For the 3D case, several modifications are introduced. Firstly, $Z_{clipping}$ is applied to each sensing cell \mathcal{S}_i , constraining it within the vertical limits defined by \min_z and \max_z :

$$\mathcal{S}_i = \{\mathbf{q} \in \mathcal{Q} \mid \|\mathbf{q} - \mathbf{p}_i\| \leq r_{s,i}, \quad \min_z \leq q_z \leq \max_z\} \quad (2.11)$$

where \min_z and \max_z define the vertical bounds within which the sensing region \mathcal{S}_i is restricted. This ensures that the UAV cannot exceed these limits, as it follows the computed

centroid \mathbf{c}_{V_i} . By constraining the sensing radius, the UAV remains confined within the specified region, preventing it from moving outside the vertical interval \min_z to \max_z .

Secondly, Z_{rule} is introduced to enhance UAV avoidance. Rule rotates computed centroid by ϕ

$$\dot{\phi}_i(A_i) = \begin{cases} \text{sgn}(\omega_i) \cdot dt, & \text{if } \|\mathbf{c}_{A_i} - \mathbf{p}_i\|_z < d_6 \wedge \|\mathbf{c}_{S_i} - \mathbf{c}_{A_i}\|_z > d_5 \\ \vee (\|\mathbf{p}_i - \mathbf{c}_{S_i}\|_{xy} - \|\mathbf{p}_i - \mathbf{c}_{A_i}\|_{xy}) > d_7, \\ -\text{sgn}(\phi_i) \cdot dt, & \text{otherwise.} \end{cases} \quad (2.12)$$

where the directional influence ω_i is given by a weighted combination:

$$\omega_i = \frac{w_1 \cdot \|\mathbf{c}_{S_i} - \mathbf{p}_i\|_z + w_2 \cdot \left(\frac{\theta_i}{\pi} - 1\right)}{w_1 + w_2}, \quad (2.13)$$

with

$$\theta_i = \text{atan2}(g_x - p_{ix}, g_y - p_{iy}), \quad (2.14)$$

ensuring it remains in $[0, 2\pi]$. The weights w_1 and w_2 balance the contribution of vertical distance and directional influence.

Convergence Back to Zero If no condition for modification is met, ϕ converges back to zero:

$$\dot{\phi}_i = \begin{cases} -dt, & \phi_i > 0, \\ dt, & \phi_i < 0, \\ 0, & \phi_i = 0. \end{cases} \quad (2.15)$$

Constraint on ϕ A constraint ensures that vertical avoidance does not increase separation:

$$\phi_i = 0, \quad \text{if } |\phi_i| = \frac{\pi}{4} \wedge \|\mathbf{p}_i - \mathbf{c}_{S_i}\|_z > \|\mathbf{p}_i - \mathbf{c}_{A_i}\|_z. \quad (2.16)$$

This ensures that if vertical modification makes the drone farther from the reference, it is reset.

■ 2.4 Simulation and Results Analysis

Description of simulation environment, used tools, Description of few simulation scenarios and result analysis.

■ Simulation Environment

The term 'agent' refers to the UAVs used in the simulation. For this simulation, I relied on the framework provided by [2] Each UAV obtains its global position from the ROS simulator, RViz. The positions of other UAVs were estimated using blinking LEDs mounted on each UAV, based on the method outlined in [11]. Below, I list some relevant constraints for each UAV:

Parameter	Value
Maximal horizontal velocity [m s^{-1}]	4.0
Horizontal acceleration [m s^{-2}]	2.0
Maximal ascending velocity [m s^{-1}]	2.0
Vertical ascending acceleration [m s^{-2}]	1.0
Maximal descending velocity [m s^{-1}]	2.0
Vertical descending acceleration [m s^{-2}]	1.0

Table 2.1: Motion constraints of the UAV.

■ Simulation Scenarios

Several experiments were conducted to evaluate and ensure the safe behavior of the UAVs during interactions. Different sets of UAVs were used in these experiments, with $N = 5, 10$, and 15 , and data was collected from them for analysis. Each UAV was first flown from ground to its initial position, and once all UAVs were in their starting positions, the RBL algorithm was initiated.

For most agent interactions, experiments were conducted in both circular and spherical formations, with the circular formation being initially conducted in [1]. The circular formation was chosen as it promotes more predictable and consistent interactions between agents, as opposed to random initial positions and goal locations, which could lead to less structured or less frequent interactions. Similarly, the spherical formation was introduced to extend the experiment into 3D, providing a more comprehensive test scenario. Both structured formations help to better evaluate the performance of the RBL algorithm in environments where agents are more likely to encounter each other. The UAVs were evenly distributed along the perimeter of the circle or the surface of the sphere. The goal position was placed on the opposite side of the circle or sphere. The radius of both the circle and the sphere was set to 5 meters.

TODO table of parameters used for this experiment. Sensing radius $r_s = 4.5\text{m}$, update rate 10 Hz, encumbrance 0.5 m, $d1 = d3 = d5 = 0.5$, $d2 = d4 = d6 = 1.0$. For $z_{clipping} - min_z = 1.0$ m, $max_z = 10.0$

In the next tables

■ $N = 5$ circular

	SR [%]	\bar{L} [m]	\bar{t} [s]	\bar{t}_{\max} [s]	\bar{v} [m/s]
RBL 2D	100.00	21.06 ± 0.10	25.15 ± 0.21	25.15 ± 0.19	0.83 ± 0.01
RBL 3D	100.00	20.77 ± 0.29	26.04 ± 0.51	26.79 ± 0.27	0.79 ± 0.02
RBL 3D _{clipped}	100.00	20.60 ± 0.24	26.73 ± 0.47	27.39 ± 0.28	0.77 ± 0.02
RBL 3D _z	100.00	20.97 ± 0.52	25.54 ± 0.97	26.72 ± 0.60	0.81 ± 0.03

■ **N = 10 circular**

	SR [%]	\bar{L} [m]	\bar{t} [s]	\bar{t}_{\max} [s]	\bar{v} [m/s]
RBL 2D	100.00	22.95 ± 1.64	30.79 ± 2.28	34.73 ± 0.77	0.74 ± 0.07
RBL 3D	100.00	22.22 ± 0.89	30.05 ± 2.61	34.39 ± 4.19	0.73 ± 0.05
RBL 3D _{clipped}	100.00	22.31 ± 0.69	30.22 ± 1.83	33.22 ± 0.93	0.73 ± 0.04
RBL 3D _z	100.00	22.38 ± 0.88	28.80 ± 2.30	32.35 ± 1.25	0.77 ± 0.05

■ **N = 15 circular**

	SR [%]	\bar{L} [m]	\bar{t} [s]	\bar{t}_{\max} [s]	\bar{v} [m/s]
RBL 2D	100.00	23.56 ± 1.75	33.89 ± 2.48	38.75 ± 1.45	0.69 ± 0.06
RBL 3D	100.00	22.36 ± 0.97	30.65 ± 3.07	35.77 ± 3.72	0.72 ± 0.07
RBL 3D _{clipped}	100.00	22.32 ± 0.81	30.69 ± 2.61	34.50 ± 0.47	0.72 ± 0.06
RBL 3D _z	100.00	22.64 ± 0.95	29.67 ± 2.54	34.27 ± 0.88	0.76 ± 0.06

■ **N = 10 sphere**

	SR [%]	\bar{L} [m]	\bar{t} [s]	\bar{t}_{\max} [s]	\bar{v} [m/s]
RBL 2D	100.00	00.00 ± 0.00	00.00 ± 0.00	00.00 ± 0.00	0.00 ± 0.00
RBL 3D	100.00	00.00 ± 0.00	00.00 ± 0.00	00.00 ± 0.00	0.00 ± 0.00
RBL 3D _{clipped}	100.00	00.00 ± 0.00	00.00 ± 0.00	00.00 ± 0.00	0.00 ± 0.00
RBL 3D _z	100.00	00.00 ± 0.00	00.00 ± 0.00	00.00 ± 0.00	0.00 ± 0.00

■ **Practical Experiment Setup**

■ **Comparisons**

■ **2.5 Summary and Key Insights**

Recap of modifications. Faced challenges and solutions applied

■ 3 UAV Navigation Using the RBL Algorithm and LiDAR Sensing

■ 3.1 Introduction

TODO

■ Motivation

The importance of UAV navigation in environments with obstacles

■ Problem Statement

Challenges of UAV movement using LiDAR-based sensing

■ Objectives

Implementing RBL with LiDAR for obstacle avoidance and path planning

■ Chapter Overview

Summary of what this chapter covers

■ 3.2 LiDAR-Based Perception and Point Cloud Processing

■ Overview of LiDAR for UAV Navigation

Light Detection and Ranging (LiDAR) is a crucial sensing technology widely used in applications such as SLAM [13], autonomous vehicles [10], UAVs TODOcite, and precision agriculture [3]. It provides high-resolution spatial data about the surrounding environment, making it a valuable tool for perception and navigation in dynamic and complex environments. For UAV applications, LiDAR serves several essential functions:

- **3D Mapping** – Capturing a detailed representation of terrain, structures, and obstacles.
- **Obstacle Detection** – Identifying objects and estimating their position relative to the UAV for collision avoidance.
- **Autonomous Path Planning** – Assisting navigation algorithms by providing spatial information for decision-making.
- **Terrain Following** – Helping the UAV maintain a safe altitude by detecting variations in ground elevation.

LiDAR offers several benefits that make it an attractive choice for UAV-based navigation:

- **High Accuracy** – Provides precise distance measurements, crucial for obstacle avoidance and localization.
- **Environment Agnostic** – Functions effectively in various conditions, including low-light environments and featureless terrain where cameras may fail.

- **Fast Data Acquisition** – Captures thousands to millions of points per second, enabling real-time processing.
- **Rich Depth Information** – Unlike cameras that provide only 2D images, LiDAR generates accurate depth data, improving spatial awareness and 3D perception.

Despite its advantages, LiDAR also presents certain challenges and limitations:

- **Computational Complexity** – Processing large point clouds in real-time requires significant computational power, which may be a limitation for UAVs with low processing resources.
- **Sensor Noise and Artifacts** – External factors such as vibrations and motion of UAV can introduce errors in point cloud data.
- **Limited Field of View (FoV)** – The placement of the LiDAR sensor on the UAV affects its coverage, requiring strategies to compensate for blind spots.
- **Environmental Interference** – Performance may degrade in challenging conditions such as fog, rain, or dense vegetation due to light deviation.
- **Power Consumption** – LiDAR sensors can consume a significant amount of power, which reduces the overall flight time of the UAV.
- **Interference with Other LiDARs** – LiDAR sensors can experience interference when multiple units are used nearby, potentially leading to faulty measurements.

■ Point Cloud Data Acquisition

LiDAR systems determine object distances by emitting laser pulses and measuring the time it takes for the reflected light to return. This process, known as Time-of-Flight (ToF), involves scanning the environment with laser beams directed at varying horizontal and vertical angles. The reflected light, modulated in intensity, phase, or frequency, is captured by a receiver, which uses a lens to focus the signal onto a photodetector. This detector converts the light into an electrical signal via the photoelectric effect [7].

The system calculates distance based on the light's travel time, considering its near-light-speed propagation. To distinguish transmitted from received signals, the laser's wavelength is often adjusted. Subsequent signal processing filters and analyzes the electrical signal, accounting for surface material and environmental variations. The output is a 3D point cloud representing the scanned environment, along with reflected laser energy intensities. All these data points are stored in a ROS message of type *sensor_msgs :: PointCloud2*.

■ Preprocessing Techniques

To efficiently process LiDAR data and reduce computational complexity, the raw point cloud undergoes downsampling and filtering. The point cloud density is reduced using a voxel grid filter. Subsequently, points associated with the UAV's structure are removed based on its known encumbrance.

- **Voxel Grid Downsampling** – The raw LiDAR point cloud often contains a large number of points, which can be computationally expensive to process in real-time. To address this, we apply a voxel grid filter using the Point Cloud Library (PCL) [12]. This method partitions the 3D space into a grid of voxels with a given resolution (leafSize) and retains a single representative point per voxel. The filtering process reduces the number of points while preserving the overall structure of the environment.
- **Filtering Points Corresponding to the UAV Structure** – LiDAR sensors mounted on UAVs can capture unwanted points originating from the UAV itself, such as reflections

from its frame or rotor rods. To prevent these points from interfering with navigation, additional filtering step has been applied. Each point in the downsampled cloud is converted to an Eigen 3D vector for easy mathematical operations. The Euclidean distance between each point in pointcloud and the UAV's position \mathbf{p}_i is computed. Points within a predefined encumbrance radius around the UAV are discarded to remove self-detected points.

TODO add images of not downsampled and downsampled and close up on the uav

The resulting filtered point cloud contains only relevant environmental features while eliminating unnecessary points, improving efficiency in decision-making processes.

■ Surface Reconstruction and Triangulation

To obtain a continuous surface representation from the point cloud, normal estimation and triangulation are performed. This process involves estimating surface normals, combining them with point positions, and applying a triangulation algorithm to generate a polygonal mesh.

- **Normal Estimation** – Surface normals are estimated using the Point Cloud Library (PCL) `TODOCite`. A k-d tree is employed to efficiently find neighboring points, and the normal at each point is computed based on its local neighborhood. This provides information about the surface curvature and orientation.
- **Point Cloud and Normal Merging** – Once the normals are estimated, they are combined with the original point cloud to create a representation that includes both spatial position and surface orientation.
- **Triangulation Using Greedy Projection** – The point cloud is converted into a polygonal mesh using the `**Greedy Projection Triangulation (GP3)**` method. This algorithm forms triangles between neighboring points while enforcing constraints on edge length, surface angles, and normal consistency. A k-d tree is used to accelerate the search for nearest neighbors, ensuring efficient mesh generation.
- **Results** – The output is a polygonal mesh that approximates the underlying surface of the point cloud. This mesh can be used for visualization, collision detection, or further geometric processing.

Greedy Projection Triangulation (GP3), pcl lib and parametres Generating triangular mesh - How GP3 constructs a surface from point cloud data

■ 3.3 Using the found triangles for cell A partition

TODO

■ Overview

the next step is to utilize these triangles to partition the navigation space, specifically modifying cell A for the RBL algorithm. This process ensures that the UAV has a structured representation of obstacles and free space.

- Finding the Closest Point on a Triangle
- Plane Calculation for Slicing Cell A
- Integration with the RBL Algorithm
- 3.4 Implementation and Integration on UAV

TODO

- Challenges in Integration



(a) A UAV, the T650 model.

Figure 3.1: TODO just place holder, put livox mounted on the drone

For modification of cell A 2 planes are defined using real knowledge of how LiDAR is mounted on the uav and livox vertical fov Let $\mathbf{e}_z = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$ be the unit vector along the z-axis, $R_{\text{off}} \in SO(3)$ the offset rotation, and $R_{\text{rpy}} \in SO(3)$ the roll-pitch-yaw rotation. $\alpha_1, \alpha_2, \alpha_3$

Then the resulting vector is given by:

$$\mathbf{n} = R_{\text{rpy}} \cdot R_{\text{off}} \cdot \mathbf{e}_z$$

Modified cell S:

$$\mathcal{S}_i = \tag{3.1}$$

livox - 360 * 60 deg - account for centroid calculation

- Software and Hardware setup

LiDAR sensor config, uav platform specifications

- 3.5 Simulation and Experimental Results

TODO

- Simulation Setup

virtual environment modeling, tools used

■ Performance in Simulated Environments

Success rates, obstacle avoidance, efficiency metrics - same as in the rbl

■ Real-World Experiments in a Forest Environment

■ Comparative Analysis

Simulation vs. real-world performance

■ 3.6 Conclusion

TODO Summary of contributions and some directions for future research

REDO after this

■ 3.7 Introduction

Motivation for using 3d lidar and challenges

■ 3.8 3D LiDAR Sensor Model and Simulation Setup

Overview of LiDAR used. Simulation configuration

■ 3.9 Object Detection and Approximation

Methods for extracting objects from LiDAR point clouds. Approximating detected objects with simple shapes. Handling noisy or incomplete data

[3D Surface Approximation from Point Clouds](#) ← This one seems promising. I would like to try this.

[Alpha Shape: A Generalization of the Convex Hull](#)

■ 3.10 Integration with RBL Algorithm

Modifications to ensure safe navigation and how approximated objects influence Voronoi cells

■ 3.11 Simulation Results

Example scenarios - in rviz with drone and also in real life - me holding a branch with leafs or something like that

■ 3.12 Discussion

Limitations and possible improvements

■ 3.13 Summary

■ 4 Researching on possible enhancements of the algorithm for example using neural networks or learning-based techniques.

tune the parameters of RBL to suit 3D

I will have to read something first, but what I found is that I could try object detection and classification using models like [PointNet](#), [PointNet++](#) or [VoxelNet](#)

Pointcloud denoising

Segmentation of LiDAR data. [RangeNet++](#), [SalsaNext](#) to differentiate between terrain trees and free space

NN approaches for approximating point clouds with simple convex shapes:

[CvxNet: Learnable Convex Decomposition](#) by Deng et al. (CVPR 2020)

[Label-Efficient Learning on Point Clouds using Approximate Convex Decompositions](#) by Gadelha et al. (Arxiv 2020)

[Region Segmentation via Deep Learning and Convex Optimization](#) by Sonntag and Morgenshtern (Arxiv 2019)

[Point Density-Aware Voxels for LiDAR 3D Object Detection](#)

■ 5 Conclusion

Summarize the achieved results. Can be similar as an abstract or an introduction, however, it should be written in past tense.

6 References

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■ A Appendix A