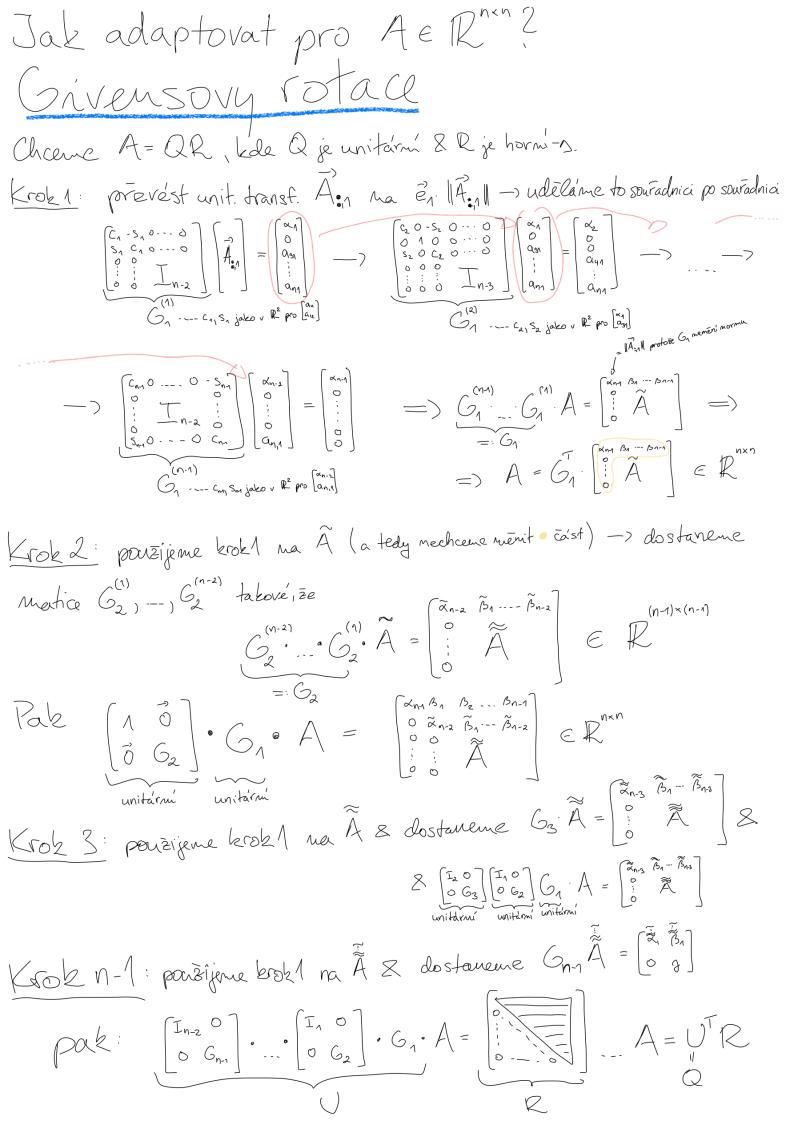
Preduáska 19 -	QR faletorizace II.
opácko - chceme algoritums bude stabilm 2	na výpotet A = QP, Etery' používa uniterní transformace
MA-QRN C C. Emach UFQQN & C. Emach	vypocet probable aplikaci transf. matic X'',, X''', fi X''' X''' A = R & X''' = V + e
- Oboje motivovaho mune	
$\frac{1}{\sqrt{2}}$	-> chai majit unitarmi matice Q=UT OB Majaké vijeR -> pak A=QR & R= [0, r2]
m) jale vyuntoval versor per provi	CEFlexe podél printy Survailour que
$A_{s_1} = \ A_{s_1}\ \cdot e_1$ $A_{s_1} = \ A_{s_1}\ \cdot e_1$	$A_{i,1} = A_{i,1} \cdot e_1$
Lingebral: $U = \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix}$ Odvozen: Hedejme $V = \begin{bmatrix} c-s \\ s & c \end{bmatrix}$, Pak	$ \overrightarrow{e_1} \cdot \overrightarrow{A_{i,1}} \times \sqrt{2} \cdot \overrightarrow{e_1} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{q} \cdot \overrightarrow{A_{i,1}} = \overrightarrow{q} \cdot $

 $= \| \overrightarrow{A}_{\mathbf{s}_1} \| \cdot \overrightarrow{e_1}$ Lingdoal
Ain na suerq= $\vec{A}_{i,1} = \vec{q} \cdot \vec{q}^T \vec{A}_{i,1}$)= I-2qq, $\bigcup A_{\bullet, 1} = \left[S \cdot \alpha_{11} + C \cdot \alpha_{12} \right] = \left[O \right]$ volba @ m > odpavída drážku výše) $=) \begin{array}{c} C = Q_{11} / \sqrt{Q_{11}^2 + Q_{12}^2} \\ =) \\ S = -Q_{12} / \sqrt{Q_{11}^2 + Q_{12}^2} \\ \end{array} \begin{array}{c} | \text{Volba} \stackrel{\leftarrow}{\bullet} | \text{m} > \text{odpovide} \\ \text{evolba} \stackrel{\leftarrow}{\bullet} | \text{m} > \text{odpovide} \\ \text{evolute} \text{ is possible osy} \\ \text{followe's te' na obrazku} \end{array}$ chai stabilitu \rightarrow t_j : <u>ne dai</u> delit $\approx 0 =$) \Rightarrow dai velkou l'Il dole $= > \overrightarrow{Q} = \frac{\overrightarrow{A}_{:,1} + sgn(a_{ii}) \cdot \overrightarrow{e}_{1} \cdot || \overrightarrow{A}_{:,1} ||}{|| \overrightarrow{A}_{:,1} + sgn(a_{ii}) \cdot \overrightarrow{e}_{1} \cdot || A_{:,1} ||}|$



Householderovy reflexe

Krok 1: porevest unit transf. A:1 Ma e1. || A:1 || $Z H_1 := \overline{1} - 2 \vec{q}_1 \vec{q}_1 \qquad pak \qquad H_1 A = \begin{bmatrix} q_1 & q_2 & \dots & q_{n-1} \\ \vdots & \widetilde{A} & \dots & q_{n-1} \\ \vdots & \widetilde{A} & \dots & q_{n-1} \end{bmatrix}$ $\underbrace{\downarrow}_{2} \widetilde{A} = \begin{bmatrix} \widetilde{\gamma}_{1} & \widetilde{\gamma}_{1} & \dots \widetilde{\gamma}_{r_{n-2}} \\ \vdots & \widetilde{A} \end{bmatrix}$ unitarmí & H2:= I - 2 q2 q2 m> pak $= > \underbrace{\begin{bmatrix} I_{1} & O \\ O & H_{2} \end{bmatrix}}_{\text{unitarni}} \cdot \underbrace{H_{1}}_{1} A = \underbrace{\begin{bmatrix} (e_{1} & V_{1} & V_{2} & \cdots & V_{n-1} \\ o & \widetilde{e}_{1} & \widetilde{e}_{1} & \cdots & \widetilde{e}_{n-2} \\ \vdots & \vdots & \widetilde{e}_{n} & \widetilde{e}_{n} & \cdots & \widetilde{e}_{n-2} \\ \vdots & \vdots & \widetilde{e}_{n} & \widetilde{e}_{n} & \widetilde{e}_{n} \end{bmatrix}}_{\text{unitarni}}$

Stabilita výpoch:

pro Householder-QR i Givens-QR plati.

NA-QRN < C. Emad. NAN . NI-QRN < C. Emad.

Porovnám ceny výpoch: pobud aj + D + j Chouseholder ~ 3n3+ O(n2) m, ale pokud maine A Fidhon (rebo aspon její spodní-s Edst), pak Givensovy

rotace nemus: clélat v seehny operace m, lze pocitat pouze pro +0 prvky - u House holdera nikoliv, tam v zdy pozitáme stejme.

Aplikace na resem AZ=5:

/ samostatue spocitaime A=QR a poté resime RX = QTB pri výpoctu A=QR aplikujeme matice G; nebo Hi zároven i ma príslusnou cast pravé strany B m> to vlastné odpovída aplikaci Ginebolli na [AIB] -> dostaveme [RiZ] a vyresine $\mathbb{Z}\vec{x}=\vec{c}$.

Analogické výpočtu LU-faktorízace vs. Ganssové eliminaci coby aplikaci LU.