

BACHELOR THESIS

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Modern evolutionary strategies for reinforcement learning problems

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Dedication. It is nice to say thanks to supervisors, friends, family, book authors and food providers.

Title: Modern evolutionary strategies for reinforcement learning problems

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Abstract: Abstracts are an abstract form of art. Use the most precise, shortest sentences that state what problem the thesis addresses, how it is approached, pinpoint the exact result achieved, and describe the applications and significance of the results. Highlight anything novel that was discovered or improved by the thesis. Maximum length is 200 words, but try to fit into 120. Abstracts are often used for deciding if a reviewer will be suitable for the thesis; a well-written abstract thus increases the probability of getting a reviewer who will like the thesis.

Keywords: evolutionary strategies reinforcement learning novelty search neuroevolution



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Introduction

Reinforcement learning has been getting a lot of publicity in recent years, including competing with the best players in DotA 2 [1], playing Texas hold'em poker [2] or mastering Go, chess, shogi and other games [3]. Other than that reinforcement learning has been applied to many domains such as robot control [4], energy consupmtion optimisation [5]...

Chapter 1 Important first chapter

Chapter 2

Theory

2.1 Reinforcement learning

The key problem that reinforcement learning is trying to solve is controlling an *agent* in an *environment*. The agent interacts with the environment by selecting some action and the environment responds by presenting the agent with a new situation. The environment also provides a numerical reward to the agent whose task is to maximise it over time.

More formally, the agent interacts with the environment in discrete (if the problem has continuous time, it is discretised) time steps $t=1,2,3,\ldots$. At each time step the agent receives $S_t \in \mathcal{S}$, a representation of internal state of the environment. Based on that it selects an action $A_t \in \mathcal{A}$. This results in the agent receiving a reward $R_{t+1} \in \mathcal{R} \subset \mathbb{R}$ in addition to a new state S_{t+1} in the next step generating a sequence or *trajectory* beginning like this:

$$S_0, A_0, R_1, S_1, A_1, R_2, S_2, A_2, R_3, \dots$$
 (2.1)

The random variables S_t and R_t depend only on the preceding state and action based on function $p: \mathcal{S} \times \mathcal{R} \times \mathcal{S} \times \mathcal{A} \rightarrow [0, 1]$ characterising *dynamics* of the problem with following definition:

$$p(s', r|s, a) = \Pr\{S_t = s', R_t = r|S_{t-1} = s, A_{t-1} = a\}.$$
(2.2)

This can, however, be viewed as an restriction on information contained in state rather than restriction on the environment. If the state does contain all information that influence the future then it has the *Markovian property* and the problem at hand is a *Markov decision process*.

To formally describe what is the goal of reinforcement learning expected return G_t needs to be defined first. It is a function of the reward sequence, in the

simplest case an ordinary sum of rewards

$$G_t = \sum_{i=t+1}^T R_i, \tag{2.3}$$

where T is the final time step.

This approach works only if the there is a final step in the interaction which would divide the interaction into subsequences called *episodes*. Each episodes ends when the environment reaches a *terminal state* and is reset into its initial state afterwards. Such tasks are called *episodic tasks*.

Contrary to that there are tasks which do not break into episodes, they continue indefinitely. They are called *continuing tasks* For these the definition 2.3 doesn't work as the sum could possibly be infinite. To calculate expected reward for such tasks a modified approach is needed. A *discount rate* $\gamma \in [0,1]$ is introduced to define *discounted return*

$$G_t = \sum_{i=0}^{\infty} \gamma^i R_{t+i+1}. \tag{2.4}$$

The discount rate makes future reward worth less at the moment of decision. If $\gamma < 1$ and the reward are bounded, then the infinite sum 2.4 is finite. For $\gamma = 0$ the agent is said to be "myopic" taking into account only the immediate reward and ignoring the future. Otherwise as γ approaches 1 the future rewards have bigger weight and influence the agent's decision more. Succesive returns are related in a way

A common occurrence in reinforcement learning is an estimating *value function* which estimate how beneficial it is for the agent to be in that state. This is defined by the expected return which is dependent on the actions that the agent will perform. Therefore a value function must be defined with respect to such way of acting called *policy*.

Policy is a function $\pi: \mathcal{S} \times \mathcal{A} \to [0,1]$ returning probability of selecting each action in given state meaning that agent following policy π at time t would select action $A_t = a$ if in state $S_t = s$ with probability $\pi(a|s)$. The policy function is changed by reinforcement learning based on the agent's experience.

For state s and policy π the *state-value function* $v_{\pi}(s)$ gives the expected return when starting in state s and following policy π , formally (for MDPs)

$$v_{\pi}(s) = \mathcal{E}_{\pi}[G_t|S_t = s],$$
 (2.5)

where $E_{\pi}[.]$ is expected value when following policy π in every timestep.

Action-value function $q_{\pi}(s, a)$ for policy π is defined similarly. It gives the expeted return of taking action a in state s while following policy π , formally

$$q_{\pi}(s, a) = \mathcal{E}_{\pi}[G_t | S_t = s, A_t = a].$$
 (2.6)

[6]

2.1.1 Methods

Methods of reinforcement learning can be divided into 3 categories:

- classical (tabular),
- · policy gradient-based and
- · evolutionary.

Classical methods rely on updating *Q-values* for each state-action pair therefore they require having discrete sets of actions and states. Based on the Q-values a policy is derived, such as an ε -greedy policy which (in training) chooses a random action with probability ε and the currently best action in all other cases. One of the most well known algorithms is *Q-learning*. In it the Q-values are updated each step via following formula:

$$q(s_t, a_t) = q(s_t, a_t) + \alpha \left(r_t + \gamma \max_{a} q(s_{t-1}, a) - q(s_t, a_t) \right),$$
 (2.7)

where α is the learning rate.

Algorithm 1 Q-Learning

```
1: parameters: learning rate \alpha \in (0, 1]
 2: initialise: q(s,a) for all s \in \mathcal{S} and a \in \mathcal{A} arbitrarily, except for
    q(terminal, \cdot) = 0
3: for each episode do
        initialise s \in \mathcal{S}
 4:
        repeat
 5:
             choose a from s using policy derived from q
 6:
             take action a, observe s', r
 7:
             q(s, a) = q(s, a) + \alpha \left(r + \gamma \max_{a} q(s', a) - q(s, a)\right)
8:
 9:
        until s is terminal state
10:
11: end for
```

Policy-gradient based methods are methods that utilise the gradient in policy space. They are one of the few optimisation strategies able to handle reinforcement learning tasks that are high-dimensional and have continuous state and action space. One of the most known algorithms from this group is *REINFORCE*.

Another, not as known, class of policy-gradient based algorithms are PEPG (Parameter exploring policy gradient).[7] They use samples from parameter

Algorithm 2 REINFORCE

```
1: parameters: step size \alpha>0

2: input: differentiable policy parametrisation \pi(a|s,\theta)

3: initialise: policy parameters \theta atrbitrarily

4: for each episode do

5: generate S_0, A_0, R_1, \ldots, S_{T-1}, A_{T-1}, R_T by following \pi(\cdot|\cdot,\theta)

6: for each timestep t \in \{0, 1, \ldots, T-1\} do

7: G = \sum_{k=t+1}^{T} \gamma^{k-t-1} R_k

8: \theta = \theta + \alpha \gamma^t G \nabla \ln \pi(A_t, S_t, \theta)

9: end for

10: end for
```

space to estimate the log-likelyhood on parameter level. In traditional policy gradient methods the policy is probabilistic, it returns a distribution from which the next action is selected and final gradient is calculated by differentiating the policy with respect to parameters. This however causes high variance in samples over more episodes thus a noisy gradient estimate. PEPG circumvent this issue by having a probability distribution over policy parameters with a deterministic policy.

Evolutionary methods utilise only *fitness* describing the overall performance of the agent. Exploration is done via changing parameters that influence the agent's behaviour. However the basis of this class of algorithms is not derived from the mathematical principles of reinfocement learning. They are further described in following chapters.

2.2 Evolutionary algorithms

Evolutionary algorithms (EA) are a type of optimisation metaheuristics inspired by the process of bilogical evolution. At first a number of possible solutions to the problem at hand is generated (population) and each solution (individual) is encoded (via a domain-specific encoding) and evaluated giving us the value of its fitness. Fitness is a function describing how good that particular individual is and it is everything that is needed for creation of Then a new population is created using a crossover (combination) of 1 or more individuals which are selected using the operator of parental selection. Each of the newly created individuals has a chance to be mutated via the mutation operator. Finally a new population is selected from offsprings and possibly the parents based of fitness and enters the next iteration of the EA and the following generation is chosen using environmental selection operator. The algorithm repeats until the stop condition is

Algorithm 3 PGPE (Policy Gradients with Parameter-based Exploration) with symmetric sampling

```
1: parameters: step size \alpha > 0, number of histories n
 2: initialise: \mu, \sigma (both n dimensional) to preselected initial values, m=0
            for i \in 1, \ldots, n do
 4:
                  sample \epsilon^i \sim \mathcal{N}(0, I\sigma^2)
 5:
                  \theta^+ = \mu + \epsilon^i
 6:
                  \theta^- = \mu - \epsilon^i
 7:
                  evaluate policies \pi(\cdot|\cdot,\theta^+) and \pi(\cdot|\cdot,\theta^-) and get rewards r^{+i},r^{-i}
 8:
 9:
            end for
            Set matrix T as T_{ij} = \epsilon_i^j
10:
            Set matrix S as S_{ij} = \frac{(\epsilon_i^j)^2 - \sigma_i^2}{\sigma_i}
11:
           r_T = [(r^{+1} - r^{-1}), \dots, (r^{+n} - r^{-n})]^T
r_S = [\frac{(r^{+1} + r^{-1})}{2}, \dots, \frac{(r^{+n} + r^{-n})}{2}]^T
Update \mu = \mu + \alpha T r_T
12:
13:
14:
            Update \sigma = \sigma + \alpha S r_S
16: until stop criterion is fullfilled
```

met, usually a set number of iterations or small improvement of fitness between 2 generations.

There are many variands of EAs such as genetic algorithms (most common), genetic programming, evolutionary programming, neuroevolution or evolutionary strategies that are further described in following chapter. [8] [9]

2.3 Evolutionary strategies

Evolutionary strategies (ES) are a type of optimisation metaheuristic which further specialises EA and restricts their level of freedom. The selection for crossover is unbiased, mutation is parametrised and thus controllable, individuals which should be put to next generation are chosen ordinally based on fitness and individuals contain not only the problem solution but also control parameters.

More formally ES $(\mu/\rho,\kappa,\lambda)$ has μ individuals in each generation, which produces λ offsprings, each created by crossover of ρ individuals and each individual is able to survive for up to κ generations as described in algorithm 5. This notation further generalizes the old (μ,λ) and $(\mu+\lambda)$ notations, where the "," notation means $\kappa=1$ and "+" notation $\kappa=\infty$.

Algorithm 4 Evolutionary algorithm

```
1: initialize population P^0 with n individuals
 2: set t = 0
 3: repeat
       Q^t = \{\}
 4:
       for i \in \{1 ... m\} do
 5:
            p_1, \ldots, p_{\rho} = ParentalSelection(P^t)
 6:
            q = Crossover(p_1, \dots, p_{\rho})
 7:
            q = Mutation(q) with chance p
 8:
            Q^t = q \cup Q^t
        end for
10:
        P^{t+1} = EnvironmentalSelection(Q^t \cup P^t)
11:
        increment t
12.
13: until stop criterion fullfilled
```

To design an ES one must first select an appropriate representation for an individual and the most natural one is prefered in most cases, if all parameters are of one type (e.g. a real number) a simple vector will suffice, if the types are mixed, a tuple of vectors is required. This however causes an increased complexity of the variation operator.

As for design of the variation operator there are some guidelines that should be followed when designing it.

Reachability every solution should be reachable from any other solution in a finite number of applications of the variation operator with probability p > 0

Unbiasedness the operator should not favour any particular subset of solution unless provided with information about problem at hand

Control the operator should be parametrised in such way that the size of the distribution can be controlled (practice had shown that decreasing it as the optimal solution is being approached is necessary)

A big part of designing efficient evolutionary strategy algorithms is adapting the covariance matrix of the used multivariate normal distribution that is commonly used as variation operator. It is assumed that setting the covariance matrix Σ of the distribution proportional to the inverse Hessian matrix of Taylor expansion of the fitness function. This would align the hyperellipsoid of equal probabilities of the mutation distribution with the hyperellipsoid of equal fitness values.[10][8]

Algorithm 5 $(\mu/\rho, \kappa, \lambda)$ -ES

```
1: initialize population P^0 with \mu individuals
      2: set age for each p \in P^0 to 1
      3: set t = 0
                   repeat
                                                Q^t = \{\}
      5:
                                                for i \in \{1 \dots \lambda\} do
     6:
                                                                        select \rho parents p_1, \ldots, p_{\rho} \in P^t uniformly at random
     7:
                                                                         q = variation(p_1, \dots, p_o) with age 0
                                                                        Q^t = q \cup Q^t
      9:
                                                  end for
10:
                                                 P^{t+1} = \text{select } \mu \text{ best (wrt. fitness) individuals from } Q^t \cup \{p \in P^t : p 
11:
                       age(p) < \kappa
                                                increment age by 1 for each p \in P^{t+1}
12:
13:
                                                increment t
14: until stop criterion fullfilled
```

2.3.1 CMA-ES

The aforementioned idea is used in Covariance Matrix Adaptation Evolutionary Strategy algorithm. In it the population of new individuals is generated by sampling a multivariate normal distribution. The individuals are sampled via following equation for generation $t \in \mathbb{N}_0$:

$$x_k^{t+1} \sim m^t + \sigma^t \mathcal{N}(0, C^t), \ k \in \{1, 2, \dots, \lambda\},$$
 (2.8)

where

 x_k^{t+1} is k-th individual from generation t+1,

 m^t is mean value of the search distribution at generation t,

 σ^t is the step size at generation t,

 C^t is the covariance matrix at generation t and

 λ is the population size.

At each step the mean is moved to the weighted average of μ selected individuals (parents) from the current generation. The individuals are selected based on their fitness and the weights are parameters of the algorithm. Then the covariance matrix C^t is updated using the covariance matrix from previous generation, the evolution steps and the new individuals. To control the step size σ^t only information from evolution steps is used.[11]

2.4 Evolutionary strategies as replacement for reinfocement learning

Black-box optimisation is an alternative approach to solving RL tasks also known as Direct policy search or neurevolution when applied to neural networks. It has several attractive properties such as indifference to distribution of rewards, no need for backpropagation and tolerance of arbitrarily long episodes.

Compared to reinfocement learning using evolutionary strategies has the advantage of not needing a gradient of the policy performance. Also as the state transition function is not known the gradient can't be computed using backpropagation-like algorithm. Thus some noise needs to be added to make the problem smooth and the gradient to be estimable. Here is where reinfocement learning and evolutionary strategies differ, reinfocement learning adds noise in the action space (actions are chosen from a distribution) while evolutionary strategies add noise in the parameter space (parameters perturbed while actions are deterministic).

Not requiring backpropagation has several advantages over other RL methods. First the amount of computation necessary for one episode of ES is much lower (about one third, potentially even less for memory usage). Not calculating gradient using analytic methods also protects these methods from suffering from *exploding gradient* which is a common issue with recurrent neural networks. And last, the network can contain elements that are not differentiable such as hard attention.

Also ES are easily paralellisable. First, contrary to RL, where value function is inherently linear procedure and has to be performed more times to improve a given policy. Furthermore it operates on whole whole episodes, therefore it does not require frequent communication between workers. And finally, as the only information received by each worker is the reward, it is possible to communicate only the reward inbetween workers. That, however, requires synchronising seeds known to other workers beforehand and recreating perturbations based on that information. Thus the required is extremely low comapred to communication of whole gradients which would be required for paralellisation of a policy gradient based algorithm.

2.4.1 OpenAI Evolutionary Strategy

These ideas are explored in OpenAI-ES algorithm. The agent acting in the envrionment is represented be a policy π_{θ} with parameter vector θ and $f(\cdot)$ is the reward returned by the environment. As we need to introduce some noise, the population is distribution $p_@y$ is instantiated as an an isotropic multivariate Gaussian

with mean ψ and covariance $\sigma^2 I$. Then $\mathbb{E}_{\theta \sim p_{\psi}} f(\theta) = \mathbb{E}_{\epsilon \sim N(0,I)} f(\theta + \sigma \epsilon)$. Thus the gradient approximation is calculated as follows:

$$\nabla_{\theta} \mathbb{E}_{\theta \sim p_{\psi}} f(\theta) = \nabla_{\theta} \mathbb{E}_{\epsilon \sim N(0,I)} f(\theta + \sigma \epsilon) \approx \frac{1}{n\sigma} \sum_{i=1}^{n} f(\theta_{i}) \epsilon_{i}, \tag{2.9}$$

where $\theta_i = \theta + \sigma \epsilon_i$, $\epsilon_i \sim N(0, I)$ and n is the population size.

The resulting algorithm uses SGD (or Stochastic Gradient Ascent - SGA in this case) or other gradient based optimisation technique for parameter vector θ update.

Algorithm 6 OpenAl-ES

```
1: Input: Learning rate \alpha, noise standard deviation \sigma, initial policy parameters
    \theta_0, n number of workers
 2: initialize n workers with known random seeds, and initial parameters \theta_0
 3: set t = 0
 4: repeat
         for i \in \{1 \dots n\} do
 5:
              sample \epsilon_i \sim \mathcal{N}(0, I)
              compute returns f_i = f(\theta_t + \sigma \epsilon_i)
 7:
         end for
 8:
         Send all scalar returns f_i from each worker to every other worker
 9:
         for i \in \{1 ... n\} do
10:
              reconstruct all perturbations \epsilon_j for j \in \{1, \dots, n\} using known ran-
11:
              set \theta_{t+1} = \theta_t + \alpha \frac{1}{n\sigma} \sum_{i=1}^n f_i \epsilon_i
12:
         end for
13:
         increment t
15: until stop criterion fullfilled
```

As the ES could be seen as method for computing a derivative estimate using finite differences in randomly chosen direction it would suggest that it would scale poorly with dimensions of parameters θ same as the finite differences method. In theory the number of necessary optimisation steps should scale linearly with the dimension. That however doesn't mean that larger networks optimised using ES will perform worse than smaller ones, that depends on the difficulty (intrinsic dimension) of the problem. The network will perform the same however it will take more optimisation steps to do so.

In practice ES performs slightly better on larger networks and it is hypothesised that it is for the same reason as why it is easier to optimise large networks

using standard gradient based methods: larger networks have fewer local minima

Due to perturbing the parameters and not the actions ES are invariant to the frequency at which the agent acts in the envirionment. Tradtional MDP-based reinforcement learning methods rely on *frameskip* as one their parameters that is crucial to get right for the optimization to be successful. While this is solvable for problems that do not require long term planning and actions, long term strategic behaviour poses a challenge and reinfocement learning needs hiearchy to be successful unlike evolutionary strategy. [12]

2.4.2 Novelty search

While the main drive in of improvement in ES is the value of fitness (how "good" the result is), novelty search takes a different approach. Novelty search is focused on finding different solutions, as it is inspired by nature's drive towards diversity. Each policy has its novelty calculated with respect to previous policies and search is directed to parts of search space with high novelty. This approach makes it less succeptible to local optima created by deceptive rewards than reward-based method.

Each policy π gets assigned its domain-dependent behavorial characteristics $b(\pi)$ (e.g. final position of the agent) and it is added to an archive set A of characteristics of previous policies. Then the novelty $N(b(\pi_{\theta}),A)$ is calculated as average distance from k nearest neighbours from the archive set A.

$$N(\theta, A) = N(b(\pi_{\theta}), A) = \frac{1}{|S|} \sum_{j \in S} \|(\pi_{\theta}) - b(\pi_{j})\|_{2}$$

$$S = kNN(b(\pi_{\theta}), A)$$
(2.10)

Combination with evolution strategies

To find and follow the gradient of expected novelty with respected to θ^t we use the framework outlined in 2.4.1.

With archive A and sampled parameters $\theta_t^i = \theta_t + \sigma \epsilon_i$, the gradient estimate can be calculated via following formula:

$$\nabla_{\theta_t} \mathbb{E}_{\epsilon \sim \mathcal{N}(0,I)}[N(\theta_t + \sigma \epsilon)|A] \approx \frac{1}{n\sigma} \sum_{i=1}^n N(\theta_t^i, A) \epsilon_i$$
 (2.11)

It is possible because archive A is fixed during one iteration and is updated only at the end. Only characteristics corresponding to each θ^t are added to A, as adding each sampled would cause the archive A to inflate too much increasing the complexity of calculation of nearest-neighbours.

To encourage additional diversity an initial meta-population of M, selection of M is domain dependent, agents is created. While it is possible to optimise the behaviour of a single agent and reward it for behaving differently than its ancestors, this way we get the benefits of population-based exploration. Each agent has parameters θ^m and is being rewarded for behaviour different from all prior agents, thus we get M differently behaving policies.

Describe?

M random parameter vectors are initialised and in each iteration one is selected to be updated. The selection probability is proportional to its novelty.

$$P(\theta^m) = \frac{N(\theta^m, A)}{\sum_{i=1}^M N(\theta^i, A)}$$
(2.12)

To perform the update step, we need to calculate the gradient estimate of expected novelty with respect to θ_t^m using equation 2.11 where n is the number of perturbations. When we get the gradient estimate we use SGD (or in this case Stochastic Gradient Ascent) with learning rate α to update the parameters θ^m

$$\theta_{t+1}^m := \theta^m + \alpha \frac{1}{n\sigma} \sum_{i=1}^n N(\theta_t^{i,m}, A) \epsilon_i.$$
 (2.13)

After updating the individual, a new behaviorial characteristics $b(\pi_{\theta_{t+1}^m})$ is calculated and added to the archive A.

This process is repeated for a predetermined number of times as novelty search is not supposed to converge to a "best" solution and returns the best performing policy which is being preserved during the run of the algorithm.

Combination with reward based exploration

While NS-ES helps agents avoid local optima and deceptive reward signals, it also completly discards reward which might cause the performance to suffer. Therefore NSR-ES, an improved version of NS-ES, uses both reward (fitness) and novelty for computation of the update step. NSR-ES is in many ways similar to NS-ES, it calculates both novelty and reward at once and it operates on entire episodes. The only difference is, that the calculation of the gradient estimate is based on the average of reward and novelty.

Specifically, for parameter vector $\theta_t^{m,i} = \theta_t^m + \sigma \epsilon_i$ we calculate the reward $f(\theta_t^{m,i})$ and novelty $N(\theta_t^{m,i}, A)$, rank-normalise both values independently (as both values usually have completely different scales), calculate the average and set it as weight for corresponding ϵ_i for gradient estimation. Then the estimated gradient is used to update the parameter vector via SGD (or other gradient based optimisation method) simirally as in equation 2.13:

$$\theta_{t+1}^m := \theta^m + \alpha \frac{1}{n\sigma} \sum_{i=1}^n \frac{N(\theta_t^{i,m}, A) + f(\theta_t^{i,m})}{2} \epsilon_i.$$
 (2.14)

Algorithm 7 NS-ES

19:

20:

21: end for

end for

```
1: Input: Learning rate \alpha, noise standard deviation \sigma, initial policy parameters
    \theta_0, n number of workers, T number of iterations
 2: initialize n workers with known random seeds, empty archive A, and initial
    parameters \{\theta_0^1,\ldots,\theta_0^M\}
 3: set t = 0
 4: for i \in \{1 ... M\} do
         calculate b(\pi_{\theta_0^i})
         add b(\pi_{\theta_n^i}) to A
 6:
 7: end for
 8: for t \in \{0 \dots T - 1\} do
         sample \theta_t^m from \{\theta_t^1, \dots, \theta_t^M\}
         for i \in \{1 \dots n\} do
10:
               sample \epsilon_i \sim \mathcal{N}(0, I)
11:
               compute characteristics b(\theta_t^m + \sigma \epsilon_i)
12:
               compute n_i = N(b(\theta_t^m + \sigma \epsilon_i), A)
13:
          end for
14:
         Send all novelties n_i from each worker to every other worker
15:
         for i \in \{1 ... n\} do
16:
               reconstruct all perturbations \epsilon_j for j \in \{1, \dots, n\} using known ran-
17:
    dom seeds
              set \theta^m_{t+1} = \theta^m_t + \alpha \frac{1}{n\sigma} \sum_{j=1}^n n_i \epsilon_i add b(\theta^m_{t+1}) to A
18:
```

Intuitively, following the approximated gradient based on both novelty and reward directs the search areas of the parameter-space with both high novelty and reward. This can, however, be improved further.

While NSR-ES uses a linear combination of reward and novelty to approximate that is static for the whole duration of the training. Contrary to that NSRAdapt-ES (NSRA-ES) dynamically changes the ratio of reward gradient $f(\theta_t^{i,m})$ and novelty gradient $N(\theta_t^{i,m}, A)$ based on how the training is currently progressing. This way, it will give more weight to the reward (thus following the performance gradient) when making progress and more weight to the novelty (following novelty gradient) when stuck in a local optima to give more incentive to find different approaches.

Formally, a parameter w is used to control the ratio of reward and novelty used for calculation of gradient estimate. For a specific w at a given generation

Algorithm 8 **NSR-ES**

```
1: Input: Learning rate \alpha, noise standard deviation \sigma, initial policy parameters
     \theta_0, n number of workers, T number of iterations
 2: initialize n workers with known random seeds, empty archive A, and initial
     parameters \{\theta_0^1,\ldots,\theta_0^M\}
 3: set t = 0
 4: for i \in \{1 ... M\} do
          calculate b(\pi_{\theta_0^i})
          add b(\pi_{\theta_0^i}) to A
 7: end for
 8: for t \in \{0 \dots T - 1\} do
          sample \theta_t^m from \{\theta_t^1,\dots,\theta_t^M\}
          for i \in \{1 \dots n\} do
10:
               sample \epsilon_i \sim \mathcal{N}(0, I)
11:
               compute characteristics b(\theta_t^m + \sigma \epsilon_i)
12:
               compute n_i = N(b(\theta_t^m + \sigma \epsilon_i), A)
13:
               compute f_i = f(\theta_t^m + \sigma \epsilon_i)
14:
15:
          end for
          Send all novelties and rewards n_i, f_i from each worker to every other
16:
          for i \in \{1 ... n\} do
17:
               reconstruct all perturbations \epsilon_j for j \in \{1, \dots, n\} using known ran-
18:
     dom seeds
               set \theta^m_{t+1}=\theta^m_t+lpharac{1}{n\sigma}\sum_{j=1}^nrac{n_i+f_i}{2}\epsilon_i add b(\theta^m_{t+1}) to A
19:
20:
          end for
```

parameter vector θ_t^m is updated (SGD used) via following expression:

$$\theta_{t+1}^m := \theta_t^m + \alpha \frac{1}{n\sigma} \sum_{i=1}^n (1-w) N(\theta_t^{i,m}, A) \epsilon_i + w f(\theta_t^{i,m}) \epsilon_i.$$
 (2.15)

[13]

22: end for

21:

Algorithm 9 NSRA-ES

```
1: Input: Learning rate \alpha, noise standard deviation \sigma, initial policy parameters
     \theta_0, n number of workers, T number of iterations
 2: initialize n workers with known random seeds, empty archive A, and initial
     parameters \{\theta_0^1, \dots, \theta_0^M\}
 3: set t = 0, t_{best} = 0, f_{best} = -\infty
 4: for i \in \{1 ... M\} do
          calculate b(\pi_{\theta_0^i})
          add b(\pi_{\theta_0^i}) to A
 7: end for
 8: for t \in \{0 \dots T - 1\} do
          sample \theta_t^m from \{\theta_t^1, \dots, \theta_t^M\}
 9:
          for i \in \{1 \dots n\} do
10:
               sample \epsilon_i \sim \mathcal{N}(0, I)
11:
               compute characteristics b(\theta_t^m + \sigma \epsilon_i)
12:
               compute n_i = N(b(\theta_t^m + \sigma \epsilon_i), A)
13:
               compute f_i = f(\theta_t^m + \sigma \epsilon_i)
14:
          end for
15:
          Send all novelties and rewards n_i, f_i from each worker to every other
16:
     worker
          for i \in \{1 ... n\} do
17:
               reconstruct all perturbations \epsilon_i for j \in \{1, \dots, n\} using known ran-
18:
     dom seeds
               set \theta_{t+1}^m = \theta_t^m + \alpha \frac{1}{n\sigma} \sum_{j=1}^n \frac{n_i + f_i}{2} \epsilon_i
19:
               add b(\theta_{t+1}^m) to A
20:
          end for
21:
          if f(\theta_{t+1}^m) > f_{best} then
22:
               w = max(1, w + \delta_w)
23:
               f_{best} = f(\theta^m_{t+1})
24:
               t_{best} = 0
25:
          else
26:
               t_{best} + = 1
27:
          end if
28:
          if t_{best} \geq t_w then
29:
               w = min(0, w - \delta_w)
30:
               t_{best} = 0
31:
32:
          else
          end if
33:
34: end for
```

Chapter 3 Results and discussion

Conclusion

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