Implementation of a Linear Session Type System

Second assignment of the Languages for Concurrency and Distribution, A.Y. 2023/2024

Christian Micheletti July 5, 2024



Outline



- 1 Structure
 - Session Types
 - Software features
- 2 Language
 - Syntax
 - Runtime
- 3 Types
 - Basic types

Session Types



The paper Fundamentals of Session Types presents a π -calculus equipped with a (linear) type system to check against errors that the system can incur into.

Such language features linear types, which allow checking whether a given channel is used by exactly one process.

Session Types - The π -calculus



This π -calculus' features are incrementally presented through five sections:

- basics and fundamentals features, as scope restriction, in sections 2 and 3;
- recursive types, needed to write useful unrestricted types, in section 4;
- unbounded computations, in section 5, that enable infinite behaviours;
- **branching and selection**, in section 6 (not implemented).

The implementation process follows this very same organization, and will be presented accordingly.

Software features



The software is written in Haskell and it features:

- a code interpreter, that executes the code in Concurrent Haskell;
- a **type checker**, parallelized using the Eval monad;
- a type inferrer.

The paper has several examples of the expected behaviour of the type checker, that are implemented here as unit tests to avoid regressions.

Language - Process Syntax



Chapter 2's original syntax Implementation

$$P := \overline{x} v.P$$

$$x(x).P$$

$$P \mid P$$
if $v \text{ then } P \text{ else } P$

$$0$$

$$(\nu \times x)P$$

Language - Precomputation



After parsing, the program is precomputed lifting all bindings over all parallel compositions, as expressed in the following **structural congruence**:

$$(\nu xy)P|Q \equiv (\nu xy)(P|Q)$$

Language - Operational Semantics



The code interpreter prints debug information about the program executed, along with a timestamp and a description of what the process did at that time.

Output format

[TIMESTAMP | ThreadId THREAD_ID]: MESSAGE

Program behaviour is defined according to the **operational semantics** presented in chapter 2.

Runtime - Concurrent Haskell



The language runtime is implemented in concurrent Haskell, using:

- the IO monad, along with a local state that maps variables to channels and literals, to model threads;
- and the MVar type to model channels.

Each thread is created with the

forkIO :: IO () -> IO ThreadId

function, that simply creates a new thread, returning its id.

Runtime - Channels (1/2)



Plain MVars can await for value insertion with the function

but the dual operation

does not await the variable to be ready to accept a new value.

Runtime - Channels (2/2)



Channels are represented as tuples of MVar, meaning (value, idle):

- value :: MVar v, containing the passed value, which needs to be evaluated;
- idle :: MVar (), which has a () value in it when the channel is ready to receive.

Then, the Channel datatype further distinguishes whether it is a read end or a write end. Read ends and write ends share the same MVars.

Runtime - Program Behaviour (1/3)



Inaction

The process 0 just prints STOP and ends the thread.

Branching

The process if v then P_1 else P_2 prints two debug messages, both starting with BRANCHING:

- the guard before evaluation;
- and then, after evaluation in the local state.

After that, the run continues as the appropriate process.

Runtime - Program Behaviour (2/3)



Binding

The process $(\nu xy).P$ just prints BINDING followed by the two bounded variables. Then, it creates two MVars, one for the value and one for the lock and associates in the local state both variables with the respective ends.

The run proceeds in the same thread as prescribed by P.

Fork

The process $P_1|P_2$ prints FORK followed by the two new processes ids.

To prevent a concurrent program to end before all forked threads terminate, this code constructs two MVars that are notified when the two new threads finish. This process doesn't do anything more than awaiting for both threads to finish.

Runtime - Program Behaviour (3/3)



Sending

The process $\overline{x}v.P$ prints SENDING followed by the value:

- before evaluation;
- and after evaluation.

Then the process sends the value over the channel x and proceeds as prescribed by P.

Receiving

The process x(v).P prints RECEIVING followed by:

- the newly bound variable name;
- and the value received.

Then the process proceeds as prescribed by P.

Basic Types - Syntax



Implementation of qualifier, pretypes and types are fully compliant to Chapter 3's original syntax:

$$q ::= lin$$
 $T :== bool$
 un end
 $p ::= ?T.T$ qp
 $!T.T$ $\Gamma ::= \emptyset$
 $\Gamma, x : T$

Contexts are implemented as hash maps of types

Basic Types - Duality



Duality is partially defined as follows:

```
dualType :: SpiType -> SpiType
dualType End = End
dualType Boolean = error "..."
dualType (Qualified q (Receiving t1 t2)) =
    Qualified q (Sending t1 (dualType t2))
dualType (Qualified q (Sending t1 t2)) =
    Qualified q (Receiving t1 (dualType t2))
dualType (Recursive a p) = Recursive a (dualType p)
dualType (TypeVar x) = TypeVar
```

Basic Types - Context



Contexts support the following operations:

- (nondeterministic) **context split** $\Gamma = \Gamma_1 \circ \Gamma_2$: the function ndsplit :: Context -> [(Context, Context)] creates all possible combinations of dividing linear variables, mantaining unrestricted variables;
- **update** $\Gamma + (x : T)$: the function update k t inserts k : t in the context only if the variable k was not present, or it was yet defined unrestricted with type t;
- override Γ , (x : T): this represents newly bounded variables, possibly shadowing preexisting definitions.

Basic Types - Typing Rules (1)



Sequent calculus rules are modeled as instnces of the context transition **monad**:

```
newtype CT a = CT
    (Context -> TypeErrorBundle TypeError (a, Context))
instance Monad CT where
    return :: a -> CT a
    (>>=) :: CT a -> (a -> CT b) -> CT b
```

Rules can be composed and propagate context side effects A check rule can either hold and return () or fail and return an error:

```
class TypeCheck a where
    check :: a -> CT ()
```

Basic Types - Typing Rules (2)



Unrestricted requirement

 $un(\Gamma)$ holds when all entries in the context are unrestricted:

```
unGamma :: CT ()
unGamma = CT (\context -> if all unrestricted context
    then Right ((), context)
    else Left "Error message...")
```

Basic Types - Typing Rules (3)



Context update

```
\Gamma + (x:T) \text{ throws an error if the conditions arent met:}
\text{update } :: \text{String } \text{-> SpiType } \text{-> CT } \text{()}
\text{update } \text{k } \text{t} = \text{do}
\text{may } \text{-- liftPure } \text{(M.lookup k)}
\text{case may of}
\text{Just found } \text{-> unless (predicate Un t \&\& found } \approx \text{ t)}
\text{(throwError "Error message..")}
\text{Nothing } \text{-> sideEffect (M.insert k t)}
```

Basic Types - Typing Rules (4)



Context update

Context transitions can even return useful values:

```
extract :: String -> CT SpiType
extract k = do
    t <- get k
    unless (predicate Un t) (delete k)
    return t</pre>
```

This is used to optimize some context splits in the [T-Rec] and [T-Send] rules

Basic Types - Typing Rules (5)



Context split require to nondeterministically check over all possible split if there is one that satisfies the rule.

Chapter 8 "Algorithmic type checking" shows a set of equivalent rules that can be checked with a deterministic algorithm.

Basic Types - Typing Rules (6)



Example: T-IN

$$\frac{\Gamma_1 \vdash x: \mathit{q?T.U} \quad (\Gamma_2 + x: \mathit{U}), y: \mathit{T} \vdash \mathit{P}}{\Gamma_1 \circ \Gamma_2 \vdash x(y).\mathit{P}} \ [\text{T-In}]$$

In this case the rule holds following those observations:

- if x is not present in $\Gamma_1 \circ \Gamma_2$ the left assumption can never be verified:
- if $\Gamma_1 \circ \Gamma_2$ contains the claim $x : \operatorname{un} T.U$, then both Γ_1, Γ_2 contain such claim;
- if $\Gamma_1 \circ \Gamma_2$ contains the claim x : lin T.U, then Γ_1 must contain that claim and Γ_2 must not.

Basic Types - Typing Rules (7)



Notice that in order to type $\Gamma_1 \vdash x : q?T.U$, as for the rule [T-VAR], Γ_1 must not contain any linear claim.

Hence, Γ_2 must contain all linear claims in $\Gamma_1 \circ \Gamma_2$, of course except for x if it was linear.

Basic Types - Typing Rules (8)



Hence the algorithm for this rule is presented as follows:

Example: T-IN

```
check (Rec x y p) = do
   xType <- extract x -- If not present, the monadic
        -- bind will make the whole rule fail.
        -- The function extract will preserve
    (t, u) = case xType of
            Qualified _ (Receiving t u) ->
                return (t. u)
            -> throwError "..."
   update x u
   replace y t
    check p
```

Basic Types - Fir



Other typing rules implementations follow similar reasoning.

One could think of an intuitive way to parallelize the [T-PAR]:

[T-Par]

$$\frac{\Gamma_1 \vdash P_1 \quad \Gamma_2 \vdash P_2}{\Gamma_1 \circ \Gamma_2 \vdash P_1 | P_2} \text{ [T-PAR]}$$

The algorithm checks all possible splits of $\Gamma_1 \circ \Gamma_2$

```
check (Par p1 p2) = do
    splits <- liftPure ndsplit
    -- Compute all possible splits
    runs <- return () -< (candidate <$> splits)
    liftEither $ foldChoice runs
        {- `using` parList rdeepseg -}
    where
        candidate (c1, c2) = (return () -<
            [ c1 |> check p1
            , c2 \mid > check p2
            ] {- <&> (`using` parList rdeepseg) -}
            ) >- return ()
```

It seems natural to desire to parallelize this code in the points with comments...

Basic Types - Typing Rules (11)



... but this would imply loss in performance. Consider the following program:

Example: assets/well-formed-ill-typed/multiple.spi

```
a1 >< a2: lin?bool.end .
b1 > b2: lin?bool.end.
c1 > < c2: lin?bool.end.
d1 > < d2: lin?bool.end .
e1 >< e2: lin?bool.end .
f1 > f2: lin?bool.end.
x > < v: rec x. ?bool.x .
   x1 > y1: lin?bool.lin!bool.end .
       x2 >< y2: lin?bool.lin!bool.end .
            x << true . y >> z . if z then 0 else 0
            y \gg z . if z
              then x << false . 0
               else 0
             y1 >> n . y1 << false . x2 << false . x2 >> n .0
             a1 << true . b1 << true . c1 << true
               . d1 << true . e1 << true . f1 << true . 0
            a2 >> e , b2 >> e , c2 >> e , d2 >> e , e2 >> e ,
```

```
SPARKS: 651264 (0
                   converted, 58321
                   overflowed, 0 dud, 429960
                   GC'd, 15527 fizzled)
                           time 0.001s
                     INIT
                                         (0.001s elapsed)
Running the program
                     MUT time 2.987s (2.981s elapsed)
                     GC time 3.961s (3.972s elapsed)
                     EXIT time 0.000s (0.007s elapsed)
                    Total time 6.949s (
                                          6.961s elapsed)
SPARKS: 3540338 (98151
converted, 87210 overflowed,
0 dud, 2443757 GC'd, 632692
fizzled)
INIT time 0.002s ( 0.002s
elapsed) MUT time 23.487s
( 6.104s elapsed) GC time
29.159s ( 9.701s elapsed)
EXIT time 0.071s ( 0.004s
elapsed) Total time 52.720s (
15.811s elapsed)
```