

CSEN 502 Theory of Computation, Winter Term 2021  
Assignment1

Exercise 1-1

Reading

Read Chapter 0 to page 20 of the text. You may skip the section on Boolean logic.

Exercise 1-2

Exercises from Textbook

Sipser (pp 25 - 27 International Edition): Solve exercises 0.3<sup>1</sup>, 0.4<sup>2</sup> (skip e), 0.5, 0.6, and 0.7

Exercise 1-3

In each of the following cases, determine whether the relation  $\rho$  is reflexive, symmetric, anti-symmetric, asymmetric or transitive.

- (a)  $\rho \subseteq \mathbb{Z} \times \mathbb{Z}$ , where  $a \rho b$  if and only if there is  $n \in \mathbb{Z}$  such that  $a = bn$ .
- (b) For a given universe  $\mathcal{U}$  and  $C \subseteq \mathcal{U}$ , where  $C \neq \emptyset$ , define  $\rho \subseteq P(\mathcal{U}) \times P(\mathcal{U})$  ( $\rho$  is a set of ordered pairs of sets over  $\mathcal{U}$ ) such that  $A \rho B$  if and only if  $A \cup C = B \cup C$ .
- (c)  $\rho \subseteq \mathbb{Z} \times \mathbb{Z}$  where  $x \rho y$  if and only if  $x + y$  is odd.
- (d)  $\rho \subseteq (\mathbb{Z} \times \mathbb{Z}) \times (\mathbb{Z} \times \mathbb{Z})$  where  $(a, b) \rho (c, d)$  if and only if  $a \leq c$ .

Exercise 1-4

Extra Problem

In each of the following cases, and by filling the appropriate *circles*, indicate whether the relation  $\mathcal{R}$  on the *set of line segments in the plane* is reflexive (r), symmetric (s), anti-symmetric (an), asymmetric (as), or transitive (t).

- a)  $(a, b) \in \mathcal{R}$  if and only if  $a$  and  $b$  are not equal in length.  
r ☐ s ☐ an ☐ as ☐ t ☐
- b)  $(a, b) \in \mathcal{R}$  if and only if  $b$  is longer than 10 cm.  
r ☐ s ☐ an ☐ as ☐ t ☐
- c)  $(a, b) \in \mathcal{R}$  if and only if  $a$  and  $b$  have at least two common points.  
r ☐ s ☐ an ☐ as ☐ t ☐

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<sup>1</sup>Exercise 0.4 in normal edition

<sup>2</sup>Exercise 0.1 in normal edition

**Exercise 1-5****Programming**

Using your favorite programming language, implement an abstract data type for sets. Your implementation should include functions/methods/clauses for checking set membership, checking subset relations among sets, and computing set intersections, unions and differences.