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# Deep Learning Assignment 1

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Anonymous Author(s)

Affiliation

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email

## 1 MLP backprop and NumPy implementation

### 1.1 Analytical derivation of gradients

#### Question 1.1 a)

##### 1. Cross entropy module

$$\frac{\partial L}{\partial x^{(N)}} = - \sum_i t_i \frac{1}{x_i^{(N)}} = \frac{1}{x_{\text{argmax}(t)}^{(N)}}$$

##### 2. Softmax module

$$\begin{aligned} \frac{\partial x_i^{(N)}}{\partial \tilde{x}_j^{(N)}} &= \\ &= \frac{\exp(\tilde{x}_j^{(N)})}{\sum_{i=1}^{d_N} \exp(\tilde{x}_i^{(N)})} - \left( \frac{\exp(\tilde{x}_j^{(N)})}{\sum_{i=1}^{d_N} \exp(\tilde{x}_i^{(N)})} \right)^2 \text{ if } i = j \\ &= - \frac{\exp(\tilde{x}_i^{(N)})}{\sum_{i=1}^{d_N} \exp(\tilde{x}_i^{(N)})} \frac{\exp(\tilde{x}_j^{(N)})}{\sum_{i=1}^{d_N} \exp(\tilde{x}_i^{(N)})} \text{ if } i \neq j \\ &= \delta_{ij} (x_i^{(N)} - x_i^{N2}) + (1 - \delta_{ij}) (-x_i x_j) \end{aligned}$$

##### 3. ReLU module

$$\begin{aligned} \frac{\partial x^{(l < N)}}{\partial \tilde{x}^{(l < N)}} &= \\ &= 1 \text{ if } \tilde{x}^{(l)} \geq 0 \\ &= 0 \text{ if } \tilde{x}^{(l)} < 0 \end{aligned}$$

##### 4. Linear module

$$\begin{aligned} \frac{\partial \tilde{x}^{(l)}}{\partial x^{(l-1)}} &= W^{(l)} \\ \frac{\partial \tilde{x}^{(l)}}{\partial W^{(l)}} &= x^{(l-1)} \\ \frac{\partial \tilde{x}^{(l)}}{\partial b^{(l)}} &= 1 \end{aligned}$$

#### Question 1.1 b)

$$1. \frac{\partial L}{\partial \tilde{x}^{(N)}} = \frac{\partial L}{\partial x^{(N)}} \frac{\partial x^{(N)}}{\partial \tilde{x}^{(N)}} = \sum_i t_i \frac{1}{x_i^{(N)}} (\delta_{ij} (x_i^{(N)} - x_i^{N2}) + (1 - \delta_{ij}) (-x_i x_j))$$

$$2. \frac{\partial L}{\partial \tilde{x}^{(l < N)}} = \frac{\partial L}{\partial x^{(N)}} \frac{\partial x^{(N)}}{\partial \tilde{x}^{(N)}} \frac{\partial \tilde{x}^{(N)}}{\partial x^{(N-1)}} \frac{\partial x^{(N-1)}}{\partial \tilde{x}^{(N-1)}} \prod_{n=l}^{N-1} \frac{\partial \tilde{x}^{(n+1)}}{\partial x^{(n)}} \frac{\partial x^{(n)}}{\partial \tilde{x}^{(n)}}$$

32	<b>1.2 NumPy implementation</b>
33	<b>2 PyTorch MLP</b>
34	<b>3 Custom Module: Batch Normalization</b>
35	<b>3.1 Automatic differentiation</b>
36	<b>4 PyTorch CNN</b>