

# Benchmarking

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## Benchmarking of the different functions in the bendDNA package

In this R Markdown file all the different functions included in the bendDNA package are benchmarked. This will be done by looking at every function individually, testing and timing the functions for different parameter values.

The testing is done  $x$  times (depending on which function) and summary statistics are given in a summary table. These are then plotted using violin plots comparing every different parameter value. The CRAN microbenchmark package is used for making both the summary table and plot.

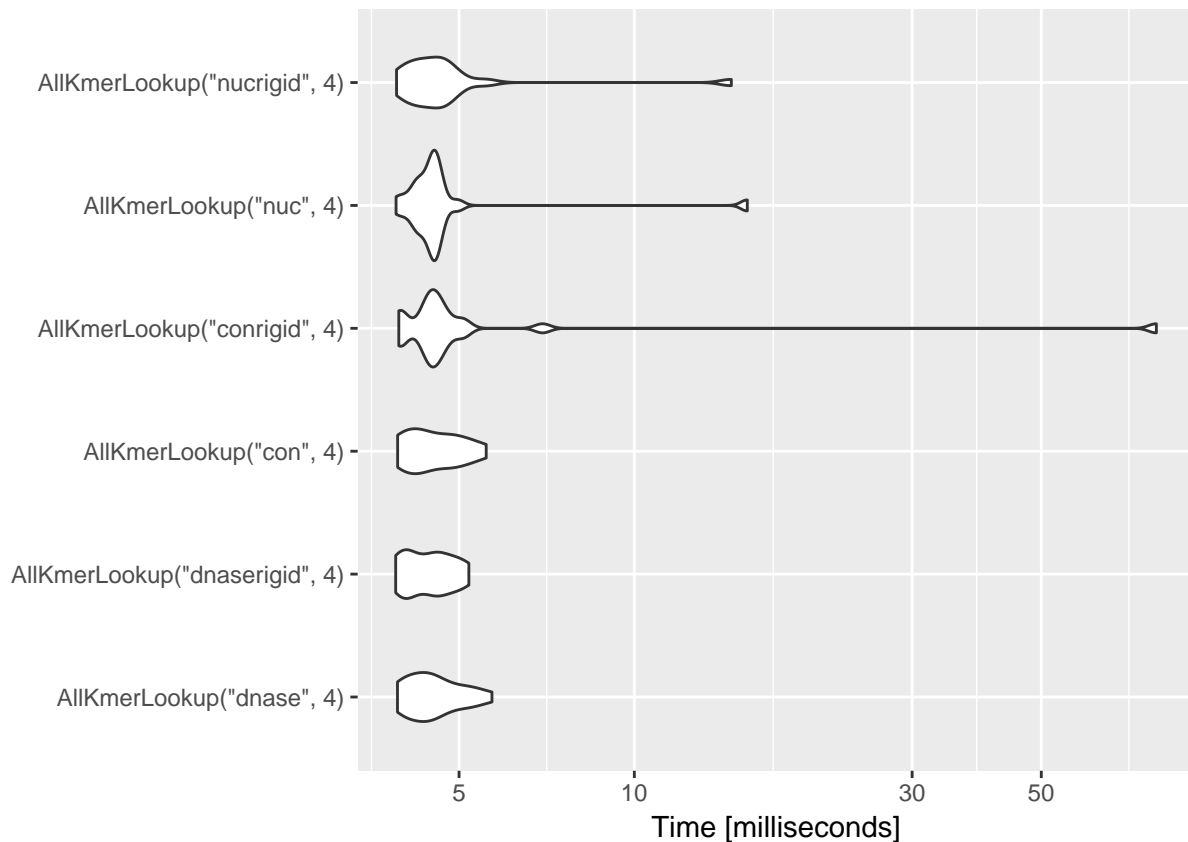
### AllKmerLookup

Function for producing all possible k-mers and calculating their average bendability coefficients.

Usage: AllKmerLookup(scale, k, sequence.out = F)

Parameters that can be used include: - Scale - Number of consecutive trinucleotides - Whether to output the sequences

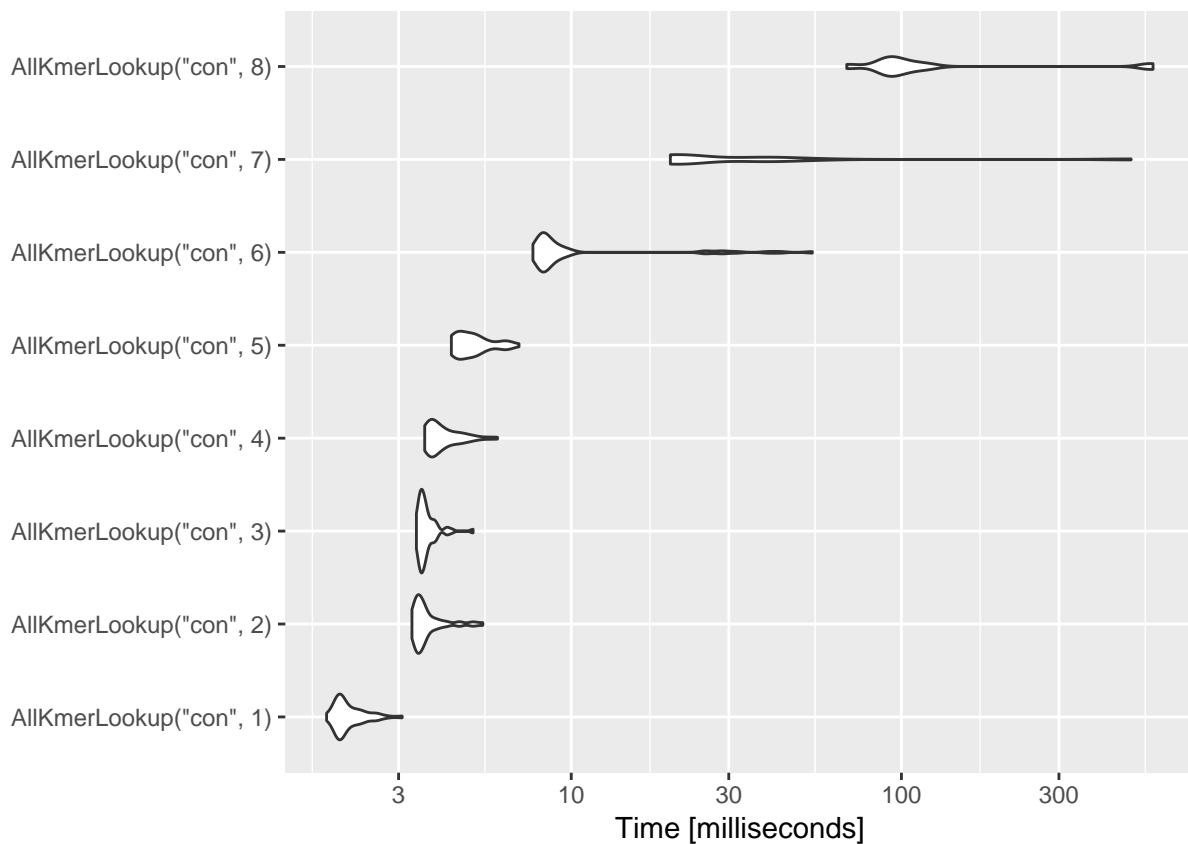
### Different lookup tables



FALSE Unit: milliseconds

FALSE		expr	min	lq	mean	median
FALSE		AllKmerLookup("dnase", 4)	3.919518	4.130370	4.541840	4.437062
FALSE		AllKmerLookup("dnaserigid", 4)	3.891980	4.055586	4.444487	4.499967
FALSE		AllKmerLookup("con", 4)	3.921678	4.100402	4.544324	4.376587
FALSE		AllKmerLookup("conrigid", 4)	3.940036	4.348240	8.309063	4.507796
FALSE		AllKmerLookup("nuc", 4)	3.897380	4.266707	4.987922	4.500237
FALSE		AllKmerLookup("nucrigid", 4)	3.904939	4.193274	5.001934	4.467840
FALSE		uq	max	neval	cld	
FALSE	4.813680	5.694882	20	a		
FALSE	4.766163	5.198125	20	a		
FALSE	4.909522	5.566373	20	a		
FALSE	4.751855	78.813120	20	a		
FALSE	4.583659	15.632712	20	a		
FALSE	4.741866	14.676996	20	a		

### Number of consecutive trinucleotides



FALSE Unit: milliseconds

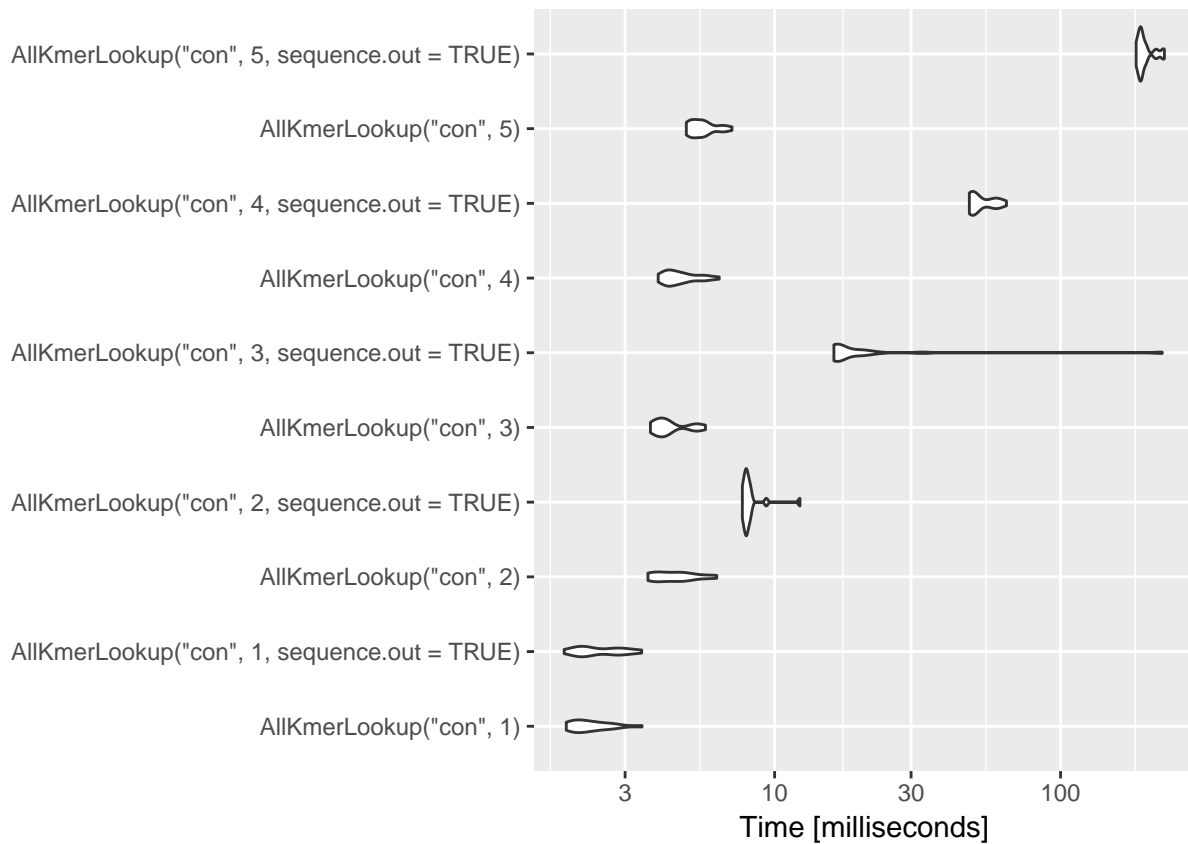
FALSE		expr	min	lq	mean	median
FALSE		AllKmerLookup("con", 1)	1.815862	1.974608	2.134628	2.018884
FALSE		AllKmerLookup("con", 2)	3.292633	3.407642	3.691139	3.523192
FALSE		AllKmerLookup("con", 3)	3.396843	3.491336	3.659703	3.570978
FALSE		AllKmerLookup("con", 4)	3.598786	3.751592	4.112475	3.908718
FALSE		AllKmerLookup("con", 5)	4.334202	4.557742	5.086885	4.974856
FALSE		AllKmerLookup("con", 6)	7.654911	8.103611	12.662260	8.409225
FALSE		AllKmerLookup("con", 7)	19.961514	20.532243	56.451853	21.567062

```

FALSE AllKmerLookup("con", 8) 68.306180 89.619734 161.829188 97.077831
FALSE      uq      max neval cld
FALSE  2.239185  3.076112   50  a
FALSE  3.764011  5.397909   50  a
FALSE  3.714336  5.043159   50  a
FALSE  4.410335  5.978357   50  a
FALSE  5.372531  6.948113   50  a
FALSE  9.413537 53.739875   50  a
FALSE 39.966221 496.320223   50  b
FALSE 116.783675 578.312584   50  c

```

## Sequence Out



```

## Unit: milliseconds
##
##      expr      min      lq
## AllKmerLookup("con", 1) 1.868238 2.005926
## AllKmerLookup("con", 1, sequence.out = TRUE) 1.835840 2.127955
## AllKmerLookup("con", 2) 3.605805 3.846354
## AllKmerLookup("con", 2, sequence.out = TRUE) 7.712686 7.870891
## AllKmerLookup("con", 3) 3.678699 3.914658
## AllKmerLookup("con", 3, sequence.out = TRUE) 16.118669 16.392156
## AllKmerLookup("con", 4) 3.915738 4.220271
## AllKmerLookup("con", 4, sequence.out = TRUE) 47.972101 48.881380
## AllKmerLookup("con", 5) 4.911411 5.130902
## AllKmerLookup("con", 5, sequence.out = TRUE) 183.746992 189.793923
##      mean      median      uq      max neval cld

```

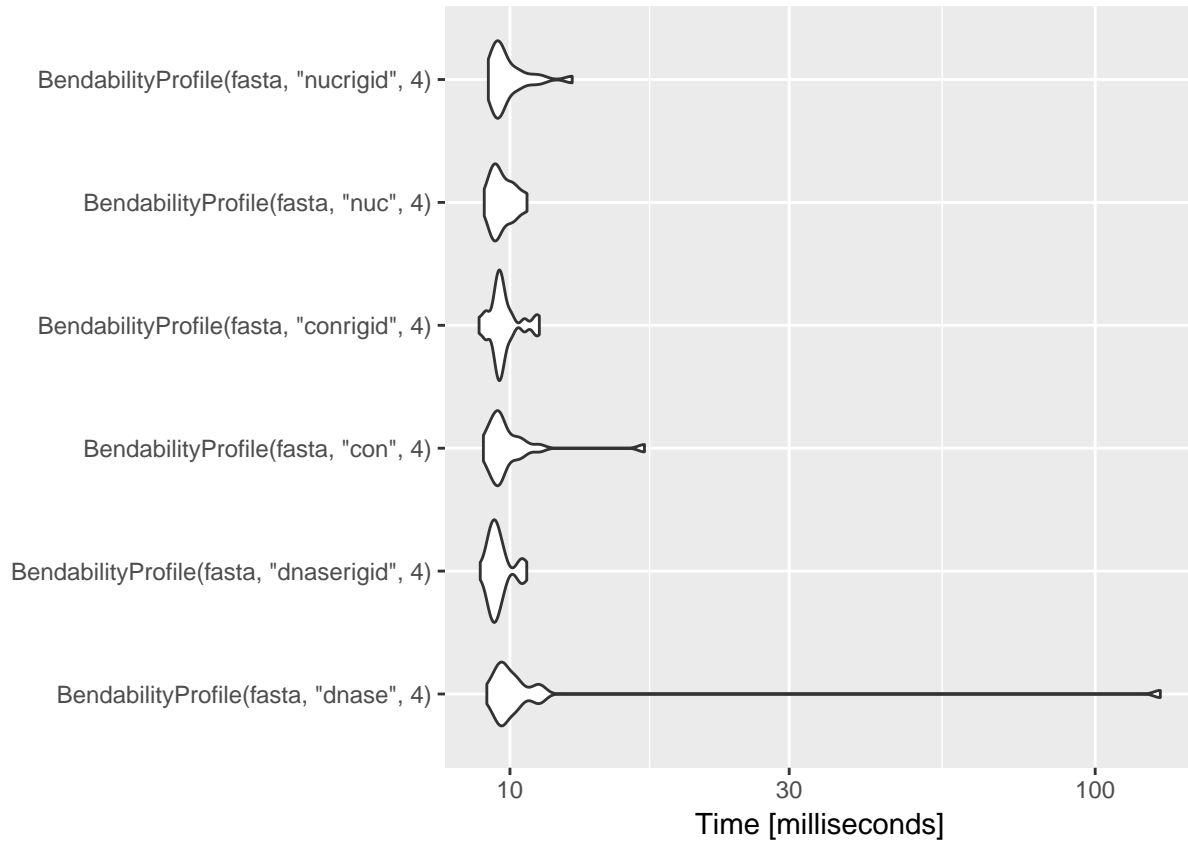
##	2.297176	2.175200	2.498362	3.439499	20	a
##	2.485430	2.178441	2.851761	3.428701	20	a
##	4.536792	4.491058	4.911950	6.273712	20	a
##	8.262844	7.983742	8.166515	12.263948	20	a
##	4.356151	4.140629	4.746186	5.732139	20	a
##	28.872542	16.747715	19.931816	226.734788	20	b
##	4.717757	4.522645	5.022101	6.401141	20	a
##	53.043822	49.896492	58.689892	64.674998	20	c
##	5.626416	5.468642	5.790184	7.092820	20	a
##	197.329989	191.534730	199.069231	230.663484	20	d

## BendabilityProfile

Splits sequence into k-mers with two-nucleotide overlap and calculates average bendability per k-mer according to the chosen scale.

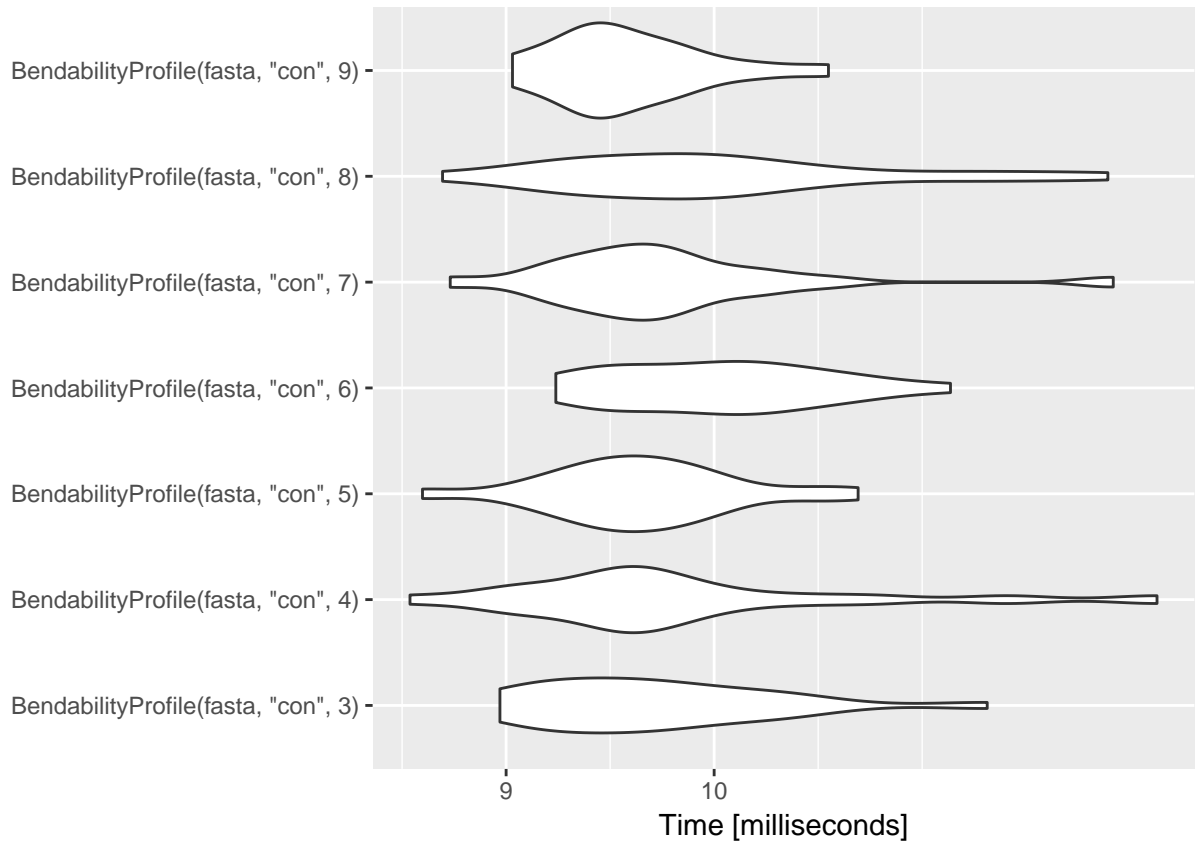
Parameters that can be used include: - Scale - Number of consecutive trinucleotides

### Scale



```
## Unit: milliseconds
##
##          expr      min      lq      mean
##  BendabilityProfile(fasta, "dnase", 4) 9.130602 9.634377 15.962650
##  BendabilityProfile(fasta, "dnaserigid", 4) 8.896802 9.239132 9.566047
##      BendabilityProfile(fasta, "con", 4) 9.007492 9.419476 10.090880
##  BendabilityProfile(fasta, "conrigid", 4) 8.855766 9.464292 9.752816
##      BendabilityProfile(fasta, "nuc", 4) 9.037729 9.366831 9.724036
##  BendabilityProfile(fasta, "nucrigid", 4) 9.184597 9.444045 9.949656
##  median      uq      max neval cld
## 9.773955 10.373842 129.20961 20 a
## 9.443504 9.696742 10.68351 20 a
## 9.602520 10.142203 16.97557 20 a
## 9.613589 9.873576 11.22562 20 a
## 9.569853 10.066879 10.69484 20 a
## 9.606840 10.204297 12.77420 20 a
```

## Number of consecutive trinucleotides



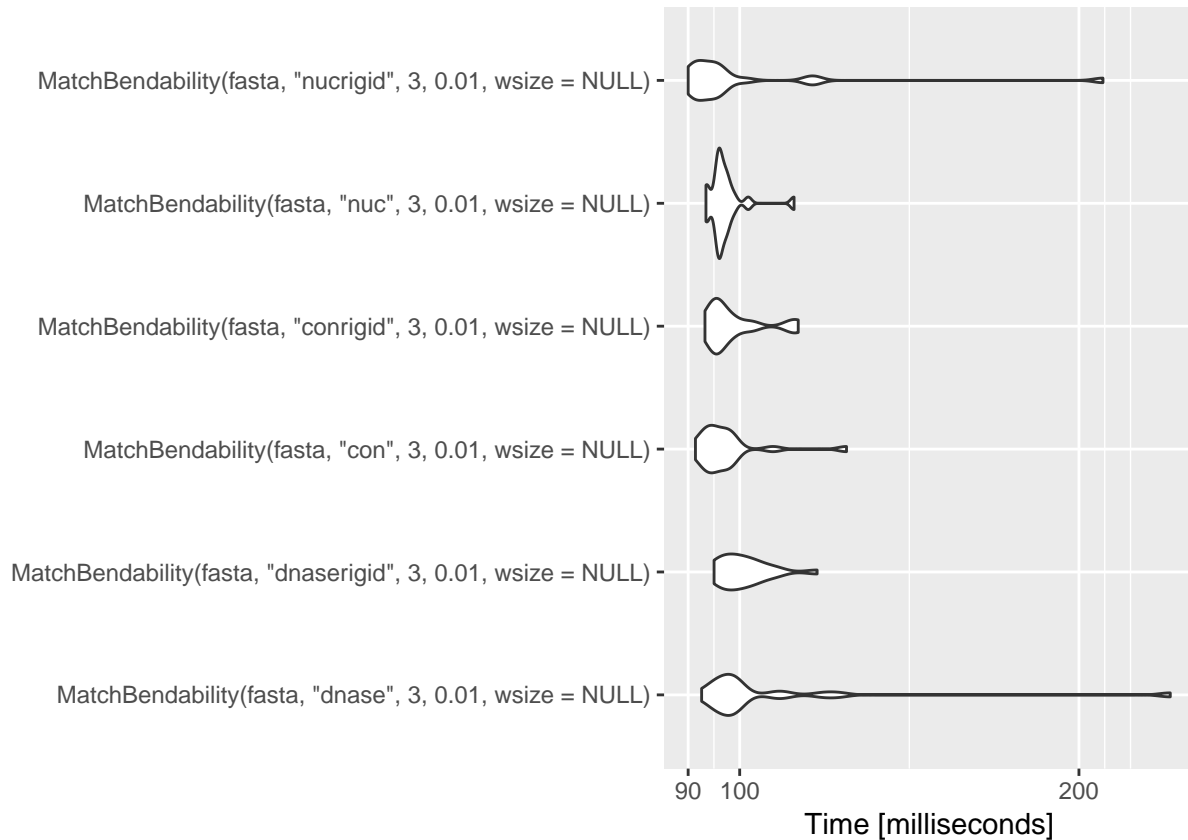
```
## Unit: milliseconds
##               expr      min      lq      mean      median
## BendabilityProfile(fasta, "con", 3) 8.971856 9.247501 9.718826 9.665964
## BendabilityProfile(fasta, "con", 4) 8.572290 9.373040 9.841017 9.651656
## BendabilityProfile(fasta, "con", 5) 8.626825 9.372501 9.644825 9.626548
## BendabilityProfile(fasta, "con", 6) 9.229413 9.560134 10.035616 10.003435
## BendabilityProfile(fasta, "con", 7) 8.748855 9.406787 9.780651 9.695662
## BendabilityProfile(fasta, "con", 8) 8.714838 9.416237 10.024223 9.907054
## BendabilityProfile(fasta, "con", 9) 9.029090 9.349283 9.580004 9.482651
##      uq      max neval cld
## 10.073089 11.48317   20   a
## 10.021254 12.51449   20   a
##  9.900304 10.75640   20   a
## 10.338206 11.27151   20   a
##  9.942691 12.24019   20   a
## 10.385992 12.20671   20   a
##  9.778814 10.59603   20   a
```

## MatchBendability

Calculates bendability profile of query sequence and finds all other sequences which have similar (or same) profile.

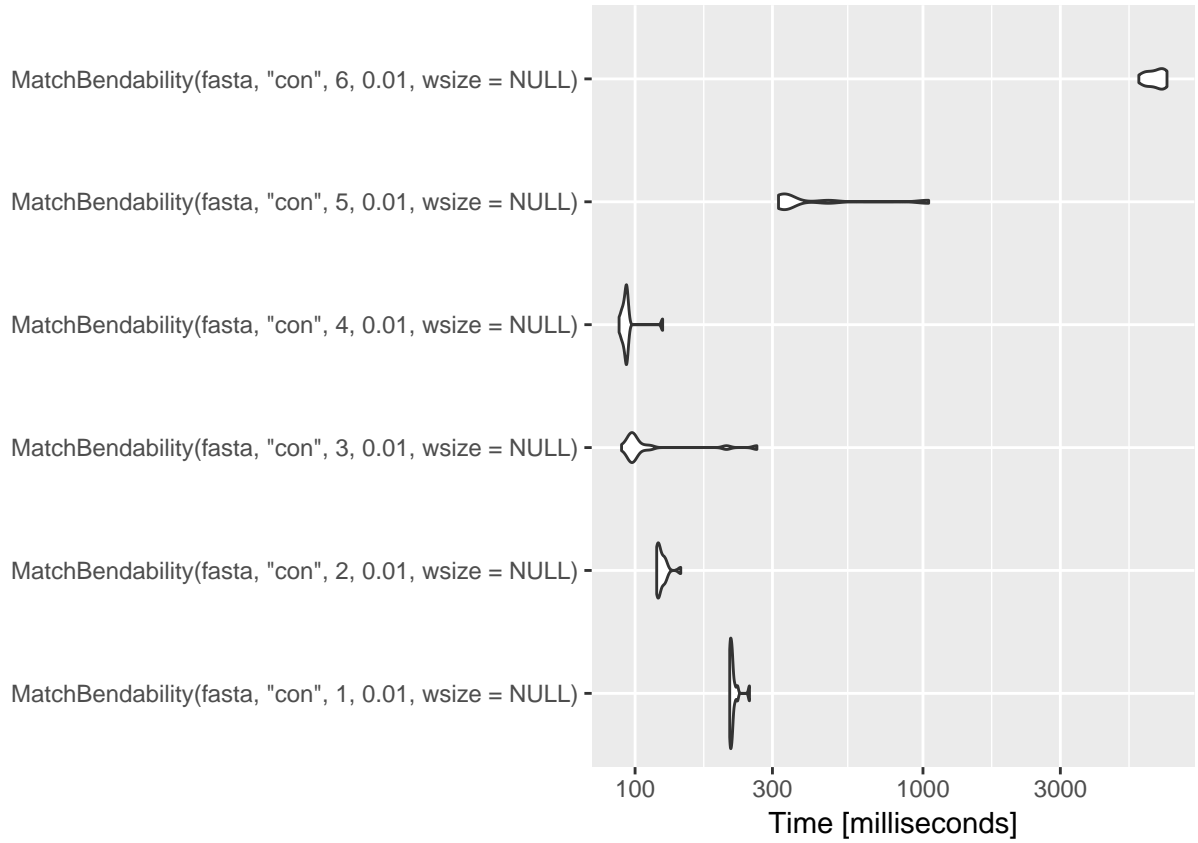
Parameters that can be used include: - Scale - Number of consecutive trinucleotides - Tolerance - wsize - output.list - random.out

### Scale



```
## Unit: milliseconds
##
##                               expr      min
##      MatchBendability(fasta, "dnase", 3, 0.01, wsize = NULL) 92.51658
##      MatchBendability(fasta, "dnaserigid", 3, 0.01, wsize = NULL) 94.89831
##      MatchBendability(fasta, "con", 3, 0.01, wsize = NULL) 91.35352
##      MatchBendability(fasta, "conrigid", 3, 0.01, wsize = NULL) 93.14832
##      MatchBendability(fasta, "nuc", 3, 0.01, wsize = NULL) 93.33569
##      MatchBendability(fasta, "nucrigid", 3, 0.01, wsize = NULL) 90.00904
##      lq      mean      median      uq      max neval cld
## 95.59377 107.79314 98.57809 103.62314 241.0360    20  a
## 97.05569 100.96857 100.11398 103.40824 117.1417    20  a
## 93.74119 97.41295 95.41694 98.13425 124.3916    20  a
## 95.04707 98.80212 96.14722 100.22009 112.7022    20  a
## 95.55678 97.13291 96.07109 97.41557 111.7502    20  a
## 91.48095 101.79910 94.43827 96.40991 210.0697    20  a
```

## Number of consecutive sequences



## Unit: milliseconds

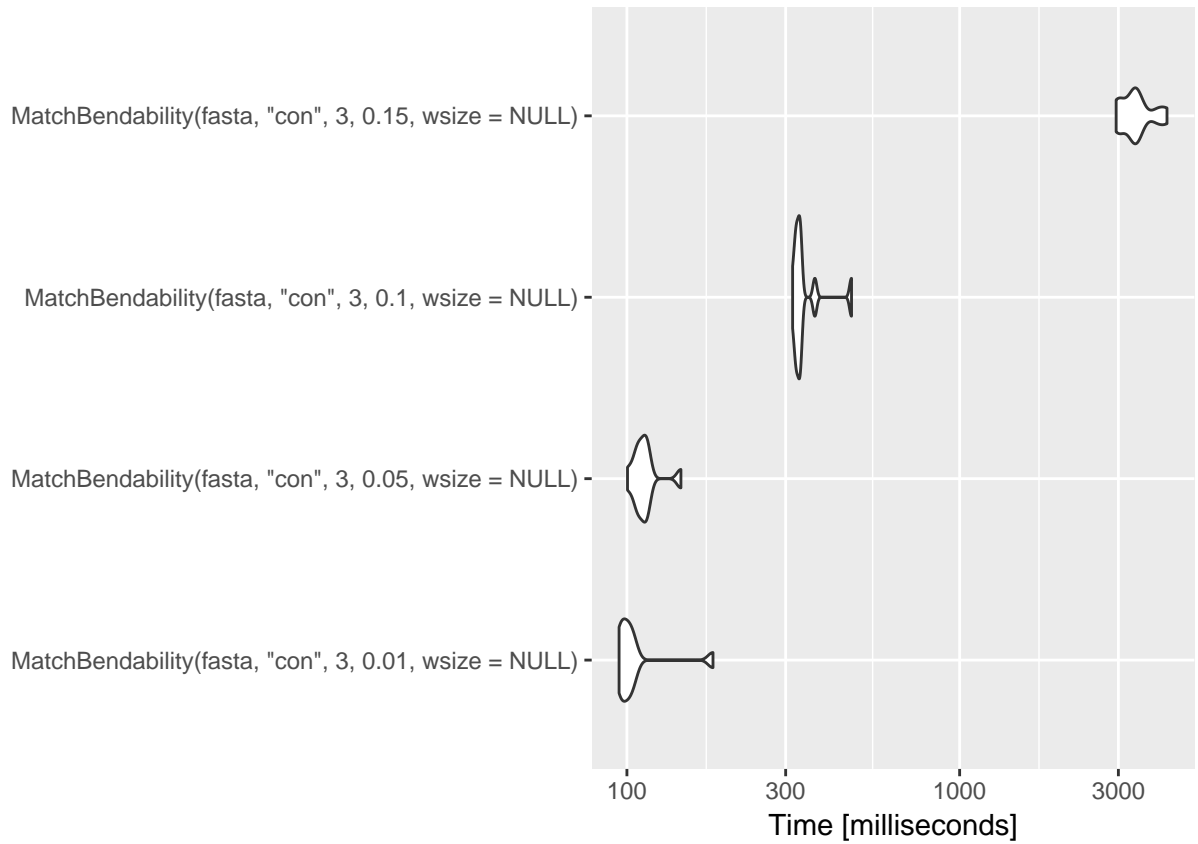
##	expr	min
##	MatchBendability(fasta, "con", 1, 0.01, wsize = NULL)	213.17010
##	MatchBendability(fasta, "con", 2, 0.01, wsize = NULL)	118.89705
##	MatchBendability(fasta, "con", 3, 0.01, wsize = NULL)	89.76066
##	MatchBendability(fasta, "con", 4, 0.01, wsize = NULL)	88.00581
##	MatchBendability(fasta, "con", 5, 0.01, wsize = NULL)	314.94795
##	MatchBendability(fasta, "con", 6, 0.01, wsize = NULL)	5620.04823

##	lq	mean	median	uq	max	neval	cld
##	214.02511	218.98269	216.34286	218.38172	249.6871	15	ab
##	119.94537	123.76159	121.10006	125.90240	144.1236	15	a
##	96.04112	117.32280	99.31945	104.19306	264.9813	15	a
##	91.31789	94.42945	93.07327	93.76252	124.6805	15	a
##	326.96000	443.49845	332.88355	403.64166	1046.6390	15	b
##	6033.04322	6430.73386	6513.14677	6781.04809	7039.0110	15	c

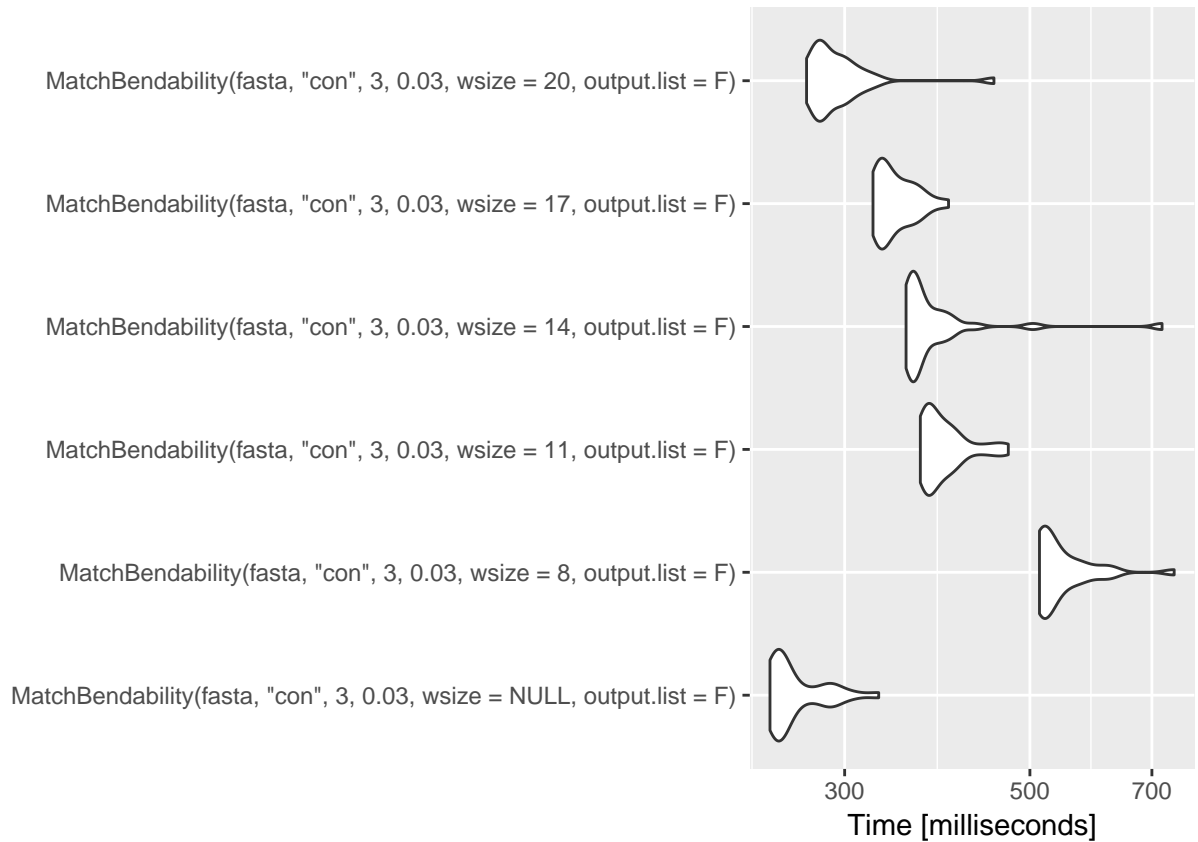


## Tolerance



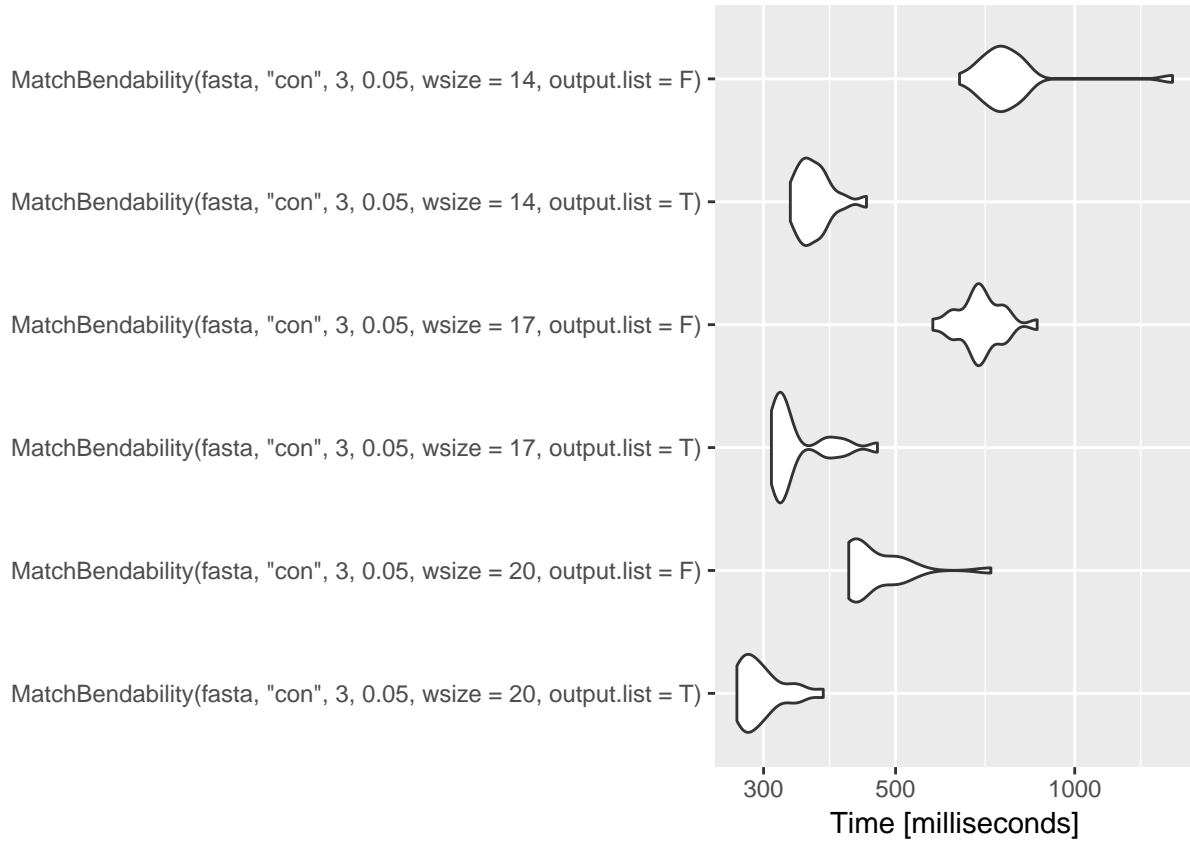
```
## Unit: milliseconds
##
##      expr      min
## MatchBendability(fasta, "con", 3, 0.01, wsize = NULL) 94.72823
## MatchBendability(fasta, "con", 3, 0.05, wsize = NULL) 100.40961
## MatchBendability(fasta, "con", 3, 0.1, wsize = NULL) 314.82052
## MatchBendability(fasta, "con", 3, 0.15, wsize = NULL) 2953.85780
##      lq      mean      median      uq      max neval cld
## 95.39993 107.5737 99.94444 104.3010 181.4328 10 a
## 107.13310 113.6325 111.76481 115.2027 145.3245 10 a
## 322.60717 344.8043 330.04691 333.7000 473.2135 10 a
## 3054.20801 3406.8254 3362.35606 3474.8965 4199.7447 10 b
```

## Window size



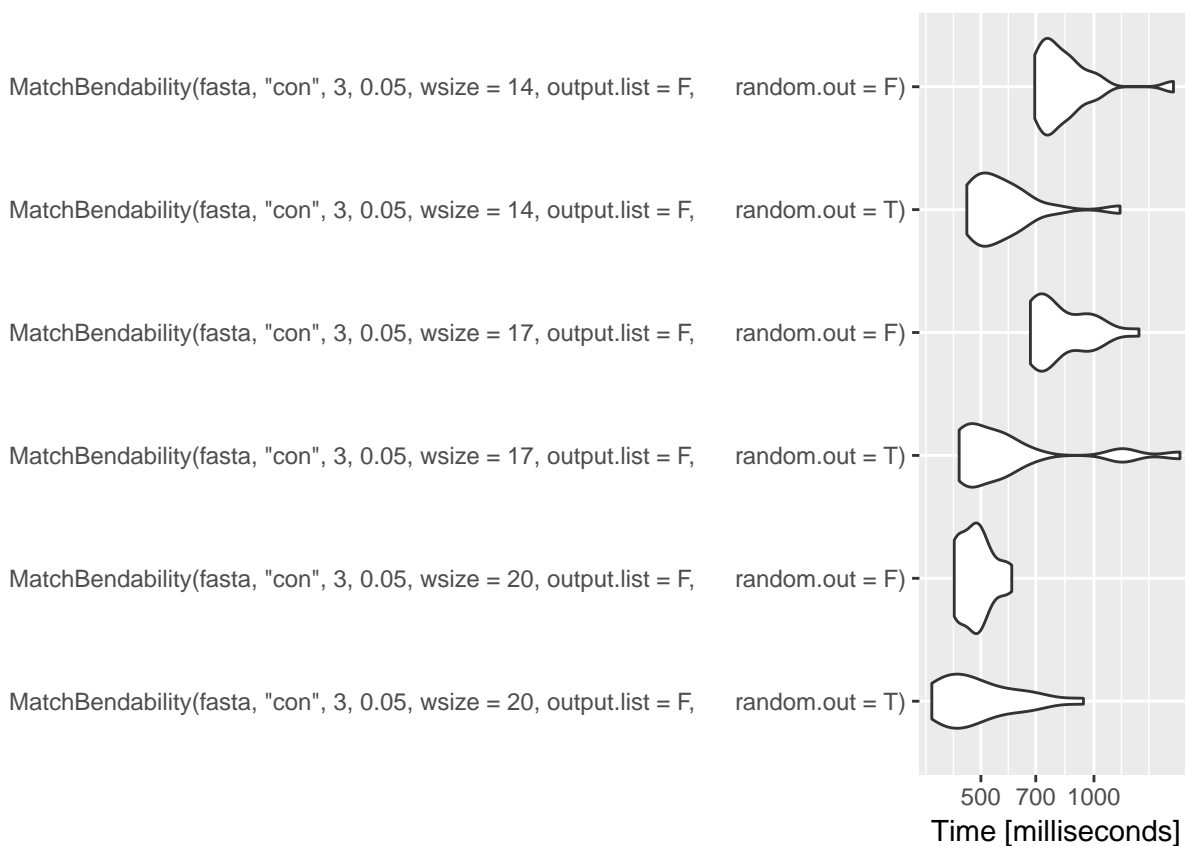
```
## Unit: milliseconds
##
##                                     expr
## MatchBendability(fasta, "con", 3, 0.03, wsize = NULL, output.list = F)
##   MatchBendability(fasta, "con", 3, 0.03, wsize = 8, output.list = F)
##   MatchBendability(fasta, "con", 3, 0.03, wsize = 11, output.list = F)
##   MatchBendability(fasta, "con", 3, 0.03, wsize = 14, output.list = F)
##   MatchBendability(fasta, "con", 3, 0.03, wsize = 17, output.list = F)
##   MatchBendability(fasta, "con", 3, 0.03, wsize = 20, output.list = F)
##      min      lq      mean  median      uq      max neval  cld
## 244.1812 248.5392 262.5597 252.7967 271.9979 329.5461    30  a
## 513.3709 515.8028 547.4515 530.0222 561.9142 744.3189    30  e
## 369.6090 375.5787 395.4637 385.9496 404.6659 471.0974    30  d
## 355.3656 360.8180 388.4465 365.5680 387.7665 719.8790    30  d
## 324.3923 330.8091 345.7495 339.4505 357.8996 399.5229    30  c
## 270.0865 279.0945 295.6261 285.1169 300.9691 452.8319    30  b
```

## Output List



```
## Unit: milliseconds
##
##                                     expr
## MatchBendability(fasta, "con", 3, 0.05, wsize = 20, output.list = T)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 20, output.list = F)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 17, output.list = T)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 17, output.list = F)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 14, output.list = T)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 14, output.list = F)
##      min      lq    mean  median      uq      max neval  cld
## 270.6281 277.8643 298.8592 290.6919 307.5168 377.9696    20  a
## 417.1378 425.4082 467.1603 435.7913 493.8248 722.9810    20  b
## 309.2946 317.1653 342.8729 323.4957 356.0437 466.0667    20  a
## 577.5178 667.0139 697.3933 688.5150 733.6146 864.6614    20  c
## 332.7561 350.3564 366.5674 362.1495 376.9642 446.7877    20  a
## 640.3478 713.9341 785.1070 752.0359 802.7059 1460.2552    20  d
```

## Random Out



```
## Unit: milliseconds
##
## MatchBendability(fasta, "con", 3, 0.05, wsize = 20, output.list = F, random.out = T)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 20, output.list = F, random.out = F)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 17, output.list = F, random.out = T)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 17, output.list = F, random.out = F)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 14, output.list = F, random.out = T)
## MatchBendability(fasta, "con", 3, 0.05, wsize = 14, output.list = F, random.out = F)
##      min      lq      mean      median      uq      max      neval      cld
## 370.1209 409.2126 509.7598 472.7507 567.2708 937.5145      20      a
## 424.6685 442.3714 486.6252 484.5398 509.3196 604.2903      20      a
## 437.6301 465.1447 645.3722 539.9174 609.3383 1694.5142      20      a
## 677.4220 710.4433 830.8216 763.5334 938.7872 1318.0219      20      b
## 458.7838 491.0835 587.6018 543.2046 627.1972 1173.5770      20      a
## 695.6092 744.5702 853.0123 790.6196 873.9008 1628.3651      20      b
```

## ClusterAndConsensus

Intended to present output of function MatchBendability in a more human-friendly format. The output can contain very large numbers of highly similar sequences, so clustering and calculating a consensus can help provide a clearer picture. DISCLAIMER: due to the nature of bendability problem and limitations of IUPAC extended genetic alphabet, output of this function is not intended for further machine use. Not all sequences which can be inferred from consensus output will have satisfied the initial bendability requirements (for example AA/TT will be marked as WW, same as AT/TA).

Parameters that can be used include: - Cutoff - sample.seq

## Cutoff

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## =====
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## Time difference of 0.54 secs
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## Time difference of 0.16 secs
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## Time difference of 0.27 secs
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```

```

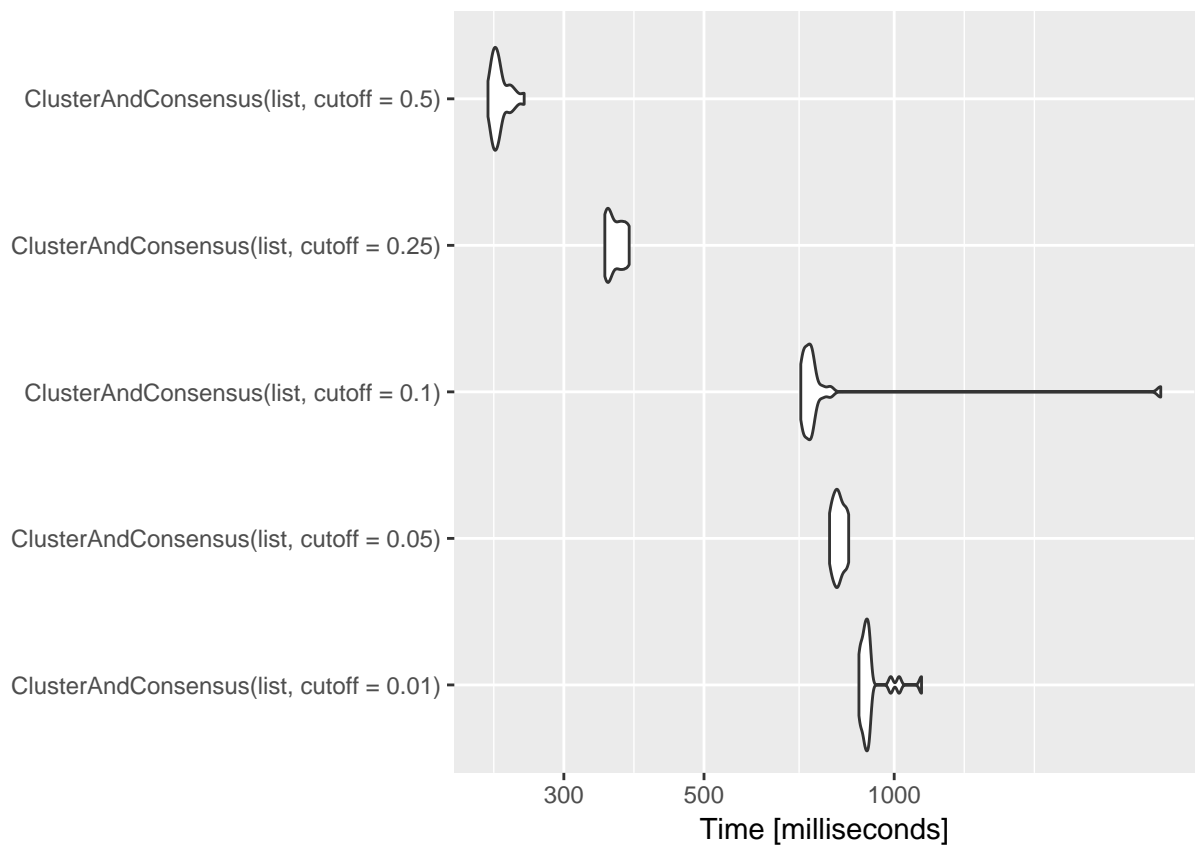
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##
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## Time difference of 0.29 secs
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## Time difference of 0.13 secs
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## Time difference of 0.16 secs
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## Time difference of 0.16 secs
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## Time difference of 0.3 secs
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## Time difference of 0.25 secs
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## Time difference of 0.27 secs

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```

## Unit: milliseconds

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```

##                               expr      min      lq      mean
## ClusterAndConsensus(list, cutoff = 0.01) 879.4863 893.0848 920.1664
## ClusterAndConsensus(list, cutoff = 0.05) 790.1144 803.7156 817.3361
## ClusterAndConsensus(list, cutoff = 0.1) 711.4730 718.9919 830.8027
## ClusterAndConsensus(list, cutoff = 0.25) 348.3419 351.7409 362.2762
## ClusterAndConsensus(list, cutoff = 0.5) 227.5318 231.8292 237.6747
##      median      uq      max neval cld
## 903.0080 913.3711 1104.8399    20  b
## 815.4793 831.3965 847.1934    20  b
## 735.3835 743.0333 2641.9503    20  b
## 359.8545 371.7647 380.6694    20  a
## 235.5897 240.7449 259.6222    20  a

```

# Sample.seq

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## Time difference of 0.07 secs
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## Time difference of 0.02 secs
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## Time difference of 0.05 secs
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## Time difference of 0.01 secs
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## Time difference of 0.05 secs
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## Time difference of 0.04 secs

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## Time difference of 0.02 secs
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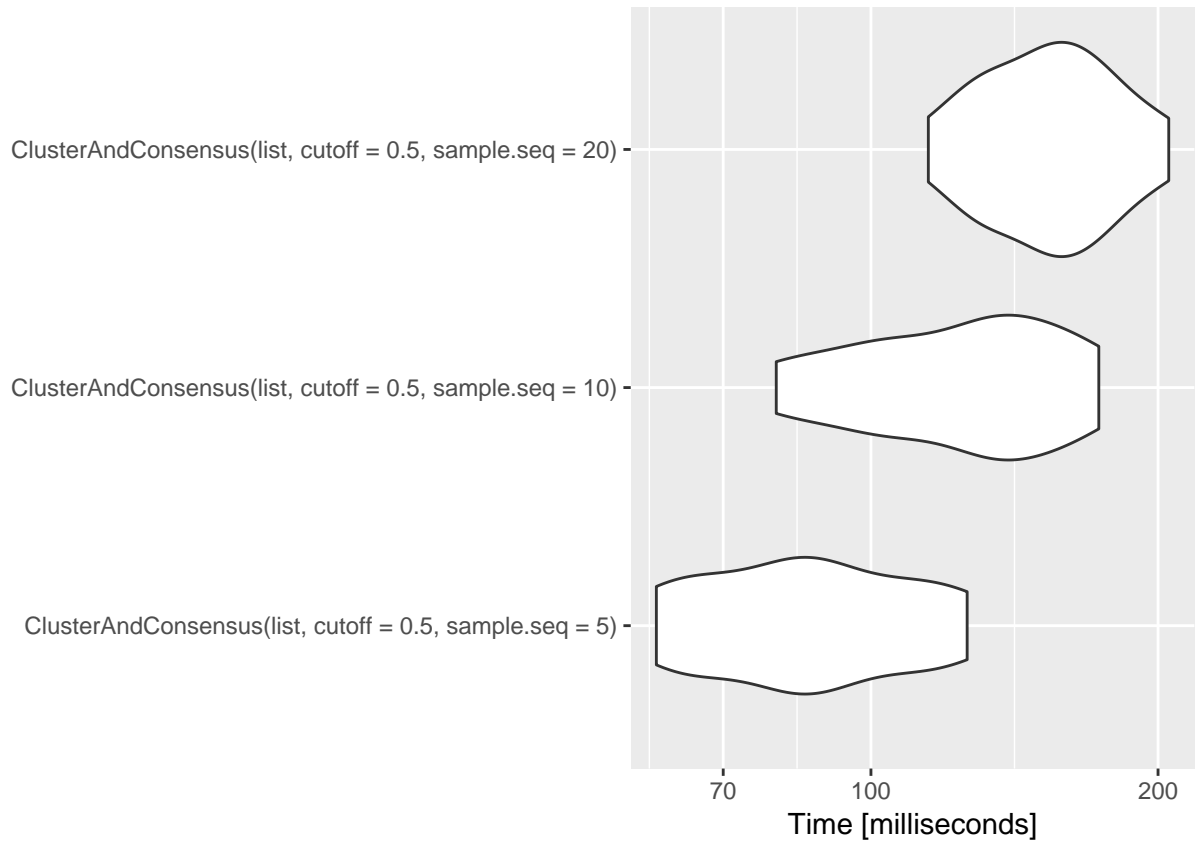
```



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## Time difference of 0.04 secs
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## Time difference of 0.01 secs
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## Time difference of 0.02 secs
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## =====
##
## Time difference of 0.01 secs

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```
## Unit: milliseconds
##
##      expr      min
## ClusterAndConsensus(list, cutoff = 0.5, sample.seq = 5) 59.56813
## ClusterAndConsensus(list, cutoff = 0.5, sample.seq = 10) 79.56527
## ClusterAndConsensus(list, cutoff = 0.5, sample.seq = 20) 114.86360
##      lq      mean   median      uq      max neval cld
## 68.6882  87.92426  86.12624 106.1674 126.1475   20  a
## 103.1893 126.69119 131.33648 147.4662 173.3567   20  b
## 134.0257 155.34378 154.00721 170.6218 205.2474   20  c
```