

9. quantum country

aantekeningen uit quantum country

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Quantum Computing for the Very Curious

Q: write the following in ket notation

$$\begin{pmatrix} \sqrt{0.7} \\ \sqrt{0.3} \end{pmatrix}$$

$$\sqrt{0.7} |0\rangle + \sqrt{0.3} |1\rangle$$

Q: It is useful to think of the left to right of a quantum wire as a passage of ...

A: time

Q: What is the matrix representation of the X-gate

$$A: X \equiv \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$$

Q: How many computational basis states does a qubit have?

A: 2

Q: How can you compute the length of $H \begin{pmatrix} 1 \\ 3 \end{pmatrix}$ without explicitly computing the product of the Hadamard gate and the vector? What is the length?

A: Hadamard operator leaves the length unchanged. The length is $\sqrt{1^2 + 3^2} = \sqrt{10}$

Q: Suppose we have a qubit in the state

$$\frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

. What is the probability of a measurement in the computational basis will give the result 0? What is then its posterior state?

A: 50 %, $|0\rangle$

Q: What are three types of physical systems that potentially can be used to store qubits?

A: photons, electrons, atoms, doped diamonds

Q: What do we call the two-dimensional vector space where the state of a qubit lives?

A: State space

Q: What is the inverse of a Hadamard gate?

A: Hadamard gate

Q: What does the Hadamard gate do to the state $|0\rangle$?

A: $|+\rangle$

Q: After we measure $\alpha|0\rangle + \beta|1\rangle$ in the computational base, is it still in the state $\alpha|0\rangle + \beta|1\rangle$?

A: No, its posterior state is either $|0\rangle$ or $|1\rangle$

Q: How can the following circuit be simplified?



A:

—————

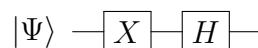
Q: What is the result of the operator product XX ?

A: I

Q: How many dimensions does the state vector of a qubit have?

A: 2

Q: How can the following circuit be written?



$HX|\Psi\rangle$ or $XH|\Psi\rangle$

A: $HX|\Psi\rangle$

Q: Is $\alpha|0\rangle + \beta|1\rangle$ the same as $\beta|1\rangle + \alpha|0\rangle$? Why?

A: same, order does not matter in plus operator

Q:How large is the matrix representing a single qubit gate?

A:2x2

Q:What is a quantum gate that can distinguish $|+\rangle$ and $|-\rangle$?

A:H

Q:Suppose we have a bit in the quantum state $|1\rangle$. What is the probability a measurement in the computational basis gives the result 0? and 1?

A:0, 1

Q:A superposition of quantum states is the same as a .. of quantum states

A: linear combination

Q:What are the three Pauli matrices:

A:XYZ (and I)

Q:What is $X|0\rangle$

A: $|1\rangle$

Q:What does the normalisation condition for the quantum states mean for the probabilities for a measurement in the computational basis?

A: They add up to 1

Q:Suppose we measure $|+\rangle$ or $|-\rangle$. Are the probability distributions of the outcome the same or different for these qubits?

A:The same

Q:What is a geometric interpretation of U being a unitary operation?

A:length preserving, e.g. rotation or reflection.

Q:What is the second quantum gate Alice applies to her qubits in the teleportation protocol? A:A Hadamard gate to the first qubit i.e. the one that started as $|\psi\rangle$

Q:Where does the term classical in the term 'classical bits' come from?

A:classical physics

Q:Suppose we have a quantum state $\sqrt{0.8}|01\rangle + \sqrt{.2}|10\rangle$ and we measure the first qubit in the computational basis. Supposing we

get 0 as the outcome, what is the corresponding state of the second qubit?

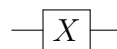
A: $|1\rangle$ with 100 % certainty

Q: What is the amplitude of the $|1\rangle$ state in the ket $\sqrt{0.7}|0\rangle + \sqrt{0.3}|1\rangle$

A: $\sqrt{0.3}$

Q: What is a quantum circuit showing the X gate being applied to a single qubit?

A:



Q: Suppose we have a quantum state $\sqrt{0.8}|01\rangle + \sqrt{.2}|10\rangle$ and measure the first qubit in the computational basis. Supposing we get one as an outcome, what is the corresponding state of the second qubit?

A: $|0\rangle$ with 100 % certainty

Q: How do the probabilities for the measurement outcomes in the teleportation protocol depend upon the amplitudes α and β in the state $\alpha|0\rangle + \beta|1\rangle$ being teleported?

A: They are independent. They do not depend on α and β at all.

Q: We use the term ket interchangeably with the term

A: (column) vector

Q: Why can't quantum teleportation be used to transmit a quantum state $|\Psi\rangle$ faster than light?

A: To teleport $|\psi\rangle$ to Bob, Alice must send Bob two bits of classical information. The transmission of classical information is limited by the speed of light.

Q: How are the two computational basis states of a qubit usually written?

A: $|0\rangle$ and $|1\rangle$

Q: How does the X gate act on a general state of a qubit?

A: Interchanges the coefficients

Q: Why is it that systems which make good quantum wires are often hard to build quantum gates for?

A: Systems which make good quantum wires interact weakly with other systems; to do a quantum gate we need to manipulate the qubit, and it is hard to manipulate a system which only weakly interacts with other systems.

Q: how many qubits are involved in a teleportation protocol?

A: 3

Q: Why do we rather write $X|0\rangle$ rather than $X(|0\rangle)$?

A: It is a matrix operation on a vector rather than a function applied on an argument.

Q: Why would a neutrino make a good quantum wire?

A: Neutrinos interact very weakly with other matter, which could make it very stable.

Q: How many qubits are directly involved in Alice's part of the teleportation protocol?

A: 2

Q: How many qubits are directly involved in Bob's part of the teleportation protocol?

A: 1

Q: Why are quantum wires often hard to implement?

A: Because qubits are fragile, and their state can easily be disturbed.

Q: In the quantum teleportation protocol, what is the 2-bit state initially shared between Alice and Bob?

A: $\frac{|00\rangle + |11\rangle}{\sqrt{2}}$

Q: What is the quantum circuit notation for a quantum wire?

A:

Q: What do we call the two-dimensional vector space where the state of a qubit lives?

A: state space

Q: What is the result of applying the X-gate to the quantum state

$$\frac{|0\rangle - |1\rangle}{\sqrt{2}}$$

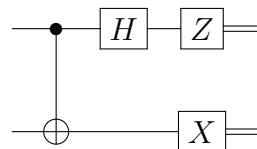
A: $X \frac{|0\rangle - |1\rangle}{\sqrt{2}} = \frac{|1\rangle - |0\rangle}{\sqrt{2}}$

Q: How do the probabilities for the measurement outcomes in the teleportation protocol depend upon the amplitudes α and β in the state $\alpha|0\rangle + \beta|1\rangle$ being teleported?

A: They are independent - they do not depend on those amplitudes at all.

Q: What is the total quantum circuit that Alice applies in a teleportation protocol?

A:



Q: We could rewrite the sequence: $|\Psi\rangle \xrightarrow{X} \xrightarrow{H}$ as..

A: $HX|\Psi\rangle$

Q: After a measurement, is a qubit in the state $\alpha|0\rangle + \beta|1\rangle$ still in that state?

A: No

Q: Suppose we have a qubit in the state $\frac{|0\rangle + |1\rangle}{\sqrt{2}}$. What is the probability that a measurement in the computational basis will give the result 0? What is the posterior state if that outcome occurs?

50 %, $|0\rangle$

Q: Suppose we have the state $|0\rangle$. What is the probability a measurement in the computational base gives the result 0? What is the probability the measurement gives the result 1?

A: 100 %, 1

Q: Suppose we have a qubit in the state

$$\frac{|0\rangle + |1\rangle}{\sqrt{2}}$$

. what is the probability that a measurement in the computational basis will give the result 1? What is the posterior state if that outcome occurs?

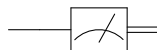
A: 50 %, $|1\rangle$

Q: Suppose we have the state $|1\rangle$. What is the probability a measurement in the computational base gives the result 0? What is the probability the measurement gives the result 1?

A: 0, 1

Q: How do we denote a computational basis measurement in the circuit model?

A:



Q: Suppose we do computational basis measurements for either $|+\rangle$ or $|-\rangle$. Are the probability distributions for outcomes the same or different for these states?

A: The same

Q: Suppose you had a device that could exactly determine the state of a qubit. How could such a device be used as part of a scheme to communicate infinite classical information, using a single qubit.

A: The sender of the classical bits could encode the (infinite string of) bits in the binary expansion of the real part of the amplitude α in the state $\alpha|0\rangle + \beta|1\rangle$. The receiver of the qubit could figure out α and thus the entire string of bits.

Q: What does the normalization condition for quantum states mean about the probabilities for a measurement in the computational basis?

A: Their probabilities for measurement outcomes sum up to 1.

Q: What is a quantum circuit with which we can distinguish the states $|+\rangle$ and $|-\rangle$?

H \rightarrow measurement

General single-qubit gates

$$U^\dagger \equiv (U^T)^*$$

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix}^* = \begin{pmatrix} a^* & b^* \\ c^* & d^* \end{pmatrix}$$

$$Z \equiv \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

ASo Z leaves $|0\rangle$ unchanged and maps $|1\rangle$ to $-|1\rangle$ Show that X, H, I, Z are unitary

we get into complex numbers, skip for course.

$$Y \equiv \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$$

rotation

$$Y \equiv \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix}$$

Q:A single qubit is represented as a 2x2 ... matrix

A:Unitary

Q:what is H^\dagger ? A:H

Q:What is the algebraic condition defining unitarity for a matrix U?

A: $UU^\dagger = I$

Q:How large is the matrix representing a single qubit-state?

A:2x2

Q:What are three common names for the dagger operation?

A: adjoint operation, dagger operation, transpose complex conjugate, Hermitian conjugate operation

Q:What notation we use to denote Pauli matrices?

A:I, X, H, Z

Q:What is the element in the bottom left corner of a Y-gate?

A:

What does it mean if a matrix is unitary?

Unitary operators preserve the length of their inputs. (cf. rotations, reflections).

This means that once normalised, as quantum gates do not change length, the outcome is normalised.

Unitary matrices are the only matrices that preserve length, they are the exact class that preserve length.

Holds also for N dimensions

Proof ...

how can you compute the length of

$$\left\| \begin{pmatrix} 3 \\ 10 \end{pmatrix} \right\|$$

$$\sqrt{10}$$

$$\text{important } \|U|\psi\rangle\| = \||\psi\rangle\|$$

Why are unitaries the only matrices which preserve length?

$$(M|\psi\rangle)^\dagger = \langle\psi|M^\dagger$$

$$\|M|\psi\rangle\|^2 = \langle\psi|M^\dagger M|\psi\rangle$$

$M|e_j\rangle$ is the j th column of M and that $\langle e_j|M|e_k\rangle$ is the jk th element of M .

summary of teleportation protocol

Q: What is the starting state of for the teleportation protocol?

A: $|000\rangle$

- a. Initial state: Alice has a qubit $|\psi\rangle$. Alice and Bob each prepare a bit in the $|0\rangle$ state, entangle these through a H and CNOT gate and each take one qubit of this now entangled pair.
- b. Alice applies a CNOT between $|\psi\rangle$ and her qubit, applies a H-gate to the first bit of the outcome. She measures both her qubits in the computational basis getting results $z=0$ or 1 and $x=0$ or 1 . The probability of each of the outcomes $(00, 01, 10, 11)$ is $\frac{1}{4}$.
- c. Classical communication: Alice broadcasts both classical bits z and x .
- d. Bob recovers the quantum state of $|\psi\rangle$. Bob applies Z^z and X^x and recovers $|\psi\rangle$.

Alice no longer possesses $|\psi\rangle$. It is teleported not copied!

review questions

What is the first gate Alice applies to her qubits in the teleportation protocol

CNOT with $|\psi\rangle$ as the control and the other as target

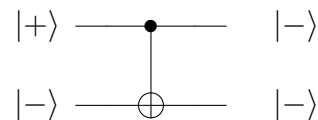
How many classical bits Alice has to send to Bob in the teleportation protocol?

2

To recover the teleported state Bob applies combinations of the Pauli .. and .. matrices

X and Z

Dit circuit moet je eens uitschrijven.



$$CNOT|C,T\rangle = CNOT|+, -\rangle$$

$$CNOT = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}, |+\rangle = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}, |-\rangle = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix}$$

$$CNOT|+-\rangle = CNOT\left(\begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix} \otimes \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix}\right) = \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} 1 \\ -1 \\ 1 \\ -1 \end{pmatrix} =$$

$$\frac{1}{2} \begin{pmatrix} 1 \\ -1 \\ -1 \\ 1 \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 1 \\ -1 \end{pmatrix} \otimes \begin{pmatrix} 1 \\ -1 \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix} \otimes \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix} = |-, -\rangle$$

NB in Quantum inspire levert dit als antwoord de hele computational basis op met gelijke kansen. Ik kan daar geen $|-\rangle$ terugvinden

Nou dat is wat! In de Hadamard basis (hoe heet deze pendant van de computational basis) is de toestand van de control bit niet behouden!

Nu is de inverse van een CNOT natuurlijk de CNOT. Wat betekent dat voor het bovenstaande circuit? [is ook van rechts naar links te lezen]

quantum country, QC for the very curious part 3

Een qc programma ziet er altijd zo uit:

- Start in een gedefinieerde basis meestal computational basis (cb), z-richting.
- pas een aantal CNOT en single qubit operatoren toe
- eindig met een meting in de cb

Q:What is the initial step of a quantum computation? A:preparation (most often in the cb)

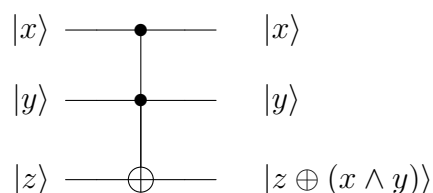
Q:What is the last step in a qcomputation? A: a measurement in the cb

Q: is the product of two unitary matrices also unitary A: Yes (apply them one by one and you'll see)

Q: Suppose I introduced a gate $e^{i\theta} I$. Does it affect the outcome of a circuit? A: N, the resulting phase shift does not influence the amplitudes of the coefficients of the state vectors. The amplitudes determine the measurement.

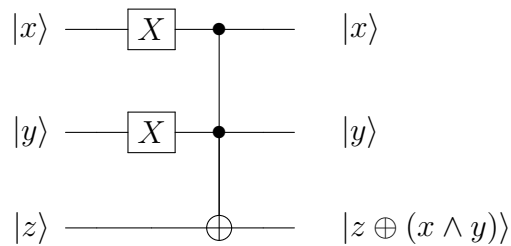
Q: the X-operation and the -X operation are the same except a ... factor. A: global phase factor

A toffoli gate can be used to model a AND gate.



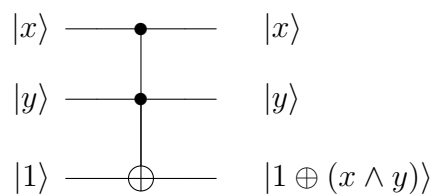
exercise: build a NAND gate. A NAND is the negation of an AND gate

Solution:



Er is nog een simpeler oplossing:

Solution:



Q: What is the problem of storing the amplitudes of a many quantum system in a classical computer? A: The number of amplitudes increases quickly with the amount of qubits,

Q: what number theoretical problem quantum computers appear to be good in solving? A: factoring numbers into prime factors.

Q: What is the name of the quantum algorithm to find prime factors of a number? A: Shor's algorithm

Q: Can quantum computers simulate the standard model or quantum gravity? A: unknown (2x)

Q: There were successes in simulating QFT by .. A: John Preskill and colleagues

Exercise: show that the Toffoli gate is reversible. Solution: The x , y give no problem, they are just copied (in the circuit). If the z is unchanged, its reverse will not change it either, since y and x are unchanged. If it is changed, the repetitive application will change it back, resulting in the identity operator in all cases where the Toffoli has been applied twice. In matrix operation the problem is only in the lower right corner. Squaring this matrix yields identity.

quantum country, how quantum teleportation works

Q:What quantum circuit prepares a

$$\frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

state at the start of a teleportation?

A: (0,0) H CNOT

Q:If Bob prepares the state

$$\frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

, shared at the start of the teleportation protocol, why does it not matter which qubit he sends to Alice?

A:Because the states are symmetrical.

Q:Is it possible to use quantum teleportation to transmit information faster than light?

A:No

How quantum teleprotation works**The teleprotation protocol****How to remember the teleprotation protocol**

Does teleportation protocol allow faster than light communication?

How partial measurements work

Q:What quantum circuit prepares a

$$\frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

state at the start of a teleportation?

A: (0,0) H CNOT

If Bob prepares the state

$$\frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

, shared at the start of the teleportation protocol, why does it not matter which qubit he sends to Alice? A: Because the states are symmetrical.

Q: Is it possible to use quantum teleportation to transmit information faster than light?

A: No

How partial measurements work

Suppose we measure the first two qubits of a three bit system in the computational basis. What are the possible states of the outcome?

$|00\rangle, |10\rangle, |01\rangle, |11\rangle$

Q: Suppose we do a measurement in the cb of the first two bits of a three bit system. What are the possible outcomes?

A: 00, 01, 10, 11

Q: Suppose we have a quantum state $\sqrt{0.8}|0\rangle + \sqrt{0.2}|1\rangle$ and measure the first qubit in the computational basis. What is the probability the measurement gives 1 as an outcome

A: 0.2

Q: Suppose we have a quantum state $\sqrt{0.8}|0\rangle + \sqrt{0.2}|1\rangle$ and measure the first qubit in the computational basis. What is the probability the measurement gives 0 as an outcome

A: 0.8

Verifying that the teleportation protocol works

$$(\alpha|0\rangle + \beta|1\rangle) \frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

expand:

$$\frac{\alpha|000\rangle + \alpha|011\rangle + \beta|100\rangle + \beta|111\rangle}{\sqrt{2}}$$

Apply CNOT to the first two qubits:

Outcome	Probability	Bob's state
00	$\frac{1}{4}$	$\alpha 0\rangle + \beta 1\rangle = \psi\rangle$
01	$\frac{1}{4}$	$\alpha 1\rangle + \beta 0\rangle = X \psi\rangle$
10	$\frac{1}{4}$	$\alpha 0\rangle - \beta 1\rangle = Z \psi\rangle$
11	$\frac{1}{4}$	$\alpha 1\rangle - \beta 0\rangle = XZ \psi\rangle$

Tabel 9.1: metingen

$$\frac{\alpha |000\rangle + \alpha |011\rangle + \beta |110\rangle + \beta |101\rangle}{\sqrt{2}}$$

Now we apply a Hadamard to the first qubit

$$\frac{\alpha |000\rangle + \alpha |100\rangle + \alpha |011\rangle + \alpha |111\rangle + \beta |010\rangle - \beta |110\rangle + \beta |001\rangle - \beta |101\rangle}{2}$$

$$\frac{|00\rangle (\alpha |0\rangle + \beta |1\rangle) + |01\rangle (\alpha |1\rangle + \beta |0\rangle) + |10\rangle (\alpha |0\rangle - \beta |1\rangle) + |11\rangle (\alpha |1\rangle - \beta |0\rangle)}{2}$$

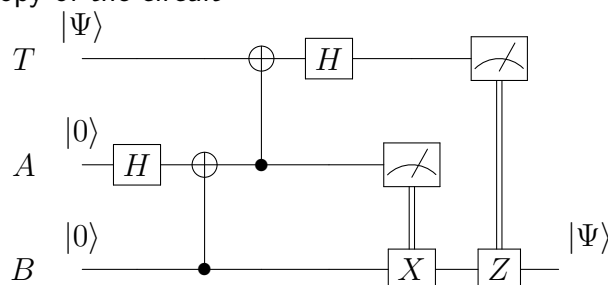
When Alice measures in the computational base, the outcome is $|00\rangle$ with probability given by $\frac{\alpha^2 + \beta^2}{4} = \frac{1}{4}$

The resulting state for Bob is $\alpha |0\rangle + \beta |1\rangle$

The results for the other outcomes of the measurements in Alice's computational basis are:

Now Bob's state is very similar to the original $|\psi\rangle$. He is only a few Pauli gates off. He has to do either nothing, apply X, apply Z or apply ZX respectively. The protocol he has to apply is encoded in the classical bits.

Here a copy of the circuit



Note1: The classical bits reveal nothing about state $|\psi\rangle$. Note2: If Eve steals the classical bits she cannot retrieve $|\psi\rangle$.

The measurements are saying how the states are changed to $|\psi\rangle$, $|X\psi\rangle$, $|Z\psi\rangle$, and $XZ|\psi\rangle$. without giving any information on $|\psi\rangle$!

Note3: It does not matter where Bob is in this story. Alice may broadcast the classical bits over the internet.

What are the probabilities for the outcomes of the teleportation protocol?

$\frac{1}{4}$ for all outcomes

Suppose Alice doesn't know where Bob is. How can she transmit the two classical bits so Bob can complete the teleportation protocol.

Summary of the teleportation protocol

staat hierboven

Q: what is the starting state for a teleportation protocol?

A:

$$|\psi\rangle \frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

Q: How many classical bits does Alice send to Bob in the teleportation protocol?

A: 2

Q: To recover the teleported state, Bob applies a gate .. and ..

A: X, Z

Q: What is the first gate Alice applies to her qubits in the teleportation protocol?

A: CNOT with $|\Psi\rangle$ as control and one of the entangled qubits as target

Q:

aantekeningen uit EdEx course

Which statements are true for physical qubits

- +physical qubits can be in superposition
- physical qubits consist of one or more physical qubits
- physical qubits have longer coherence time than physical qubits
- +physical qubits are physically realised qubits
- physical qubits are three level qubits

Which statements are true for logical qubits

- +logical qubits can be in superposition
- +logical qubits consist of one or more physical qubits
- +logical qubits have longer coherence time than physical qubits
- logical qubits are physically realised qubits
- logical qubits are three level qubits

One important fact about comparing classical and quantum computers is that everything a quantum computer can do a classical computer can also do. However, a lot of classical computer memory is needed to simulate a small number of qubits.

To simulate n qubits on a classical computer, you need 64×2^n classical bits (working with double precision floating point numbers).

There are classical computers that have access to about 5000 terabytes (500×10^{14} bits) of memory. How many logical bits are needed to perform a computation that cannot be simulated on a classical computer?

- about 5
- =about 50
- about 500
- about 5000

When evaluating a design for a new quantum computer, it is helpful to have a checklist of known requirements that the computer has to fulfil. The DeVincenzo criteria provide such a checklist.

Which five of the following statements are DeVincenzo criteria for the implementation of quantum computation?

- A quantum system must have the ability to work at room temperature
- +Good qubits are needed, the quantum state cannot be lost
- +A quantum system must have a universal set of quantum gates (a universal set of gates is a set such that any of the possible gates can be rewritten in a sequence of the gates in the universal set).
- It must be possible to send qubits between two locations.
- +A quantum system must be scalable, with well-defined qubits
- +It must be possible to perform measurements on a qubits in a quantum system
- A quantum system must have the ability to be faster than a classical computer
- +A quantum system must be able to initialize qubits to a fixed state, such as the zero state.
- It must be possible to transfer stationary qubits (qubits on a quantum chip) to flying qubits (qubits that are sent to another location over a quantum channel and back).

flimpje: Main takaways:

- A quantum internet is composed of end nodes, repeaters and control traffic.
- An entangled state between two qubits is the essence of the power of a quantum internet.
- Qubits can be entangled at a very long distance, but when we make the same measurement on both qubits, they will give the same outcome. This feature is called maximum coordination.
- when two qubits are maximally entangled, it is impossible for any other qubit to have a share of this entanglement, making it inherently private.
-

Quantum versus classical internet

In the lecture, some aspects of a quantum internet were introduced. You will compare these with those of a classical internet.

Which of the following features are possible on a quantum internet, but not on a classical internet?

- +Secure communication
- Faster than light communication
- Anonymous communication
- +Secure cloud computing

Size of an end node

In the lecture Stefanie discussed the end nodes of a quantum internet, and said that a large quantum computer is not necessary in order to have a functioning end node.

Why can the quantum computers at the end nodes be very small?

- Because the number of nodes is very small
- =Because one qubit at each end node is enough to have entanglement over the whole network.
- Because we can use repeaters to increase the number of qubits at each node.

In the video, Stefanie explained features of the entanglement between two qubits.

Which of the following statements are true about the entanglement of qubits?

- =Measuring one qubit of a pair of maximally entangled qubits is enough to know the state of the other qubit as well.
- Only two qubits can be entangled.
- Qubits can be copied.
- =Maximal entanglement is inherently private.

5. The nature of entanglement

What is the definition of maximal coordination?

- Maximum coordination means that, if measured, one qubit sends a message to the other qubit, telling it to give the same output.
- =Maximum coordination means that, if measured the same way, two entangled qubits always give the same outcome.
- Maximum coordination means that one entangled qubit is a copy of the other.

Why is a quantum computer with few (i.e. about five) logical qubits also relevant?

- It can do some tasks exponentially faster than a classical computer.
- =It is useful for scientists and quantum software engineers to test their concepts.
- =It is already possible to securely communicate with just two end nodes, each with one qubit.
- It is possible to solve some problems with five qubits that a classical computer cannot solve.

There are two more DiVincenzo criteria:

- f. The ability to interconvert stationary and flying qubits
- g. The ability to faithfully transmit flying qubits between specified locations

(info from Menno's lecture 'from one to many qubits')

- =A quantum internet requires flying qubits
- A flying qubit is always a photon
- Any qubit interacting with other qubits is a flying qubit
- The ability to apply quantum gates to flying qubits is required for quantum communication.

Main takeaways

- There is a great symmetry in multiplying and factoring: multiplying is easy, factoring is difficult.
- This symmetry is used in cryptography
- Shor's quantum factoring algorithm: an algorithm which makes factoring possible in reasonable time, something that is not possible on a classical computer.

Shor's algorithm brings the problem of factoring from exponential to polynomial.

Een van Marcel Vonks werkbladen https://www.nemosciencemuseum.nl/media/filer_public/12/3b/123bdffb-0ec0-4e97-a4fc-5dfd5801c28a/quantum_en_relativiteit_quantum_en_relativiteit_rekenen_met_elektronen_leerling.pdf

De quirky simulator <https://www.quantum-quest.nl/quirky/QuirkyQuest4.html>

Weblessen (careljan shouten) <https://webcolleges.uva.nl/Mediasite/Catalog/catalogs/default>

Quantum secure authentication (twente) <https://nymus3d.nl/portfolio/project/quantum-secure-authentication>

Why Everything You Thought You Knew About Quantum Physics is Different - with Philip Ball <https://www.youtube.com/watch?v=q7v5NtV8v6I>

Quantum mechanics is weird:

- Quantum objects can be both particles and waves (particle-wave duality)
- Quantum objects can be at more than one state at the time (superposition)
- You cannot know exactly two properties of an quantum object (Heisenberg uncertainty principle)
- Quantum objects can affect one another at huge distances instantly (entanglement)
- You can't measure anything without disturbing it (qm is subjective)

quantum random walk Quantum random walks - an introductory overview <https://arxiv.org/pdf/quant-ph/0303081.pdf>

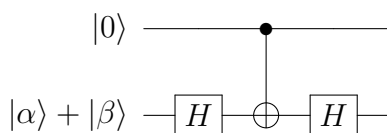
Wolfram demonstrations <https://demonstrations.wolfram.com/QuantumRandomWalk/>

<https://demonstrations.wolfram.com/QuantumTeleportation/>

Aantekeningen Annemarije

opg 14

eerst met $|0\rangle$ als controle $\begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \alpha |0\rangle + \beta |1\rangle$



$$H \begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \end{pmatrix}$$

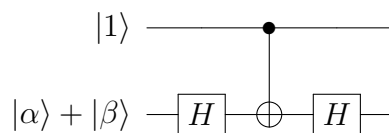
$$CNOT(|0\rangle, H(\alpha + \beta)) = CNOT\left(\begin{pmatrix} 1 \\ 0 \end{pmatrix} \otimes H\begin{pmatrix} \alpha \\ \beta \end{pmatrix}\right) =$$

$$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \\ 0 \\ 0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \\ 0 \\ 0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \otimes \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \end{pmatrix}$$

Het tweede bit is het target. Hierop laten we nogmaals H los:

$$H \frac{1}{\sqrt{2}} \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \end{pmatrix} = \frac{1}{\sqrt{2}} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \alpha + \beta + \alpha - \beta \\ \alpha + \beta - \alpha + \beta \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 2\alpha \\ 2\beta \end{pmatrix} = \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$

Nu met met $|1\rangle$ als controle $\begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \alpha|0\rangle + \beta|1\rangle$



$$H \begin{pmatrix} \alpha \\ \beta \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} \alpha + \beta \\ \alpha - \beta \end{pmatrix}$$

$$CNOT(|1\rangle, H(\alpha + \beta)) = CNOT\left(\begin{pmatrix} 0 \\ 1 \end{pmatrix} \otimes H\begin{pmatrix} \alpha \\ \beta \end{pmatrix}\right) =$$

$$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} 0 \\ 0 \\ \alpha + \beta \\ \alpha - \beta \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ \alpha - \beta \\ \alpha + \beta \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 1 \end{pmatrix} \otimes \begin{pmatrix} \alpha - \beta \\ \alpha + \beta \end{pmatrix}$$

Het tweede bit is het target. Hierop laten we nogmaals H los:

$$H \frac{1}{\sqrt{2}} \begin{pmatrix} \alpha - \beta \\ \alpha + \beta \end{pmatrix} = \frac{1}{\sqrt{2}} \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} \alpha - \beta \\ \alpha + \beta \end{pmatrix} = \frac{1}{2} \begin{pmatrix} \alpha - \beta + \alpha + \beta \\ \alpha - \beta - \alpha - \beta \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 2\alpha \\ -2\beta \end{pmatrix} = \begin{pmatrix} \alpha \\ -\beta \end{pmatrix}$$

Heb ik een rekenfout gemaakt? De oplossing in kansdichtheid lijkt gelijk.