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> restart:
```

```
Gegevens:
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```
> m:=.5;
g:=9.81;
A:=20*10^(-4);
theta:=25/360*(2*Pi);
rho:=1.293;
mu:=0.06695880134;
nb_frames:= 35;
Cd:='Cd';
```

```
m := 0.5
g := 9.81
A := 1/500
θ := 5/36 π
ρ := 1.293
μ := 0.06695880134
nb_frames := 35
Cd := Cd
```

(1)

```
Symbolische differentiaalvergelijking
```

```
> vgl_symb:=-'mu'*'m'*'g'*sin(Pi/2-'theta')-1/2*'rho'*'A'*diff(x(t),t)^2*'Cd'+ 'm'*'g'*cos(Pi/2-'theta')='m'*diff(x(t),t$2);
```

$$vgl_symb := -\mu m g \cos(\theta) - \frac{1}{2} \rho A \left(\frac{d}{dt} x(t) \right)^2 Cd + m g \sin(\theta) = m \left(\frac{d^2}{dt^2} x(t) \right) \quad (2)$$

```
> vgl:=-mu*m*g*sin(Pi/2-theta)-1/2*rho*A*diff(x(t),t)^2*Cd+m*g*cos(Pi/2-theta)=m*diff(x(t),t$2);
```

$$vgl := -0.3284329206 \sin\left(\frac{13}{36} \pi\right) - 0.001293000000 \left(\frac{d}{dt} x(t) \right)^2 Cd + 4.905 \cos\left(\frac{13}{36} \pi\right) = 0.5 \left(\frac{d^2}{dt^2} x(t) \right) \quad (3)$$

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Opgelost met beginvoorwaarden
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```
> dsolve({vgl,x(0)=0,D(x)(0)=0});
```

$$x(t) = \frac{1}{129300} \frac{1}{Cd} \left(-3 t \sqrt{\left(-471848629262 \sin\left(\frac{13}{36} \pi\right) + 7046850000000 \cos\left(\frac{13}{36} \pi\right) \right) Cd} + 500000000 \ln\left(\frac{1}{2} e^{\frac{3}{250000000} t \sqrt{\left(-471848629262 \sin\left(\frac{13}{36} \pi\right) + 7046850000000 \cos\left(\frac{13}{36} \pi\right) \right) Cd} + \frac{1}{2}} \right) \right) \quad (4)$$

```
> convert( '(4)' , 'string' );
```

$$x(t) = \frac{1}{129300} \cdot (-3 \cdot t \cdot ((-471848629262 \cdot \sin(13/36 \cdot \pi) + 7046850000000 \cdot \cos(13/36 \cdot \pi)) \cdot C_d)^{1/2} + 500000000 \cdot \ln(1/2 \cdot \exp(3/250000000 \cdot t \cdot ((-471848629262 \cdot \sin(13/36 \cdot \pi) + 7046850000000 \cdot \cos(13/36 \cdot \pi)) \cdot C_d)^{1/2}) + 1/2)) / C_d \quad (5)$$

Deze vergelijking wordt in Excel ingevuld om de luchtweerstandscoefficiënt C_d te vinden.