

Optimization techniques

Bloom filters

Bloom filters

- Probabilistic data structure, check membership for a value in a set.
- How it works: S , set of n values $\rightarrow \text{const} * n$ bits
calculate $\text{hash}(v) \in [1, \text{const} * n]$
set bit $\text{hash}(v)$ to 1

Test $w \in S \rightarrow h(w) = 1$?

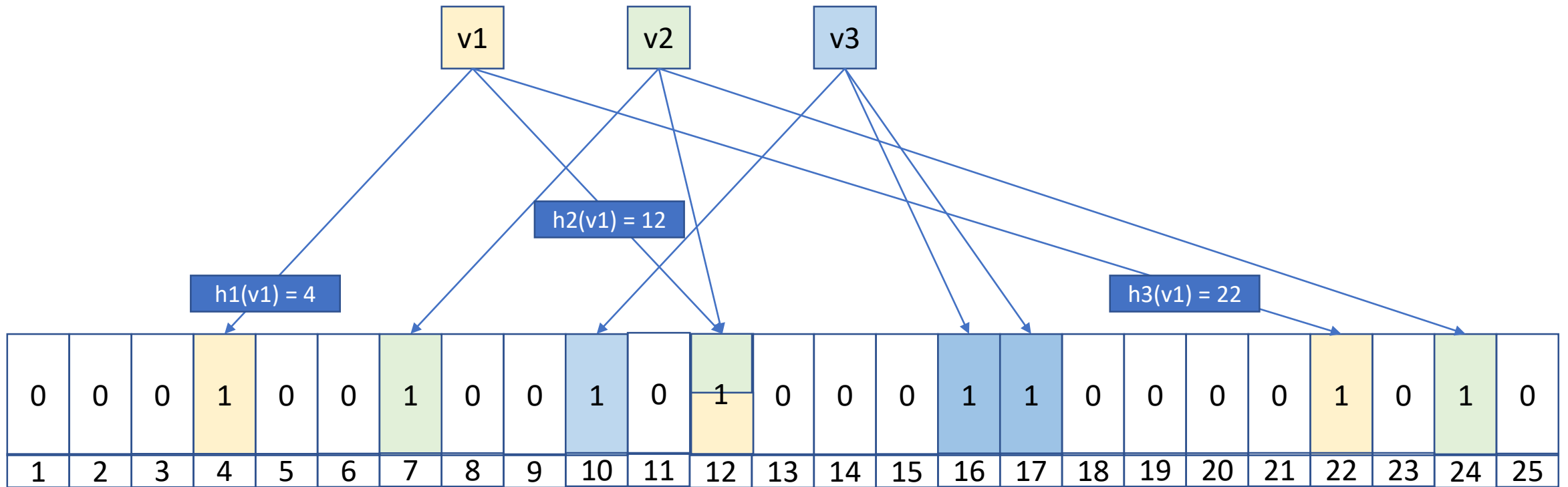
- Small probability of **false positive**. $w_1 \in S, w_2 \notin S \quad h(w_1) = h(w_2)$

Bloom filters

- To reduce the probability of false positives use $k > 1$ independent hash functions.

- How it works: S , set of n values $\rightarrow \text{const} * n$ bits
calculate $h_1(v), h_2(v) \dots h_k(v) \in [1, \text{const} * n]$
set bits $h_1(v), h_2(v) \dots h_k(v)$ to 1

Test $w \in S \rightarrow h_1(w) = 1$ and $h_2(w) = 1 \dots$ and $h_k(w) = 1$?



Small probability of **false positive**.

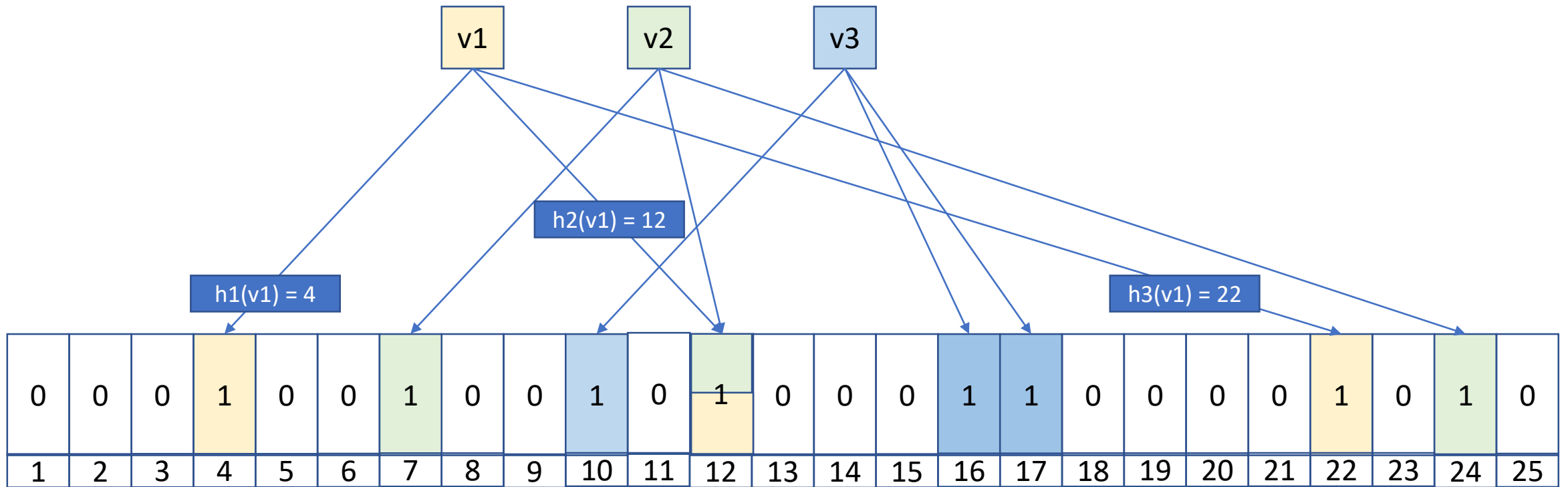
Probability of **false negative** = 0.

Bloom filters

- Used only to add elements or the test membership.
- Once an element is added to the filter it cannot be removed.
- If all bits are set to 1, the probability of false positives increases.
More space → more accuracy.
- More hash functions
Latency → more accuracy.

Bloom filters – independent hashing

- A family of hash functions $H = \{h: U \rightarrow [1..m]\}$ is k-independent if $\forall (x_1, x_2 \dots x_k) \in U^k$ and $\forall (y_1, y_2 \dots y_k) \in [1..m]^k$:
 - $Pr_{h \in H} [h(x_1) = y_1 \wedge h(x_2) = y_2 \dots \wedge h(x_k) = y_k] = \frac{1}{m^k}$
- $h(x_1)$ uniformly distributed.
- $h(x_1), h(x_2), \dots, h(x_k)$ independent random variables.



Small probability of **false positive**.

false positive. Value w : $B[h_1(w)] = 1 \ B[h_2(w)] = 1 \ \dots \ B[h_k(w)] = 1$

Probability of **false negative** = 0.

Each hash of w equals a hash of an element in the set

Bloom filters – accuracy

- m size of array, n number of elements in S, k number of hash functions.
- Probability of false positive:

$$P = \left(1 - \left(1 - \frac{1}{m}\right)^{kn}\right)^k \quad \text{or}$$

$$P = \left(1 - e^{-\frac{kn}{m}}\right)^k$$

- $m = 10 * n$ and $k = 7 \simeq 0,01$

Bloom filters – accuracy

- m size of array, n number of elements in S, k number of hash functions.

- Probability of false positive:

$$P = \left(1 - \left(1 - \frac{1}{m} \right)^{kn} \right)^k \text{ or}$$

$h(w) \neq h1(v1)$

- m = 10 * n and k = 7 \simeq 0,01

Bloom filters – accuracy

- m size of array, n number of elements in S, k number of hash functions.

- Probability of false positive:

$$P = \left(1 - \left(1 - \frac{1}{m} \right)^{kn} \right)^k \quad \text{or}$$

$h_1(w) \neq h_1(v_1)$

$h_1(w) \neq h_1(v_1)$

.....

$h_1(w) \neq h_n(v_1)$

$h_1(w) \neq h_1(v_2)$

...

$h_1(w) \neq h_n(v_2)$

...

- $m = 10 * n$ and $k = 7 \simeq 0,01$

Bloom filters – accuracy

- m size of array, n number of elements in S, k number of hash functions.

- Probability of false positive:

$$P = \left(1 - \left(1 - \frac{1}{m} \right)^{kn} \right)^k \quad \text{or}$$

$$h_1(w) = h_1(v_1)$$

or

$$h_1(w) = h_1(v_1)$$

.....

$$h_1(w) = h_n(v_1)$$

or

$$h_1(w) = h_1(v_2)$$

...

$$h_1(w) = h_n(v_2)$$

...

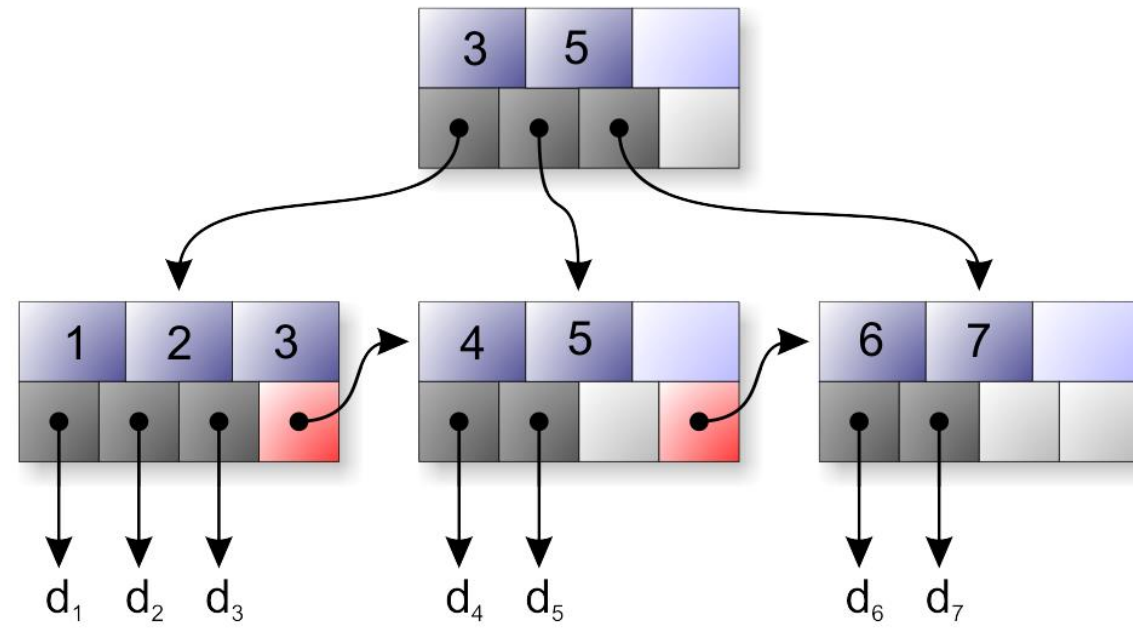
- $m = 10 * n$ and $k = 7 \simeq 0,01$

Log Structured Merge-tree

Log Structured Merge Trees

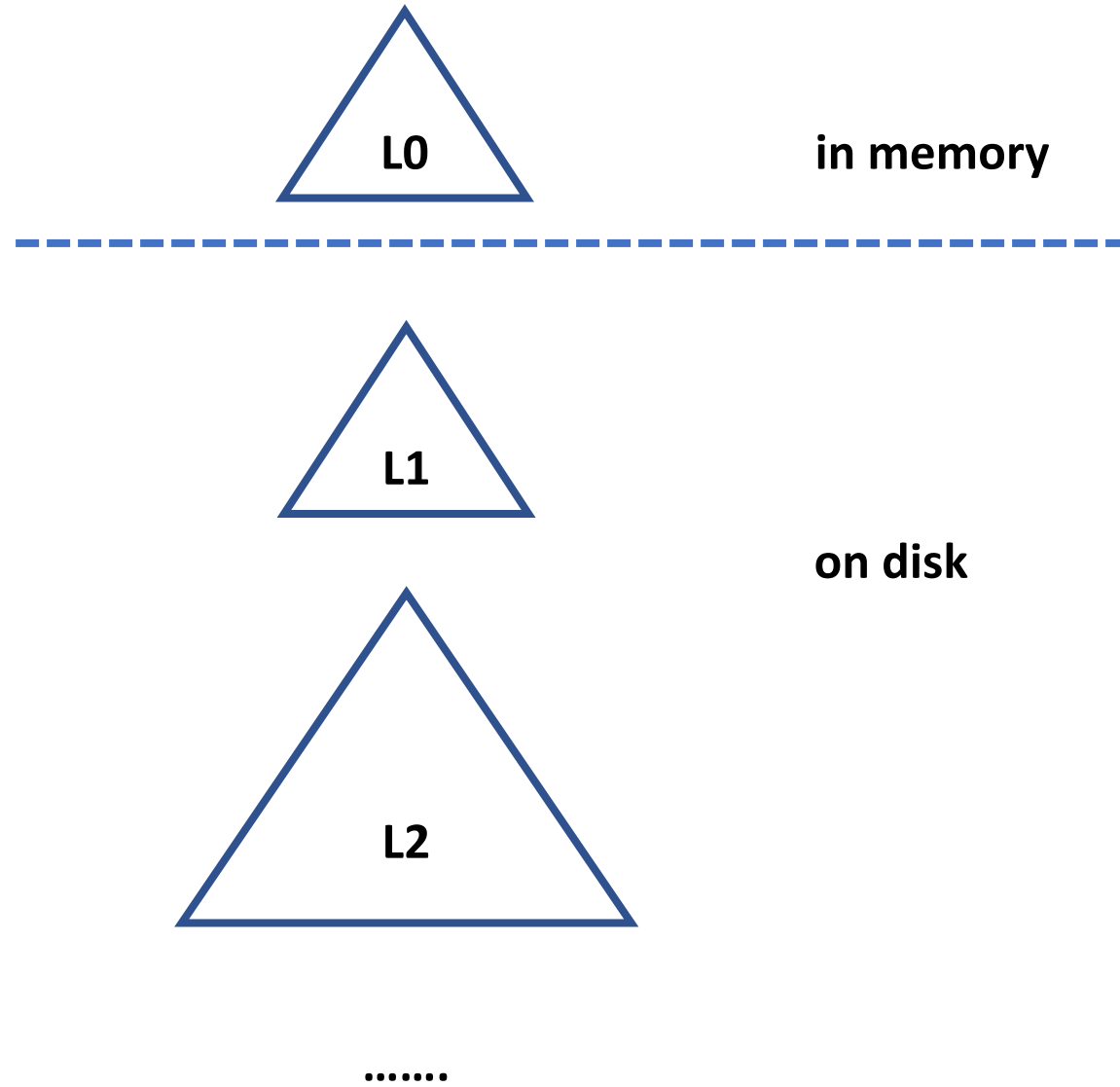
- Optimize I/O operations.
- Used by: Bigtable, LevelDB, Apache Cassandra etc.
- Data organized in B+ trees.
- Advantages: leaves sequentially located,
leaves are full.

B+ tree



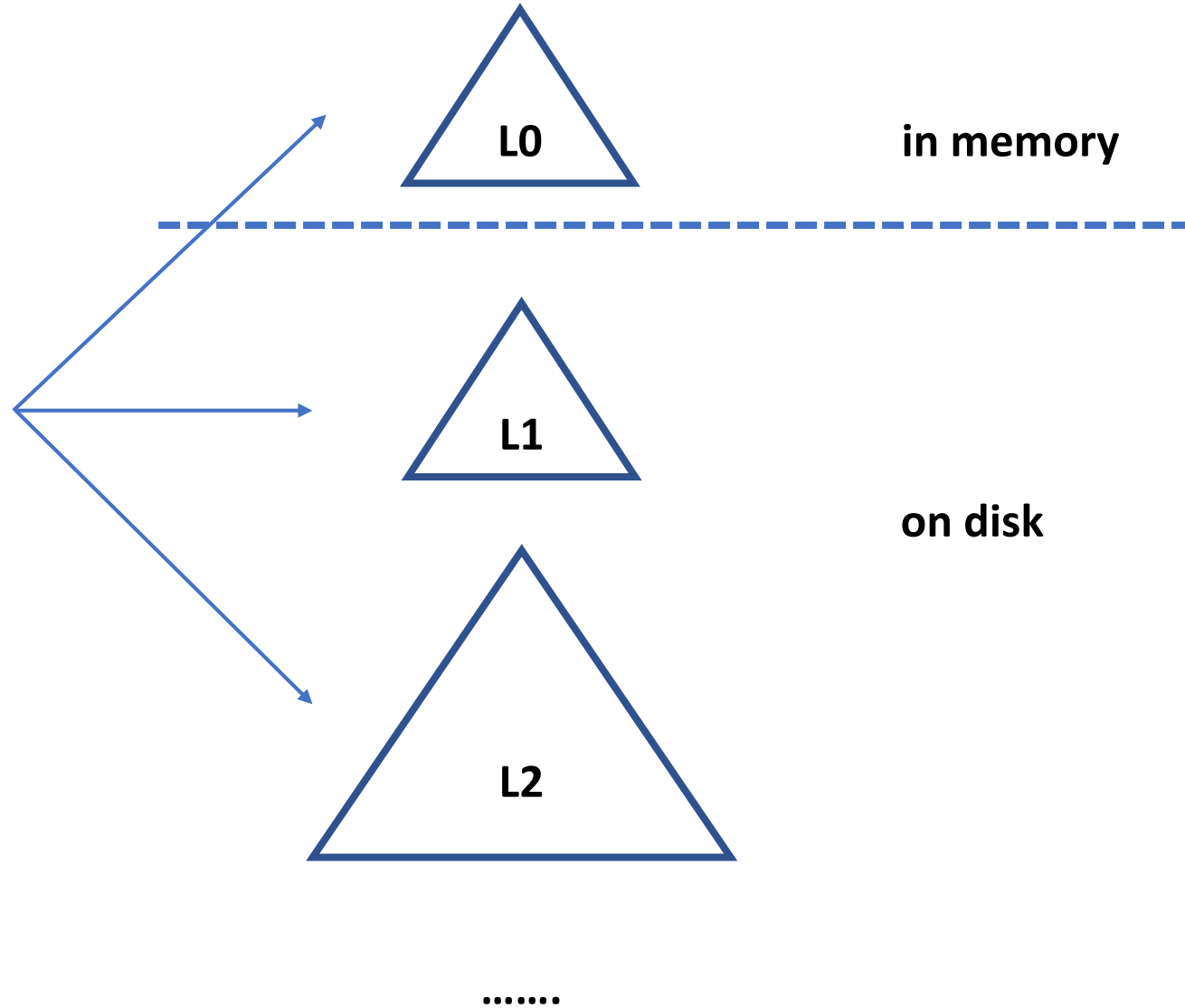
<https://commons.wikimedia.org/wiki/File:Btree.png>

LSMT

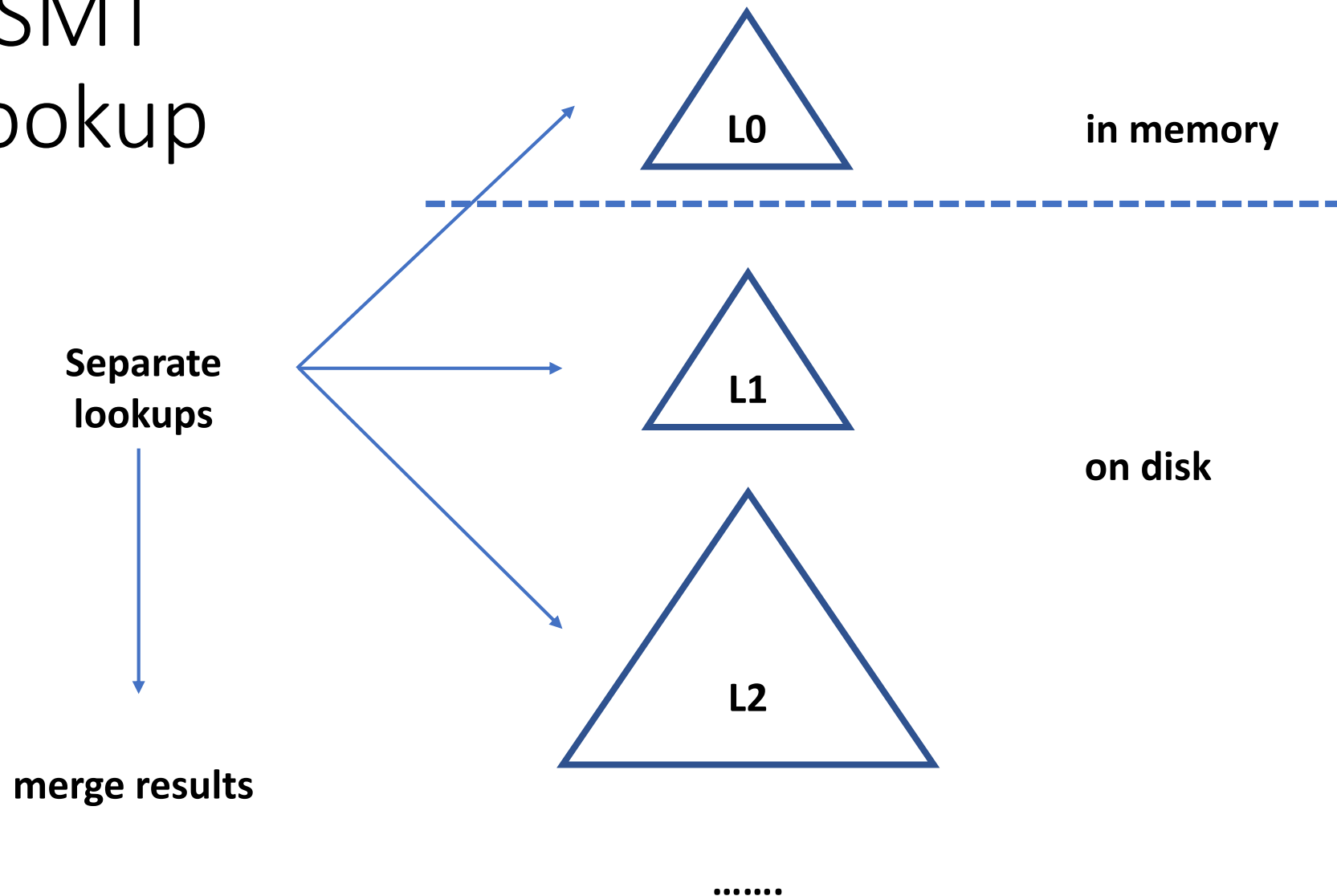


LSMT lookup

**Separate
lookups**

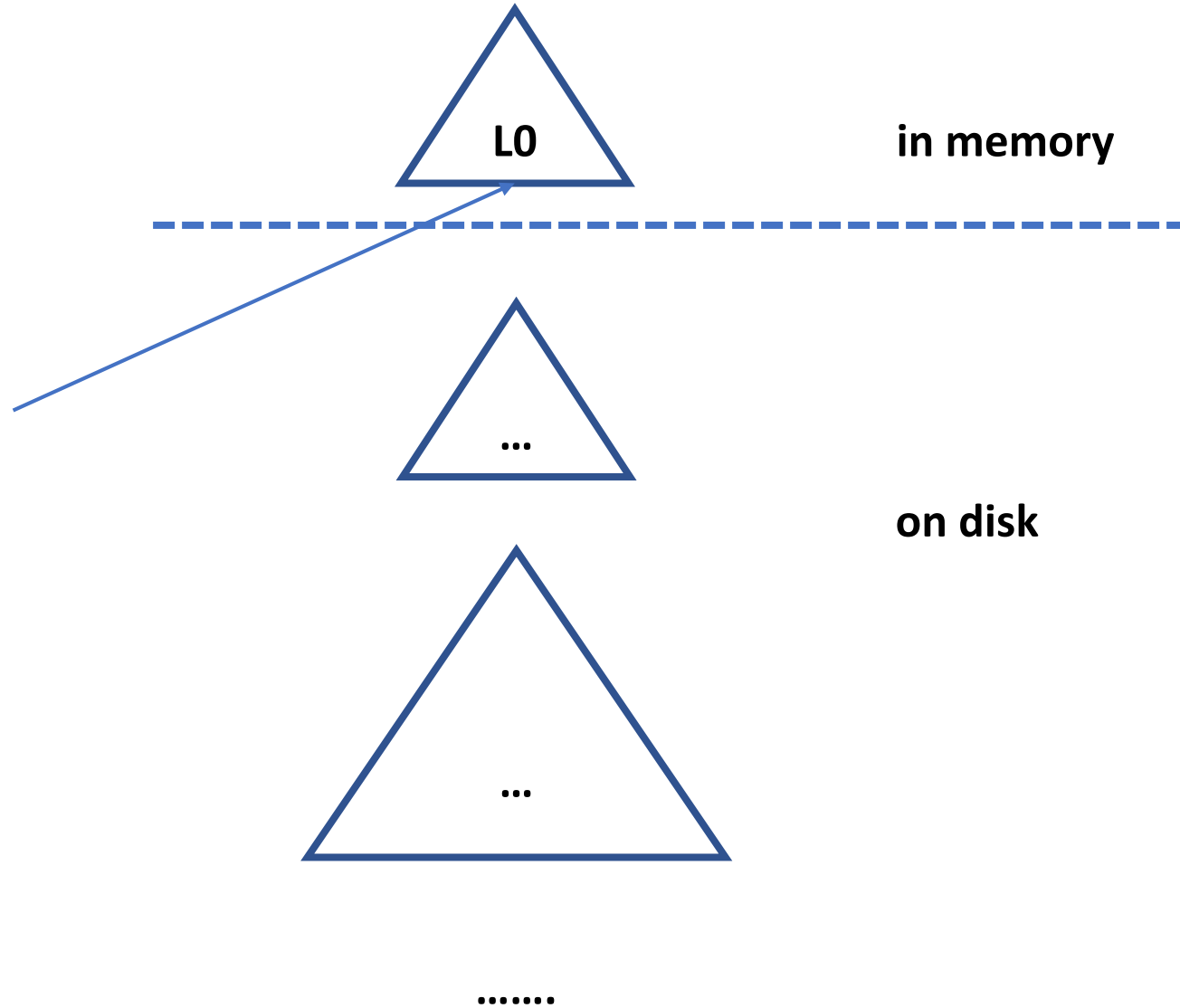


LSMT lookup



LSMT insert

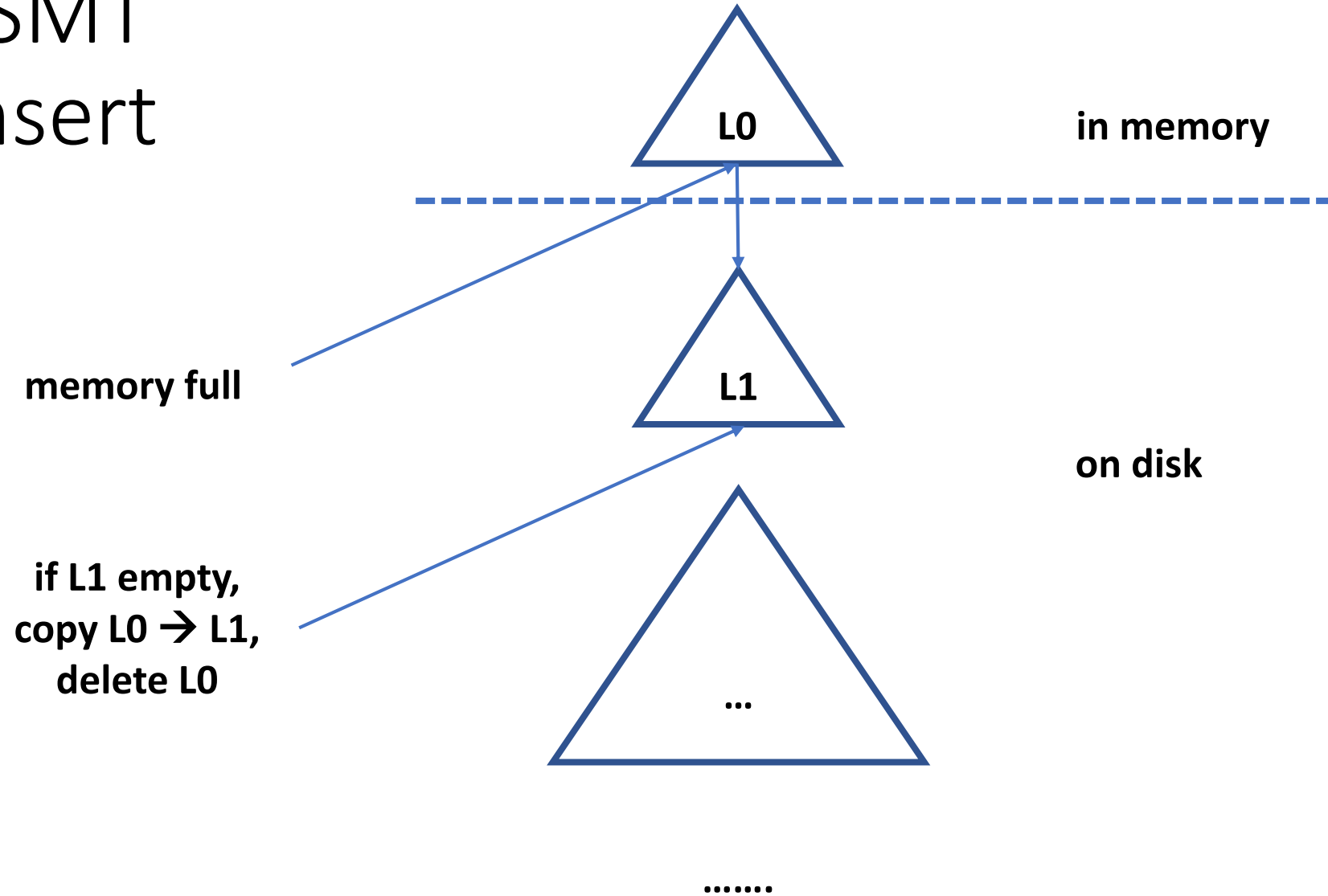
**insert if
memory
available**



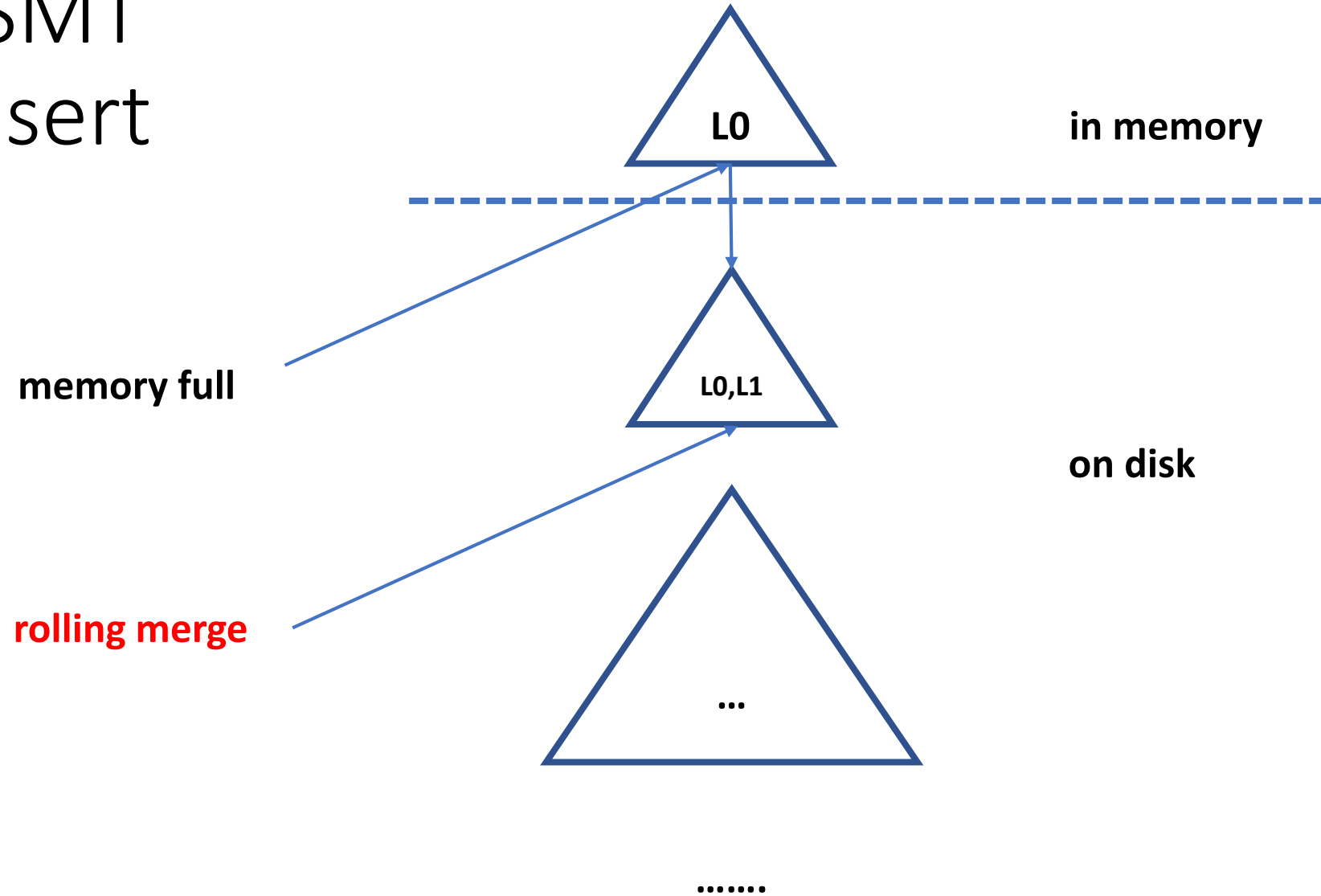
in memory

on disk

LSMT insert

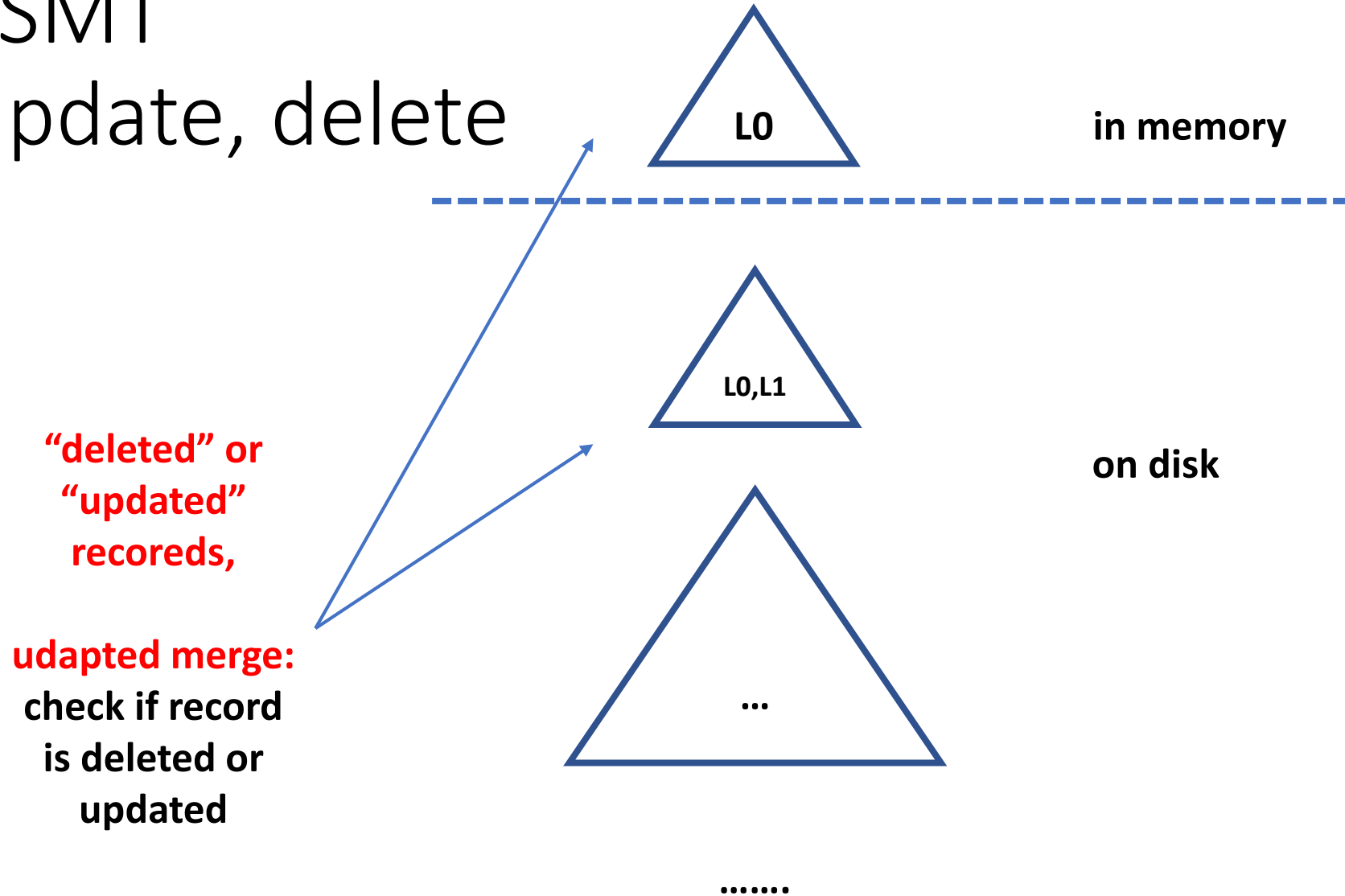


LSMT insert

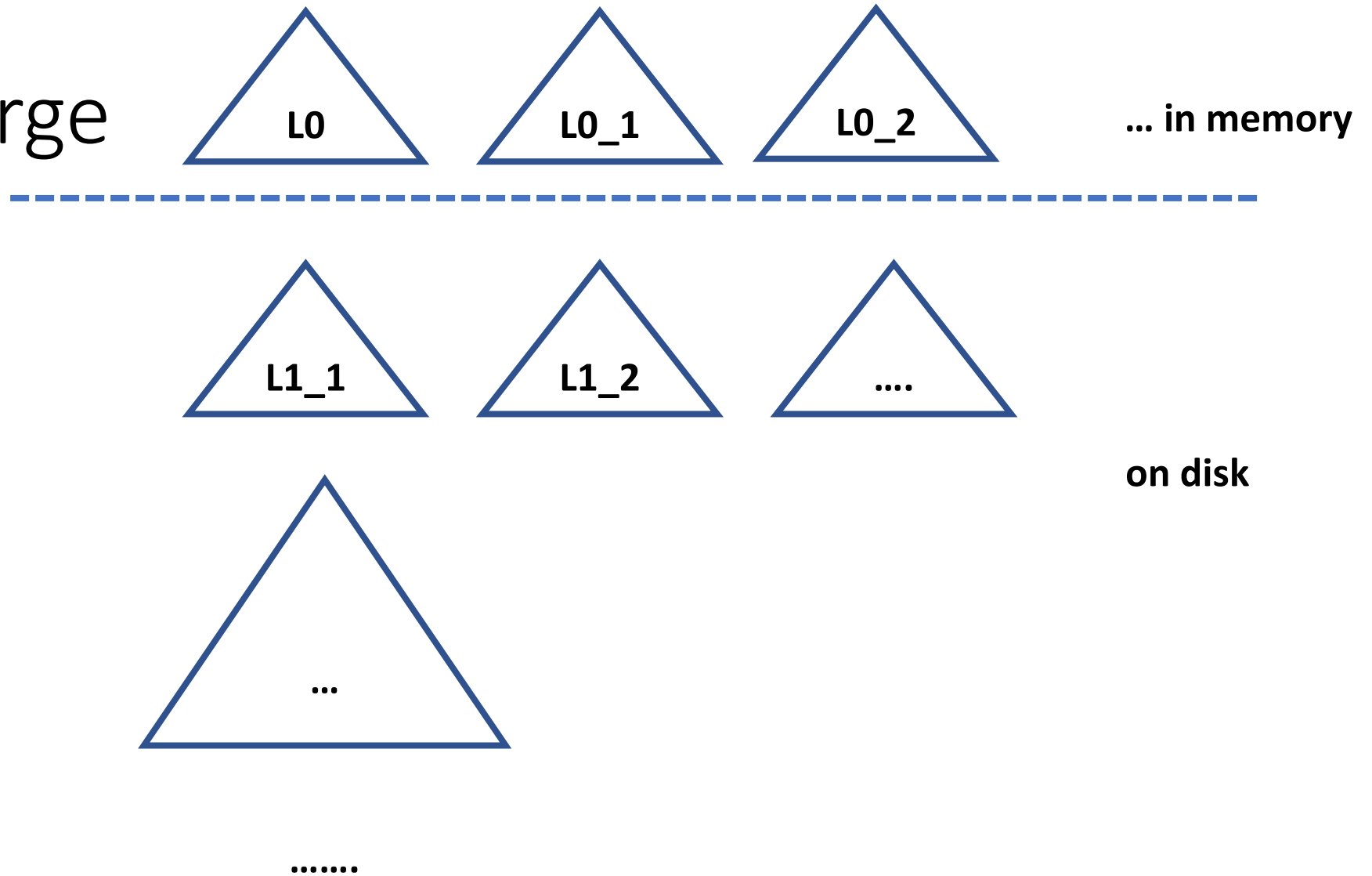


LSMT

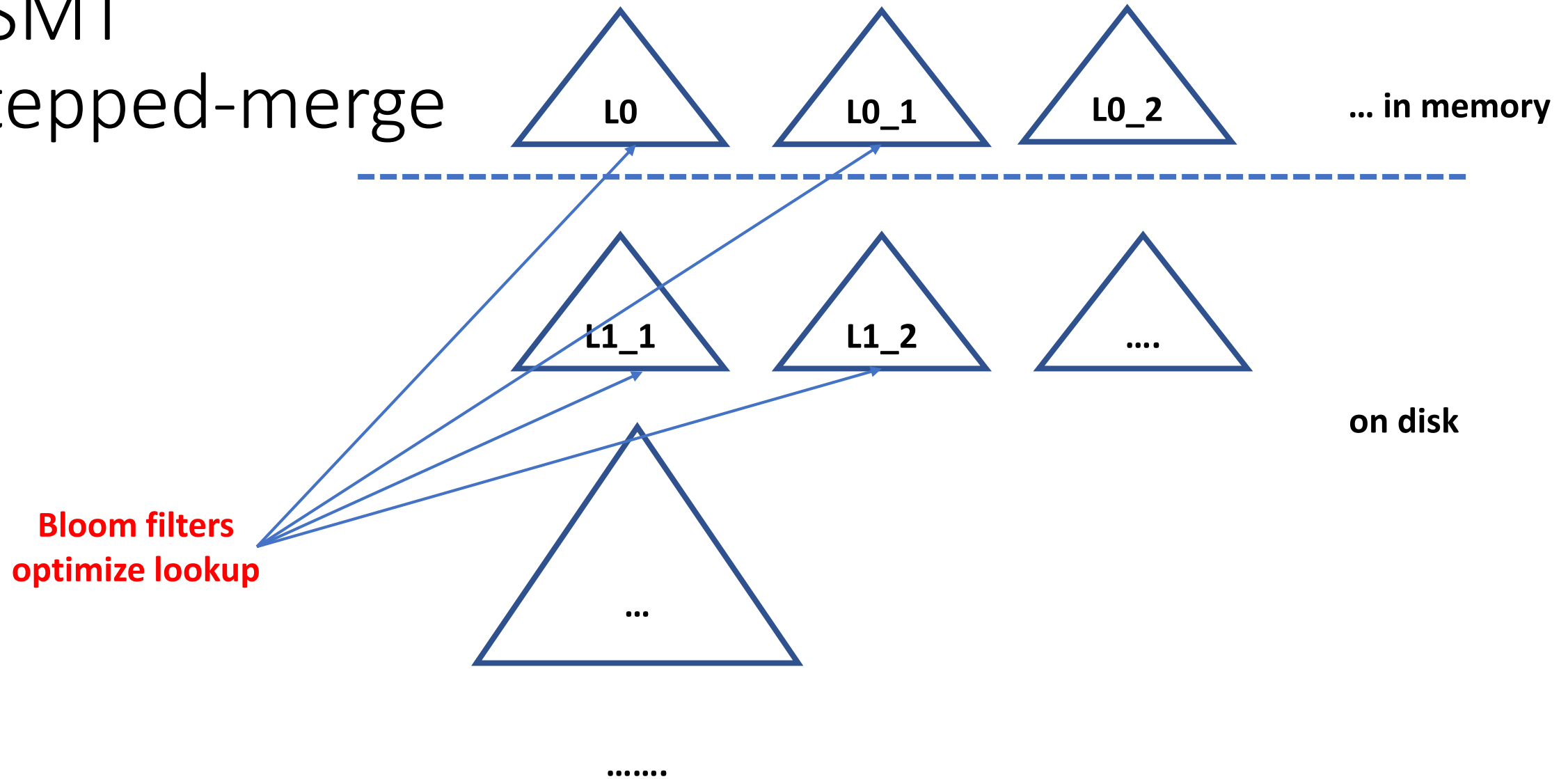
update, delete



LSMT stepped-merge



LSMT stepped-merge



Materialized views

Materialized views

- redundant data, contents can be inferred from the definition
- immediate view refresh
- deferred view refresh
- incremental update: modify only the affected parts of the materialized view

Materialized views

- Join operation
- Selection
- Projection
- Aggregation