

Teambook – Que Perdió

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Estructuras de Datos

Sparse Table

```
1.  const int tam = 1000010;
2.  const int logTam = 21;
3.
4.  int logTable[tam];
5.  int sparseTable[logTam][tam];
6.  int a[tam], n; // a[] es el arreglo original. n es el tamaño del arreglo.
7.
8.  void makeSparseTable()
```

```

9.  {
10.  logTable[0] = logTable[1] = 1;
11.
12.  for (int i = 2; i <= n; i++)
13.  {
14.      logTable[i] = logTable[i >> 1] + 1;
15.  }
16.
17.  for (int i = 0; i < n; i++)
18.  {
19.      sparseTable[0][i] = i;
20.  }
21.
22.  for (int k = 1; (1 << k) < n; k++)
23.  {
24.      for (int i = 0; i + (1 << k) <= n; i++)
25.      {
26.          int x = sparseTable[k-1][i];
27.          int y = sparseTable[k-1][i - (1 << (k-1))];
28.          sparseTable[k][i] = a[x] <= a[y] ? x : y;
29.      }
30.  }
31. }
32.
33. int queryST(int i, int j)
34. {
35.     int k = logTable[j - i];
36.     int x = sparseTable[k][i];
37.     int y = sparseTable[k][j - (1 << k) + 1];
38.     return a[x] <= a[y] ? x : y;
39. }

```

Segment Tree Iterative

```

1.  const int N = 1e5; // limit for array size
2.  int n; // array size
3.  int t[2 * N];
4.
5.  void build() { // build the tree
6.      for (int i = n - 1; i > 0; --i) t[i] = t[i<<1] + t[i<<1|1];
7.  }
8.
9.  void modify(int p, int value) { // set value at position p
10.     for (t[p += n] = value; p > 1; p >>= 1) t[p>>1] = t[p] + t[p^1];

```

```

11. }
12.
13. int query(int l, int r) { // sum on interval [l, r)
14.     int res = 0;
15.     for (l += n, r += n; l < r; l >>= 1, r >>= 1) {
16.         if (l&1) res += t[l++];
17.         if (r&1) res += t[--r];
18.     }
19.     return res;
20. }

```

Fenwick Tree

```

1.  #define clr(a,h)  memset(a,(h),sizeof(a))
2.
3.  int BIT[tam];
4.
5.  void update(int pos, int val)
6.  {
7.      pos++;
8.      while(pos < 200010)
9.      {
10.         BIT[pos] += val;
11.         pos += (pos & -pos);
12.     }
13. }
14.
15. int query(int pos)
16. {
17.     pos++;
18.     int res = 0;
19.     while(pos > 0)
20.     {
21.         res += BIT[pos];
22.         pos -= (pos & -pos);
23.     }
24.     return res;
25. }
26.
27. int main()
28. {
29.     clr(BIT,0);
30.     for(int i = n - 1; i >= 0; i--)
31.     {

```

```

32.   inv +=query(a[i]);
33.   update(a[i],1);
34. }
35. }

```

Fenwick Tree 2D

```

1.  #include <iostream>
2.
3.  using namespace std;
4.
5.  const int tam = 1000;
6.
7.  int BIT[tam][tam];
8.  int n, m;
9.
10. void update(int row, int col, int val)
11. {
12.     row++; col++;
13.     for (int i = row; i <= n; i += (i & -i))
14.     {
15.         for (int j = col; j <= m; j += (j & -j))
16.         {
17.             BIT[i][j] += val;
18.         }
19.     }
20. }
21.
22. int query(int row, int col)
23. {
24.     int res = 0;
25.     row++; col++;
26.     for (int i = row; i > 0; i -= (i & -i))
27.     {
28.         for (int j = col; j > 0; j -= (j & -j))
29.         {
30.             res += BIT[i][j];
31.         }
32.     }
33.     return res;
34. }

```

Segment Tree persistente

```

1.  struct node{

```

```

2.     ptr iz;
3.     ptr der;
4.     int val; //0.0
5.     int numero;
6.     node(){
7.         numero=-1;
8.         val=0;
9.     }
10. };
11. node nodos[tam];int cnodos=0;
12. node NUL;
13. ptr getnode()
14. {
15.     nodos[cnodos].iz=nodos[cnodos].der=&NUL;
16.     //if (cnodos>=tam)
17.         //tle(); no
18.     return &nodos[cnodos++];
19. }
20. void clr(){
21.     NUL.iz=NUL.der=&NUL;
22. }
23.
24. void insertar(ptr nuevo,ptr antnodo,int iz,int der,int pos,int numero)
25. {
26.     if (iz==der)
27.     {
28.
29.         (*nuevo).val=(*antnodo).val+1;
30.         (*nuevo).numero=numero;
31.         return;
32.     }
33.     int mid=(iz+der)/2;
34.     if (pos<=mid)
35.     {
36.         (*nuevo).der=(*antnodo).der;
37.         (*nuevo).iz=getnode();
38.         insertar((*nuevo).iz,(*antnodo).iz,iz,mid,pos,numero);
39.     }
40.     else
41.     {
42.         (*nuevo).iz=(*antnodo).iz;
43.         (*nuevo).der=getnode();
44.         insertar((*nuevo).der,(*antnodo).der,mid+1,der,pos,numero);
45.     }

```

```

46. (*nuevo).val=(*(*nuevo).iz).val+(*(*nuevo).der).val;
47. }
48.
49. int query(ptr noda,ptr nodob,ptr resta1,ptr resta2,int kth,int iz,int de
    r)
50. {
51.     if (iz==der)
52.     {
53.         return iz;// numero
54.     }
55.     int valiz=(*(*noda).iz).val+(*(*nodob).iz).val-(*(*resta1).iz).val-
        (*(*resta2).iz).val;
56.     int mid=(iz+der)/2;
57.     if (kth>valiz)
58.     {
59.         query((*noda).der,(*nodob).der,(*resta1).der,(*resta2).der,kth-
            valiz,mid+1,der);//kth-valiz ***
60.     }
61.     else
62.     {
63.         query((*noda).iz,(*nodob).iz,(*resta1).iz,(*resta2).iz,kth,iz,mid);
64.     }
65. }

```

Treap

```

1. #include <bits/stdc++.h>
2.
3. using namespace std;
4. struct node{
5.     int key, pri, siz;
6.     node *l, *r;
7. };
8. typedef node* pnode;
9. int sz(pnode t)
10. {
11.     return (t?t->siz:0);
12. }
13. void up_sz(pnode t)
14. {
15.     if(t) t->siz = sz(t->l) + 1 + sz(t->r);
16. }
17. void split(pnode t, pnode &l, pnode &r, int val)
18. {

```

```

19.     if(!t) r = l = NULL;
20.     else if(t->key <= val) split(t->r, t->r, r, val), l = t;
21.     else split(t->l, l, t->r, val), r = l;
22.     up_sz(t);
23. }
24. void merge(pnode &t, pnode l, pnode r)
25. {
26.     if(!l || !r) t=(l?l:r);
27.     else if(l->pri >= r->pri) merge(l->r, l->r, r), t = l;
28.     else merge(r->l, l, r->l), t=r;
29.     up_sz(t);
30. }
31. void insert(pnode &t, pnode it)
32. {
33.     if(!t) t = it;
34.     else if(it->pri > t->pri) split(t, it->l, it->r, it->key), t = it;
35.     else insert((t->key <= it->key?t->l:t->r), it);
36.     up_sz(t);
37. }
38. void erase(pnode &t, int val)
39. {
40.     if(!t) return;
41.     else if(t->key == val) {pnode temp = t; merge(t, t->l, t-
        >r); free(temp);}
42.     else erase((t->key <= val?t->l:t->r),val);
43.     up_sz(t);
44. }
45. pnode init(int val)
46. {
47.     pnode ret = (pnode)malloc(sizeof(node));
48.     ret->key = val, ret->siz = 1, ret->pri = rand(), ret->l = ret-
        >r = NULL;
49.     return ret;
50. }

```

HLD

```

1. #include <bits/stdc++.h>
2. #define clr(a,h) memset(a, (h), sizeof(a))
3.
4. using namespace std;
5.
6. /*
7. Cambiar:

```

```

8.      - Valor que se guarda en cada nodo en HLD
9.      - Operador en Segment Tree
10.     - Operador en queryUp y query
11. Inicializar:
12.     - root para LCA
13.     - chainNo = 0 para HLD
14.     - Llenar chainHead[] con -1 para HLD
15.     - actPosInBase = 0 para Segment Tree
16. */
17.
18. const int tam = 10010;
19. const int Log2Tam = 15;
20.
21. int nodeCost[tam];
22.
23. vi g[tam];
24. //HLD
25. int chainNo, chainPos[tam], chainIdx[tam], chainHead[tam], chainSize[tam];
26. //DFS
27. int dp[tam][Log2Tam], depth[tam], subTreeSize[tam];
28. int n, m, root;
29. //SegTree
30. int segTree[tam*4], posInBase[tam], baseArray[tam], actPosInBase;
31. int segTreeQ[tam*4];
32.
33. void DFS(int v, int p, int d)
34. {
35.     dp[v][0] = p;
36.     depth[v] = d;
37.     subTreeSize[v] = 1;
38.     for (int i = 0; i < g[v].size(); i++)
39.     {
40.         int u = g[v][i];
41.         if (u == p) continue;
42.         DFS(u, v, d+1);
43.         subTreeSize[v] += subTreeSize[u];
44.     }
45. }
46.
47. void HLD(int v, int p)
48. {

```

```

49.     if (chainHead[chainNo] == -
1) chainHead[chainNo] = v;
50.     chainIdx[v] = chainNo;
51.     chainPos[v] = chainSize[chainNo];
52.     chainSize[chainNo]++;
53.     posInBase[v] = actPosInBase;
54.     baseArray[actPosInBase++] = nodeCost[v]; // Aqui guardamos lo que queremos trabajar
55.                                             // con el Segment Tree
56.
57.     int bestChild = -1, maxSize = -1;
58.     for (int i = 0; i < g[v].size(); i++)
59.     {
60.         int u = g[v][i];
61.         if (u == p) continue;
62.         if (subTreeSize[u] > maxSize)
63.         {
64.             maxSize = subTreeSize[u];
65.             bestChild = u;
66.         }
67.     }
68.
69.     if (bestChild != -1) HLD(bestChild, v);
70.
71.     for (int i = 0; i < g[v].size(); i++)
72.     {
73.         int u = g[v][i];
74.         if (u == p || u == bestChild) continue;
75.         chainNo++;
76.         HLD(u, v);
77.     }
78. }
79.
80. void initLCA()
81. {
82.     clr(dp, -1);
83.     DFS(root, -1, 0);
84.     return;
85.     for (int pot = 1; pot < Log2Tam; pot++)
86.     {
87.         for (int v = 0; v < n; v++)
88.         {
89.             if (dp[v][pot-1] == -1) continue;

```

```

90.         dp[v][pot] = dp[ dp[v][pot-1] ][pot-1];
91.     }
92. }
93. }
94.
95. int LCA(int a, int b)
96. {
97.     // b siempre debajo o al mismo nivel que a
98.     if (depth[a] > depth[b]) swap(a, b);
99.
100.    int diff = depth[b] - depth[a];
101.    for (int pot = Log2Tam-1; pot >= 0; pot--)
102.    {
103.        if ( ( diff & (1 << pot) ) )
104.        {
105.            b = dp[b][pot];
106.        }
107.    }
108.    if (a == b) return a;
109.    for (int pot = Log2Tam-1; pot >= 0; pot--)
110.    {
111.        if (dp[a][pot] != dp[b][pot])
112.        {
113.            a = dp[a][pot];
114.            b = dp[b][pot];
115.        }
116.    }
117.    int lca = dp[a][0];
118.    return lca;
119.}
120.
121.void initSegTree(int b, int e, int nodo)
122.{
123.    int L = 2 * nodo + 1, R = L + 1, mid = (b + e) / 2
124.    ;
125.    if (b == e)
126.    {
127.        segTree[nodo] = baseArray[b];
128.        return;
129.    }
130.    initSegTree(b, mid, L);
131.    initSegTree(mid+1, e, R);

```

```

132.    // Funcion del Segment Tree que queremos hacer sob
    re el arbol
133.    segTree[nodo] = segTree[L] > segTree[R] ? segTree[
    L] : segTree[R];
134.}
135.
136.void updateSegTree(int b, int e, int nodo, int pos, in
    t val)
137.{
138.    int L = 2 * nodo + 1, R = L + 1, mid = (b + e) / 2
    ;
139.    if (b == e)
140.    {
141.        segTree[nodo] = val;
142.        return;
143.    }
144.    if (pos <= mid) updateSegTree(b, mid, L, pos, val)
    ;
145.    else updateSegTree(mid+1, e, R, pos, val);
146.
147.    segTree[nodo] = segTree[L] > segTree[R] ? segTree[
    L] : segTree[R];
148.}
149.
150.int querySegTree(int b, int e, int nodo, int i, int j)
151.{
152.    int L = 2 * nodo + 1, R = L + 1, mid = (b + e) / 2
    ;
153.    if (i <= b && e <= j) return segTree[nodo];
154.    if (j <= mid) return querySegTree(b, mid, L, i, j)
    ;
155.    else if (i > mid) return querySegTree(mid+1, e, R,
    i, j);
156.    else
157.    {
158.        int r1 = querySegTree(b, mid, L, i, j);
159.        int r2 = querySegTree(mid+1, e, R, i, j);
160.        return r1 > r2 ? r1 : r2;
161.    }
162.}
163.
164.int queryUp(int u, int v)
165.{

```

```

166.   int uChain, vChain = chainIdx[v], ans = -1;
167.   while (true)
168.   {
169.       uChain = chainIdx[u];
170.       if (uChain == vChain)
171.       {
172.           if (u == v) break;
173.           int queryAns = querySegTree(0, actPosInBas
e-1, 0, posInBase[v]+1, posInBase[u]);
174.           if (queryAns > ans)
175.           {
176.               ans = queryAns;
177.           }
178.           break;
179.       }
180.       int queryAns = querySegTree(0, actPosInBase-
1, 0, posInBase[ chainHead[uChain] ], posInBase[u]);
181.       if (queryAns > ans) ans = queryAns;
182.       u = chainHead[uChain];
183.       u = dp[u][0];
184.   }
185.   return ans;
186.}
187.
188.int query(int a, int b)
189.{
190.   int lca = LCA(a, b);
191.   int r1, r2;
192.   r1 = queryUp(a, lca);
193.   r2 = queryUp(b, lca);
194.   return r1 > r2 ? r1 : r2;
195.}

```

Grafos

LCA

```

1.  #include <bits/stdc++.h>
2.  #define clr(a,h)      memset(a, (h), sizeof(a))
3.
4.  using namespace std;
5.
6.  const int tam = 1010; // Max Nodos
7.  const int Log2Tam = (log(tam)/log(2)) + 3;

```

```

8.
9.  vector< vi > g;
10. int dp[tam][Log2Tam], depth[tam];
11. int n, m, root; // nodos, aristas, raiz del arbol
12.
13. void initDFS(int v, int p, int d)
14. {
15.     dp[v][0] = p; // padre inmediato
16.     depth[v] = d;
17.     for (int u : g[v])
18.     {
19.         if (u == p) continue;
20.         initDFS(u, v, d+1);
21.     }
22. }
23.
24. void initLCA()
25. {
26.     clr(dp, -1);
27.     initDFS(root, -1, 0);
28.     for (int pot = 1; pot < Log2Tam; pot++)
29.     {
30.         for (int v = 0; v < n; v++)
31.         {
32.             if (dp[v][pot-1] == -1) continue;
33.             dp[v][pot] = dp[ dp[v][pot-1] ][pot-1];
34.         }
35.     }
36. }
37.
38. int LCA(int a, int b)
39. {
40.     // b siempre debajo o al mismo nivel que a
41.     if (depth[a] > depth[b]) swap(a, b);
42.
43.     int diff = depth[b] - depth[a];
44.     for (int pot = Log2Tam-1; pot >= 0; pot--)
45.     {
46.         if ( ( diff & (1 << pot) ) )
47.         {
48.             b = dp[b][pot];
49.         }
50.     }
51.     if (a == b) return a;

```

```

52. for (int pot = Log2Tam-1; pot >= 0; pot--)
53. {
54.     if (dp[a][pot] != dp[b][pot])
55.     {
56.         a = dp[a][pot];
57.         b = dp[b][pot];
58.     }
59. }
60. int lca = dp[a][0];
61. return lca;
62. }
63.
64. int main()
65. {
66.     /*
67.     Iniciar el arbol en el grafo g
68.     Asignar la raiz en la variable root
69.
70.     Llamar initLCA() luego de crear el arbol
71.     LCA(a, b) devuelve el LCA de los nodos a y b
72.     */
73.     return 0;
74. }

```

Centroid Decomposition

```

1. int n;
2. vector<int> grafo[tam];
3. int hijos[tam], padre[tam]; bool marcado[tam];
4. void dfsHijos(int num, int pad)
5. {
6.     //<<num<<endl;
7.     hijos[num]=1;
8.     padre[num]=pad;
9.     int num2;
10.    for (int i = 0; i < grafo[num].size(); ++i)
11.    {
12.        num2=grafo[num][i];
13.        if (num2==pad || marcado[num2]==true) continue;
14.        dfsHijos(num2, num);
15.        hijos[num]+=hijos[num2];
16.    }
17. }
18. void operaciones(int num, int compsize);

```

```

19. void descomponer(int num)
20. {
21.    dfsHijos(num, num);
22.    queue<int> cola;
23.    cola.push(num);
24.    int maxx, minn, centroide, num2, auxnum;
25.    minn=hijos[num]; centroide=num;
26.    int compsize=0;
27.    while(!cola.empty())
28.    { compsize++;
29.      auxnum=cola.front(); cola.pop();
30.      maxx=hijos[num]-hijos[auxnum];
31.      for (int i = 0; i < grafo[auxnum].size(); ++i)
32.      {
33.          num2=grafo[auxnum][i];
34.          if (padre[auxnum]==num2 || marcado[num2]==1) continue;
35.          maxx=max(maxx, hijos[num2]);
36.          cola.push(num2);
37.      }
38.      if (minn>maxx)
39.      {
40.          minn=maxx;
41.          centroide=auxnum;
42.      }
43.    }
44.    //cout<<centroide<<" "<<compsize<<endl; para revisar
45.    operaciones(centroide, compsize);
46.    marcado[centroide]=1;
47.    for (int i = 0; i < grafo[centroide].size(); ++i)
48.    {
49.        num2=grafo[centroide][i];
50.        if (marcado[num2]==1) continue;
51.        descomponer(num2);
52.    }
53. }
54. // memset(marcado, false, sizeof marcado);

```

MinCost-MaxFlow

```

1. struct Edge
2. {
3.     int from, to, capacity, cost;
4. };
5.

```



```

6.  vector<vector<int>> adj, cost, capacity;
7.
8.  const int INF = 1e9;
9.
10. void shortest_paths(int n, int v0, vector<int>& d, vector<int>& p) {
11.     d.assign(n, INF);
12.     d[v0] = 0;
13.     vector<int> m(n, 2);
14.     deque<int> q;
15.     q.push_back(v0);
16.     p.assign(n, -1);
17.
18.     while (!q.empty()) {
19.         int u = q.front();
20.         q.pop_front();
21.         m[u] = 0;
22.         for (int v : adj[u]) {
23.             if (capacity[u][v] > 0 && d[v] > d[u] + cost[u][v]) {
24.                 d[v] = d[u] + cost[u][v];
25.                 p[v] = u;
26.                 if (m[v] == 2) {
27.                     m[v] = 1;
28.                     q.push_back(v);
29.                 } else if (m[v] == 0) {
30.                     m[v] = 1;
31.                     q.push_front(v);
32.                 }
33.             }
34.         }
35.     }
36. }
37.
38. int min_cost_flow(int N, vector<Edge> edges, int K, int s, int t) {
39.     adj.assign(N, vector<int>());
40.     cost.assign(N, vector<int>(N, 0));
41.     capacity.assign(N, vector<int>(N, 0));
42.     for (Edge e : edges) {
43.         adj[e.from].push_back(e.to);
44.         adj[e.to].push_back(e.from);
45.         cost[e.from][e.to] = e.cost;
46.         cost[e.to][e.from] = -e.cost;
47.         capacity[e.from][e.to] = e.capacity;
48.     }
49.

```

```

50. int flow = 0;
51. int cost = 0;
52. vector<int> d, p;
53. while (flow < K) {
54.     shortest_paths(N, s, d, p);
55.     if (d[t] == INF)
56.         break;
57.
58.     // find max flow on that path
59.     int f = K - flow;
60.     int cur = t;
61.     while (cur != s) {
62.         f = min(f, capacity[p[cur]][cur]);
63.         cur = p[cur];
64.     }
65.
66.     // apply flow
67.     flow += f;
68.     cost += f * d[t];
69.     cur = t;
70.     while (cur != s) {
71.         capacity[p[cur]][cur] -= f;
72.         capacity[cur][p[cur]] += f;
73.         cur = p[cur];
74.     }
75. }
76.
77. if (flow < K)
78.     return -1;
79. else
80.     return cost;
81. }

```

DP

SOS DP

```

1. //iterative version
2. for(int mask = 0; mask < (1<<N); ++mask){
3.     dp[mask][-1] = A[mask]; //handle base case separately (leaf states)
4.     for(int i = 0; i < N; ++i){
5.         if(mask & (1<<i))
6.             dp[mask][i] = dp[mask][i-1] + dp[mask^(1<<i)][i-1];
7.         else

```

```

8.     dp[mask][i] = dp[mask][i-1];
9. }
10.  F[mask] = dp[mask][N-1];
11. }
12. //memory optimized, super easy to code.
13. for(int i = 0; i < (1<<N); ++i)
14.     F[i] = A[i];
15. for(int i = 0; i < N; ++i) for(int mask = 0; mask < (1<<N); ++mask){
16.     if(mask & (1<<i))
17.         F[mask] += F[mask^(1<<i)];
18. }

```

Geometría

Convex Hull - Graham's Scan

```

1. struct point
2. {
3.     double x,y;
4.     point() {x=y=0;}
5.     point(double X, double Y): x(X), y(Y) {}
6. };
7. double dist(point a, point b)
8. {
9.     return hypot(a.x-b.x,a.y-b.y);
10. }
11. point tovec(point a, point b)
12. {
13.     return point(b.x-a.x, b.y-a.y);
14. }
15. double cross(point a, point b)
16. {
17.     return a.x*b.y - a.y*b.x;
18. }
19. bool collinear(point a, point b, point c)
20. {
21.     return fabs(cross(tovec(a,b), tovec(a,c))) < EPS;
22. }
23. bool ccw(point a, point b, point c)
24. {
25.     return cross(tovec(a,b), tovec(a,c)) >= 0;
26. }
27. point pivot;
28. bool anComp(point a, point b)

```

```

29. {
30.     if(collinear(pivot, a, b))
31.         return dist(pivot, a) < dist(pivot, b);
32.     a = tovec(pivot, a), b = tovec(pivot, b);
33.     return atan2(a.y,a.x) < atan2(b.y,b.x);
34. }
35. vector<point> ch(vector<point> p)
36. {
37.     int n = p.size(), i, j;
38.     if(n<=3)
39.     {
40.         if(p[0].x!=p[n-1].x||p[0].y!=p[n-1].y) p.pb(p[0]);
41.         return p;
42.     }
43.     int in=0;
44.     for(int i = 0; i < n; i++)
45.         if(p[i].y < p[in].y || p[i].x < p[in].x && p[i].y == p[in].y)
46.             in = i;
47.     pivot = p[in];
48.     for(int i = 0; i < n; i++)
49.     {
50.         cout<<p[i].x<<' '<<p[i].y<<endl;
51.     }
52.     cout<<endl;
53.     swap(p[0],p[in]);
54.     cout<<pivot.x<<' '#<<pivot.y<<endl;
55.     sort(++p.begin(), p.end(),anComp);
56.     for(int i = 0; i < n; i++)
57.     {
58.         cout<<p[i].x<<' '<<p[i].y<<endl;
59.     }
60.     cout<<endl;
61.     i = 2;
62.     vector<point> s = {p[n-1], p[0], p[1]};
63.     while(i < n && s.size()>0)
64.     {
65.         j = s.size();
66.         if(ccw(s[j-2],s[j-1],p[i]) || j == 2)
67.         {
68.             s.pb(p[i]);
69.             i++;
70.         }
71.         else
72.             s.pop_back();

```

```

73. }
74. return s;
75. }

```

Convex Hull – Monotone Chain

```

1. #include <bits/stdc++.h>
2. using namespace std;
3. #define rep(i,a,b) for(int i = a; i <= b; ++i)
4. #define invrep(i,b,a) for(int i = b; i >= a; --i)
5. typedef long long int ll;
6. // -----
7. // Convex Hull: Andrew's Montone Chain Algorithm
8. // -----
9.
10. struct Point {
11.     ll x, y;
12.     bool operator<(const Point& p) {
13.         return x < p.x || (x == p.x && y < p.y);
14.     }
15. };
16.
17. ll cross(Point& a, Point& b, Point& c) {
18.     ll dx0 = b.x - a.x, dy0 = b.y - a.y;
19.     ll dx1 = c.x - a.x, dy1 = c.y - a.y;
20.     return dx0 * dy1 - dx1 * dy0;
21. }
22.
23. vector<Point> upper_hull(vector<Point>& P) {
24.     // sort points lexicographically
25.     int n = P.size(), k = 0;
26.     sort(P.begin(), P.end());
27.
28.     // build upper hull
29.     vector<Point> uh(n);
30.     invrep (i, n-1, 0) {
31.         while (k >= 2 && cross(uh[k-2], uh[k-1], P[i]) <= 0) k--;
32.         uh[k++] = P[i];
33.     }
34.     uh.resize(k);
35.     return uh;
36. }
37.
38. vector<Point> lower_hull(vector<Point>& P) {

```

```

39.     // sort points lexicographically
40.     int n = P.size(), k = 0;
41.     sort(P.begin(), P.end());
42.
43.     // collect lower hull
44.     vector<Point> lh(n);
45.     rep (i, 0, n-1) {
46.         while (k >= 2 && cross(lh[k-2], lh[k-1], P[i]) <= 0) k--;
47.         lh[k++] = P[i];
48.     }
49.     lh.resize(k);
50.     return lh;
51. }
52.
53. vector<Point> convex_hull(vector<Point>& P) {
54.     int n = P.size(), k = 0;
55.
56.     // set initial capacity
57.     vector<Point> H(2*n);
58.
59.     // Sort points lexicographically
60.     sort(P.begin(), P.end());
61.
62.     // Build lower hull
63.     for (int i = 0; i < n; ++i) {
64.         while (k >= 2 && cross(H[k-2], H[k-1], P[i]) <= 0) k--;
65.         H[k++] = P[i];
66.     }
67.
68.     // Build upper hull
69.     for (int i = n-2, t = k+1; i >= 0; i--) {
70.         while (k >= t && cross(H[k-2], H[k-1], P[i]) <= 0) k--;
71.         H[k++] = P[i];
72.     }
73.
74.     // remove extra space
75.     H.resize(k-1);
76.     return H;
77. }

```

Puntos y Líneas

```

1. #include <bits/stdc++.h>
2. #define EPS 1e-9

```

```

3. struct line {double a,b,c;}; // ax + by + c = 0
4. bool areParallel(line a, line b)
5. {
6.     return((fabs(a.a-b.a)<EPS)&&(fabs(a.b-b.b)<EPS));
7. }
8. bool areSame(line a, line b)
9. {
10.    return areParallel(a,b)&&(fabs(a.c-b.c)<EPS);
11. }
12. struct point
13. {
14.     double x,y;
15.     point() {x=y=0;}
16.     point(double _x, double _y) : x(_x), y(_y) {}
17.     point operator+(point a) const
18.     {
19.         a.x+=x;
20.         a.y+=y;
21.         return a;
22.     }
23. };
24. double dist(point a, point b)
25. {
26.     return hypot(a.x-b.x,a.y-b.y);
27. }
28. void toline(point a, point b, line &l) //dados dos puntos
29. {
30.     if(fabs(a.x-b.x)<EPS)
31.         {l.a = 1, l.b = 0, l.c = -a.x; return;}
32.     l.a = -(a.y - b.y) / (a.x - b.x);
33.     l.b = 1;
34.     l.c = -l.a * a.x - a.y;
35. }
36. void tolinegr(point a, double gr, line &l) // a linea dado el gradiente
37. {
38.     l.a = -gr;
39.     l.b = 1;
40.     l.c = a.x * gr - a.y;
41. }
42. point tovec(point a, point b)
43. {
44.     return point(b.x-a.x,b.y-a.y);

```

```

45. }
46. point translate (point p, point v)
47. {
48.     return point(p.x+v.x,p.y+v.y);
49. }
50. point scale(point v, double sc)
51. {
52.     return point(v.x*sc,v.y*sc);
53. }
54. point rotate(point v, double theta) //rotacion antihoraria
55. {
56.     theta *= acos(-1)/180.0;
57.     return point(v.x*cos(theta)-
58.         v.y*sin(theta),v.x*sin(theta)+ v.y*cos(theta));
59. }
60. bool areIntersect(line l1, line l2, point &p) //interseccion de lineas
61. {
62.     if(areParallel(l1,l2)) return false;
63.     p.x = (-l1.c*l2.b + l2.c*l1.b) / (l1.a*l2.b-
64.         l2.a*l1.b);
65.     if(fabs(l1.b) > EPS) p.y = -(l1.a*p.x + l1.c);
66.     else
67.         p.y = -(l2.a*p.x + l2.c);
68.     return true;
69. }
70. point clos(point a, line l, line &pe) //closest point in a line and perpendicular line from a
71. {
72.     if(fabs(l.a) < EPS)
73.     {
74.         pe.a = 1, pe.b = 0, pe.c = -a.x;
75.         return point(a.x,-l.c);
76.     }
77.     if(fabs(l.b) < EPS)
78.     {
79.         pe.a = 0, pe.b = 1, pe.c = -a.y;
80.         return point(-l.c,a.y);
81.     }
82.     tolinegr(a, 1/(l.a),pe);
83.     areIntersect(l,pe,a);
84.     return a;
85. }

```

```

84. point reflexion(point p, point a, point b) // del punto
    p a linea ab
85. {
86.     line l,li;
87.     toline(a,b,li);
88.     point p1 = clos(p,li,l);
89.     p1 = p1+(tovec(p,p1));
90.     return p1;
91. }
92. double norm_sq(point a)
93. {
94.     return a.x * a.x + a.y * a.y;
95. }
96. double dot(point a, point b)
97. {
98.     return a.x*b.x + b.y*a.y;
99. }
100. double angle(point a, point b, point c) //b el del medio
101. {
102.     a = tovec(b,a), b = tovec(b,c);
103.     double res = dot(a,b);
104.     res = acos(res / (sqrt(norm_sq(a))*sqrt(norm_sq(b)
        )))
105.     res*= 180.0/acos(-1);
106.     return res;
107. }
108. double cross(point a, point b) //producto cruz
109. {
110.     return a.x * b.y - a.y * b.x;
111. }
112. bool left(point a, point b, point c) //ccw
113. {
114.     c = tovec(b,c);
115.     a = tovec(b,a);
116.     return (cross(c,a)>0.0);
117. }
118. bool colinear(point a, point b, point c)
119. {
120.
121.     c = tovec(b,c);
122.     a = tovec(b,a);
123.     return (fabs(cross(c,a))<EPS);
124. }

```

```

125. double distToLine(point p, point a, point b, point &c)
    //con producto punto halla el punto
126. {
127.     //c = a + u*ab
128.     point ab = tovec(a,b), ap = tovec(a,p);
129.     double u = dot(ab,ap) / norm_sq(ab);
130.     c = translate(a, scale(ab,u));
131.     return dist(p,c);
132. }
133. double distToline1(point p, point a, point b) //con pr
    oducto cruz solo distancia
134. {
135.     point ap = tovec(a,p), ab = tovec(a,b);
136.     return fabs(cross(ab,ap)/hypot(ab.x,ab.y));
137. }

```

Poligonos

```

1. struct point{
2.     double x,y;
3.     point(){x=y=0;}
4.     point(double X, double Y): x(X), y(Y) {}
5.     point operator+(point a) const
6.     {
7.         a.x+=x;
8.         a.y+=y;
9.         return a;
10.    }
11.    bool operator<(point a) const
12.    {
13.        return (a.x == x? a.y < y : a.x < x);
14.    }
15. };
16. double dist(point a, point b)
17. {
18.     return hypot(a.x-b.x, a.y-b.y);
19. }
20. point tovec(point a, point b)
21. {
22.     return point(b.x-a.x,b.y-a.y);
23. }
24. double norm(point a)
25. {
26.     return hypot(a.x,a.y);
27. }

```

```

28. double dot(point a, point b)
29. {
30.     return a.x*b.x + a.y*b.y;
31. }
32. double cross(point a, point b)
33. {
34.     return a.x*b.y - a.y*b.x;
35. }
36. bool ccw(point a, point b, point c)
37. {
38.     return cross(tovec(a,b),tovec(a,c)) >= 0; //depende
        si se acepta colinear o no
39. }
40. double an(point a, point b, point c)
41. {
42.     a = tovec(b,a), b = tovec(b,c);
43.     return acos(dot(a,b)/(norm(a)*norm(b)));
44. }
45. double perimeter(const vector<point> &p)
46. {
47.     double result = 0.0;
48.     for(int i = 0; i<p.size()-1; i++)
49.     {
50.         result += dist(p[i],p[i+1]);
51.     }
52.     return result;
53. }
54. double area(const vector<point> &p)
55. {
56.     double result = 0.0;
57.     for(int i=0;i<p.size()-1;i++)
58.     {
59.         result += p[i].x*p[i+1].y - p[i].y*p[i+1].x;;
60.     }
61.     return fabs(result)/2.0;
62. }
63. point lineIntersectSeg(point p, point q, point A, point
    B)
64. {
65.     double a = B.y - A.y;
66.     double b = A.x - B.x;
67.     double c = B.x * A.y - A.x * B.y;
68.     double u = fabs(a * p.x + b * p.y + c);
69.     double v = fabs(a * q.x + b * q.y + c);

```

```

70.     return point((p.x * v + q.x * u) / (u+v), (p.y * v
        + q.y * u) / (u+v));
71. }
72. vector<point> cutPolygon(point a, point b, const vector
    <point> &Q)
73. {
74.     vector<point> P;
75.     for (int i = 0; i < (int)Q.size(); i++) {
76.         double left1 = cross(tovec(a, b), tovec(a, Q[i]
            )), left2 = 0;
77.         if (i != (int)Q.size()-
            1) left2 = cross(tovec(a, b), tovec(a, Q[i+1]));
78.         if (left1 > -
            EPS) P.push_back(Q[i]); // Q[i] is on the left of ab ;
            left1 < EPS para la derecha
79.         if (left1 * left2 < -
            EPS) // edge (Q[i], Q[i+1]) crosses line ab
80.             P.push_back(lineIntersectSeg(Q[i], Q[i+1],
                a, b));
81.     }
82.     if (!P.empty() && (P.back().x != P.front().x || P.b
        ack().y != P.front().y))
83.         P.push_back(P.front()); // make P's first point
            = P's last point
84.     return P;
85. }
86. bool isConvex(const vector<point> &p)
87. {
88.     int sz = p.size();
89.     if(sz<=3) return false;
90.     bool left = ccw(p[0],p[1],p[2]);
91.     cout<<left<<endl;
92.     for(int i = 1; i < sz - 1; i++)
93.     {
94.         cout<<i<< ' '<<ccw(p[i],p[i+1],p[((i+2)==sz)? 1:
            i+2])<<endl;
95.         if(ccw(p[i],p[i+1],p[((i+2)==sz)? 1:i+2])!=left
            )
96.             return false;
97.     }
98.     return true;
99. }
100. bool isIn(const vector<point> &p, point a)
101. {

```

```

102. double ang = 0;
103. int sz = p.size();
104. if(sz == 0) return false;
105. for(int i = 0; i<sz-1;i++)
106. {
107.     if(ccw(a,p[i],p[i+1]))
108.         ang += an(p[i],a,p[i+1]);
109.     else
110.         ang -= an(p[i],a,p[i+1]);
111. }
112. cout<<ang<<endl;
113. return fabs(ang - 2.0*PI) < EPS;
114.}

```

Triangulos y Circulos

```

1. struct point
2. {
3.     double x,y;
4.     point() {x=0.0; y = 0.0;}
5.     point(int _x, int _y) : x(_x), y(_y) {}
6.     point operator+(point b) const
7.     {
8.         b.x += x;
9.         b.y+=y;
10.        return b;
11.    }
12. };
13. struct line
14. {
15.     double a,b,c;
16. };
17. double dist(point a, point b)
18. {
19.     return hypot(fabs(a.x-b.x),fabs(a.y-b.y));
20. }
21. point tovec(point a, point b)
22. {
23.     return point(b.x-a.x,b.y-a.y);
24. }
25. point translate(point a, point b)
26. {
27.     a= a+b;
28.     return a;
29. }

```

```

30. point scale(point a, double s)
31. {
32.     a.x*=s;
33.     a.y*= s;
34.     return a;
35. }
36. void pointsToLine(point a, point b, line &l) //linea da
    dos 2 puntos
37. {
38.     if(fabs(a.x-b.x)<EPS)
39.     {
40.         l.a = 1, l.b = 0, l.c = -a.x;
41.     }
42.     else
43.     {
44.         l.a = -(a.y-
45.         b.y) / (a.x - b.x), l.b = 1, l.c = -l.a * a.x - a.y;
46.     }
47. double rInCircle(double ab, double bc, double ca)
48. {
49.     double s = (ab+bc+ca)/2;
50.     return sqrt(s*(s-ab)*(s-bc)*(s-ca));
51. }
52. double rInCircle(point a, point b, point c)
53. {
54.     return rInCircle(dist(a,b),dist(b,c),dist(c,a));
55. }
56. bool areParallel(line a, line b)
57. {
58.     return (fabs(a.a-b.a)<EPS)&&(a.b == b.b);
59. }
60. bool areIntersect(line a, line b, point &c)
61. {
62.     if(areParallel(a,b)) return false;
63.     c.x = (b.c*a.b-a.c*b.b) / (a.a*b.b-b.a*a.b);
64.     if(a.b == 0.0) c.y = -(b.b*c.x + b.c);
65.     else c.y = -(a.b*c.x + a.c);
66.     return true;
67. }
68. double areaTri1(double a, double b, double c) //heron
69. {
70.     double s = (a+b+c)/2;
71.     return sqrt(s*(s-a)*(s-b)*(s-c));

```

```

72. }
73. double areaTri(point a, point b, point c)
74. {
75.     return areaTri1(dist(a,b),dist(b,c),dist(a,c));
76. }
77. line perp(line a, point p) //perpendicular
78. {
79.     line res;
80.     if(a.b=0)
81.     {
82.         res.a = 0, res.b = 1, res.c = -p.y;
83.     }
84.     else
85.         if(fabs(a.a)<EPS)
86.         {
87.             res.a = 1, res.b = 0, res.c = -p.y;
88.         }
89.         else
90.         {
91.             res.a = -1.0/a.a, res.b = 1, res.c = -
res.a*p.x-p.y;
92.         }
93. }
94. }
95. bool circumCircle(point a, point b, point c, point &ctr
, double &r) //circuncentro completo
96. {
97.     double area = areaTri(a,b,c);
98.     if(fabs(area)<EPS) return 0;
99.     line l1, l2;
100.     pointsToLine(a,b,l2);
101.     pointsToLine(a,c,l2);
102.     point p1 = point((a.x+b.x)/2.0,(a.y+b.y)/2.0), p2
= point((a.x+c.x)/2.0,(a.y+c.y)/2.0);
103.     l1 = perp(l1,p1), l2 = perp(l2,p2);
104.     areIntersect(l1,l2,ctr);
105.     r = dist(a,b)*dist(b,c)*dist(a,c)/(4.0*areaTri(a,b
,c));
106.     return true;
107. }
108. bool isInCircum(point a, point b, point c, point p) //
si esta dentro del circulo circunscrito
109. {
110.     double r;

```

```

111.     point ctr;
112.     if(!circumCircle(a,b,c,ctr,r)) return false;
113.     return dist(ctr,p) <= r ;
114. }
115. bool inCircle(point a, point b, point c, point &ctr) /
/incentro
116. {
117.     double r = rIncircle(a,b,c);
118.     if(r< EPS) return false;
119.     line l1,l2;
120.     point p1;
121.     double ratio = dist(a,b) / dist(a,c);
122.     p1 = translate(b, scale(tovec(b,c),ratio/(1+ratio)
));
123.     pointsToLine(a,p1,l1);
124.     ratio = dist(b,a) / dist(b,c);
125.     p1 = translate(a, scale(tovec(a,c),ratio/(1+ratio)
));
126.     pointsToLine(b,p1,l2);
127.     areIntersect(l1,l2,ctr);
128.     return true;
129. }
130. line toLinep(point a, point b, point c) //para mediatr
iz
131. {
132.     line l;
133.     if(b.x == c.x)
134.     {
135.         l.a = 0, l.b = 1 , l.c = -a.y;
136.     }
137.     else
138.         if(b.y == c.y)
139.         {
140.             l.a = 1, l.b = 0, l.c = -a.x;
141.         }
142.         else
143.         {
144.             l.a = 1/((b.y-a.y)/(b.x-
a.x)), l.b = 1, l.c = -l.a*a.x-a.y;
145.         }
146.         return l;
147.     }
148. point circum(point a, point b, point c) //circuncentro

```



```

149.{
150.    line l1, l2;
151.    l1 = toLinep(point((a.x+b.x)/2,(a.y+b.y)/2),a,b);

152.    l2 = toLinep(point((a.x+c.x)/2,(a.y+c.y)/2),a,c);

153.    areIntersect(l1,l2,a);
154.    return a;
155.}
156.bool circle2PtsRad(point a, point b, double r, point &
    c) //dados 2 puntos y un radio
157.{
158.    double det = (a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-
    b.y);
159.    det = r * r / det - 0.25;
160.    if(det < 0.0) return false;
161.    det = sqrt(det);
162.    c.x = (a.x + b.x) * 0.5 + (b.y-a.y) * det;
163.    c.y = (a.y + b.y) * 0.5 + (a.x-
    b.x) * det;
164.    return true;
165.}

```

Matematicas

Catalan

```

1.  ll cata(int n)
2.  {
3.      ll bino[n+1];
4.      memset(bino,0ll,sizeof(bino));
5.      bino[0]=1;
6.      for(int i=1;i<=2*n;i++)
7.          for(int j=min(i,n);j>0;j--)
8.              bino[j]+=bino[j-1];
9.      return bino[n]/(n+1);
10. }
11.
12. int main()
13. {
14.     ll scat[26];//super catalan
15.     scat[0]=scat[1]=1;
16.     for(int i=2;i<26;i++)
17.         scat[i]=(3*(2*i-1)*scat[i-1]-(i-2)*scat[i-2])/((i+1);

```

```

18.     ll cat[26];
19.     for(int i=0;i<26;i++)
20.         cat[i]=cata(i);
21.     return 0;
22. }

```

Euclides Extendido

```

1.  ll gcd(ll a, ll b){return b==0? a:gcd(b,a%b);}
2.
3.  int x, y, d;
4.  void extendedEuclid(int a, int b)//ecuacion diofantica ax + by = 1
5.  {
6.      if(b==0) {x=1; y=0; d=a; return;}
7.      extendedEuclid(b,a%b);
8.      int x1=y;
9.      y = x-(a/b)*y;
10.     x=x1;
11. }

```

Phi de Euler, Criba

```

1.  bitset<100000> bi;
2.  vi primos;
3.  vector<ll> pric;
4.  void criba()
5.  {
6.      bi.set();
7.      for(int i=2;i<100000;i++)
8.          if(bi[i])
9.              {
10.                 for(int j=i+i;j<100000;j+=i)
11.                     bi[j]=0;
12.                 primos.push_back(i);
13.                 pric.push_back((ll)i*(ll)i);
14.             }
15. }
16. int euler(int n)
17. {
18.     int res=n;
19.     for(int i=0;pric[i]<=n;i++)
20.     {
21.         if(n%primos[i]==0)
22.         {
23.             res-= res/primos[i];

```

```

24.     while(n%primos[i]==0) n/=primos[i];
25. }
26. }
27. if(n!=1) res-=res/n;
28. return res;
29. }

```

Criba modificada

```

1. int phi[2000001]; //eulerphi
2. void criba()
3. {
4.     for(int i=0;i<2000001;i++) phi[i]=i;
5.     for(int i=2;i<2000001;i++)
6.     {
7.         if(phi[i]==i)
8.             for(int j=i;j<2000001;j+=i)
9.                 phi[j]-=phi[j]/i;
10.    }
11. }
12. int crib[1000001]; //number of prime factors
13. void criba()
14. {
15.     memset(crib,0,sizeof(crib));
16.     for(int i=2;i<1000001;i++)
17.         if(crib[i]==0)
18.             for(int j=i;j<1000001;j+=i)
19.                 crib[j]++;
20. }

```

Pollard Rho y Miller-Rabin

```

1. ll mulmod(ll a, ll b, ll c) //multiplicacion modular binaria
2. {
3.     ll x=0, y=a % c;
4.     while(b > 0)
5.     {
6.         if(b % 2 == 1) x = (x + y) % c;
7.         y = (y * 2) % c;
8.         b /= 2;
9.     }
10.    return x % c;
11. }
12. ll gcd(ll a, ll b) {return (b==0? a : gcd(b,a%b));}
13. ll poll(ll n) //numero grande p = a*b devuelve a (a y b primos)

```

```

14. {
15.     srand (time(NULL));
16.     ll x = rand()%(n-2) + 2, y = x, c = rand()%(n-1) + 1, d = 1;
17.     while(d==1)
18.     {
19.         x = (mulmod(x, x, n) + c) % n;
20.         y = (mulmod(y, y, n) + c) % n;
21.         y = (mulmod(y, y, n) + c) % n;
22.         d = gcd((x>y?x-y:y-x),n);
23.         if(d == n) return poll(n);
24.     }
25.     return d;
26. }
27. ll modpow(ll b, ll e, ll m)
28. {
29.     if(e == 0) return 1;
30.     //return (modpow((b*b) % m, e/2, m) * (e & 1? b : 1)) % m;
31.     return mulmod(modpow(mulmod(b,b,m), e/2, m), (e & 1? b : 1), m);
32. }
33. bool mill(ll n, int k) //k = 10 es seguro
34. {
35.     ll p = n - 1;
36.     int r = 0;
37.     bool pp;
38.     while(p % 2 == 0)
39.     {
40.         p /= 2;
41.         r++;
42.     }
43.     for(int i=0; i < k; i++)
44.     {
45.         ll a = rand()%(n-4) + 2;
46.         ll exp = modpow(a,p,n);
47.         if(exp == 1 || exp == n-1) return true;
48.         pp = false;
49.         for(int j = 0; j < r; j++)
50.         {
51.             exp = mulmod(exp, exp, n);
52.             if(exp == 1) return false;
53.             if(exp == n-1) {pp = true; break;}
54.         }
55.         if(!pp) return false;
56.     }

```

```

57.
58.     return true;
59. }

```

Strings

Algoritmo Z

```

1.  typedef vector<ll>    vll;
2.  vector<int> alz(string a)
3.  {
4.      int n = a.size();
5.      vi res(n);
6.      int left=0,right=0;
7.      for(int k=1;k<n;k++)
8.      {
9.          if(right<k)
10.         {
11.             right=left+k;
12.             while(right<n&&a[right]==a[right-left])
13.                 right++;
14.             res[k] = right - left;
15.             right--;
16.         }
17.         else
18.         {
19.             int k1 = k - left;
20.             if(res[k1]< right - k + 1)
21.                 res[k] = res[k1];
22.             else
23.             {
24.                 left=k;
25.                 while(right<n&&a[right] == a[right-left])
26.                     right++;
27.                 res[k] = right - left;
28.                 right--;
29.             }
30.         }
31.     }
32.     return res;
33. }
34. int main()
35. {
36.     string a,b;

```

```

37.     cin>>a>>b;
38.     vector<int> v = alz(b+'$'+a);
39.     int ta = a.size();
40.     int tb = b.size();
41.     ta = ta + tb + 1;
42.     for(int i=tb+1;i<ta;i++)
43.     {
44.         if(v[i]==tb)
45.             cout<<i-tb-1<<endl;
46.     }
47.     return 0;
48. }

```

Suffix Array, LCP

```

1.  #include <bits/stdc++.h>
2.
3.  using namespace std;
4.
5.  typedef vector<int>    vi;
6.
7.  struct suffix
8.  {
9.      int index;
10.     int rank[2];
11. };
12.
13. int cmp(struct suffix a, struct suffix b)
14. {
15.     return (a.rank[0] == b.rank[0])? (a.rank[1] < b.rank[1] ? 1: 0):
16.           (a.rank[0] < b.rank[0] ? 1: 0);
17. }
18.
19. vector<int> buildSuffixArray(vi txt, int n)
20. {
21.     struct suffix suffixes[n];
22.
23.     for (int i = 0; i < n; i++)
24.     {
25.         suffixes[i].index = i;
26.         suffixes[i].rank[0] = txt[i];
27.         suffixes[i].rank[1] = ((i+1) < n)? (txt[i + 1])
28.         : -1;

```

```

29.
30.     sort(suffixes, suffixes+n, cmp);
31.
32.     int ind[n];
33.     for (int k = 4; k < 2*n; k = k*2)
34.     {
35.         int rank = 0;
36.         int prev_rank = suffixes[0].rank[0];
37.         suffixes[0].rank[0] = rank;
38.         ind[suffixes[0].index] = 0;
39.
40.         for (int i = 1; i < n; i++)
41.         {
42.             if (suffixes[i].rank[0] == prev_rank &&
43.                 suffixes[i].rank[1] == suffixes[i-
44. 1].rank[1])
45.             {
46.                 prev_rank = suffixes[i].rank[0];
47.                 suffixes[i].rank[0] = rank;
48.             }
49.             else
50.             {
51.                 prev_rank = suffixes[i].rank[0];
52.                 suffixes[i].rank[0] = ++rank;
53.             }
54.             ind[suffixes[i].index] = i;
55.         }
56.         for (int i = 0; i < n; i++)
57.         {
58.             int nextindex = suffixes[i].index + k/2;
59.             suffixes[i].rank[1] = (nextindex < n)?
60.                 suffixes[ind[nextindex]
61. ].rank[0]: -1;
62.         }
63.         sort(suffixes, suffixes+n, cmp);
64.     }
65.
66.     vector<int> suffixArr;
67.     for (int i = 0; i < n; i++)
68.         suffixArr.push_back(suffixes[i].index);
69.
70.     return suffixArr;

```

```

71. }
72.
73. vector<int> kasai(vi txt, vector<int> suffixArr)
74. {
75.     int n = suffixArr.size();
76.
77.     vector<int> lcp(n, 0);
78.     vector<int> invSuff(n, 0);
79.
80.     for (int i=0; i < n; i++)
81.         invSuff[suffixArr[i]] = i;
82.
83.     int k = 0;
84.
85.     for (int i=0; i<n; i++)
86.     {
87.         if (invSuff[i] == n-1)
88.         {
89.             k = 0;
90.             continue;
91.         }
92.
93.         int j = suffixArr[invSuff[i]+1];
94.
95.         while (i+k<n && j+k<n && txt[i+k]==txt[j+k])
96.             k++;
97.
98.         lcp[invSuff[i]] = k;
99.
100.         if (k>0)
101.             k--;
102.     }
103.
104.     return lcp;
105. }
106.
107.
108. int main()
109. {
110.     vi txt; // vector para el que sacamos Suffix Array
111.     vi suffixArr = buildSuffixArray(txt, txt.size());
112.     //vi lcp = kasai(txt, suffixArr);
113.     // Para sacar LCP debemos haber separado cada palabr
114.     // a con un separador

```

```

114. // menor que cualquier elemento del alfabeto
115. return 0;
116.}

```

Tecnicas

Algoritmo de Mo

```

1. #include <bits/stdc++.h>
2. #define mp make_pair
3. #define F first
4. #define S second
5.
6. using namespace std;
7.
8. const int INF = int(1e9 + 7);
9. typedef long long ll;
10. typedef pair<ll, ll> ii;
11.
12. pair<ii, int> q[200010];
13. ll v[200010], anss[200010];
14. int block = 450;
15.
16. bool cmp(pair<ii, int> x, pair<ii, int> y)
17. {
18.     ii a = x.F, b = y.F;
19.     int A = a.F / block, B = b.F / block;
20.     if ( A == B )
21.     {
22.         if (A & 1) return a.S < b.S;
23.         else return a.S > b.S;
24.     }
25.     return A < B;
26. }
27.
28. ll cont[1000010];
29. ll ans;
30.
31. void add(int x)
32. {
33.     ll val = cont[x]*cont[x]*x;
34.     ans -= val;
35.     cont[x]++;
36.     val = cont[x]*cont[x]*x;

```

```

37.     ans += val;
38. }
39.
40. void del(int x)
41. {
42.     ll val = cont[x]*cont[x]*x;
43.     ans -= val;
44.     cont[x]--;
45.     val = cont[x]*cont[x]*x;
46.     ans += val;
47. }
48.
49. int main()
50. {
51.     std::ios::sync_with_stdio(false); cin.tie(0);
52.     //freopen("", "r", stdin);
53.     //freopen("", "w", stdout);
54.     int n, m;
55.     cin >> n >> m;
56.     for (int i = 0; i < n; i++)
57.     {
58.         cin >> v[i];
59.     }
60.     for (int i = 0; i < m; i++)
61.     {
62.         int a, b;
63.         cin >> a >> b;
64.         a--; b--;
65.         q[i] = mp( mp(a, b), i );
66.     }
67.     sort(q, q + m, cmp);
68.     int L = 0, R = -1;
69.     ans = 0;
70.     for (int i = 0; i < m; i++)
71.     {
72.         int l = q[i].F.F, r = q[i].F.S;
73.         while (R < r)
74.         {
75.             R++;
76.             add(v[R]);
77.         }
78.         while (l < L)
79.         {
80.             L--;

```

```

81.         add(v[L]);
82.     }
83.     while (R > r)
84.     {
85.         del(v[R]);
86.         R--;
87.     }
88.     while (l > L)
89.     {
90.         del(v[L]);
91.         L++;
92.     }
93.     anss[ q[i].S ] = ans;
94. }
95. for (int i = 0; i < m; i++)
96. {
97.     cout << anss[i] << '\n';
98. }
99. return 0;
100.}
101.// PLUS ULTRA!

```

Temas Raros

FFT

```

1. typedef complex<double> cd;
2. double mul;
3. vector<cd> fft(vector<cd> a)
4. {
5.     int n = a.size();
6.     if(n==1) return a;
7.     double theta = 2.0*acos(-1)/(double)n;
8.     cd w = 1,
9.     wn = cd(cos(theta), mul*sin(theta));
10.    vector<cd> y(n), aEven(n/2), aOdd(n/2);
11.    for(int i=0;i<n/2;i++)
12.    {
13.        aEven[i] = a[2*i];
14.        aOdd[i] = a[2*i+1];
15.    }
16.    aEven = fft(aEven);
17.    aOdd = fft(aOdd);
18.    for(int i=0;i<n/2;i++)

```

```

19. {
20.     a[i] = aEven[i] + w*aOdd[i];
21.     a[n/2+i] = aEven[i] - w*aOdd[i];
22.     w*=wn;
23. }
24. return a;
25. }
26. vector<cd> ffmul(vector<cd> a, vector<cd> b) //tamaño de a debe ser
    >= al tamaño de b
27. {
28.     int n = 2*a.size();
29.     while(_builtin_popcount(n)>1) n+= (n&-n);
30.     while(a.size()<n) a.push_back(0);
31.     while(b.size()<n) b.push_back(0);
32.     mul = 1;
33.     a = fft(a);
34.     b = fft(b);
35.     for(int i=0;i<n;i++)
36.         a[i] = a[i]*b[i];
37.     mul = -1;
38.     a = fft(a);
39.     for(int i=0;i<n;i++)
40.         a[i]/=n;
41.     return a;
42. }

```

Shortcuts

Comparador – Java

```

1. import java.util.Comparator;
2. import java.util.Arrays;
3.
4. public class Employee implements Comparable<Employee> {
5.
6.     private int id;
7.     private String name;
8.     private int age;
9.     private long salary;
10.
11.     public int getId() {

```

```

12.         return id;
13.     }
14.
15.     public String getName() {
16.         return name;
17.     }
18.
19.     public int getAge() {
20.         return age;
21.     }
22.
23.     public long getSalary() {
24.         return salary;
25.     }
26.
27.     public Employee(int id, String name, int age, int salary) {
28.         this.id = id;
29.         this.name = name;
30.         this.age = age;
31.         this.salary = salary;
32.     }
33.
34.     @Override
35.     public int compareTo(Employee emp) {
36.         //let's sort the employee based on id in ascending order
37.         //returns a negative integer, zero, or a positive integer as this employee id
38.         //is less than, equal to, or greater than the specified object.
39.         return (this.id - emp.id);
40.     }
41.
42.     @Override
43.     //this is required to print the user friendly information about the Employee
44.     public String toString() {
45.         return "[id=" + this.id + ", name=" + this.name + ", age=" + this.age + ", salary=" + this.salary + "]";
46.     }
47. }
48.
49. /**

```

```

50.     * Comparator to sort employees list or array in order of Salary
51.     */
52.     public static Comparator<Employee> SalaryComparator = new Comparator<Employee>() {
53.
54.         @Override
55.         public int compare(Employee e1, Employee e2) {
56.
57.             return (int) (e1.getSalary() - e2.getSalary());
58.         }
59.     };
60.     /**
61.     * Comparator to sort employees list or array in order of Age
62.     */
63.     public static Comparator<Employee> AgeComparator = new Comparator<Employee>() {
64.
65.         @Override
66.         public int compare(Employee e1, Employee e2) {
67.
68.             return e1.getAge() - e2.getAge();
69.         }
70.     };
71.     /**
72.     * Comparator to sort employees list or array in order of Name
73.     */
74.     public static Comparator<Employee> NameComparator = new Comparator<Employee>() {
75.
76.         @Override
77.         public int compare(Employee e1, Employee e2) {
78.
79.             return e1.getName().compareTo(e2.getName());
80.         }
81.     };
82.

```

```

83. public class EmployeeComparatorByIdAndName implements C
    omparator<Employee> {
84.
85.     @Override
86.     public int compare(Employee o1, Employee o2) {
87.         int flag = o1.getId() - o2.getId();
88.         if(flag==0) flag = o1.getName().compareTo(o2.ge
            tName());
89.         return flag;
90.     }
91.
92. }
93.
94. public class JsonObjectSorting {
95.
96.     /**
97.      * This class shows how to sort custom objects arra
        y/list
98.      * implementing Comparable and Comparator interface
        s
99.      * @param args
100.     */
101.     public static void main(String[] args) {
102.         Map<Integer, String> datos = new HashMap<Integ
            er, String>();
103.         datos.put(1, "uno");
104.         datos.put(2, "dos");
105.         datos.put(3, "tres");
106.
107.         for (Map.Entry<Integer, String> entry : datos.
            entrySet()) {
108.             System.out.println("clave=" + entry.getKey
                () + ", valor=" + entry.getValue());
109.         }
110.
111.         Set<String> set = new HashSet<String>();
112.
113.         //populate set
114.
115.         for (String s : set) {
116.             System.out.println(s);
117.         }
118.
119.         //sorting custom object array

```

```

120.         Employee[] empArr = new Employee[4];
121.         empArr[0] = new Employee(10, "Mikey", 25, 1000
            0);
122.         empArr[1] = new Employee(20, "Arun", 29, 20000
            );
123.         empArr[2] = new Employee(5, "Lisa", 35, 5000);
124.         empArr[3] = new Employee(1, "Pankaj", 32, 5000
            0);
125.
126.         //sorting employees array using Comparable int
            erface implementation
127.         Arrays.sort(empArr);
128.         System.out.println("Default Sorting of Emplo
            es list:\n"+Arrays.toString(empArr));
129.
130.         //sort employees array using Comparator by Sal
            ary
131.         Arrays.sort(empArr, Employee.SalaryComparator)
            ;
132.         System.out.println("Employees list sorted by S
            alary:\n"+Arrays.toString(empArr));
133.
134.         //sort employees array using Comparator by Age
135.         Arrays.sort(empArr, Employee.AgeComparator);
136.         System.out.println("Employees list sorted by A
            ge:\n"+Arrays.toString(empArr));
137.
138.         //sort employees array using Comparator by Nam
            e
139.         Arrays.sort(empArr, Employee.NameComparator);
140.         System.out.println("Employees list sorted by N
            ame:\n"+Arrays.toString(empArr));
141.
142.         //Employees list sorted by ID and then name us
            ing Comparator class
143.         empArr[0] = new Employee(1, "Mikey", 25, 10000
            );
144.         Arrays.sort(empArr, new EmployeeComparatorById
            AndName());
145.         System.out.println("Employees list sorted by I
            D and Name:\n"+Arrays.toString(empArr));

```



```

146.     }
147.
148. }

```

Fast Input – Java

```

1.  // Working program with FastReader
2.  import java.io.BufferedReader;
3.  import java.io.IOException;
4.  import java.io.InputStreamReader;
5.  import java.util.Scanner;
6.  import java.util.StringTokenizer;
7.
8.  public class Main
9.  {
10.     static class FastReader
11.     {
12.         BufferedReader br;
13.         StringTokenizer st;
14.
15.         public FastReader()
16.         {
17.             br = new BufferedReader(new
18.                 InputStreamReader(System.in));
19.         }
20.
21.         String next()
22.         {
23.             while (st == null || !st.hasMoreElements())
24.             {
25.                 try
26.                 {
27.                     st = new StringTokenizer(br.readLine());
28.                 }
29.                 catch (IOException e)
30.                 {
31.                     e.printStackTrace();
32.                 }
33.             }
34.             return st.nextToken();
35.         }
36.
37.         int nextInt()
38.         {

```

```

39.             return Integer.parseInt(next());
40.         }
41.
42.         long nextLong()
43.         {
44.             return Long.parseLong(next());
45.         }
46.
47.         double nextDouble()
48.         {
49.             return Double.parseDouble(next());
50.         }
51.
52.         String nextLine()
53.         {
54.             String str = "";
55.             try
56.             {
57.                 str = br.readLine();
58.             }
59.             catch (IOException e)
60.             {
61.                 e.printStackTrace();
62.             }
63.             return str;
64.         }
65.     }
66.
67.     public static void main(String[] args)
68.     {
69.         FastReader s=new FastReader();
70.         int n = s.nextInt();
71.         int k = s.nextInt();
72.         int count = 0;
73.         while (n-- > 0)
74.         {
75.             int x = s.nextInt();
76.             if (x%k == 0)
77.                 count++;
78.         }
79.         System.out.println(count);
80.     }
81. }

```

