



# Search - Lecture 0

Search, knowledge, uncertainty, optimization, learning, neural network

agent: entity that perceives its environment and acts upon that environment

state: a configuration (initial state)

actions: choices that can be made in a state, Actions( $s$ )  
↓  
state

transition model: a description of what state results from performing any  
action ( $s, a$ ) result ( $s, a$ ) applicable action in any state

state space: the set of all states reachable from the initial state by any sequence of actions

goal test: way to determine whether a given state is a goal state

path cost: numerical cost associated with a given path

frontier: all the possible paths we haven't taken yet

A Search problem has 5 things

initial state, actions, transition model,  
goal test, path cost func

We would like to find the optimal solution

Node - data structure:

a state

a parent (a node that generated this node)

an action (action applied to parent to get this)

path cost (from initial state to node)

## Approach

- Start with frontier = initial state
- Repeat
  - if frontier is empty then not possible ↗ it/else
  - remove a node from the frontier ↙
  - if node contains goal state, return the solut. ↗ it/else
  - Expand node, add resulting nodes to the frontier ↘

Drawbacks: you can lose time on repeating states

## Revised Approach

- Start with a **frontier** that contains the initial state.
- Start with an empty **explored set**. ↙
- Repeat:
  - If the frontier is empty, then no solution.
  - Remove a node from the frontier. ↙ it is important how we choose
  - If node contains goal state, return the solution.
  - Add the node to the explored set.
  - **Expand** node, add resulting nodes to the frontier if they aren't already in the frontier or the explored set.

## Depth first search

DPS

we use a stack

not always optimal

Breadth-first search - BFS finds the shortest search algorithm that always expands the shallowest node in the frontier

look at maze.py

# Uninformed Search vs. Informed Search

DPS, BPS

search strategy that uses problem specific knowledge to find solutions more efficiently

## Greedy Best-First Search

search algorithm that expands the node that is closest to the goal, as estimated by a heuristic function  $h(n)$

we need to define it

Manhattan distance

$x-y$  distance

DPS no, BPS yes

doesn't always find best route

## A\* Search

search algorithm that expands node with lowest value of  $g(n) + h(n)$

$g(n)$  = cost to reach node

$h(n)$  = estimated cost to goal - Manhattan, etc.

this is optimal if

- $h(n)$  is admissible
  - $h(n)$  is consistent
- $$h(n) \leq h(n') + c$$

uses more memory

# Adversarial Search

The agent has to work against something esp.: tic-tac-toe

## Minimax

$\begin{array}{ c c c } \hline \text{o} & \text{x} & \text{x} \\ \hline \text{o} & \text{o} & \text{x} \\ \hline \text{o} & \text{x} & \text{x} \\ \hline \end{array}$	$\begin{array}{ c c c } \hline \text{x} & \text{o} & \text{x} \\ \hline \text{o} & \text{o} & \text{x} \\ \hline \text{x} & \text{x} & \text{o} \\ \hline \end{array}$	$\begin{array}{ c c c } \hline \text{o} & \text{ } & \text{g} \\ \hline \text{g} & \text{x} & \text{o} \\ \hline \text{x} & \text{o} & \text{x} \\ \hline \end{array}$
--	--	--

Min Player

0

Max Player

-1

- score

1

• Max (x) aims to maximize score

• Min (x) aims to minimize score

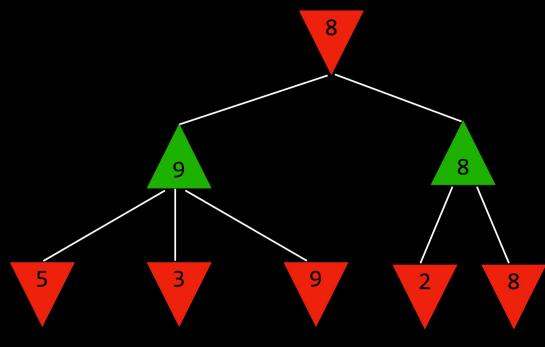
## Game

- $S_0$  : initial state
- $\text{PLAYER}(s)$  : returns which player to move in state  $s$
- $\text{ACTIONS}(s)$  : returns legal moves in state  $s$
- $\text{RESULT}(s, a)$  : returns state after action  $a$  taken in state  $s$
- $\text{TERMINAL}(s)$  : checks if state  $s$  is a terminal state
- $\text{UTILITY}(s)$  : final numerical value for terminal state  $s$

empty game array

- this is for the AI

- score



we put ourselves in the opposite players shoes

min-max-min-max ...

recursively



# Pseudo Code Minimax

- Given a state  $s$ :
  - MAX picks action  $a$  in  $\text{ACTIONS}(s)$  that produces highest value of  $\text{MIN-VALUE}(\text{RESULT}(s, a))$
  - MIN picks action  $a$  in  $\text{ACTIONS}(s)$  that produces smallest value of  $\text{MAX-VALUE}(\text{RESULT}(s, a))$

```
function MAX-VALUE(state):  
    if TERMINAL(state):  
        return UTILITY(state)  
     $v = -\infty$   
    for action in ACTIONS(state):  
         $v = \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(state, action)))$   
    return  $v$ 
```

Min-Value is the opposite

## Optimization - Alpha Beta Pruning

this is inefficient, you need to skip branches, that are worse, than what we found so far.

There are too many states  $\Rightarrow$  Depth-limited  
this needs an Evaluation  $\leftarrow$  Minimax  
Function