CS135 (Fall 2019) Final Project Option Branching Future: CTL

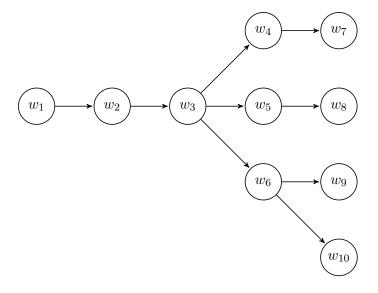
In Homework 4, you dealt with validity and satisfiability in a Linear Temporal Logic (LTL) model. This option is a modification of Homework 4, with the inclusion of some Computation Tree Logic (CTL) operators to allow for generation of models that include branching in the future. You are to create a structure that allows for branching, and then implement isValid, isSatisfied, and isSatisfiable functions in this module in the manner of HW4.

You should start with the starter code for HW4. If you are satisfied with your solution for HW4, you can begin there, too. Most edits should be made in World.hs, and will consist mainly of creating the structure to allow for branching worlds and incorporating the CTL operators into your validity and satisfiability functions.

1. Branching Structure

You should add some more worlds (a total of about twelve should do) and populate them with propositions from your parser. You will also need to change the structure of your model. In the existing World.hs, the model is represented by a list of worlds, which is adequate for representing a linear structure. For a branching structure, you will need to change this slightly. A simple way to represent branching is as a list of tuples, where each tuple is a pair representing two worlds that have an accessibility relation between them, going from the first member of the pair to the second. For example:

represents a tree structure that looks like this:



2. CTL Operators

You should make a slight change to the TProp type: the prop field should become a list [Prop] instead of a simple Prop for reasons that will be explained below.

The TemporalOperator type is now more properly a CTLOperator, and thus TProp is now a CTLProp (you can rename them if you like, or you can just remember that you're dealing with a slightly different logical construct than you were in HW4). You will need to add 4 CTL operators to this type: E, A, X and W. You can remove the past operators P and H as they will not be used. Definitions of the CTL operators follow:

- E: $E\phi$ means there Exists at least one path starting from the current world along which ϕ is true at some point.
- A: $A\phi$ means ϕ is true at some point along All paths starting from the current world.
- X: $X\phi$ means ϕ has to hold at the neXt state.
- W: $\phi W \psi$ means ϕ is true along a given path (Weakly) until ψ becomes true. W is sometimes read as "unless". Because this operator takes two propositions instead of one, it is necessary to change the prop field of TProp to a list.

- F: $F\phi$ means ϕ is true Finally somewhere along the subsequent path. Note that this definition of F has changed from the LTL definition.
- G: $G\phi$ means ϕ is true Globally at all points along the subsequent path. This definition of G has also changed from the LTL definition.

E and A are operators over all paths, while X, W, F, and G are path-specific operators. This means they can be combined in certain ways. In strict CTL (as opposed to CTL*), you may combine one all-path operator with one path-specific operator, which leads to certain interpretations. For instance, $EG\phi$ means that there exists one path starting from the current world where ϕ is true at all states along it. $AF\phi$ means that ϕ is eventually true along all paths starting from the current world. $A[\phi W\psi]$ means that along all paths starting from the current world, ϕ holds until ψ is true. See the Wikipedia page on CTL for more information:

https://en.wikipedia.org/wiki/Computation_tree_logic

With this understanding, the first aim of this task is to implement isValid, isSatisfied, and isSatisfiable functions for this new branching model and these new CTL operators, using the same interpretations of validity and satisfiability as you used in HW4. A valid CTL proposition holds at all worlds in your model. A satisfiable CTL proposition holds at at least one world in the model. As before, you should populate the worlds in your model with some propositions, and all these propositions should be in the present tense. Your validity and satisfiability functions should be able to handle all valid combinations of CTL operators (one all-path operator and one path-specific operator) and all tenses that are available in your parser (use the same parser you built for HW4, but you are not required to make any changes to it).

After that, you can choose to do one of the following options:

- Extend it with a set of logical operators: \neg , \wedge , \vee , \rightarrow , \leftrightarrow . For example, you should be able to handle $EG(p \rightarrow q)$ and $EG(p) \rightarrow AF(q)$.
- Extend it for one more level of nested temporal operators. For example, the expression AF.EG.p means "It's always possible that at some point p will hold for the rest of time".

Write-up

Your submission should also contain a write-up describing how you attacked this problem, what avenues you explored, and what problems you ran into. There is no length requirement, but you should include some use cases for testing and you should describe your strategy, process, and assumptions in some depth.