

## BIG OH NOTATIONS PRACTICE:

Big-O Notation gives an upper bound of the complexity in the worst case, helping quantify performance as the input size becomes arbitrarily large.

- $O(n+c) \rightarrow O(n)$  we neglect constant
- $O(nc) \rightarrow O(n)$  we neglect constant
- Big-Oh always depends on highest exponential.  
e.g :  $15n^2 + 6n^3 \rightarrow O(n^3)$

$O(1)$ :

```
a := 1  
b := 2  
c := a+5*b
```

SINCE these are only assignment statements,  
its time complexity will be  $O(1)$

```
i := 0  
while i<10 do  
    i := i + 1
```

Loop is independent of n

$O(n)$ :

```
i := 0  
while i < n do  
  i := i + 1
```

$f(n) = n$   
 $O(f(n)) = O(n)$

```
i := 0  
while i < n do  
  i := i + 3
```

$f(n) = n/3$   
 $O(f(n)) = O(n)$

$O(n^2)$ :

```
for (i:=0;i<n;i++)  
  for (j:=0;j<n;j++)
```

$$f(n) = n * n = n^2$$

$$O(f(n)) = O(n^2)$$

```
for (i:=0;i<n;i++)  
  for (j:=i;j<n;j++)
```

Suppose  $n = 5$

i	j	total j
0	0-4	n
1	1-4	n-1
2	2-4	n-2
3	3-4	n-3
4	4	1

$n + (n-1) + (n-2) + (n-3) + \dots + 1$  (acc  
to Sum of AP  $\rightarrow (n^2 + n)/2$

$\rightarrow O(n^2)$

$O(\log n)$ :

For binary search, complexity is  $O(\log n)$

$O(2^n)$ :

```
Int fun(int n)
{
    if (n <= 1) return n;
    return fun(n-1)+fun(n-1);
}
```

If we have a number that starts by performing one operation and then doubles the number of operations performed with each iteration, then the number of operations performed in the  $n$ th iteration is  $2^n$ .