

## Signals and Systems HW4

**Deadline: 2019/04/08 before 18:30**

**(You should submit hand-writing paper to BL B1 EE student office.)**

1. (30%) Suppose a continuous-time signal  $x(t)$  is an odd signal. Show that the Fourier transform  $X(j\omega)$  of  $x(t)$  is given by

$$X(j\omega) = -2j \int_0^{\infty} x(t) \sin(\omega t) dt$$

2. The output  $y(t)$  of a causal LTI system is related to the input  $x(t)$  by the equation

$$\frac{dy(t)}{dt} + 10y(t) = \int_{-\infty}^{\infty} x(\tau)z(t-\tau)d\tau - x(t)$$

where  $z(t) = e^{-t}u(t) + 3\delta(t)$

- (a) (20%) Find the frequency response  $H(j\omega)$  of this system.

( $H(j\omega) = \frac{Y(j\omega)}{X(j\omega)}$ , where  $X(j\omega)$  and  $Y(j\omega)$  are the Fourier transform of  $x(t)$  and  $y(t)$  respectively.)

- (b) (20%) Determine the impulse response  $h(t)$  of the system in time domain.

3. Use the Parseval's relation to obtain the value of the integral

$$\int_{-\infty}^{\infty} [\text{sinc}(\alpha t)]^2 dt$$

where  $\text{sinc}(t) = \frac{\sin(\pi t)}{\pi t}$ ,

as an explicit function of  $\alpha$ . (30%)