

Problem 2

Hot Day $\rightarrow \underbrace{0.2}_1, \underbrace{0.4}_2, \underbrace{0.4}_3$

Cold day $\rightarrow 0.5, 0.4, 0.1$

If today is hot $\rightarrow 0.6$ chance tomorrow is hot

If today is cold $\rightarrow 0.5$ chance tomorrow is cold

0.8 chance first day is hot

$$Pr(B|A) = \frac{Pr(A|B) Pr(B)}{Pr(A)} = \frac{0.128 \cdot 0.8}{0.11} = \boxed{0.93}$$

B = day is hot

A = Observation of 3 or 1 ice creams.

$$Pr(A|B) = (0.4)(0.2 \cdot 0.6 + 0.4 \cdot 0.5) = 0.128$$

$$Pr(B) = 0.8$$

$$Pr(A) = (0.8 \cdot 0.4)(0.2 \cdot 0.1) + (0.6 \cdot 0.5 + 0.5 \cdot 0.2) = 0.11$$