

4) Compute the entropy of  $X$  given  $Y$

$$H(X|Y) = - \sum_{x,y} p(x,y) \log(p(x,y)) = -E[\log(p(x,y))]$$

Rebuild the table:

	X				
	0	1	2	3	4
$p(0 Y) = 18\%$	18%	18%	23%	24%	17%
$p(1 Y) = 18\%$					
$p(2 Y) = 23\%$					
$p(3 Y) = 24\%$					
$p(4 Y) = 17\%$					

$$\begin{aligned} H(X|Y) &= [-0.18 \log(0.18)] + [-0.18 \log(0.18)] \\ &\quad + [-0.23 \log(0.23)] + [-0.24 \log(0.24)] \\ &\quad + [-0.17 \log(0.17)] = 0.45 + 0.45 + 0.49 + 0.49 \\ &= 1.88 \end{aligned}$$

$$H(X|Y) = 1.88$$