

$$D \# \frac{b}{f} : s$$

$$-5 \text{ [V]}$$

$$x(t) = 20 \sin(7t - \pi/2) - 3 \cos(5t) + 2 \cos(10t)$$

$$\omega_1 = 7$$

$$\omega_2 = 5$$

$$\omega_3 = 10$$

$$2\pi f = 7$$

$$2\pi f = 5$$

$$2\pi f = 10$$

$$f = 7/2\pi$$

$$f_2 = 5/2\pi$$

$$f_3 = 10/2\pi$$

$$f = 1.114 \text{ Hz}$$

$$f_2 = 0.796 \text{ Hz}$$

$$f_3 = 1.592 \text{ Hz}$$

$$f_3 \geq 2 f_2$$

$$7 = \frac{2\pi}{T}$$

$$f_3 \geq 3.18 \text{ Hz}$$

$$M2 \quad \frac{Y_{\max} - Y_{\min}}{X_{\max} - X_{\min}} = \frac{5V + 2.2}{25 - (-25)} = 0.17$$

$$c = -2.2 - (0.17)(-25) =$$

$$\sin(\omega t + \phi)$$

$$\frac{70}{2\pi} = \frac{1}{7} \cdot 2 \cdot \frac{1}{5} = \frac{1}{10} \cdot 70$$

$$\frac{35}{\pi} T = (10 - 14 - 7) \text{ ms} = 70$$

$$T = 2\pi$$

2)  $f_s = 5 \text{ KHz}$

$$x(t) = 3 \cos(1000\pi t) + 5 \sin(2000\pi t) + 10 \cos(11000\pi t)$$

$$\frac{11000\pi}{2\pi} = f$$

$$5500 \text{ } f_{\text{max}}$$

$$f_s > 2 f_{\text{max}} \text{ } 11 \text{ KHz}$$



$$3) \quad \omega_0 = \frac{2\pi}{T} \quad (a-b)^2 = a^2 + b^2 - 2ab$$

$$\lim_{T \rightarrow \infty} \frac{1}{T} \int_T^T |x_1(t) - x_2(t)|^2 dt$$

$$x_2(t) = \begin{cases} 1 & \text{si } 0 \leq t \leq T/4 \\ -1 & \text{si } T/4 \leq t \leq 3T/4 \\ 1 & \text{si } 3T/4 \leq t \leq T \end{cases}$$

$$\frac{1}{T} \left( \int_0^T x_1^2(t) dt + \int_0^T x_2^2(t) dt - 2 \int_0^T x_1(t) x_2(t) dt \right) \quad x_1(t) = A \cos(\omega_0 t)$$

$$A^2 \int_0^T \cos^2(\omega_0 t) dt \quad u = \omega_0 t \\ du = \omega_0$$

$$A^2 \left( \int \frac{1}{2} + \int \frac{\cos(2\omega_0 t)}{2} \right) = \frac{A^2}{2} \left( t + \frac{\sin(2\omega_0 t)}{2\omega_0} \right) \Big|_0^T = \frac{A^2}{2} (T + 0) = \frac{TA^2}{2}$$

$$\int_0^T x_2^2(t) dt = \int_0^{T/4} x_2^2(t) dt + \int_{T/4}^{3T/4} x_2^2(t) dt + \int_{3T/4}^T x_2^2(t) dt = \frac{1}{4}T + \left( \frac{3}{4}T - \frac{1}{4}T \right) + \frac{1}{4}T = T$$

$$2 \int_0^T x_1(t) x_2(t) dt = \int_0^{T/4} x_1(t) x_2(t) dt + \int_{T/4}^{3T/4} x_1(t) x_2(t) dt + \int_{3T/4}^T x_1(t) x_2(t) dt = \left( -\frac{3}{4} \right) T$$

$$= \int_0^{T/4} A \cos(\omega_0 t) dt + \int_{T/4}^{3T/4} A \cos(\omega_0 t) dt + \int_{3T/4}^T A \cos(\omega_0 t) dt = A \left( \frac{\sin(\omega_0 t)}{\omega_0} - \frac{\sin(\omega_0 t)}{\omega_0} + \frac{\sin(\omega_0 t)}{\omega_0} \right)$$

$$\frac{2A}{\omega_0} \left( \sin(\omega_0 t) \Big|_0^{T/4} - \sin(\omega_0 t) \Big|_{T/4}^{3T/4} + \sin(\omega_0 t) \Big|_{3T/4}^T \right)$$

$$(\sin(\pi/2) - \sin(0)) - (\sin(\pi/2) - \sin(\pi/2)) + (\sin(2\pi) - \sin(3\pi/2)) = \frac{2A}{\omega_0} (1 + 2 + 1)$$

$$\frac{8A}{\omega_0} = \frac{8TA}{2\pi} = \frac{4}{\pi} TA$$

$$\frac{1}{T} \left( \frac{T A^2}{2} + 1 - \frac{4}{\pi} T A \right)$$

$$\lim_{T \rightarrow \infty} \left( \frac{A^2}{2} - \frac{4}{\pi} A + 1 \right) = \delta(X_1 - X_2)$$

$$\delta(X_1 - X_2) = \left( \frac{A^2}{2} - \frac{4}{\pi} A + 1 \right)$$



$$4) \\ a) x(t) = \sum_{n=-\infty}^{\infty} C_n e^{jn\omega_0 t}$$

$$x'(t) = \sum_{n=-\infty}^{\infty} (jn\omega_0) e^{jn\omega_0 t} C_n$$

$$x''(t) = \sum_{n=-\infty}^{\infty} (jn\omega_0)^2 e^{jn\omega_0 t} C_n$$

$$x''(t) = - \sum_{n=-\infty}^{\infty} n^2 \omega_0^2 C_n e^{jn\omega_0 t}$$

$$\int_{t_1}^{t_F} x''(t) e^{-jm\omega_0 t} dt = - \sum_{n=-\infty}^{\infty} n^2 \omega_0^2 C_n \int_{t_1}^{t_F} e^{j(n-m)\omega_0 t} dt$$

Por ortogonalidad

$$\int_{t_1}^{t_F} e^{j(n-m)\omega_0 t} dt = \begin{cases} t_F - t_1 & \text{si } n=m \\ 0 & \text{si } n \neq m \end{cases}$$

$$\int_{t_1}^{t_F} x''(t) e^{-jm\omega_0 t} dt = -m^2 \omega_0^2 C_m (t_F - t_1) \Rightarrow C_n = \frac{1}{(t_F - t_1) m^2 \omega_0^2} \int_{t_1}^{t_F} x''(t) e^{jm\omega_0 t} dt$$

$$b) a_n = \frac{2}{(t_F - t_1) n^2 \omega_0^2} \operatorname{Re} \left\{ \int_{t_1}^{t_F} x''(t) e^{-jn\omega_0 t} dt \right\}$$

$$b_n = \frac{2}{(t_F - t_1) n^2 \omega_0^2} \operatorname{Im} \left\{ \int_{t_1}^{t_F} x''(t) e^{jn\omega_0 t} dt \right\}$$