

Scribe

$$4) \quad 0 + k + 2k + 2k + 3k + k^2 + 2k^2 + 2k^2 + k = 1$$

$$10k^2 + 9k = 1$$

$$k = \frac{-9 \pm \sqrt{9^2 - 4(10)(-1)}}{20} = k_1 = \frac{1}{10} \quad \text{and} \quad k_2 = -1$$

$$E[X] = \sum_x xP(x) \Rightarrow$$

$$0 \cdot 0 + \frac{1}{10} + 2 \cdot \frac{2}{10} + 3 \cdot \frac{2(1)}{10} + 4 \cdot \frac{3}{10} + 5 \cdot \left(\frac{1}{10}\right)^2 + 6 \cdot 2\left(\frac{1}{10}\right)^2 + 7 \cdot \left(\frac{1}{10}\right)^2$$

$$\mu = \frac{183}{80}$$

$$E[X^2] = 0^2 \cdot 0 + \frac{1}{10} + 2^2 \cdot \frac{2}{10} + 3^2 \cdot \frac{2}{10} + 4^2 \cdot \frac{3}{10} + 5^2 \cdot \left(\frac{1}{10}\right)^2 + 6^2 \cdot 2\left(\frac{1}{10}\right)^2 + 7^2 \cdot \left(\frac{1}{10}\right)^2 = \frac{84}{5}$$

$$V[X] = E[X^2] - (E[X])^2 = \frac{84}{5} - \left(\frac{183}{80}\right)^2 = 3,4044$$