

Scribe

$$2) \frac{1}{\theta^2} x e^{-\frac{x}{\theta}}$$

$$l(\theta) = \prod_{i=1}^n \frac{1}{\theta^2} x_i e^{-\frac{x_i}{\theta}} = \left( \frac{1}{\theta^2} x_1 e^{-\frac{x_1}{\theta}} \right) \left( \frac{1}{\theta^2} x_2 e^{-\frac{x_2}{\theta}} \right) \dots \left( \frac{1}{\theta^2} x_n e^{-\frac{x_n}{\theta}} \right)$$

$$= \frac{1}{\theta^{2n}} \cdot \prod_{i=1}^n x_i \cdot e^{-\frac{1}{\theta} \sum x_i}$$

$$l(\theta) = \ln \left( \frac{1}{\theta^{2n}} \cdot \prod_{i=1}^n x_i \cdot e^{-\frac{1}{\theta} \sum x_i} \right) = \ln \left( \frac{1}{\theta^{2n}} \right) + \ln \left( \prod_{i=1}^n x_i \right) + \ln \left( e^{-\frac{1}{\theta} \sum x_i} \right)$$

$$= \ln(1) - \ln(\theta^{2n}) + \sum_{i=1}^n \ln(x_i) - \frac{1}{\theta} \sum_{i=1}^n x_i \cdot \ln(e)$$

$$-2n \ln(\theta) + \sum_{i=1}^n \ln(x_i) - \frac{1}{\theta} \cdot \sum_{i=1}^n x_i$$

$$\frac{d}{d\theta} l(\theta) = 0 \Rightarrow -\frac{2n}{\theta} + \frac{1}{\theta^2} \cdot \sum_{i=1}^n x_i = 0 \Rightarrow \frac{1}{\theta^2} \sum_{i=1}^n x_i = \frac{2n}{\theta}$$

$$\Rightarrow \frac{\theta}{1} = \frac{2n}{\sum_{i=1}^n x_i} \Rightarrow \frac{1}{\theta} = \frac{2n}{\sum_{i=1}^n x_i} \Rightarrow \frac{1}{n} = \frac{2n\theta}{\sum_{i=1}^n x_i} = \frac{\sum_{i=1}^n x_i}{2n^2} = \theta$$

$$\frac{d^2}{d\theta^2} l(\theta) \Rightarrow \frac{2n}{\theta^2} - \frac{2}{\theta^3} \cdot \sum_{i=1}^n x_i < 0$$

$$\theta = \frac{20.87 + 13.74 + 5.24 + 2.76 + 4.87 + 2.66}{2 \cdot 6^2} = 0,692$$