

3) Cx^2y

$x^2 = y$

$[0:1]$

$$\int_0^1 \int_{x^2}^1 Cx^2y \, dy \, dx = 1 = C \int_0^1 \frac{x^2(1-x^4)}{2} \, dx$$

$$\Rightarrow \frac{2C}{21} = 1 \quad \Rightarrow \quad C = \frac{21}{2}$$

$\frac{21}{2}x^2y$

a) $P(X > Y) =$

$$\int_0^1 \int_{x^2}^x \frac{21}{2}x^2y \, dy \, dx = \frac{3}{10}$$

b) $f_{Y|X=x}(y) =$

$$f(x) = \int_0^1 \frac{21}{2}x^2y \, dx \Rightarrow \frac{21}{2}y \left[\frac{x^3}{3} \right]_0^1 = \frac{21}{2}y \cdot \frac{1}{3}$$

$$\frac{\frac{21}{2}x^2y}{\frac{21y}{6}} //$$