

Matrice

$$A = \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{pmatrix} \quad \begin{matrix} 1 \leq i \leq n \\ 1 \leq j \leq n \end{matrix}$$

1) $m = 1 \Rightarrow$ Matricea linie

$$A = (a_{11} \ a_{12} \ \dots \ a_{1n})$$

2) $n = 1 \Rightarrow$ Matricea coloana

$$A = \begin{pmatrix} a_{11} \\ a_{21} \\ \dots \\ a_{m1} \end{pmatrix}$$

3) $m = n \Rightarrow$ matrice patratica

Adunare:

$$0 + A = A + 0 = A$$

$$A + (-A) = -A + A = 0$$

Inmultire:

$$A = \begin{pmatrix} a & b \\ c & d \end{pmatrix} \quad B = \begin{pmatrix} e & f \\ g & h \end{pmatrix}$$

$$A * B = \begin{pmatrix} a * e + b * g & a * f + b * h \\ c * e + d * g & c * f + d * h \end{pmatrix}$$

$$A * B \neq B * A$$

$$(A * B) * C = A * (B * C)$$

El.neutru:

$$I_n = \begin{pmatrix} 1 & 0 & \dots & 0 \\ 0 & 1 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 1 \end{pmatrix}$$

$$A * I = I * A$$

Calculul lui A^n :

$A^n =$ se calculeaza A^1, A^2, A^3, \dots pana se observam o regula

$$\text{Daca } A = \begin{pmatrix} \cos x & \pm \sin x \\ \mp \sin x & \cos x \end{pmatrix} \Rightarrow A^n = \begin{pmatrix} \cos nx & \pm \sin nx \\ \mp \sin nx & \cos nx \end{pmatrix}$$

sau cu **BINOMUL LUI NEWTON**: $A = I + B$

$$A^n = (I + B)^n = \sum_{k=0}^n C_n^k I^{n-k} B^k$$

Relatia Canley-Hamilton:

$$\text{Tr}(x) = a + d \quad ! \quad (\text{Tr}(x))^2 = -a \Rightarrow \text{Tr}(x) = \pm i\sqrt{a}$$

$$\det(x) = a * d - b * c$$

$$A = B \Rightarrow \det A = \det B$$

$$x^2 - \text{Tr}(x) * x + \det x * I_2 = O_2$$

Determinanti:

1. de ordin 2:

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = a * d - b * c$$

2. de ordin 3:

$$\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = a * e * i + b * f * g + d * h * c - g * e * c - \\ - a * f * h - d * b * i$$

3. de ordin n:

-are **n!** termeni

-face zerouri prin adunarea si scaderea L si C

-dezvoltarea dupa o linie / o coloana:

$$\begin{vmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{vmatrix} = a_{21}(-1)^{2+1} * \begin{vmatrix} a_{12} & a_{13} & a_{14} \\ a_{32} & a_{33} & a_{34} \\ a_{42} & a_{43} & a_{44} \end{vmatrix}$$

Transpusa unei matrici:

$$A = \begin{pmatrix} a & b & c \\ d & e & f \end{pmatrix} \quad {}^tA = \begin{pmatrix} a & d \\ b & e \\ c & f \end{pmatrix} \quad a_{ij} \rightarrow a_{ji}$$