Deep Learning Fundamentals

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Summary

M1. Introduction

M2. The basic process of learning

M3. Terminology

M4. Practical considerations



Identifying the problems

Need for process automation (redundant ones, most of the time).

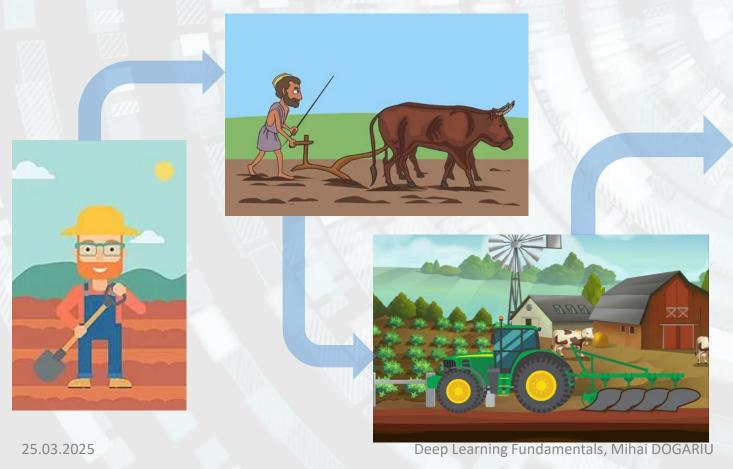
➤ Human capacity is limited and prone to erros, especially after longer time periods (approx. 6h).

➤ Increasing cost/efficiency ratio.



Solving the problems

> Externalizing/replacing human effort.



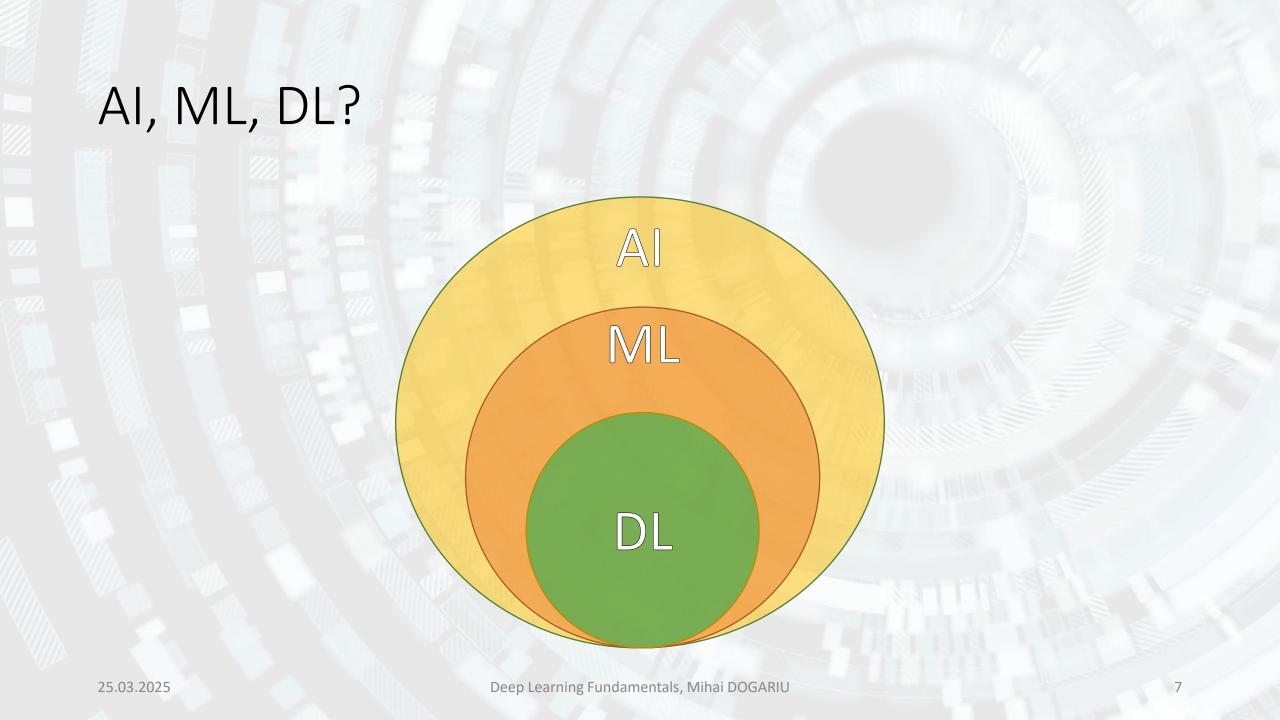


AI, ML, DL?

Artificial Intelligence (AI) = the ability of computer systems to perform tasks normally requiring human intelligence.

Machine Learning (ML) = AI subdomain in which systems are designed with the ability to learn based on previous examples.

Deep Learning (DL) = ML subdomain in which systems are designed based on the human neural network model.

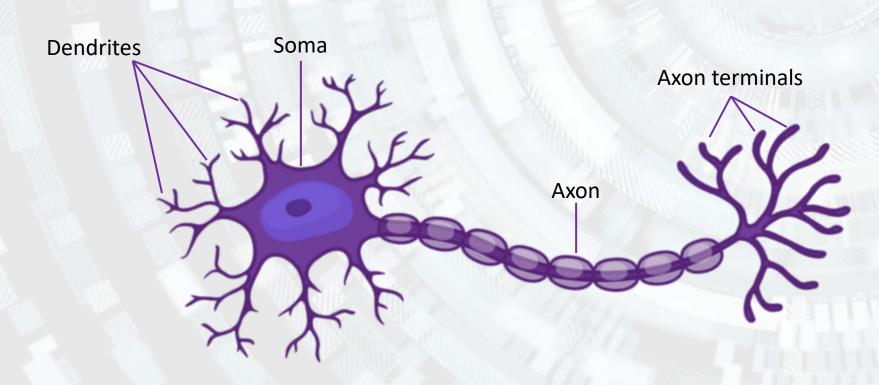


The Deep Learning Boom

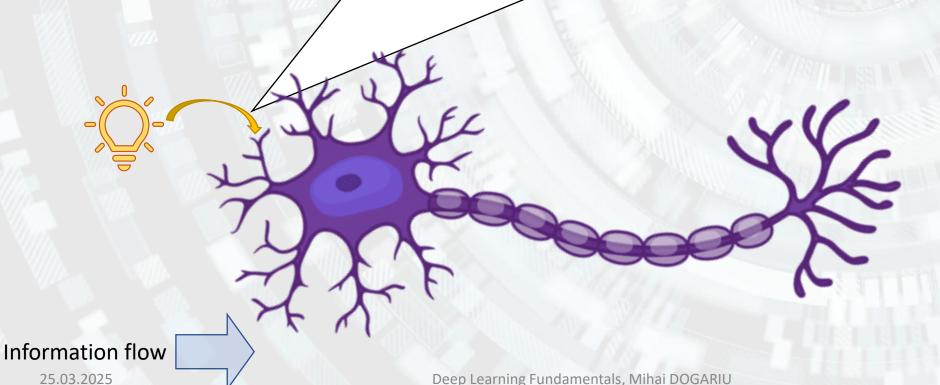
What lead to the current exponential advancement of deep learning?

- 1. Higher computing power (hardware) GPU Let's test it out unit #1
- 2. A lot more data => better results
- 3. Optimized frameworks (software): Tensorflow, PyTorch, Caffe, MXNet, DeepLearning4J etc.
- 4. Attention and financial influx from the industry: Facebook Al Research (FAIR), Google Deepmind, NVIDIA, OpenAI, Microsoft Research, AWS Deep Learning etc.

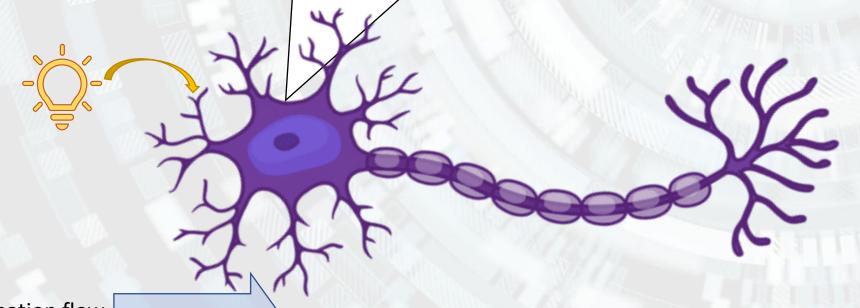
The fundamental cell of the nervous system



Dendrites are the input gate for neurons. They are connected to and receive signals from other neurons (>1000). Each dendrite weights the signal that it receives in a different manner (inhibit or excite).



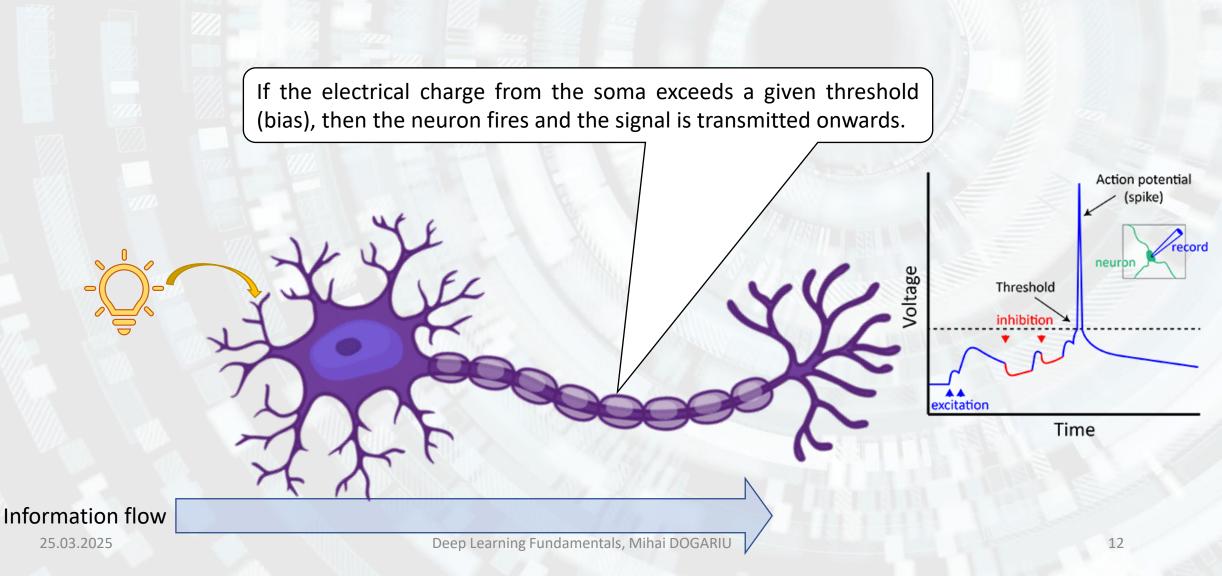
The soma gathers all synaptic signals and sums their electrical potentials.



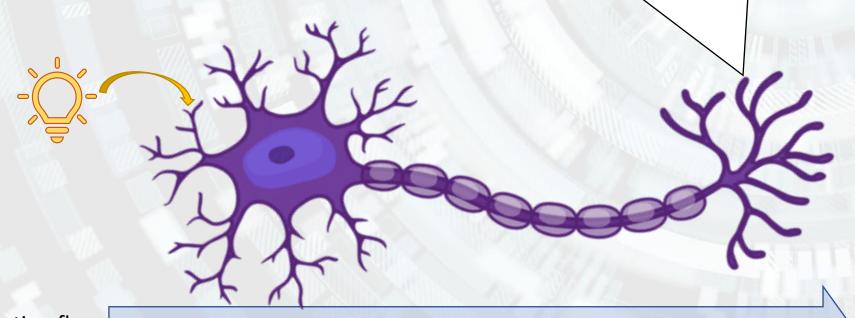
Information flow

25.03.2025

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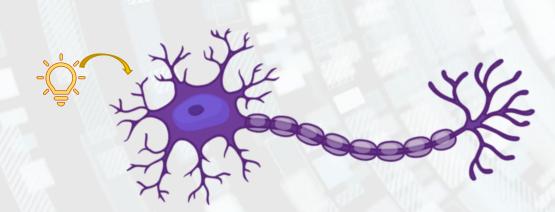


If the neuron was activated, its signal is sent to all other neurons connected to its axon terminals.



Information flow

Represents a mathematical model of the biologic neuron.



The biologic neuron Input

The artificial neuron

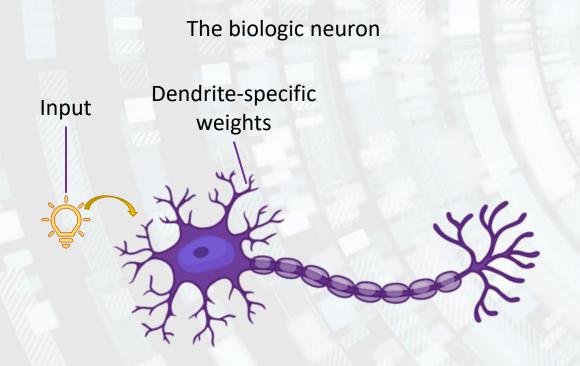
 (x_1)

 (x_2)

 (x_3)

 (x_4)

 (x_n)



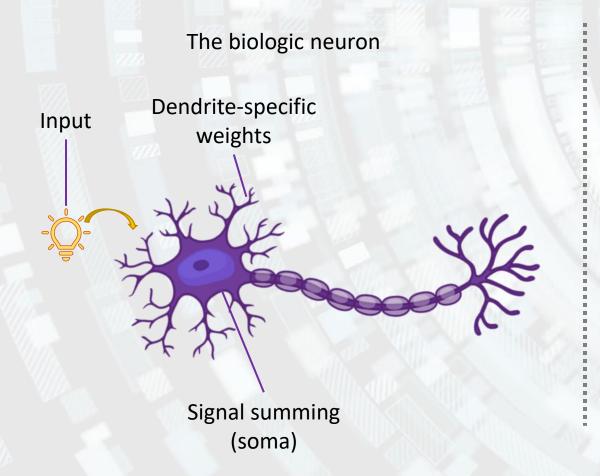
$$(x_1) \approx (w_1)$$

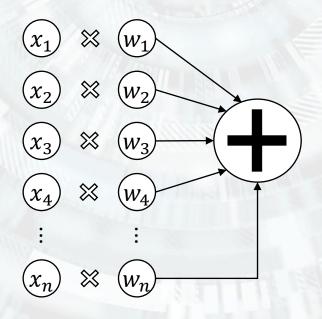
$$(x_2) \approx (w_2)$$

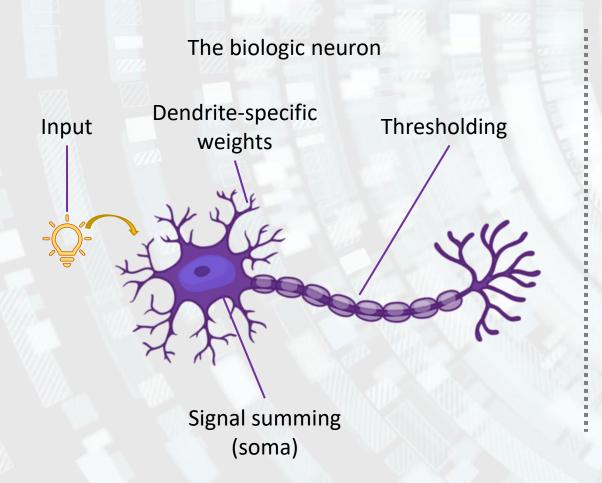
$$(x_3) \approx (w_3)$$

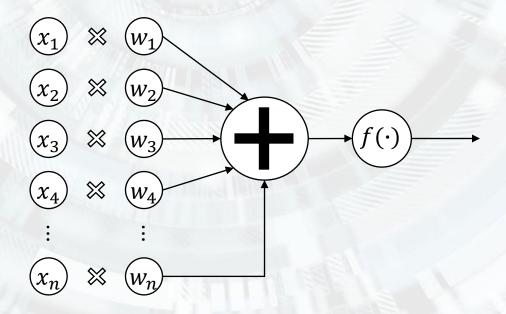
$$(x_4) \approx (w_4)$$

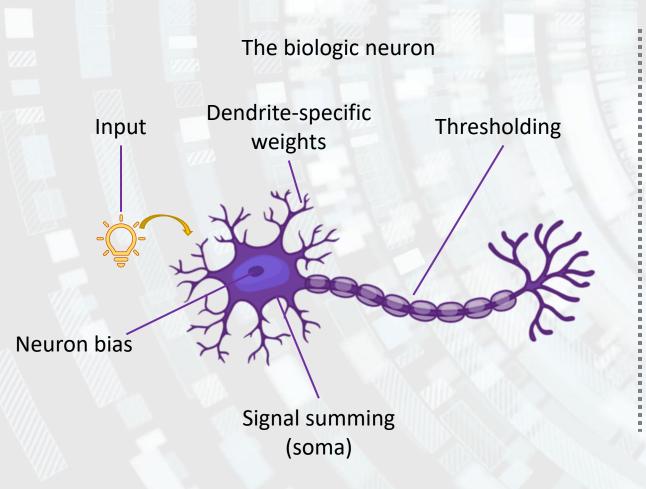
$$(x_N) \approx (n)$$

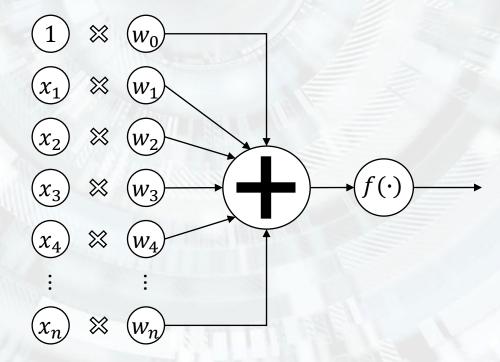










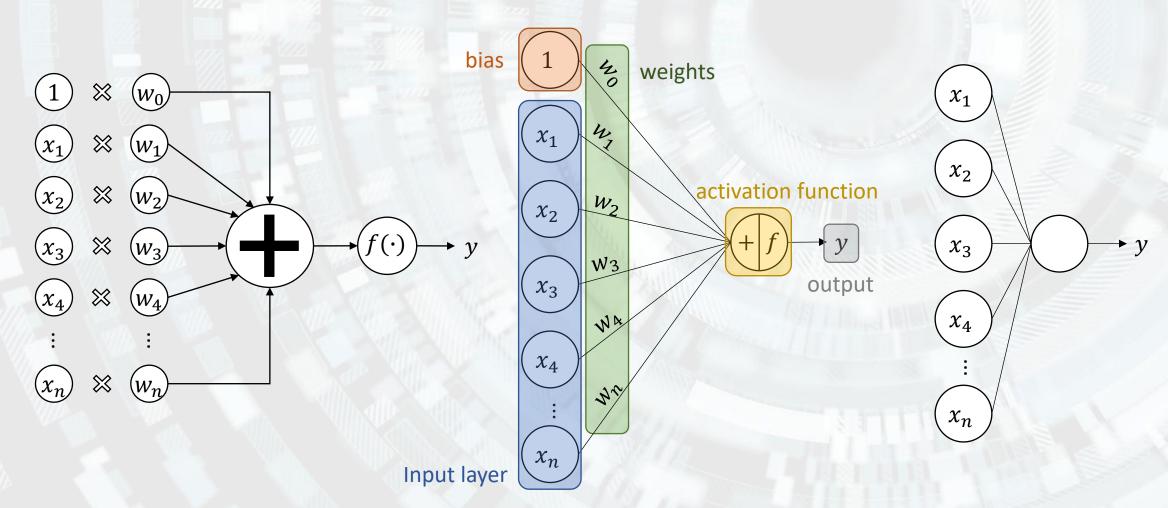


The mathematical model:

$$y = f\left(\sum_{i=0}^{n} w_i x_i\right) = f\left(\sum_{i=1}^{n} w_i x_i + b\right) = f(\mathbf{w} \cdot \mathbf{x} + b)$$

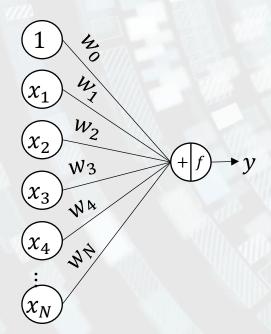
 w_i – weights; $w_0 \rightarrow b$ - bias x_i – input vector; $x_0 = 1$ n – input vector dimension $f(\cdot)$ – activation function y – neuron output.

The artificial neuron – graphical representation



Learning of an artificial neuron

Learning = iterative process through which all parameters belonging to the neuron are learned such that the model correctly classifies the input data.



What are the fixed parameters?

- input
- output
- transfer function

What are the adjustable parameters?

- weights
- bias



Learning of an artificial neuron

Algorithm:

- 1. initialize weights with a low enough value.
- 2. for each input-output pair (x_j, \widehat{y}_j) from the training set:
 - 2.1. compute the output of the system:

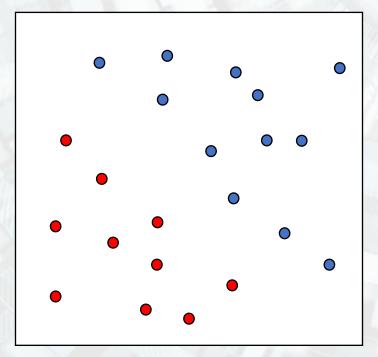
$$y_j(t) = f\left(\sum_{i=0}^n w_i x_{j,i}\right)$$

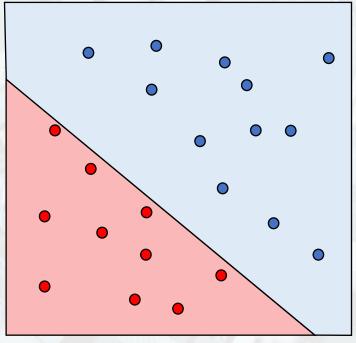
2.2. update the weights, $\forall i, 0 \leq i \leq n$:

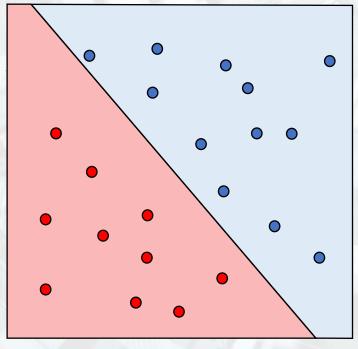
$$w_i(t+1) = w_i(t) + \alpha * (\widehat{y}_j - y_j(t)) * x_{j,i}$$

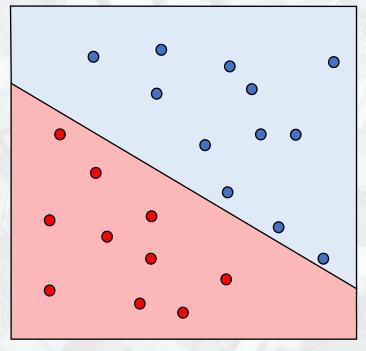
3. repeat step 2 until the iteration error is lower than a given threshold or until sufficient iterations have been run.

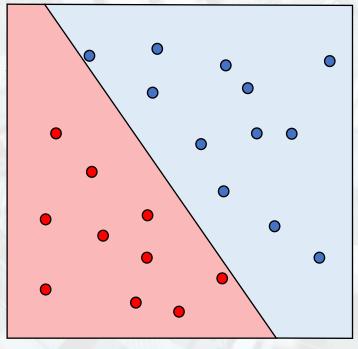
Let's test it out – unit #2







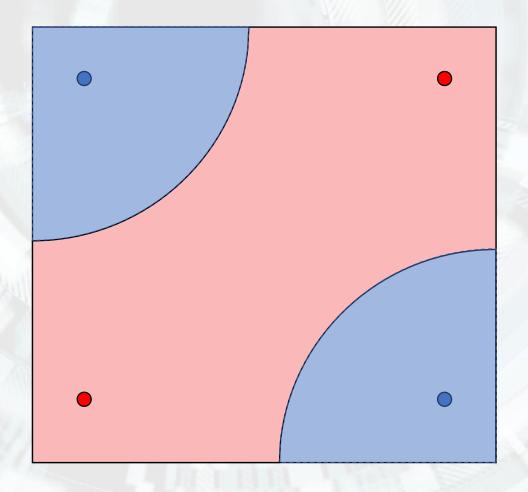




Non-linear separable space

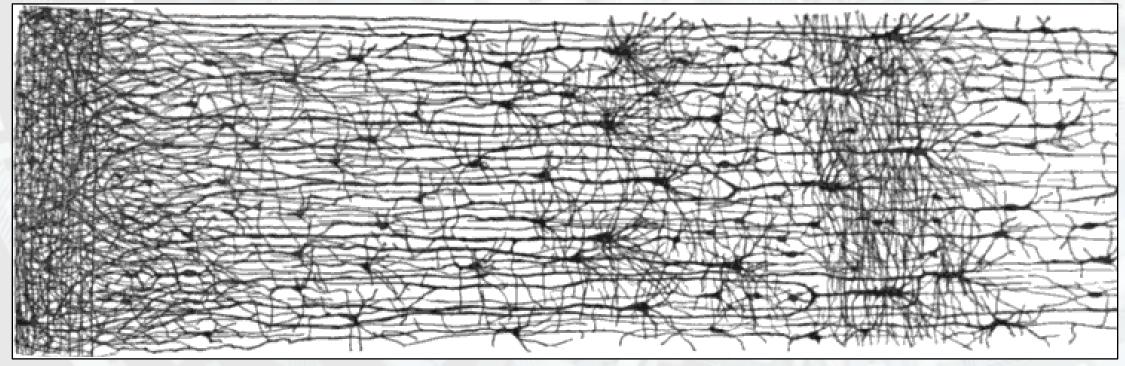
What if the space is not linearly separable (e.g. XOR function)?

- 1. Combine several linear functions in cascade?
- 2. Apply non-linearities?
- 3. Combine several non-linear functions in cascade?

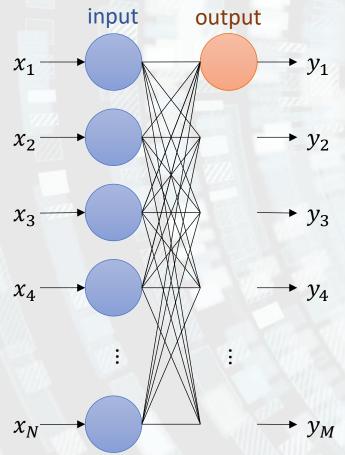


The neuron network

The nervous system is formed of an entire network of neurons. Total number is estimated to be 86.1 ± 8.1 bn.



Single-layer neuron network



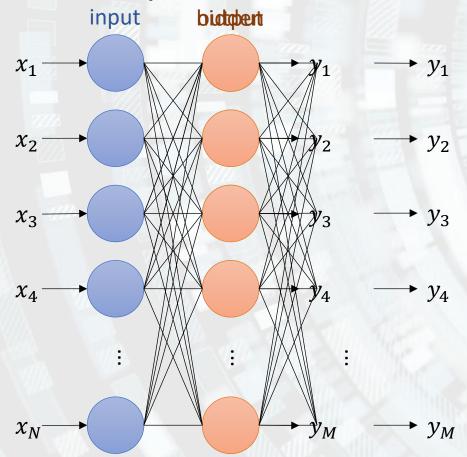
Given a thresholding function, a single neuron can classify information in only 2 classes. Moreover, this is a "hard" decision.

A partial solution: a network formed of several neurons, placed in parallel, at the same level.

- + can be adapted to multi-class problems;
- still can't model non-linear separable spaces;
- every output is binary

N can be (and usually is) different from M

Multi-layer neuron network



- + a multi-layer neuron network can classify more complex data, e.g. XOR function.
- every output is binary

N can be (and usually is) different from M

M2. The basic process of learning

The learning process

Machine learning = we say that a system "learns" from experience E regarding a set of tasks T and a performance measure P, if the performance in solving the tasks T, measured by P, grows with the experience E.

Goal: finding a function that associates an input dataset with their correct output, in the best way possible (smallest error; ideally – 0).

Consists of 2 steps:

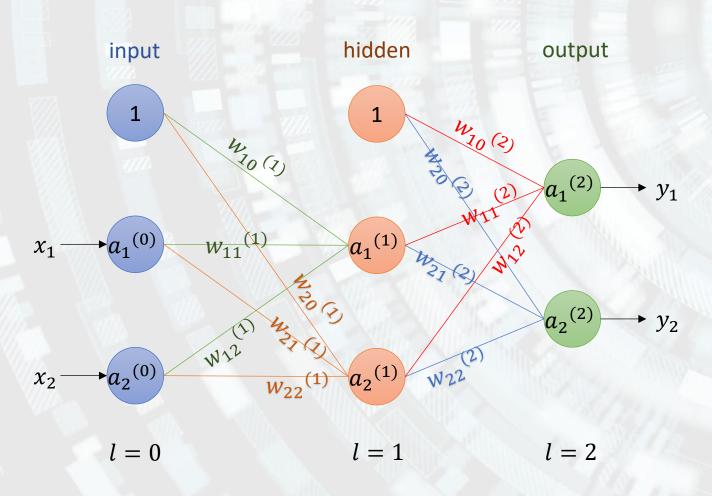
- 1. Forward propagation;
- 2. Backpropagation.

Forward propagation

- **≻Goal**: obtaining the output y = M(x);
- ➤M = transfer function of the neural network, obtained by composition off all transfer functions associated to the network's layers.
- >It involves passing the neural network from the input to the output.

It breaks down to computing the activations for each neuron inside the network, from the lower layers towards the higher ones.

Forward propagation

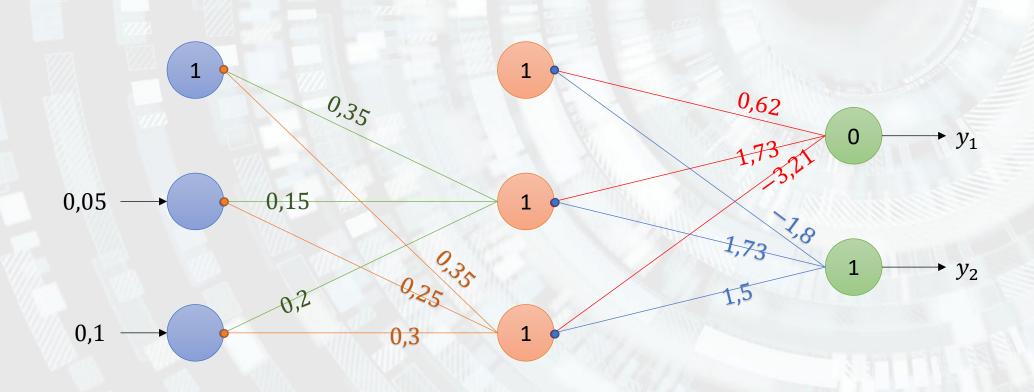


$$a_i^{(l)} = f\left(\sum_{j=0}^n w_{i,j}^{(l)} a_i^{(l-1)}\right)$$

$$a_0^{(l)} = 1$$

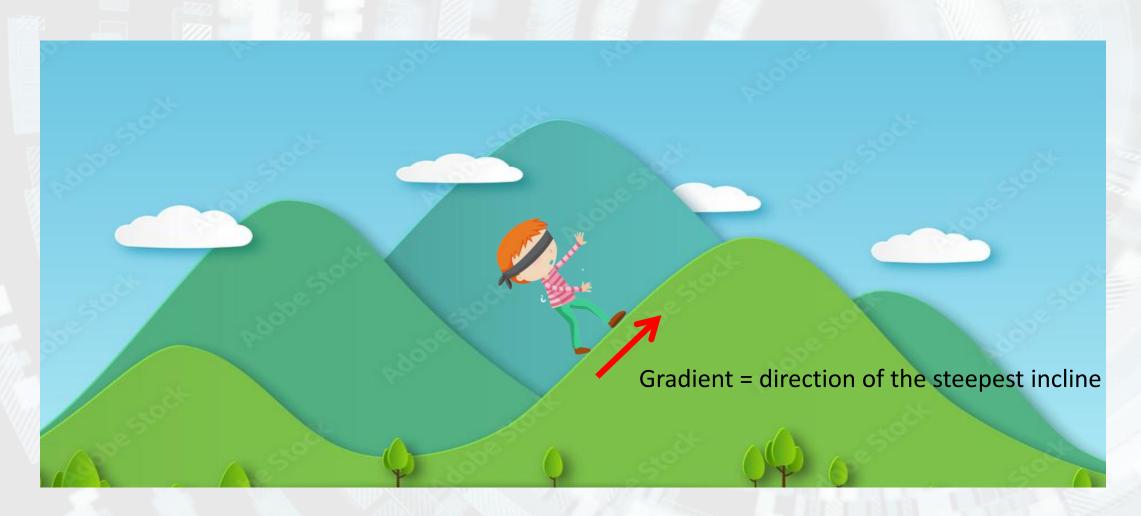
$$f(x) = \begin{cases} 1, x \ge 0 \\ 0, x < 0 \end{cases}$$

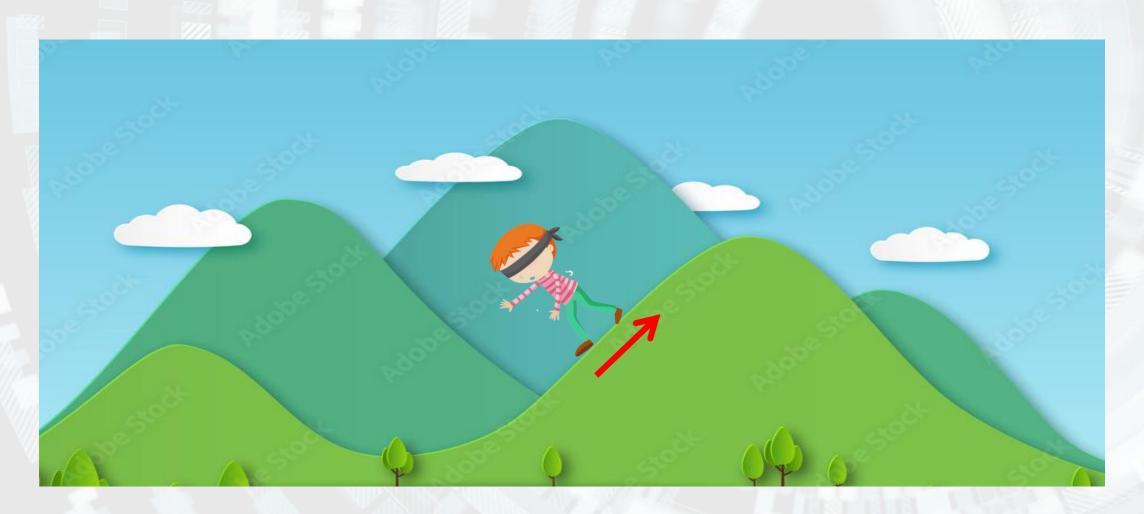
Forward propagation – numerical example



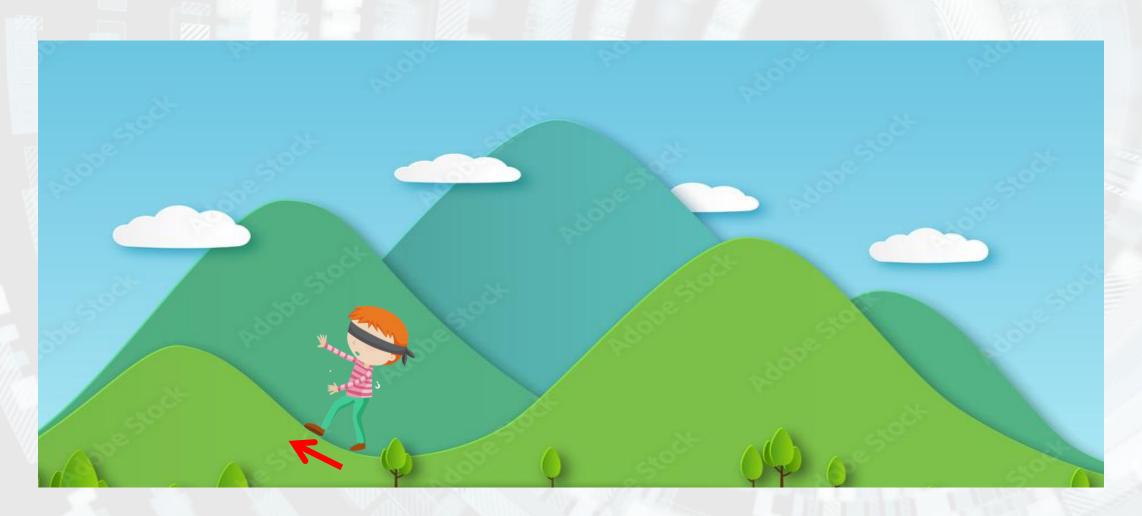
Backpropagation

- ➤ Goal: learning the internal representation of a neural network. It involves computing all weights (and biases) which bring the model's output tu a form as close as possible, ideally identical, to the desired/real output (groundtruth).
- ➤ How do we measure what it means to be "as close as possible"?➤ A: by using a cost function, e.g. mean square error.
- ➤ What rule do we use to adjust the weights?
 - A: gradient descent.













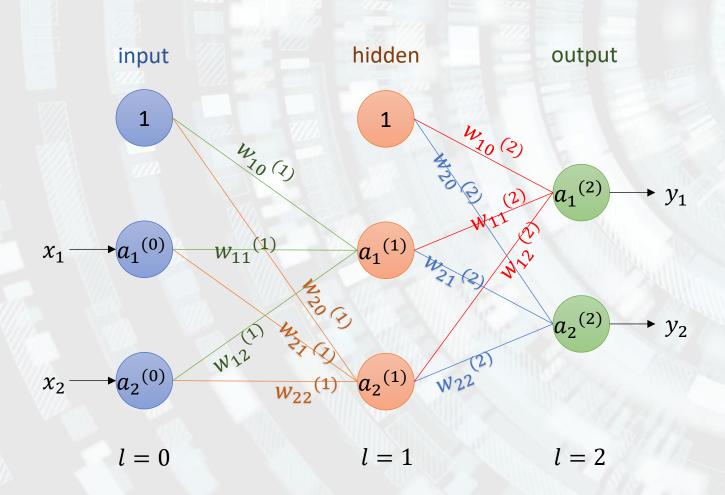
> Method to compute the gradient for a neural network's parameters.

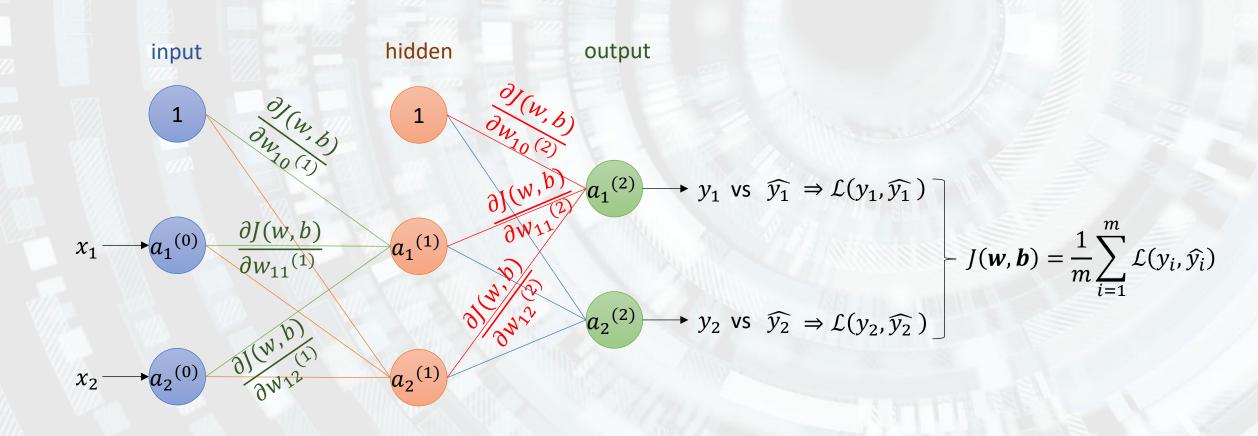
$$y = f(\mathbf{w} \cdot \mathbf{x} + b) = f(\mathbf{w}^T \mathbf{x} + b)$$

Funcție de pierdere (se calculează pe o singură pereche de eșantioane)
$$\mathcal{L}(y, \hat{y}) \overset{e.g.}{\Longrightarrow} \mathcal{L}(y, \hat{y}) = (y - \hat{y})^2$$

Funcție de cost (se calculează pe un set de perechi de eșantioane)

$$J(\boldsymbol{w}, \boldsymbol{b}) = \frac{1}{m} \sum_{i=1}^{m} \mathcal{L}(y_i, \widehat{y}_i)$$





l = 0

l=2

l = 1

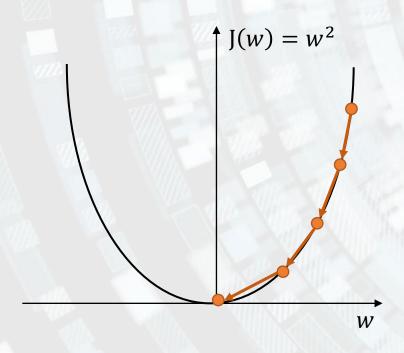
➤ Weights update follows this rule:

$$w^{(t+1)} = w^{(t)} - \alpha \frac{\partial J(w)}{\partial w^{(t)}}$$

Simplified writing:

$$w \coloneqq w - \alpha \frac{\partial J(w)}{\partial w}$$

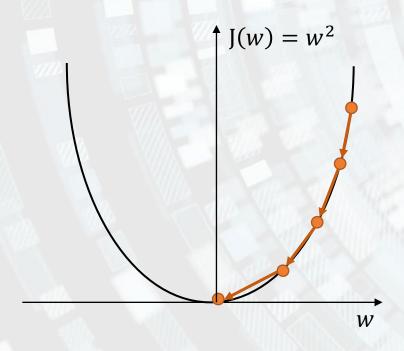
➤ Graphical example: consider the simplified case in which the cost function depends on a single variable and we choose MSE.



$$w \coloneqq w - \alpha \frac{\partial J(w)}{\partial w}$$

Ideally, we find w s.t. J(w) = 0, but, in practice, this almost never happens.

➤ Graphical example: consider the simplified case in which the cost function depends on a single variable and we choose MSE.

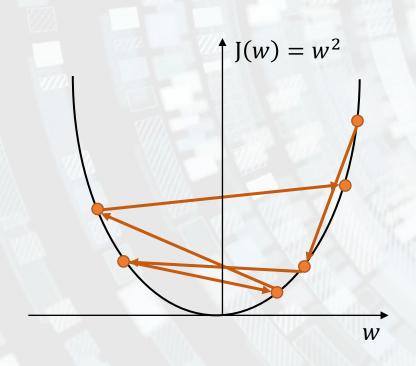


$$w \coloneqq w - \alpha \frac{\partial J(w)}{\partial w}$$

- $\frac{\partial J(w)}{\partial w}$ indicates the direction of the steepest increase
- α indicates the amplitude of the modification = learning rate

Gradient descent – learning rate impact

Same example as before, but with a **high learning rate**.

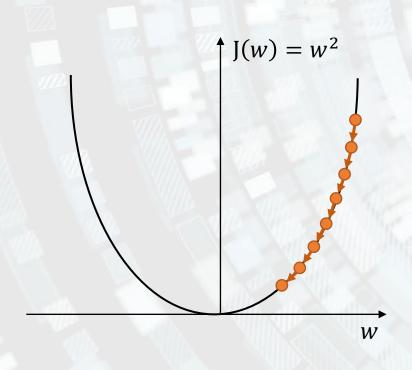


$$w \coloneqq w - \alpha \frac{\partial J(w)}{\partial w}$$

- The algorithm may miss the optimum, because each iteration brings a high displacement.
- + Due to the large steps taken, the distance to optimum is travelled faster => faster training.

Gradient descent – learning rate impact

➤ Same example as before, but with a **low learning rate**.



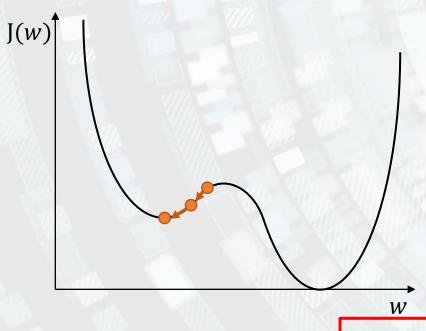
$$w \coloneqq w - \alpha \frac{\partial J(w)}{\partial w}$$

- The algorithm performs small updates => slower training.
- + Low probability to miss the optimum dure to the small steps.

Why not always use small learning rate?

Gradient descent – learning rate impact

Cost function that is not convex (local minimum is not necessarily global minimum), low learning rate.



$$w \coloneqq w - \alpha \frac{\partial J(w)}{\partial w}$$

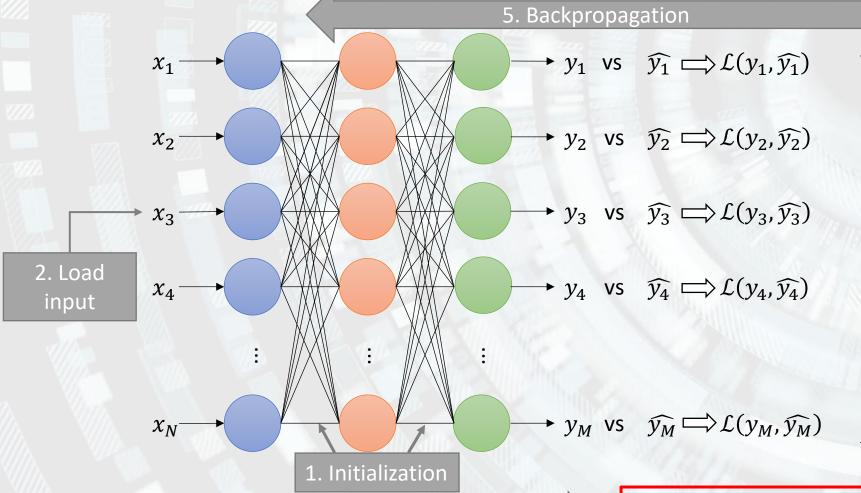
- There is a possibility that the algorithm gets stuck in a local minimum (saddle point)

Let's test it out – unit #3

General steps for neural network learning

- 1. Initialize network parameters
- 2. Load input data
- 3. Forward propagation
- 4. Compute cost function by comparing output data with groundtruth
- 5. Backpropagation + parameters update
- 6. Repeat steps 3-5 until convergence.

General steps for neural network learning



J(w,b)

4. Cost function

3. Forward propagation

Let's test it out – unit #4