

Shared Memory Programming with OpenMP

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Slides realized using material provided by Prof. Moreno Marzolla



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Credits

- Peter Pacheco, Dept. of Computer Science, University of San Francisco
<http://www.cs.usfca.edu/~peter/>
- Mary Hall, School of Computing, University of Utah
<https://www.cs.utah.edu/~mhall/>
- Salvatore Orlando, DAIS, Università Ca' Foscari di Venezia, <http://www.dais.unive.it/~calpar/>
- Tim Mattson, Intel
- Blaise Barney, OpenMP
<https://computing.llnl.gov/tutorials/openMP/> ([highly recommended!!](#))

OpenMP

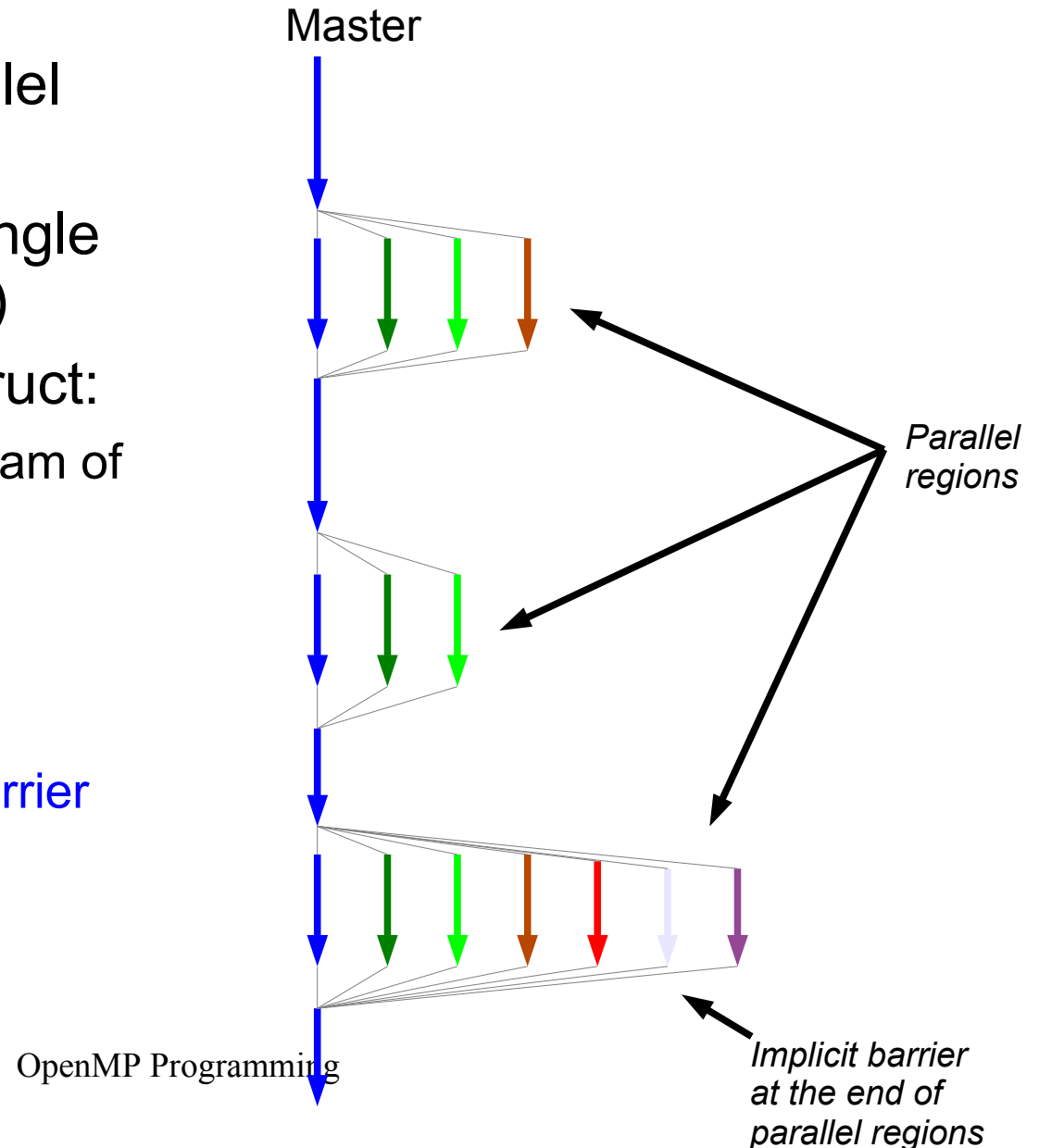
- Model for shared-memory parallel programming
- Portable across shared-memory architectures
- Incremental parallelization
 - Parallelize individual computations in a program while leaving the rest of the program sequential
- Compiler based
 - Compiler generates thread programs and synchronization
- Extensions to existing programming languages (Fortran, C and C++)
 - mainly by directives (`#pragma omp ...`)
 - a few library routines

Most OpenMP programs only use these items

OpenMP pragma, function, or clause	Concepts
<code>#pragma omp parallel</code>	Parallel region, teams of threads, structured block, interleaved execution across threads
<code>int omp_get_thread_num()</code> <code>int omp_get_num_threads()</code>	Create threads with a parallel region and split up the work using the number of threads and thread ID
<code>double omp_get_wtime()</code>	Timing blocks of code
<code>setenv OMP_NUM_THREADS N</code> <code>export OMP_NUM_THREADS=N</code>	Set the default number of threads with an environment variable
<code>#pragma omp barrier</code> <code>#pragma omp critical</code> <code>#pragma omp atomic</code>	Synchronization, critical sections
<code>#pragma omp for</code> <code>#pragma omp parallel for</code>	Worksharing, parallel loops
<code>reduction(op:list)</code>	Reductions of values across a team of threads
<code>schedule(dynamic [,chunk])</code> <code>schedule(static [,chunk])</code>	Loop schedules
<code>private(list), shared(list),</code> <code>firstprivate(list)</code>	Data environment
<code>#pragma omp master</code> <code>#pragma omp single</code>	Worksharing with a single thread
<code>#pragma omp task</code> <code>#pragma omp taskwait</code>	Tasks including the data environment for tasks.

OpenMP Execution Model

- Fork-join model of parallel execution
- Begin execution as a single process (master thread)
- Start of a parallel construct:
 - Master thread creates team of threads (worker threads)
- Completion of a parallel construct:
 - Threads in the team synchronize – **implicit barrier**
- Only the master thread continues execution



OpenMP uses Pragmas

`#pragma omp construct [clause [clause ...]]`

- *Pragmas* are special preprocessor instructions
 - They allow behaviors that are not part of the C specification
- Compilers that don't support the *pragmas* ignore them
- Most OpenMP constructs apply to the **structured block** following the directive
 - Structured block: a block of one or more statements with **one point of entry** at the top and **one point of exit** at the bottom
 - Returning from inside a parallel block is not allowed

The `#pragma omp parallel` directive

- When a thread reaches a `parallel` directive, it creates a team of threads and becomes the master of the team
 - The master has thread ID 0
- The code of the parallel region is duplicated and all threads will execute it
- There is an `implied barrier at the end of a parallel section`. Only the master thread continues execution past this point

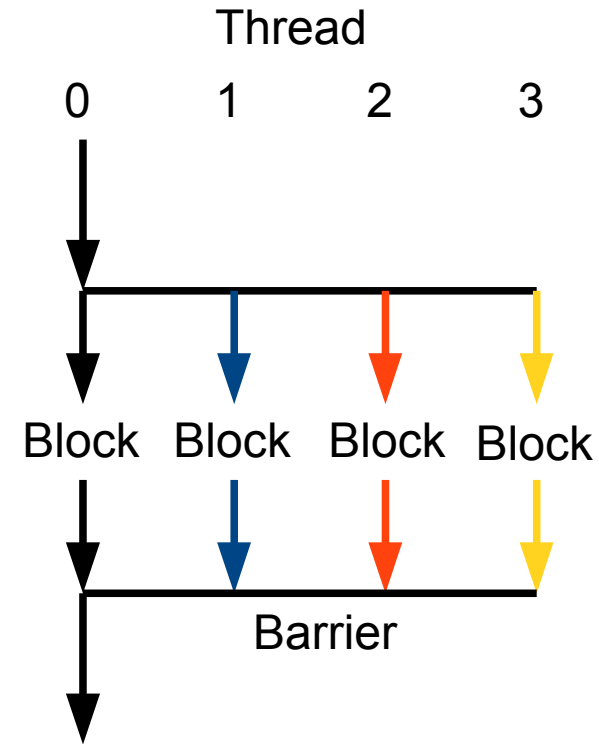
```
#pragma omp parallel [clause ...]  
clause ::=  
    if (scalar_expression) |  
    private (list) |  
    shared (list) |  
    default (shared | none) |  
    firstprivate (list) |  
    reduction (operator: list) |  
    copyin (list) |  
    num_threads (thr)
```


“Hello, world” in OpenMP

```
/* omp-demo0.c */
#include <stdio.h>

int main( void )
{
    #pragma omp parallel
    {
        printf("Hello, world!\n");
    }

    return 0;
}
```



```
$ gcc -fopenmp omp-demo0.c -o omp-demo0
$ ./omp-demo0
Hello, world!
Hello, world!
$ OMP_NUM_THREADS=4 ./omp-demo0
Hello, world!
Hello, world!
Hello, world!
Hello, world!
```

“Hello, world” in OpenMP

```
/* omp-demo1.c */
#include <stdio.h>
#include <omp.h>

void say_hello( void )
{
    int my_rank = omp_get_thread_num();
    int thread_count = omp_get_num_threads();
    printf("Hello from thread %d of %d\n",
           my_rank, thread_count);
}

int main( void )
{
    #pragma omp parallel
    say_hello();

    return 0;
}
```

```
$ gcc -fopenmp omp-demo1.c -o omp-demo1
$ ./omp-demo1
Hello from thread 0 of 2
Hello from thread 1 of 2
$ OMP_NUM_THREADS=4 ./omp-demo1
Hello from thread 1 of 4
Hello from thread 2 of 4
Hello from thread 0 of 4
Hello from thread 3 of 4
```

```

/* omp-demo2.c */
#include <stdio.h>
#include <stdlib.h>
#include <omp.h>

void say_hello( void )
{
    int my_rank = omp_get_thread_num();
    int thread_count = omp_get_num_threads();
    printf("Hello from thread %d of %d\n",
           my_rank, thread_count);
}

int main( int argc, char* argv[] )
{
    int thr = atoi( argv[1] );
    #pragma omp parallel num_threads(thr)
    say_hello();

    return 0;
}

```

```
$ gcc -fopenmp omp-demo2.c -o omp-demo2
```

```
$ ./omp-demo2 2
```

```
Hello from thread 0 of 2
```

```
Hello from thread 1 of 2
```

```
$ ./omp-demo2 4
```

```
Hello from thread 1 of 4
```

```
Hello from thread 2 of 4
```

```
Hello from thread 0 of 4
```

```
Hello from thread 3 of 4
```

Setting the number of threads programmatically

```
/* omp-demo3.c */
#include <stdio.h>
#include <stdlib.h>
#include <omp.h>

void say_hello( void )
{
    int my_rank = omp_get_thread_num();
    int thread_count = omp_get_num_threads();
    printf("Hello from thread %d of %d\n",
           my_rank, thread_count);
}

int main( int argc, char* argv[] )
{
    omp_set_num_threads(4);
    #pragma omp parallel
    say_hello();

    return 0;
}
```

```
$ gcc -fopenmp omp-demo3.c -o omp-demo3
$ OMP_NUM_THREADS=8 ./omp-demo3
Hello from thread 1 of 4
Hello from thread 2 of 4
Hello from thread 0 of 4
Hello from thread 3 of 4
```

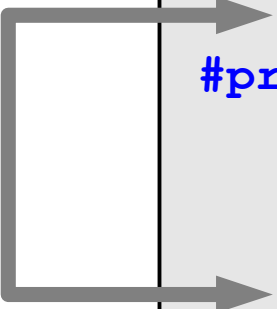
Warning

- `omp_get_num_threads()` returns the number of threads in the **currently active** pool
 - If no thread pool is active, the function returns 1
- `omp_get_max_threads()` returns (essentially) the **default size** of the thread pool

```
int main( int argc, char* argv[] )
{
    printf("Before par region: threads=%d, max=%d\n",
           omp_get_num_threads(), omp_get_max_threads());
    #pragma omp parallel
    {
        printf("Inside par region: threads=%d, max=%d\n",
               omp_get_num_threads(), omp_get_max_threads());
    }
    return 0;
}
```

See [omp-demo4.c](#)

Taking times



```
double tstart, tstop;
tstart = omp_get_wtime();
#pragma omp ...
{
    /* block of code to measure */
}
tstop = omp_get_wtime();
printf("Elapsed time: %f\n", tstop - tstart);
```


Remember: implicit barrier here

Scoping of variables

Scope

- In serial programming, the **scope** of a variable consists of the parts of a program where the variable can be used
- In OpenMP, the scope of a variable refers to the set of threads that can access the variable
- By default:
 - All variables that are visible at the beginning of a parallel block are **shared** across threads
 - All variables defined **inside** a parallel block are **private** to each thread

Variables scope in OpenMP

- `shared(x)` 
 - all threads access the same memory location
- `private(x)`
 - each thread has its own private copy of x
 - all local instances of x **are not initialized**
 - local updates to x are **lost** when exiting the parallel region
 - the original value of x is retained at the end of the block (OpenMP ≥ 3.0 only)
- `firstprivate(x)`
 - each thread has its own private copy of x
 - all copies of x **are initialized with the current value of x**
 - local updates to x are **lost** when exiting the parallel region
 - the original value of x is retained at the end of the block (OpenMP ≥ 3.0 only)
- `default(shared)` or `default(none)`
 - affects all the variables not specified in other clauses
 - `default(none)` ensures that you **must** specify the scope of each variable used in the parallel block that the compiler can not figure out by itself (**highly recommended!!**)

What is the output of this program?

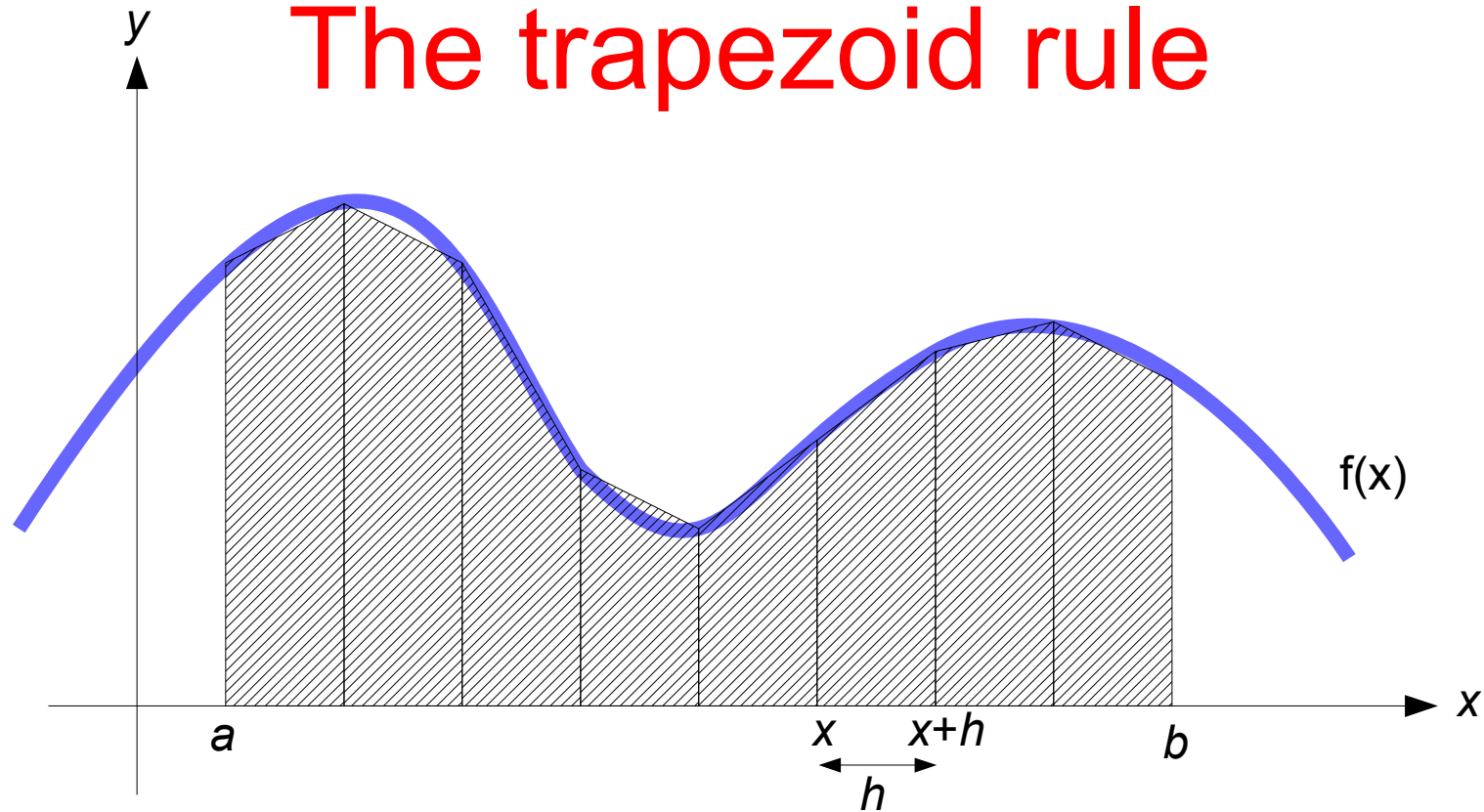
```
/* omp-scope.c */
#include <stdio.h>

int main( void )
{
    int a=1, b=1, c=1, d=1;
    #pragma omp parallel num_threads(10) \
        private(a) shared(b) firstprivate(c)
    {
        printf("Hello World!\n");
        a++;
        b++;
        c++;
        d++;
    }
    printf("a=%d\n", a);
    printf("b=%d\n", b);
    printf("c=%d\n", c);
    printf("d=%d\n", d);
    return 0;
}
```

Hint: compile with -Wall

Example: the trapezoid rule

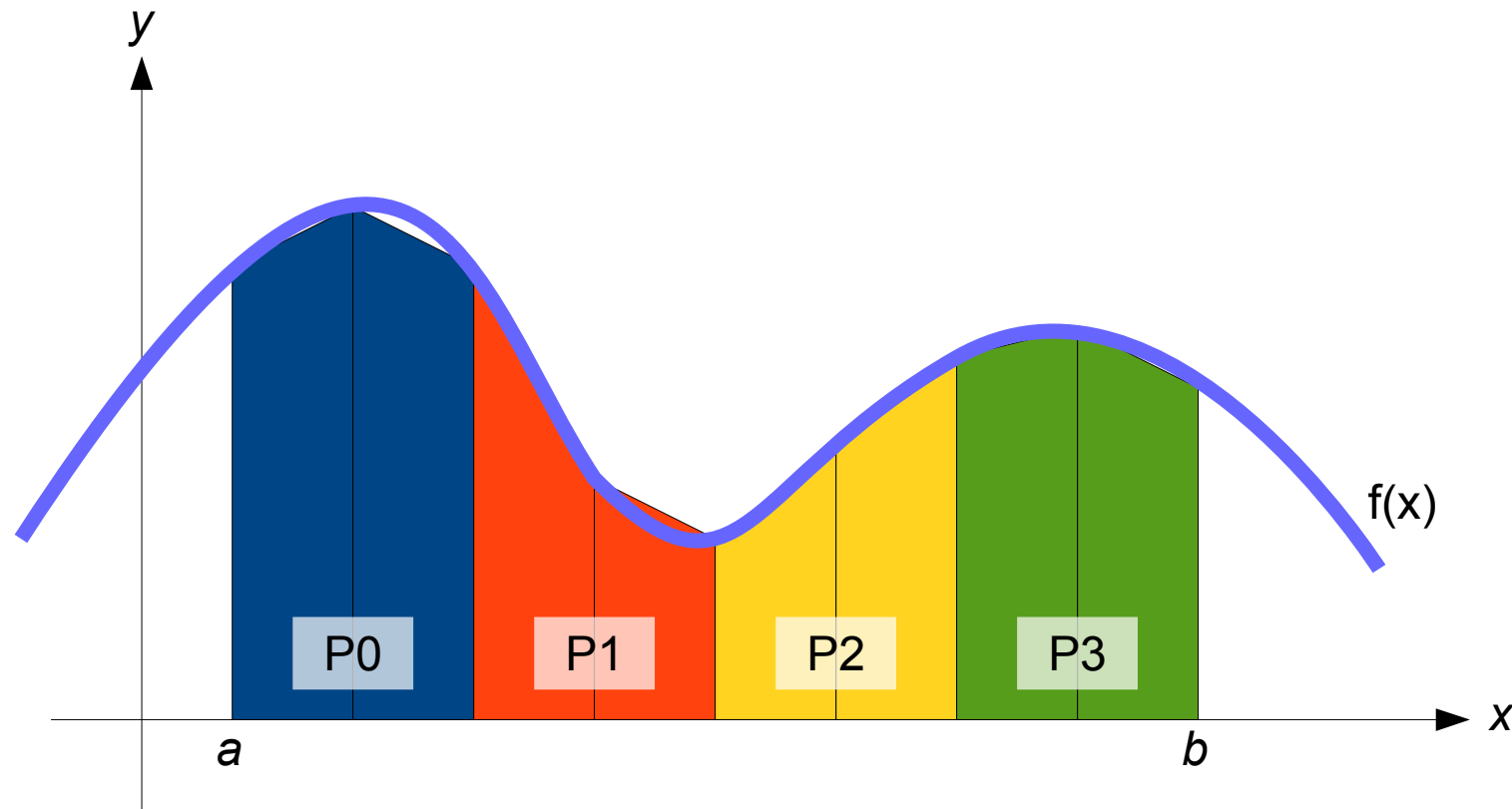
The trapezoid rule



```
/* Serial trapezoid rule */  
h = (b-a)/n;  
result = 0;  
x = a;  
for (i=0; i<n; i++) {  
    result += h*(f(x) + f(x+h))/2;  
    x += h;  
}  
return result;
```

See trap.c

Assigning trapezoids to threads



A first OpenMP version

- Split the n intervals across OpenMP threads
- Thread t stores its result in `partial_result[t]`
- The master sums all partial results
- See [omp-trap0.c](#)
 - Try adding "default(none)" to the `omp parallel` clause

A second OpenMP version

- Split the n intervals across OpenMP threads
- Thread t ...
 - ...stores its result in a **local** variable `partial_result`
 - ...updates the global result
- **omp atomic**
 - Protects updates to a *shared variable*
 - Updates must be of the form "read-update-write", e.g., `var += x`
- **omp critical**
 - Protects access to a *critical section*, which may consist of arbitrary instructions
 - All threads will eventually execute the critical section; however, only one thread at a time can be inside the critical block
- **critical** protects code; **atomic** protects memory locations
- See `omp-trap1.c`

The **atomic** directive


- The **omp atomic** directive ensures that only one thread at the time updates a shared variable

```
#pragma omp parallel
{
    double partial_result = trap(a, b, n);
    #pragma omp atomic
    result += partial_result;
}
```

- The code above forces all threads to serialize during the update of the shared variable
- We can also use the **reduction** clause

The reduction clause

- `reduction(<op> : <variable>)`



can be one of +, *, min, max, ^, &, |, &&, || (in principle also subtraction, but the OpenMP specification does not guarantee the result to be uniquely determined)

```
#pragma omp parallel reduction(+:result)
{
    double partial_result = trap(a, b, n);
    result += partial_result;
}
```

See `omp-trap2.c`

Reduction operators

- A **reduction operator** is a **binary associative** operator such as addition or multiplication
 - An operator \diamond is associative if $(a \diamond b) \diamond c = a \diamond (b \diamond c)$
- A **reduction** is a computation that repeatedly applies the same reduction operator to a sequence of operands to get a single result
 - \diamond -reduce(x_0, x_1, \dots, x_{n-1}) = $x_0 \diamond x_1 \diamond \dots \diamond x_{n-1}$

How the **reduction** clause works

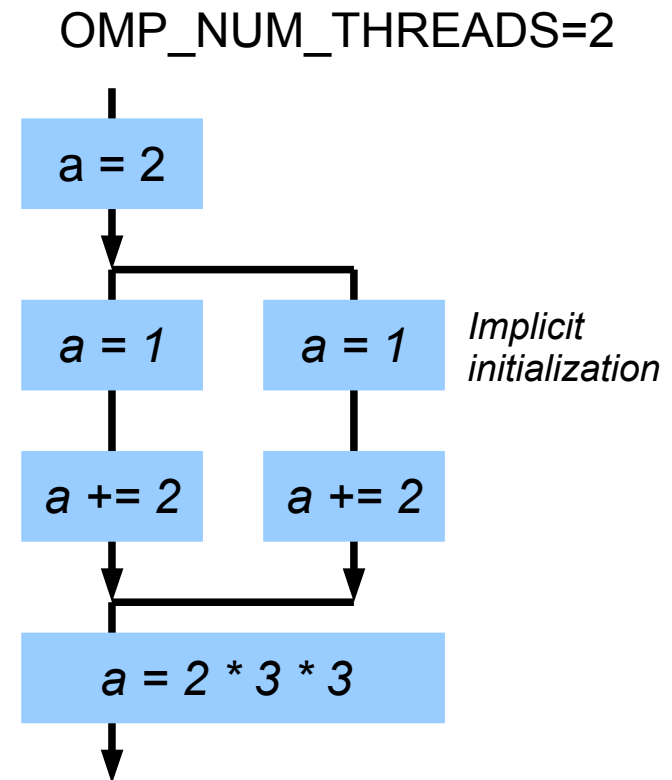
- One **private** copy of the reduction variable is created for each thread
- Each private copy is initialized with the neutral element of the reduction operator (e.g., 1 for *****, 0 for **+**)
- Each thread executes the parallel region
- When all threads finish, the reduction operator is applied to the *last* value of each local reduction variable, *and* the value the reduction variable had *before* the parallel region

```
/* omp-reduction.c */
#include <stdio.h>
int main( void )
{
    int a = 2;
    #pragma omp parallel reduction(*:a)
    {
        a += 2;
    }
    printf("%d\n", a);
    return 0;
}
```

```
$ OMP_NUM_THREADS=1 ./omp-reduction
6
$ OMP_NUM_THREADS=2 ./omp-reduction
18
$ OMP_NUM_THREADS=4 ./omp-reduction
162
```

How the **reduction** clause works

```
/* omp-reduction.c */
#include <stdio.h>
int main( void )
{
    int a = 2;
    #pragma omp parallel reduction(*:a)
    {
        /* implicit initialization a = 1 */
        a += 2;
    }
    printf("%d\n", a);
    return 0;
}
```



Some valid reduction operators

Operator	Initial value	
+	0	- is treated as + according th the OpenMP specs
-	0	
*	1	
min	largest positive number	OpenMP 3.1 and later
max	most negative number	
&	~0	
	0	
^	0	
&&	0	
	1	

The **omp for** directive

- The **omp for** directive is used inside a parallel block
- Loop iterations are assigned to the threads of the current team (the ones created with **omp parallel**)

```
#pragma omp parallel
{
  #pragma omp for
  for ( i=0; i<n; i++ ) {
    do_work(i);
  }
}
```

*The loop variable
(in this case, "i") is
private by default*

Thread 0	Thread 1	Thread 2
do_work(0)	do_work(4)	do_work(8)
do_work(1)	do_work(5)	do_work(9)
do_work(2)	do_work(6)	do_work(10)
do_work(3)	do_work(7)	do_work(11)

The **parallel for** directive

- The **parallel** and **for** directives can be collapsed in a single **parallel for**

```
double trap( double a, double b, int n )
{
    double result = 0;
    const double h = (b-a)/n;
    int i;
    #pragma omp parallel for reduction(+:result)
    for ( i = 0; i<n-1; i++ ) {
        result += h*(f(a+i*h) + f(a+(i+1)*h))/2;
    }
    return result;
}
```

See [omp-trap3.c](#)

Legal forms for parallelizable *for* statements

```
for [
    index = start ;
    index < end
    index <= end
    index > end
    index >= end
    index++
    ++index
    index--
    --index
    index += incr
    index -= incr
    index = index + incr
    index = incr + index
    index = index - incr
]
```

- Variable `index` must have integer or pointer type (e.g., it can't be a float)
- The expressions `start`, `end`, and `incr` must have a compatible type. For example, if `index` is a pointer, `incr` must have integer type
- The expressions `start`, `end`, and `incr` must not change during execution of the loop
- Variable `index` can only be modified by the “increment expression” in the “**for**” statement

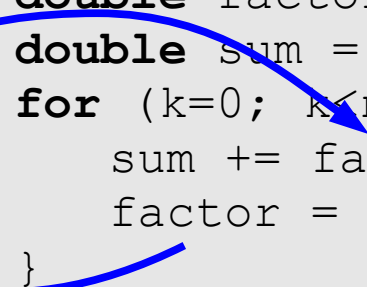
Data dependencies

- It is not possible to use a **parallel for** directive if data dependencies are present
- Example: computation of PI

$$\pi = 4 \left\{ 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots \right\} = 4 \sum_{k=0}^{+\infty} \frac{(-1)^k}{2k+1}$$

*Loop Carried
Dependency*

```
double factor = 1.0;
double sum = 0.0;
for (k=0; k<n; k++) {
    sum += factor/(2*k + 1);
    factor = -factor;
}
pi_approx = 4.0 * sum;
```



Removing the data dependency

```
double factor;  
double sum = 0.0;  
#pragma omp parallel for private(factor) reduction(+:sum)  
for (k=0; k<n; k++) {  
    if ( k % 2 == 0 ) {  
        factor = 1.0;  
    } else {  
        factor = -1.0;  
    }  
    sum += factor/(2*k + 1);  
}  
pi_approx = 4.0 * sum;
```

*factor must have
private scope*

Can my loop be parallelized?

- A quick-and-dirty test: run the loop *backwards*
 - If the program is still correct, the loop *might* be parallelizable
 - Not 100% reliable, but works most of the time

```
for (i=0; i<n; i++) {  
    /* loop body */  
}
```



```
for (i=n-1; i>=0; i--) {  
    /* loop body */  
}
```

- A better solution: *dependence analysis*
 - Outside the scope of this module
 - See Pacheco section 5.5 if you want to probe further

Scheduling loops

```
/* omp-mandelbrot.c */

...

int main( int argc, char *argv[] )
{
    int x, y;

    gfx_open( xsize, ysize, "Mandelbrot Set");
    #pragma omp parallel for private(x) schedule(dynamic,64)
    for ( y = 0; y < ysize; y++ ) {
        for ( x = 0; x < xsize; x++ ) {
            drawpixel( x, y );
        }
    }
    printf("Click to finish\n");
    gfx_wait();
    return 0;
}
```

`schedule (type, chunksize)`

- `type` can be:
 - `static`: the iterations can be assigned to the threads before the loop is executed. If `chunksize` is not specified, iterations are evenly divided contiguously among threads
 - `dynamic`: iterations are assigned to threads while the loop is executing. Default `chunksize` is 1
 - `auto`: the compiler and/or the run-time system determines the schedule
 - `runtime`: the schedule is determined at run-time using the `OMP_SCHEDULE` environment variable (e.g., `export OMP_SCHEDULE="static,1"`)
- Default schedule type is implementation dependent
 - GCC seems to use `static` by default

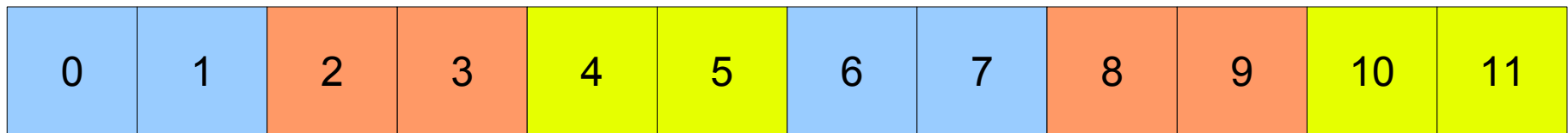
Example

Thread 0
Thread 1
Thread 2

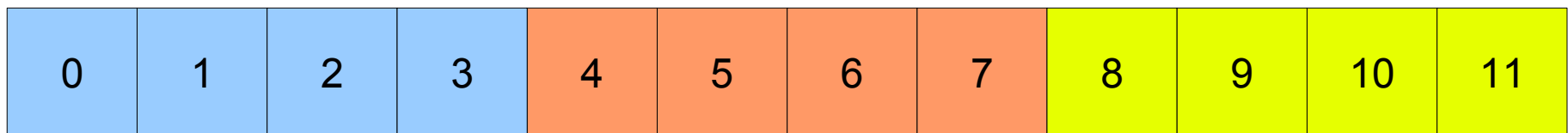
- Twelve iterations 0, 1, ... 11 and three threads
- `schedule(static, 1)`



- `schedule(static, 2)`



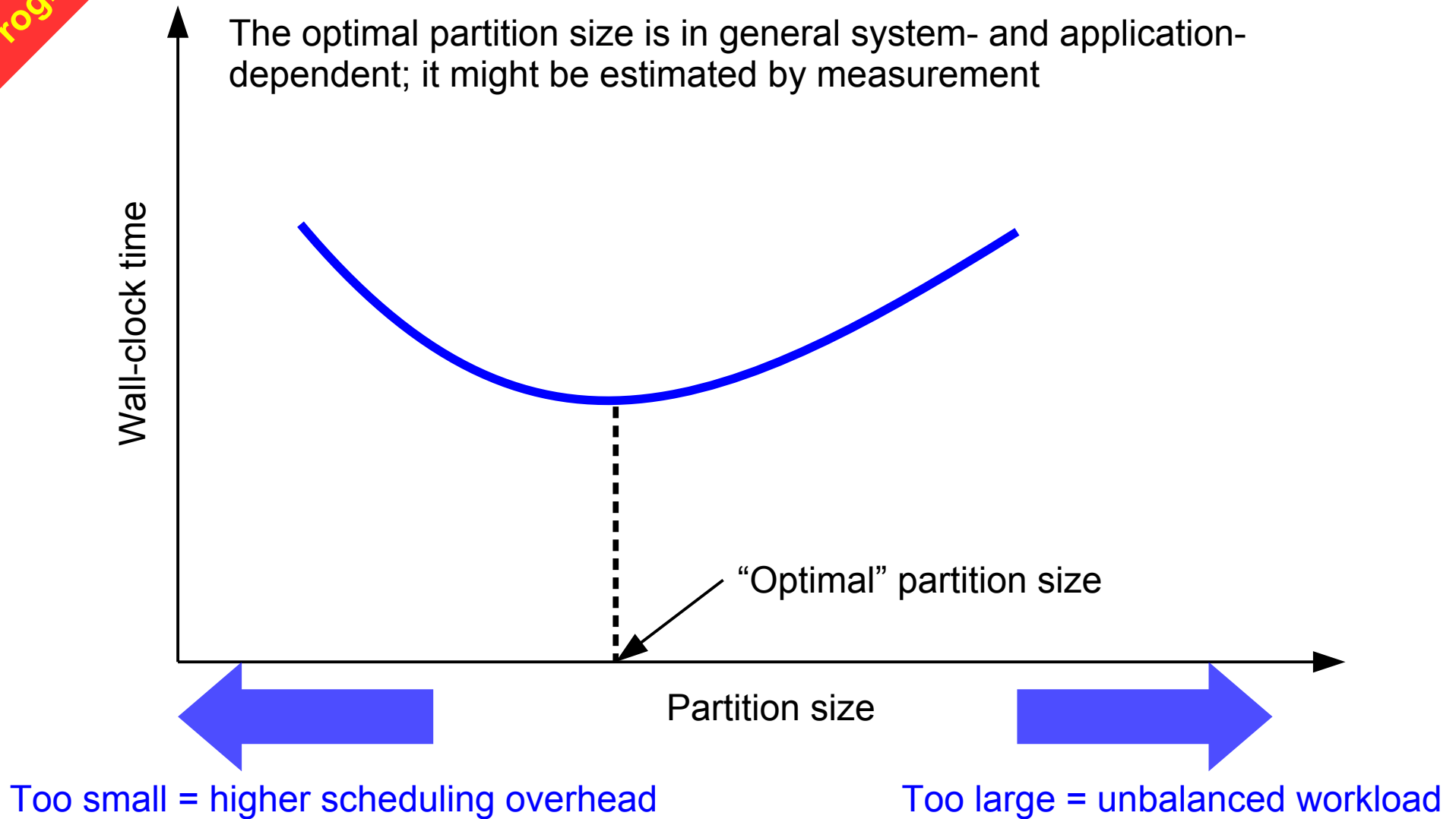
- `schedule(static, 4)` ← Default chunksize in this case



Choosing a schedule clause

Schedule clause	When to use	Note
<code>static</code>	Pre-determined and predictable work per iteration	Least work at runtime: scheduling done at compile-time
<code>dynamic</code>	Unpredictable, highly variable work per iteration	Most work at runtime: complex scheduling logic used at run-time

Choosing a block size



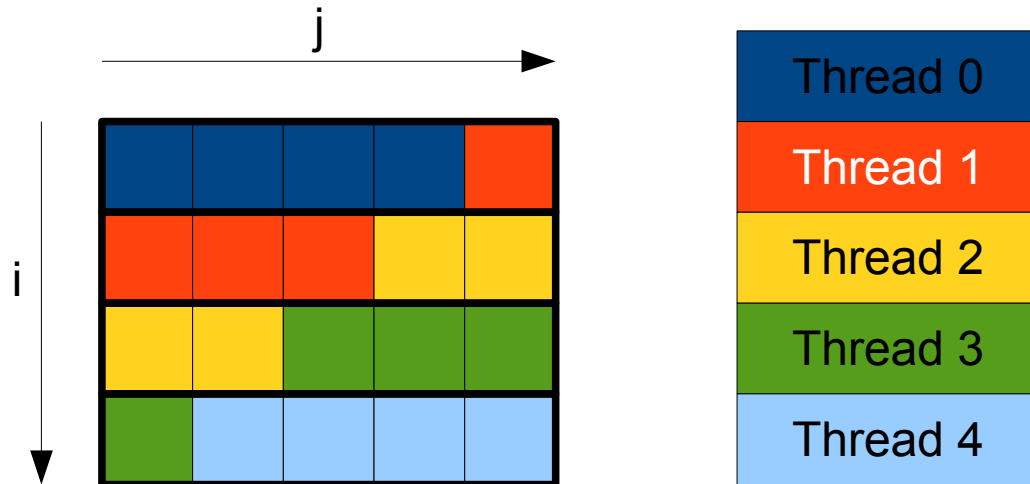
The collapse directive

- Specifies how many loops in a nested loop should be collapsed into one large iteration space and divided according to the schedule clause

```
#pragma omp parallel for collapse(2)
  for ( y = 0; y < ysize; y++ ) {
    for ( x = 0; x < xsize; x++ ) {
      drawpixel( x, y );
    }
  }
```

*collapse(2) makes
x and y private by
default*

How collapse works



```
#pragma omp parallel for num_threads(5) collapse(2)
for (i=0; i<4; i++) {
    for (j=0; j<5; j++) {
        do_work(i,j);
    }
}
```

See [omp-mandelbrot.c](#)

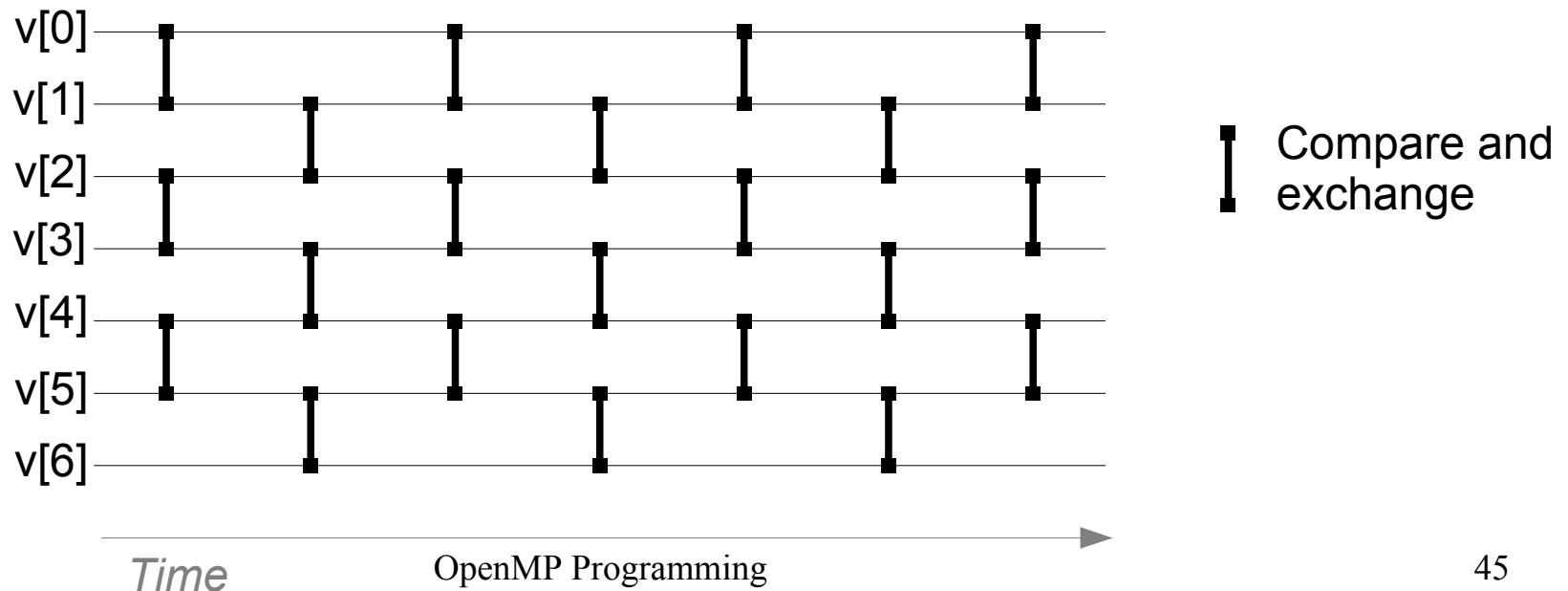
Spot the bug

```
int i, j;  
...  
#pragma omp parallel for private(temp)  
for (i=0; i<n; i++){  
    for (j=0; j<m; j++){  
        temp = b[i]*c[j];  
        a[i][j] = temp * temp + d[i];  
    }  
}
```

Example: Odd-Even Transposition Sort

Serial Odd-Even Transposition Sort

- Variant of bubble sort
- Compare all (even, odd) pairs of adjacent elements, and exchange them if in the wrong order
- Then compare all (odd, even) pairs, exchanging if necessary; repeat the step above



Serial Odd-Even Transposition Sort

- Variant of bubble sort
- Compare all (even, odd) pairs of adjacent elements, and exchange them if in the wrong order
- Then compare all (odd, even) pairs, exchanging if necessary; repeat the step above

```
for (phase = 0; phase < n; phase++) {  
    if ( phase % 2 == 0 ) {  
        for (i=0; i<n-1; i+=2) {  
            if (v[i] > v[i+1]) swap( &v[i], &v[i+1] );  
        }  
    } else {  
        for (i=1; i<n-1; i+=2) {  
            if (v[i] > v[i+1]) swap( &v[i], &v[i+1] );  
        }  
    }  
}
```

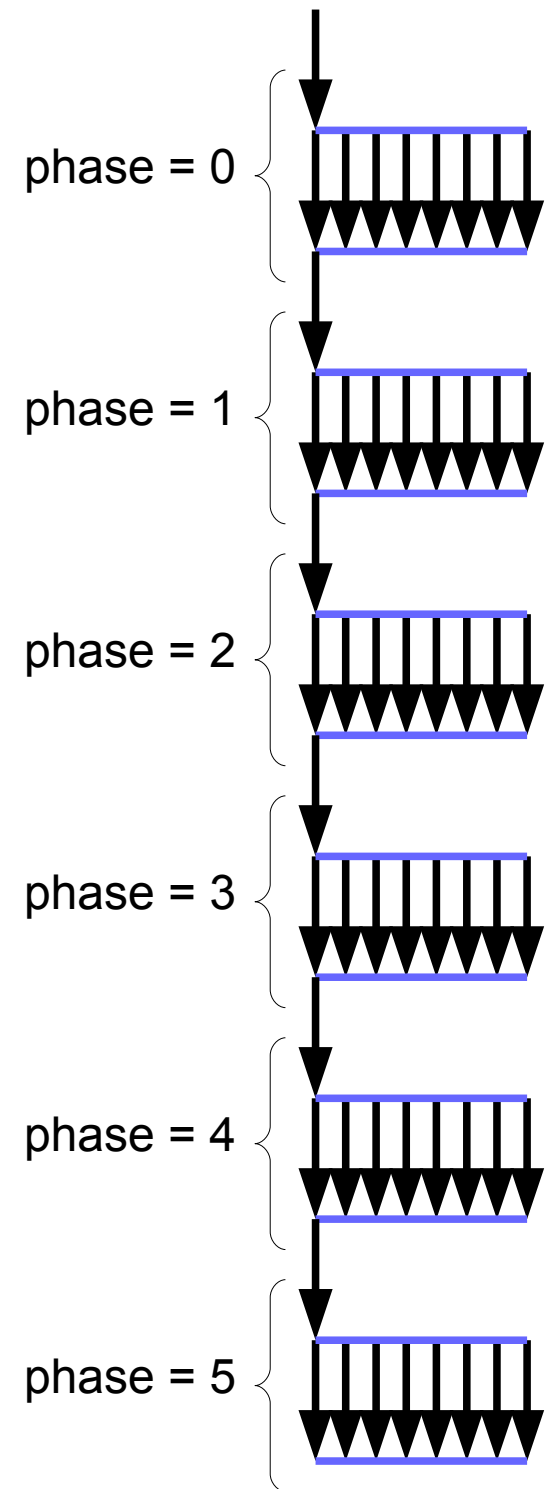
OpenMP Odd-Even Sort

```
for (phase = 0; phase < n; phase++) {  
    if ( phase % 2 == 0 ) {  
#pragma omp parallel for default(none) shared(v,n)  
        for (i=0; i<n-1; i+=2) {  
            if (v[i] > v[i+1]) swap( &v[i], &v[i+1] );  
        }  
    } else {  
#pragma omp parallel for default(none) shared(v,n)  
        for (i=1; i<n-1; i+=2) {  
            if (v[i] > v[i+1]) swap( &v[i], &v[i+1] );  
        }  
    }  
}
```

OpenMP Odd-Even S

```
for (phase = 0; phase < n; phase++) {  
    if ( phase % 2 == 0 ) {  
#pragma omp parallel for default(none) shared(  
        for (i=0; i<n-1; i+=2) {  
            if (v[i] > v[i+1]) swap( &v[i], &v[i+1])  
        }  
    } else {  
#pragma omp parallel for default(none) shared(  
        for (i=1; i<n-1; i+=2) {  
            if (v[i] > v[i+1]) swap( &v[i], &v[i+1])  
        }  
    }  
}
```

OpenMP Programming



Work-sharing constructs

OpenMP synchronization

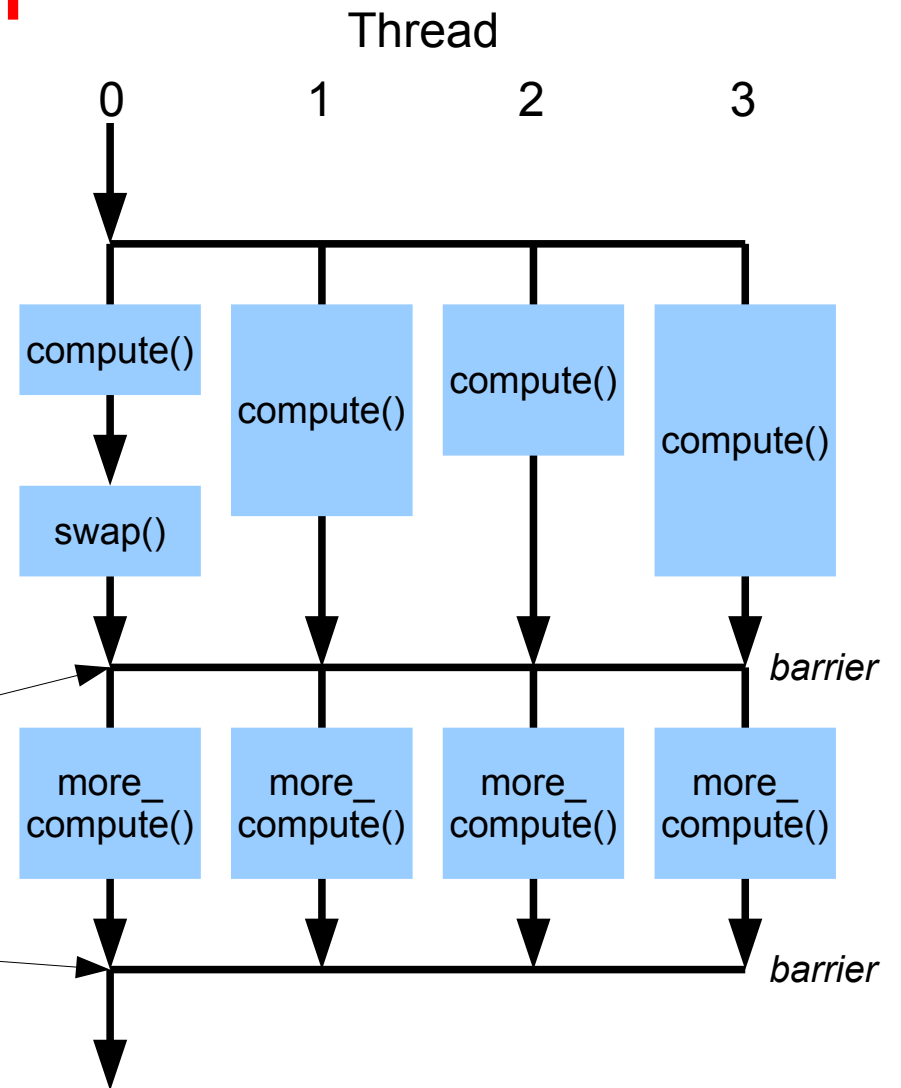
- **#pragma omp barrier**
 - All threads in the currently active team must reach this point before they are allowed to proceed
- **#pragma omp master**
 - Marks a parallel region which is executed by the master only (the thread with rank = 0); other threads just skip the region
 - There is **no implicit barrier** at the end of the block
- **#pragma omp single**
 - Marks a parallel region which is executed once by the **first thread reaching it**, whichever it is
 - **A barrier is implied** at the end of the block

Example

```
#pragma omp parallel
{
    compute();

    #pragma omp master
    swap();

    #pragma omp barrier
    more_compute();
}
```



OpenMP tasking constructs

- Not all programs have simple loops that OpenMP can parallelize
- Example: linked list traversal
 - Each node of the linked list is "processed" independently from other nodes

```
p = head;
while (p) {
    processwork(p);
    p = p->next;
}
```

- OpenMP **parallel for** works only for loops where the iteration count can be known in advance at runtime

What are OpenMP tasks?

- Tasks are independent units of work
- Tasks are composed of:
 - code to execute
 - data to compute with
- Tasks are assigned to threads for execution
 - The task assigned to a thread can be executed immediately (if the thread is not already busy) ..
 - .. or the thread may defer the execution of the task
- Tasks can be nested: a task may generate other tasks

#pragma omp task

```
#pragma omp parallel
{
    #pragma omp master
    {
        #pragma omp task
        fred();
        #pragma omp task
        barney();
        #pragma omp task
        wilma();
    }
}
```

Create a pool of threads

Only one thread (the master, in this example) forks tasks

Tasks executed by some threads in some order

All tasks complete before this barrier is released

Data scoping with tasks

- Variables can be **shared**, **private** or **firstprivate** with respect to task
 - If a variable is **shared** on a task construct, the references to it inside the construct are to the storage with that name at the point where the task was encountered
 - If a variable is **private** on a task construct, the references to it inside the construct are to new uninitialized storage that is created when the task is executed
 - If a variable is **firstprivate** on a construct, the references to it inside the construct are to new storage that is created and initialized with the value of the existing storage of that name when the task is encountered

Data scoping with tasks

- The behavior you want for tasks is usually **firstprivate**, because the task may not be executed until later (and variables may have gone out of scope)
 - Variables that are **private** when the task construct is encountered are **firstprivate** by default

```
#pragma omp parallel shared(A)
{
    int B;
    #pragma omp task
    {
        int C;
        compute(A, B, C);
    }
}
```

B is local to the current task, and hence considered private

*A is shared
B is firstprivate
C is private*

Linked list traversal with tasks

```
struct list *p, *list;
...
#pragma omp parallel
{
    #pragma omp single
    {
        p = head;
        while (p) {
            #pragma omp task firstprivate(p)
            processwork(p);
            p = p->next;
        }
    }
}
```

Creates a task with its own copy of "p" initialized to the value of "p" when the task is defined

When/Where are tasks completed?

- At thread barriers (explicit or implicit)
 - e.g., at the end of a `#pragma omp parallel` block
 - applies to all tasks generated in the current parallel region up to the barrier
- At `#pragma omp taskwait` directive
 - wait until all tasks defined `in the current task` (not in the descendants!) have completed

Example

```
#pragma omp parallel
{
    #pragma omp master
    {
        #pragma omp task
        fred();
        #pragma omp task
        barney();
        #pragma omp taskwait
        #pragma omp task
        wilma();
    }
}
```

*fred() and barney()
must complete before
wilma() starts*

Example: parallel Fibonacci with tasks

```
#include <stdio.h>
int fib( int n )
{
    int n1, n2;
    if (n < 2) {
        return 1;
    } else {
        n1 = fib(n-1);
        n2 = fib(n-2);
        return n1 + n2;
    }
}

int main( int argc, char* argv[] )
{
    int n = 10, res;
    res = fib(n);
    printf("fib(%d)=%d\n", n, res);
    return 0;
}
```

- $F_n = F_{n-1} + F_{n-2}$
– $F_0 = F_1 = 1$
- Inefficient algorithm
 $O(2^n)$

Example: parallel Fibonacci with tasks

```
#include <stdio.h>
int fib( int n )
{
    int n1, n2;
    if (n < 2) {
        return 1;
    } else {
#pragma omp task shared(n1)
        n1 = fib(n-1);
#pragma omp task shared(n2)
        n2 = fib(n-2);
#pragma omp taskwait
        return n1 + n2;
    }
}

int main( int argc, char* argv[] )
{
    int n = 10, res;
#pragma omp parallel
#pragma omp master
    res = fib(n);
    printf("fib(%d)=%d\n", n, res);
    return 0;
}
```

- Binary tree of tasks
- A task cannot complete until all tasks below it in the tree are complete
 - enforced with **taskwait**
- **n1, n2** are local, and therefore **private** to current task
 - must be **shared** on child tasks so they don't create their own **firstprivate** copies

Concluding Remarks

- OpenMP is a standard for programming shared-memory systems.
 - Uses both **special functions** and **preprocessor directives** called *pragmas*.
- OpenMP programs start multiple threads
 - By default most systems use a **block-partitioning** of the iterations in a parallelized for loop
 - OpenMP offers a variety of **scheduling options**.
- In OpenMP the **scope** of a variable is the collection of threads to which the variable is accessible.
- A **reduction** is a computation that repeatedly applies the same reduction operator to a sequence of operands in order to get a single result.

References

- A good tutorial on OpenMP is available at:
<https://hpc.llnl.gov/tuts/openMP/>