## 11.9.3.17

## EE23BTECH11017 - Eachempati Mihir Divyansh\*

**Question:** If the  $4^{th}$ ,  $10^{th}$  and  $16^{th}$  terms of a G.P. are x, y, and z, respectively. Prove that x, y, zare in G.P.

## **Solution:**

The  $n^{th}$  term of a G.P. is  $a_n = a_1 r^{n-1}$ . Given that x, y, z are the  $4^{th}$ ,  $10^{th}$  and  $16^{th}$  terms of a G.P.,

$$x = a_4 = ar^{4-1} = ar^3$$
  
 $y = a_{10} = ar^{10-1} = ar^9$   
 $z = a_{16} = ar^{16-1} = ar^{15}$ 

Consider  $\frac{y}{x}$  and  $\frac{z}{y}$ ;

$$\frac{y}{x} = \frac{ar^9}{ar^3} \tag{1}$$

$$\frac{y}{x} = r^6 \tag{2}$$

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$$\frac{z}{y} = \frac{ar^{15}}{ar^9} \tag{3}$$

$$\frac{y}{x} = r^6 \tag{4}$$

Since,  $\frac{y}{x} = \frac{z}{y}$ ;

x, y, z are in G.P.

For this G.P, with  $x = ar^3$ ,  $y = ar^9$ ,  $z = ar^{15}$ , the general term x(n) can be defined as:

$$x(n) = x \cdot (\frac{y}{x})^{n-1} \tag{5}$$

$$x(n) = x \cdot \left(\frac{y}{x}\right)^{n-1}$$

$$also, \ x(n) = x \cdot \left(\frac{z}{y}\right)^{n-1}$$

$$(5)$$

$$\therefore x(n) = \frac{y^{n-1}}{x^{n-2}} \tag{7}$$