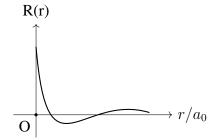
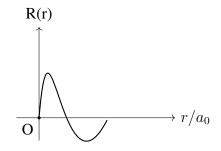
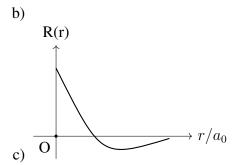
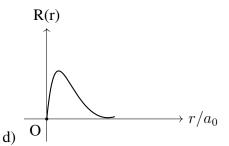
- 1) The eigenvalues of a Hermitian matrix are all
  - a) real
  - b) imaginary
  - c) of modulus one
  - d) real and positive
- 2) Which one of the following represents the 3pradial wave function of the hydrogen atom?  $(a_0 \text{ is the Bohr radius})$



a)







3) Given the following table,

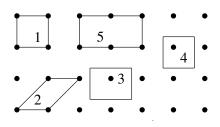
Group I	Group II
P: Stern-Gerlach exper-	1: Wave nature of particles
iment	
Q: Zeeman effect	2: Quantization of energy of electrons
	in the atoms
R: Frank-Hertz experi-	3: Existence of electron spin
ment	
S: Davisson-Germer	4: Space quantization of angular mo-
experiment	mentum

Which one of the following correctly matches the experiments from Group I to their inferences in Group II?

- a) P-2, Q-3, R-4, S-1
- b) P-1, Q-3, R-2, S-4
- c) P-3, Q-4, R-2, S-1
- d) P-2, Q-1, R-4, S-3
- 4) In spherical polar coordinates  $(r, \theta, \phi)$ , the unit vector  $\hat{\theta}$  at  $(10, \frac{\pi}{4}, \frac{\pi}{2})$  is

  - b)  $\frac{1}{\sqrt{2}} \left( \hat{j} + \hat{k} \right)$
  - c)  $\frac{1}{\sqrt{2}} \left( -\hat{j} + \hat{k} \right)$
  - d)  $\frac{1}{\sqrt{2}} \left( \hat{j} \hat{k} \right)$
- 5) The scale factors corresponding to the covariant metric tensor g in spherical polar coordinates are
  - a)  $1, r^2, r^2 \sin^2 \theta$
  - b)  $1, r^2, \sin^2 \theta$
  - c) 1, 1, 1
  - d)  $1, r, r \sin \theta$
- 6) In the context of small oscillations, which one of the following does NOT apply to the normal coordinates?

- a) Each normal coordinate has an eigenfrequency associated with it
- b) The normal coordinates are orthogonal to one another
- c) The normal coordinates are all independent
- d) The potential energy of the system is a sum of squares of the normal coordinates with constant coefficients
- 7) For the given unit cells of a two-dimensional square lattice, which option lists all the primitive cells?

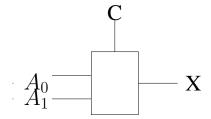


- a) 1 and 2
- b) 1,2 and 3
- c) 1,2,3 and 4
- d) 1,2,3,4 and 5
- 8) Among electric field (E), magnetic field (B), angular momentum (L), and vector potential (A), which is/are odd under parity (space inversion) operation?
  - a) E only
  - b) E & A only
  - c) E & B only
  - d) B & L only
- 9) The expression for the second overtone frequency in the vibrational absorption spectra of a diatomic molecule in terms of the harmonic frequency  $\omega$  and anharmonicity constant  $x_e$ , is
  - a)  $2\omega_e (1 x_e)$
  - b)  $2\omega_e (1 3x_e)$
  - c)  $3\omega_e (1 2x_e)$
  - d)  $3\omega_e (1 4x_e)$
- 10) Match the physical effects and order of magnitude of their energy scales given below, where  $\alpha = \frac{e^2}{4\pi\epsilon_o \hbar c}$  is the fine structure constant,  $m_e$  and  $m_p$  are the electron and proton masses, respectively.

Group I	Group II
P: Lamb shift	$1 :\sim 0 \left(\alpha^2 m_e c^2\right)$
Q: Fine structure	$2 :\sim 0 \left(\alpha^4 m_e c^2\right)$
R: Bohr energy	$3:\sim 0\left(\frac{\alpha^4m_e^2c^2}{m_p}\right)$
S: Hyperfine structure	$4 :\sim 0 \left(\alpha^5 m_p c^2\right)$

- a) P-3, Q-1, R-2, S-4
- b) P-2, Q-3, R-1, S-4
- c) P-4, Q-2, R-1, S-3
- d) P-2, Q-4, R-1, S-3
- 11) The logic expression  $\bar{A}BC + \bar{A}\bar{B}C + AB\bar{C} + A\bar{B}\bar{C}$  can be simplified to
  - a) AXORC
  - b) AANDC
  - c) 0
  - d) 1
- 12) At low temperatures (T), the specific heat of common metals is described by  $(\text{with}\alpha\text{and}\beta\text{as constants})$ 
  - a)  $\alpha T + \beta T^3$
  - b)  $\beta T^3$
  - c)  $\exp\left(-\frac{\alpha}{T}\right)$
  - d)  $\alpha T + \beta T^5$
- 13) In a 2-to-1 multiplexer as shown below, the output  $X=A_0$  if C=0 and  $X=A_1$  if C=1.

Which one of the following is the correct



implementation of this multiplexer?

