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- 53) Let u^μ denote the 4-velocity of a relativistic particle whose square $u^\mu u_\mu = 1$. If $\epsilon_{\mu\nu\rho\sigma}$ is the Levi-Civita tensor then the value of $\epsilon_{\mu\nu\rho\sigma} u^\mu u^\nu u^\rho u^\sigma$ is _____.
- 54) Consider a simple cubic monoatomic Bravais lattice which has a basis with vectors $\vec{r}_1 = 0, \vec{r}_2 = \frac{a}{4}(\hat{x} + \hat{y} + \hat{z})$, a is the lattice parameter. The Bragg reflection is observed due to the change in the wave vector between the incident and the scattered beam is given by $\vec{K} = n_1 \vec{G}_1 + n_2 \vec{G}_2 + n_3 \vec{G}_3$, where \vec{G}_1, \vec{G}_2 and \vec{G}_3 are primitive reciprocal lattice vectors. For $n_1 = 3, n_2 = 3$ and $n_3 = 2$, the geometrical structure factor is _____.
- 55) A plane electromagnetic wave of wavelength λ is incident on a circular loop of conducting wire. The loop radius is a ($a \ll \lambda$). The angle (in degrees), made by the Poynting vector with the normal to the plane of the loop to generate a maximum induced electrical signal, is _____.
- 56) An electron in a hydrogen atom is in the state $n = 3, l = 2, m = -2$. Let \hat{L}_y denote the y-component of the orbital angular momentum operator. If $(\Delta \hat{L}_y)^2 = \alpha \hbar^2$, the value of α is _____.
- 57) A sinusoidal voltage of the form $v(t) = V_o \cos(\omega t)$ is applied across a parallel plate capacitor placed in vacuum. Ignoring the edge effects, the induced *emf* within the region between the capacitor plates can be expressed as a power series in ω . The lowest non-vanishing exponent in ω is _____.
- 58) If $\sum_{k=1}^{\infty} a_k \sin(kx)$, for $-\pi \leq x \leq \pi$, the value of a_2 is _____.
- 59) Let $f_n(x) = \begin{cases} 0, & \text{if } x < -\frac{1}{2n} \\ n, & \text{if } -\frac{1}{2n} < x < \frac{1}{2n} \\ 0, & \text{if } x > \frac{1}{2n} \end{cases}$
The value of $\lim_{n \rightarrow \infty} \int_{-\infty}^{\infty} f_n(x) \sin x dx$ is _____.
- 60) Consider the Hamiltonian $\hat{H} = \hat{H}_0 + \hat{H}'$ where
 $\hat{H}_0 = \begin{pmatrix} E & 0 & 0 \\ 0 & E & 0 \\ 0 & 0 & E \end{pmatrix}$ and \hat{H}' is the time independent perturbation given by
 $\hat{H}' = \begin{pmatrix} 0 & k & 0 \\ k & 0 & k \\ 0 & k & 0 \end{pmatrix}$, where $k > 0$. If, the maximum energy eigenvalue of \hat{H} is 3 eV corresponding to $E = 2 \text{ eV}$, the value of k (rounded off to three decimal places) in eV is _____.
- 61) A hydrogen atom is in orbital angular momentum $|l, m = l\rangle$. If \vec{L} lies on a cone which makes a half angle 30° with respect to z -axis, the value of l is _____.
- 62) In the center of mass frame, two protons having energy 7000 GeV , collide to produce protons and anti-protons. The maximum number of anti-protons produced is _____.
(Assume the proton mass to be $1 \frac{\text{GeV}}{c^2}$)
- 63) Consider a gas of hydrogen atoms in the atmosphere of the Sun where the temperature is 5800 K . If a sample from this atmosphere contains 6.023×10^{23} of hydrogen atoms in the ground state, the number of hydrogen atoms in the first excited state is approximately 8×10^n , where n is an integer. The value of n is _____.
(Boltzmann constant: $8.617 \times 10^{-5} \frac{\text{eV}}{\text{K}}$)

- 64) For a gas of non-interacting particles, the probability that a particle has a speed v in the interval v to $v + dv$ is given by

$$f(v) dv = 4\pi v^2 dv \left(\frac{m}{2\pi k_B T} \right)^{\frac{3}{2}} e^{-\frac{mv^2}{2k_B T}}$$

If E is the energy of a particle, then the maximum in the corresponding energy distributions in units of $\frac{E}{k_B T}$ occurs at _____ (rounded off to one decimal place).

- 65) The Planck's energy density distribution is given by $u(\omega) = \frac{\hbar \omega^3}{\pi^2 c^3 (e^{\frac{\hbar \omega}{k_B T}} - 1)}$. At long wavelengths, the energy density of photons in thermal equilibrium with a cavity at temperature T varies as T^α , where α is _____.