

# COMPUTING MIDCURVE BY NEURAL NETWORKS

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# Agenda

1 INTRODUCTION TO MIDCURVE

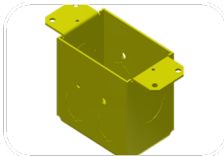
2 THE END

# MidcurveNN : Encoder-Decoder Neural Network for Computing Midcurve of a Thin Polygon

# Introduction



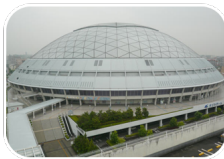
Aerospace



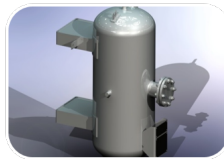
Machinery

Consumer  
Products

Energy

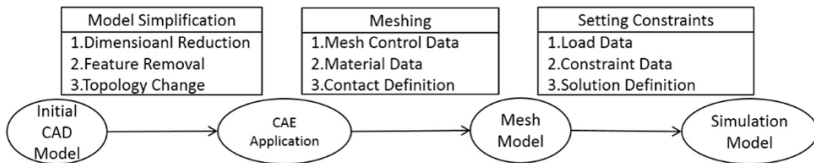


Construction

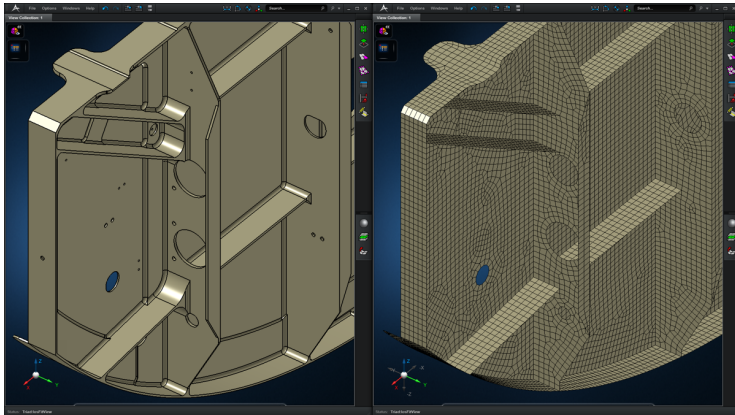
Industrial  
equipment

## Can we use shapes directly?

- ▶ CAD : Designing Shapes
- ▶ CAE : Engineering Analysis
- ▶ CAD→CAE: Simplification for quicker results.



## CAD-CAE



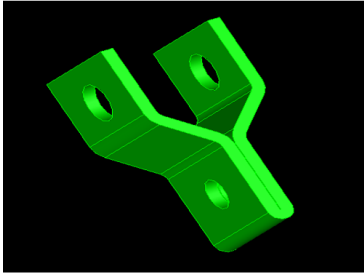
## For Shapes like Sheet Metal ...

|                           | Solid mesh       | Shell+Solid mesh | Difference (%) |
|---------------------------|------------------|------------------|----------------|
| Element number            | 344,330          | 143,063          | -58%           |
| Node Number               | 694,516          | 75,941           | -89%           |
| Total Degrees of freedom  | 2,083,548        | 455,646          | -78%           |
| Maximum Von. Mises Stress | <b>418.4 MPa</b> | <b>430 MPa</b>   | +3%            |
| Meshing + Solving time    | Out of memory    | 22 mins          | N/A (4G RAM)   |
| Meshing + Solving time    | <b>30 mins</b>   | <b>17 mins</b>   | -43% (12G RAM) |

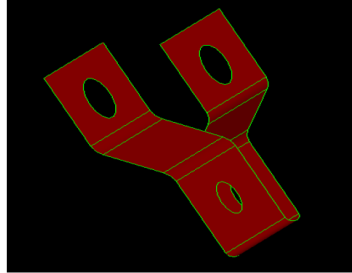
Half the computation time, but similar accuracy



# Midsurface is?



Input: Solid

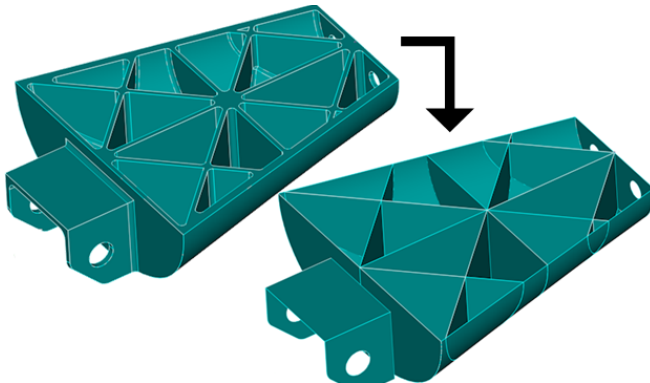


Output: Midsurface

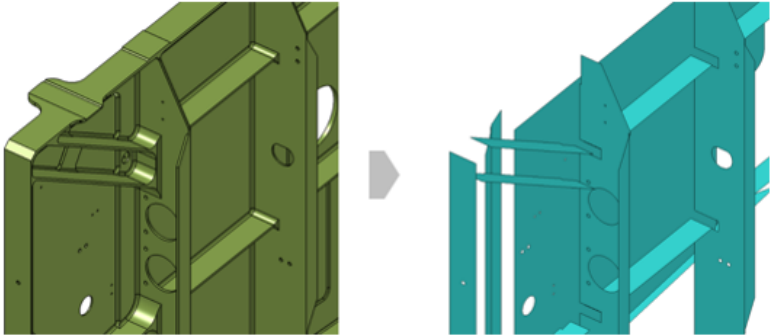
- ▶ Widely used for CAE of Thin-Walled parts
- ▶ Computation is challenging and still unsolved

## Getting Midsurface

- ▶ Going on for decades ...
- ▶ Manually by offsetting and stitching, initially
- ▶ Many CAD-CAE packages give automatic option, but ...



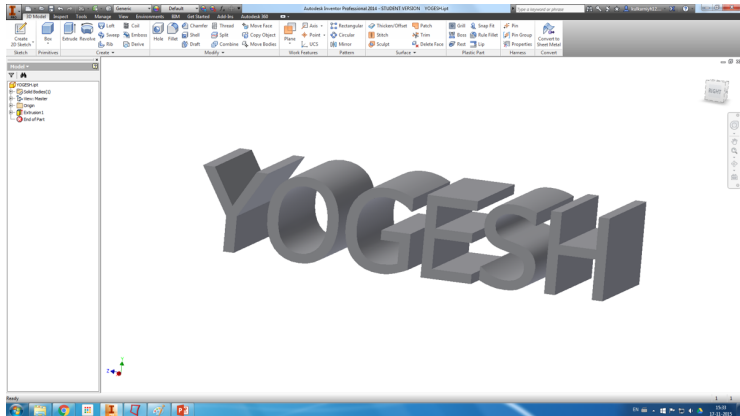
## Look at the output



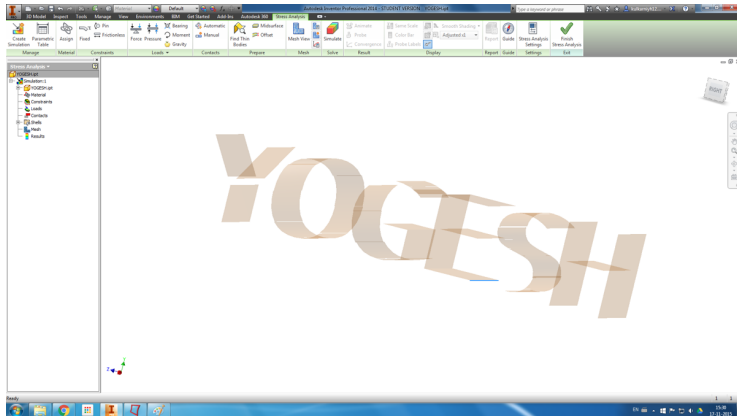
## Can't tolerate gaps

- ▶ We have thickness sampling,
- ▶ To recreate-represent the original shape
- ▶ Input and output difference not desirable

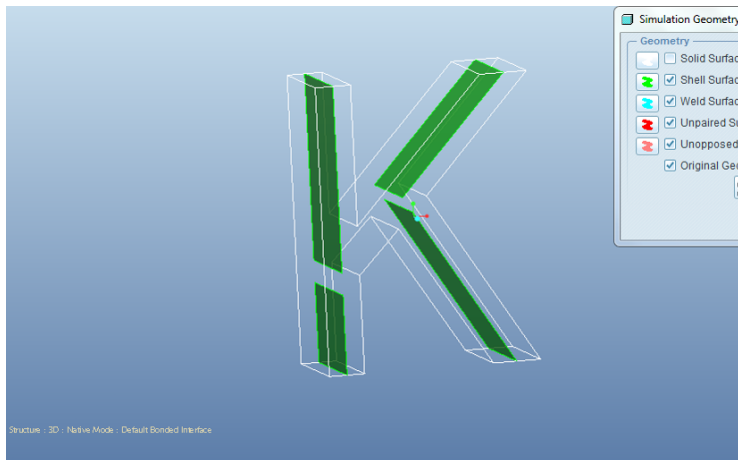
For a simple model like



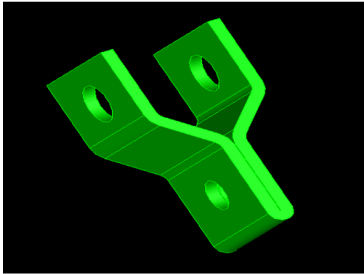
You get



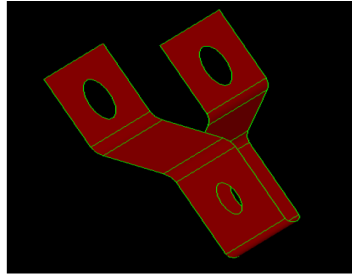
# For a far simpler shape



## Current Quality



Input: Solid



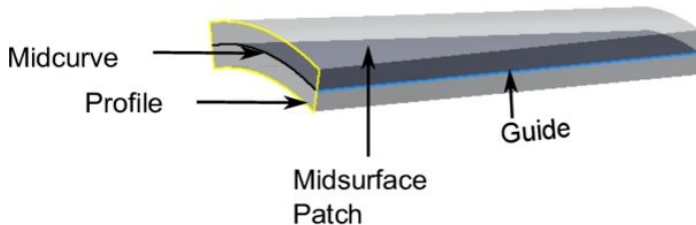
Output: Midsurface

- ▶ Errors take weeks to correct for complex parts.
- ▶ But still preferred, due to vast savings time
- ▶ From Days to hours ...



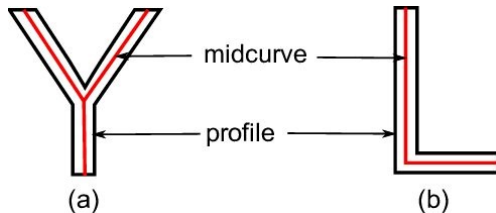
## Midsurface Computation

- Midsurface of a Patch is Midcurve of its profile extruded.
- So, it boils down to computing 1D midcurve of a 2D profile



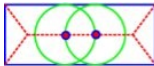
## What is a Midcurve?

- Midsurface : From 3D thin Solid to 2D Surface
- Midcurve : From 2D Profile to 1D Curve

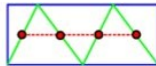


# Many Approaches

- ▶ More than 6 decades of research. . .
- ▶ Most CAD-CAE packages. . .
- ▶ Rule-based!! Heuristic!! Case-by-case basis!!



MAT



CAT

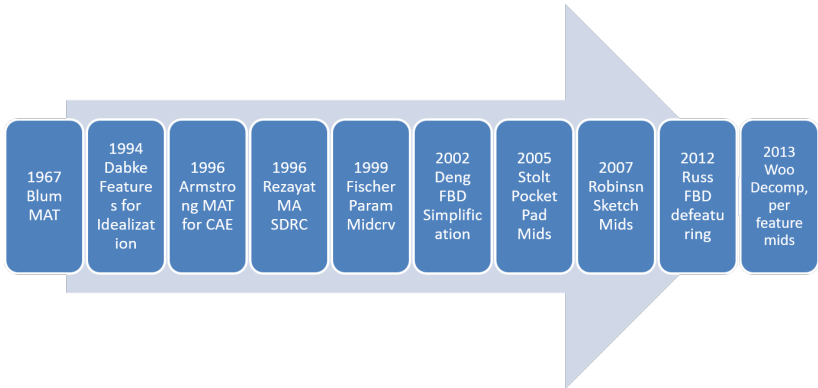


Thinning

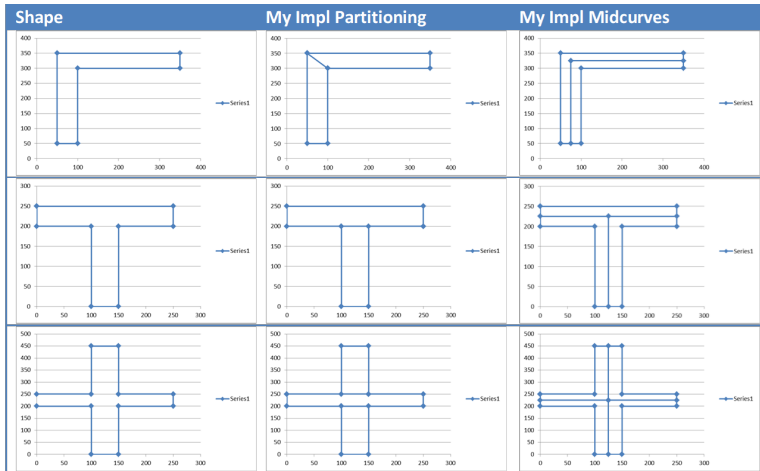


Pairs

# When-What?



## 2017: My PhD Work: Rule-based



## Limitations

- ▶ Fully rule-based
- ▶ Need to adjust for new shapes
- ▶ So, not scalable



## Idea



Can Neural Networks “learn” the dimension reduction transformation?

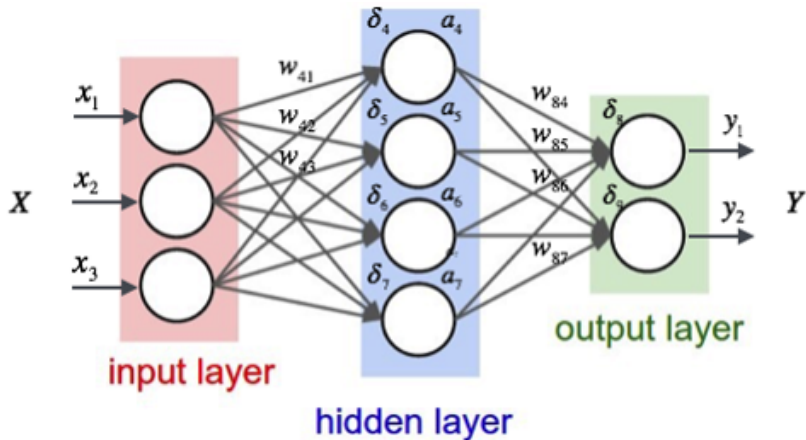
## How?

- ▶ Supply lots of training data of profiles and their corresponding midcurves and train.
- ▶ Then given an unseen profile, can Neural Network compute a midcurve, mimicking the original profile shape?





## Midcurve by Neural network

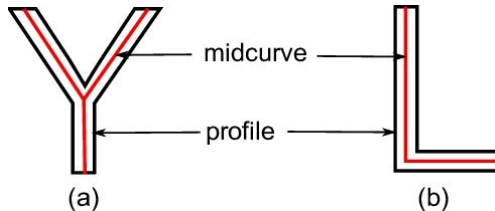


## Midcurve : The Problem

- ▶ **Goal:** Given a 2D closed shape (closed polygon) find its midcurve (polyline, closed or open)
- ▶ **Input:** set of points or set of connected lines, non-intersecting, simple, convex, closed polygon
- ▶ **Output:** another set of points or set of connected lines, open/branched polygons possible

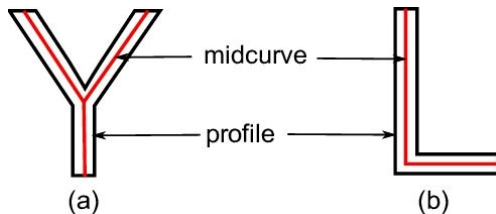
## Midcurve == Dimension Reduction

- ▶ Like PCA (Principal Component Analysis), wish to find Principal curve
- ▶ That 'represents' the original profile shape



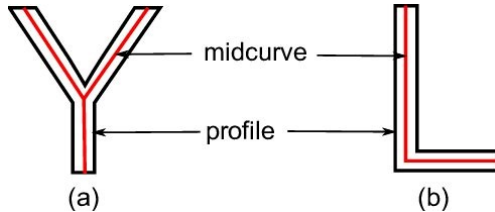
# Midcurve == Translation

- ▶ Left side (input): 2D Sketch Profile
- ▶ Right Side (output): 1D Midcurve
- ▶ Sequence 2 Sequence problem



## Midcurve ! = Auto-Encoder Decoder

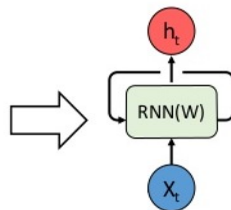
- ▶ Its not Auto-Encoder as Input and Output are different
- ▶ Its not fixed size i/o as Input and Output sizes are different



## Variable Size Encoder Decoder

- ▶ Batches need fixed lengths
- ▶ Made fixed size by Padding.

|          |         |          |          |        |         |
|----------|---------|----------|----------|--------|---------|
| Friendly | against | Scotland | at       | Murray | .       |
| Nadim    | Ladki   | <PAD>    | <PAD>    | <PAD>  | <PAD>   |
| AL-AIN   | United  | Arab     | Emirates | <PAD>  | <PAD>   |
| ROME     | 1996-12 | <PAD>    | <PAD>    | <PAD>  | <PAD>   |
| Two      | goals   | in       | the      | last   | minutes |



## Variable Size Encoder Decoder

- ▶ OK for NLP, say Machine Translations, where padding values like “-1” can be added along with other words (vectors or indices)
- ▶ But in Geometry, its not OK.
- ▶ Because any value can represent a Valid Input, even though we don't want it to be the input.

## A Twist to the problem

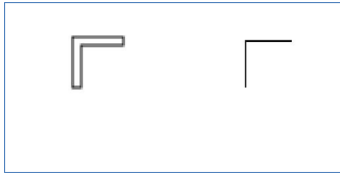


- ▶ Till we get good variable size encoder decoder network for geometry. . .
- ▶ Decided to convert this Sequence 2 Sequence problem as Image 2 Image problem.



## A Twist to the problem

- ▶ Input: Black & White Image of 2D profile
- ▶ Output: Black & White Image of 1D midcurve



# Solves ...

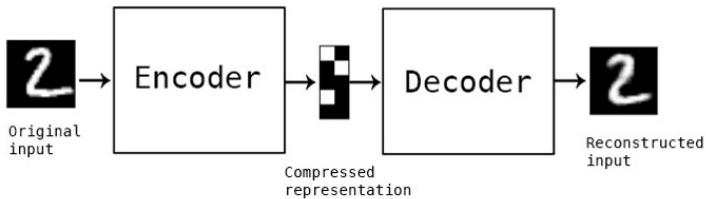
Problems of Geometric sequences

- ▶ Variable input/output sizes
- ▶ Loops need to be crossed
- ▶ Branches

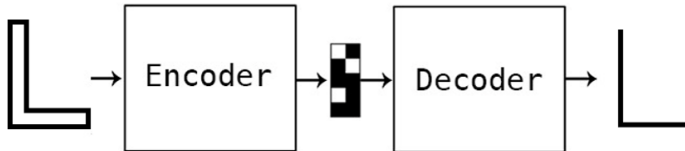
I L T X K O Y

H U S D Q W

## Reuse Image Encoder Decoder



## For Dimension Reduction



## For Deep Learning

- ▶ Need lots of data
- ▶ Had just few input output image pairs
- ▶ How to augment/populate large variations . . .

# Data Preparation

# Data

Original input and output are in the form of polylines, meaning a list of points, each having x,y coordinates

| Profile Data |      | Profile Picture | Midcurve Data |      | Midcurve Picture |
|--------------|------|-----------------|---------------|------|------------------|
| 5.0          | 5.0  |                 | 7.5           | 5.0  |                  |
| 10.0         | 5.0  |                 | 7.5           | 32.5 |                  |
| 10.0         | 30.0 |                 | 35.0          | 32.5 |                  |
| 35.0         | 30.0 |                 | 7.5           | 32.5 |                  |
| 35.0         | 35.0 |                 |               |      |                  |
| 5.0          | 35.0 |                 |               |      |                  |

## Data

| Profile Data |      | Profile Picture | Midcurve Data |      | Midcurve Picture |
|--------------|------|-----------------|---------------|------|------------------|
| 0            | 25.0 |                 | 12.5          | 0    |                  |
| 25.0         | 25.0 |                 | 12.5          | 22.5 |                  |
| 25.0         | 20.0 |                 | 25.0          | 22.5 |                  |
| 15.0         | 20.0 |                 | 0             | 22.5 |                  |
| 15.0         | 0    |                 |               |      |                  |
| 10.0         | 0    |                 |               |      |                  |
| 10.0         | 20.0 |                 |               |      |                  |
| 0            | 20.0 |                 |               |      |                  |

- For each shape, we have this pair of input and output. That's it.
- We need to start with these few samples only



## Augmentation

- ▶ Such few profile shapes, are just not enough for Neural Networks to train.
- ▶ Need more with as much diversity as possible.
- ▶ Will need to artificially augment data with transformations, like pan, rotate, mirror, etc.
- ▶ All needs to be automatically, programmatically

## Geometry to Image

- ▶ Raw input data is in the Vector format
- ▶ Converted it to fixed size (100x100) image by rasterization of drawSVG library.



**Vector format**

.svg

6KB

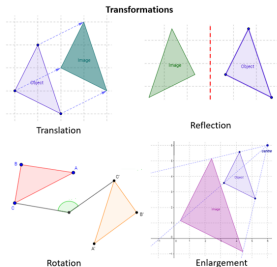


**Raster format**

.jpeg .gif .png

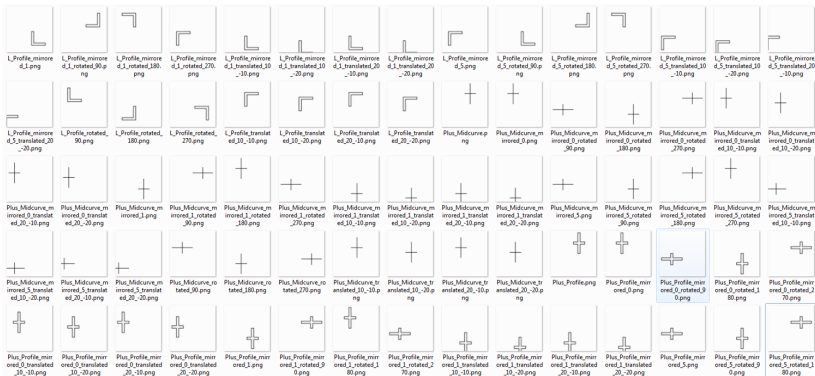
12KB

# Variations



- Inputs: I, L, Plus, T
- Operations:
  - Translated
  - Rotated
  - Mirrored
  - Mirrored Translated
  - Mirrored Rotated
- Total: 896 images (still less, but not bad)

# Training Data Samples



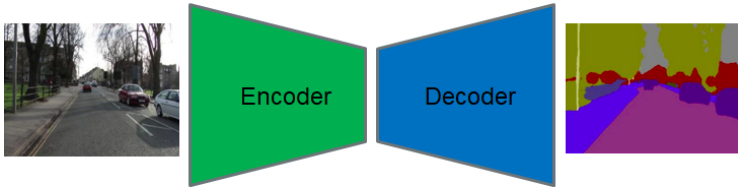
## Midcurve By Neural Network

## Options For Architectures

- ▶ Simple Encoder Decoder (one layer each)
- ▶ Dense Encoder Decoder
- ▶ Convolutional Encoder Decoder
- ▶ Pix2Pix
- ▶ ...

# Simple Encoder Decoder

# Simple Encoder Decoder

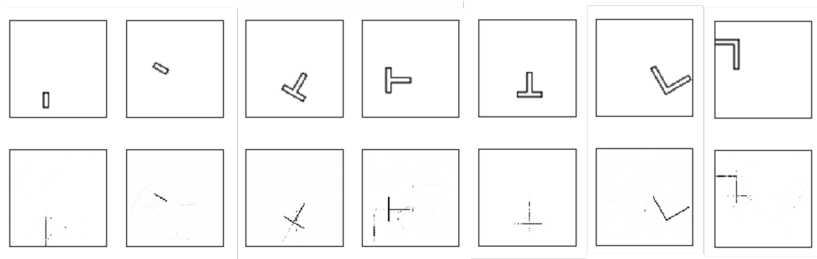




## Keras Implementation

```
1 input_img = Input(shape=(input_dim,))
3 encoded = Dense(encoding_dim,
    activation='relu', activity_regularizer=regularizers.l1(10e-5))(input_img)
    decoded = Dense(input_dim, activation='sigmoid')(encoded)
5
    autoencoder = Model(input_img, decoded)
7
    encoder = Model(input_img, encoded)
9 encoded_input = Input(shape=(encoding_dim,))
    decoder_layer = autoencoder.layers[-1]
11 decoder = Model(encoded_input, decoder_layer(encoded_input))
13 autoencoder.compile(optimizer='adadelata', loss='binary_crossentropy')
```

## Results



## Results

- ▶ Not very perfect but encouraging
- ▶ NN is correct with
  - ▶ The location (bounding box)
  - ▶ Dimension Reduction is seen
- ▶ But, still some stray points and misses

## What can be done?

- ▶ For the noise, use bounding boxes
- ▶ Feedback into error term: differencing with the known output expected
- ▶ Classify single pixel image as the skeleton, and rest as noise.

## What Next?

- ▶ Add denoiser network after the current one
- ▶ More Network Architectures
- ▶ Sequence-to-Sequence based approaches, taking closed thin polygon as input and polyline as output
- ▶ Extending to 3D, ie Midsurface

## End Notes

## Summary

- ▶ Various applications need lower dimensional representation of shapes.
- ▶ Midcurve is one- dimensional(1D) representation of a two-dimensional (2D) planar shape.
- ▶ Used in animation, shape matching, retrieval, finite element analysis, etc.

## Summary

- ▶ Approaches: Thinning, Medial Axis Transform (MAT), Chordal Axis Transform (CAT), Straight Skeletons, etc., all of which are rule-based.
- ▶ Proposing a novel method called MidcurveNN which uses Encoder-Decoder neural network for computing midcurve from images of 2D thin polygons in supervised learning manner.



## Summary

- ▶ This dimension reduction transformation from input 2D thin polygon image to output 1D midcurve image is learnt by the neural network,
- ▶ Which can then be used to compute midcurve of an unseen 2D thin polygonal shape.

# Agenda

1 INTRODUCTION TO MIDCURVE

2 THE END

# References

► xxx

Thanks ... [yogeshkulkarni@yahoo.com](mailto:yogeshkulkarni@yahoo.com)