

39)

$$2, 4, 6, 10, 16, 26, 42$$

$\xrightarrow{+2} \xrightarrow{+2} \xrightarrow{+4} \xrightarrow{+6} \xrightarrow{+10} \xrightarrow{+16}$

The value at which it increases by is found by adding the previous two differences.

$$42 + (10 + 16) = 68$$

$$68 + (16 + 26) = 110$$

40)

$$-9, -8, -4, 5, 21, 46$$

$\xrightarrow{+1} \xrightarrow{+4} \xrightarrow{+9} \xrightarrow{+16} \xrightarrow{+25}$

The value at which they are increasing are all perfect squares whose square roots are increasing by 1 each time.

$$46 + 6^2 = 82$$

$$82 + 7^2 = 131$$

41)

$$4, 9, 25, 49, 121$$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$  square roots  
 $2, 3, 5, 7, 11$

These are all prime numbers.

$$13^2 = 169$$

$$17^2 = 289$$

42)

$$6, 15, 35, 77, 143, 221$$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$  prime factoring  
 $2 \cdot 3, 3 \cdot 5, 5 \cdot 7, 7 \cdot 11, 11 \cdot 13, 13 \cdot 17$

They are all products of consecutive prime numbers

$$17 \cdot 19 = 323$$

$$19 \cdot 23 = 437$$



$$43) 4, 9, 61, 52, 63, 94, 46$$

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ 4 & 9 & 16 & 25 & 36 & 49 & 64 \end{array}$$

write it backwards

They are all perfect squares

$$9^2 = 81$$

$$81 \rightarrow 18$$

44) # of lines	max # of sections
0	1
1	2 $\rightarrow +1$
2	4 $\rightarrow +2$
3	7 $\rightarrow +3$

$$4 \Rightarrow 7+4=11$$

$$5 \Rightarrow 11+5=16$$

$\therefore$  5 lines can divide a circle into a max of 16 sections

$$45) 1X=9$$

Stage	Cubes
1	1
2	4 $\rightarrow +3$
3	10 $\rightarrow +6$
4	20 $\rightarrow +10$
5	35 $\rightarrow +15$

$$\therefore \text{stage } 9 = (((35 + (15+6)) + (15+6+7)) + (15+6+7+8)) + (15+6+7+8+9) = 165 \text{ cubes}$$

$$46) 3 \times 9 \times 8 = 216 \quad \therefore \text{the ones digit is } 6$$