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R&D Project

Qualitative Representation for Perception and Control of Mobile Platforms

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I, the undersigned below, declare that this work has not previously been submitted to this or any other university and that it is, unless otherwise stated, entirely my own work.

Date

Mihir Patil

Abstract

Your abstract

Acknowledgements

Thanks to

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Introduction

[32] says that qualitative representations can better compensate for vague data and also, that quantitative representations compute upto an unnecessary level of accuracy. qualitative representations are good for human robot interactions.

[30], Qualitative spatial calculi offer a method to describe spatial configurations in a framework based on a finite set of relations that abstracts from the underlying mathematical theory. opira is oriented point algebra [29] movement of people

Perception and control are two essential components of any successful robot navigation system. While perception deals with the spatial representations of the environment as perceived by the robot, control derives the required parameters necessary for navigation based on the perceived data. Traditionally such a task of navigation is achieved using quantitative approaches involving precise numerical information. Though useful such precise representations may not always be a prerequisite [?] [38].

Consider the case of a robot tasked with driving along a corridor towards the end without colliding with the walls. In such a scenario where precise perception and control are deemed surplus to requirements, the robot can be controlled using qualitative inputs in the context of an approximate map (spatial representations) [38]. The significant benefit of using a qualitative representation is that we no longer trying to follow a pre-planned, precise trajectory. Therefore eliminating

the need to constantly issue control commands. This implies that a qualitative approach would be more efficient [7] (in terms of CPU usage [?], battery usage etc.).

Furthermore, humans often communicate basic navigation tasks to each other using approximate spatial relationships to observable landmarks [?] [7], without requiring a precise map (for example, walk past the computers and take a left at the elevator) [38]. Hence by using qualitative representations we would be emulating a similar communication pattern which in turn facilitates a better human robot interaction [16].

- Qualitative representations(calculi) are useful in cases such as dynamic environments [?], where precise metric maps or precise trajectories often/may fail due to the constant and often unprecedented changes to the environment [38].
- Qualitative calculi can be used to make simple and intuitive inferences that can be used to achieve robust control(navigation) [13] [?] of a mobile platform.

- Most robot navigation tasks are composed of two basic steps, namely precise perception to localize the mobile robot on a given map and the control the platform along the precisely generated trajectory. While this approach works successfully in a number of cases it is not necessarily efficient [?] especially in terms of the continuous monitoring of the path by issuing a prolix of control commands.
- High level robot programming should be carried out without having to refer to numeric data. Ideally, a robot programmer should describe the task to the robot in terms that they would use to describe it when doing it themselves (“task-level” programming). People do not naturally think of physical actions in terms of joint angles or numeric co-ordinates, so high level robot programming should be done in non-numeric terms [?].
- Qualitative calculi exhibit a step forward in the direction of generalizing 2-D space [?] for use in various robotic tasks such as navigation [?] [13] and control.

1.1 Motivation

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1.2 Challenges and Difficulties

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1.3 Problem Statement

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State of the Art

Over the years, research into qualitative spatial representations has led to the development of various models which can be used to represent the visually observable space. From a more scientific perspective these models are known as “Qualitative calculi”, the current state of the art calculi rely on a single spatial primitive such as distance, direction, topology etc., to describe a set of relationships amongst the observable objects. In general each calculi comes with its own set of benefits and drawbacks as each one of them has been tailored to exploit different aspects of space[?].

For the case of robot navigation, current state of the art approaches utilize qualitative calculi that can provide both spatial and temporal information such as the QTC [?] or QRPC [?]. There exist comprehensive surveys that provide detailed information about each of the existing qualitative calculi[?], hence this state of the art aims to provide only a concise overview of the qualitative calculi that are advantageous to our application. We shall look into the relationships afforded by each of these calculi and their classification based on the domain of their utility.

2.1 Forms of qualitative spatial representations

2.1.1 Topological Representations

\square $[?]$ $[?]$: This is the most fundamental spatial representation, wherein the observed space is divided into distinctive regions based either on distinctive points in space or on separable objects found in the space. Topological representations draw heavily from the field of “Mereology” (the theory of parthood) to describe relations between the distinctive regions. Qualitative calculi such as RCC, Interval Algebra, n-intersections etc. belong to this category. Such representations deal with the “invariant properties that are under continuous deformations of objects, including translating, rotating and scaling”, and often include only spatial information while completely disregarding temporal data.

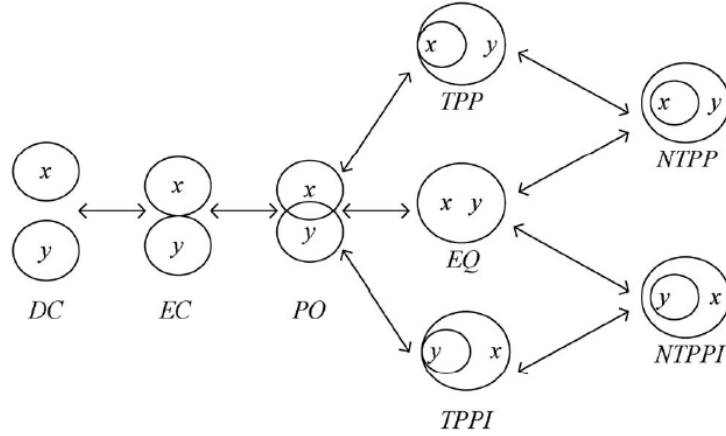
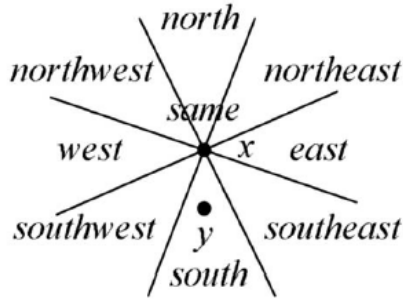


Figure 2.1: The eight jointly exhaustive and pairwise disjoint relations of region connection calculus (RCC8). The arrows show which relation is the next relation a configuration would transit to, assuming the continuous movements or deformations $[?]$, $[?]$, $[?]$.

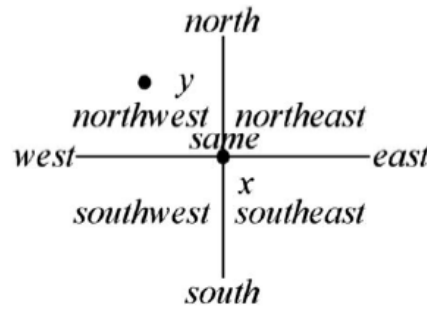
2.1.2 Directional Representations

[7] : The relative direction between two different objects can be represented using directional relations/representations. These representations rely on three

primary elements, a reference object, a reference frame and a target object to define a valid relation between two different objects. Directional representations are widely classified into two categories, point based and projection based with the discerning factor being the dimension of the objects involved and distinction of space using either cone shaped spatial sectors or by using vertical and horizontal lines to create smaller rectangular sectors. Furthermore, the directional calculus isn't restricted to using only cardinal directions, it also allows the use of nominal directional information such as left ,right etc to describe the directional relations. Qualitative calculi such as CDC, OPRA, CyCord etc utilize the directional representation. Being based of topological representations, directional representations also include only spatial information while disregarding temporal data.



(a) Cone-shaped direction relations [26]



(b) Projection-based direction relations [27]

Figure 2.2: The point based and projection based direction representations [7]

2.1.3 Distance Representations

[7] : The qualitative representation of spatial distance can be classified into two groups namely absolute and relative. This classification is made solely on the basis of the presence/absence of an extraneous referential object in the relation between two objects. This distinction can be clearly illustrated by the following example, 'the distance between A and B is 8 meters' or 'A is near B', this is a absolute approach as the distance is measured directly between two objects. Whereas saying that 'A is closer to B than that to C' classifies as a relative approaches as

this involves the comparison to a third object. Furthermore, it has been shown that absolute approaches can be qualitative or quantitative, but relative approaches are commonly qualitative [?]. Qualitative calculi such as the ARGD(or Delta) and TPCC use the distance representations to describe the observable space. Distance based relations have found to be insufficient by themselves when it comes to the task of robot manipulation/navigation and hence are often used in combination with distance representations to yield a fairly suitable and complete representation of the environment [?]. Like with the direction representations this calculi also lacks temporal data in the encoded relations and is hence unsuitable for applications involving moving objects.

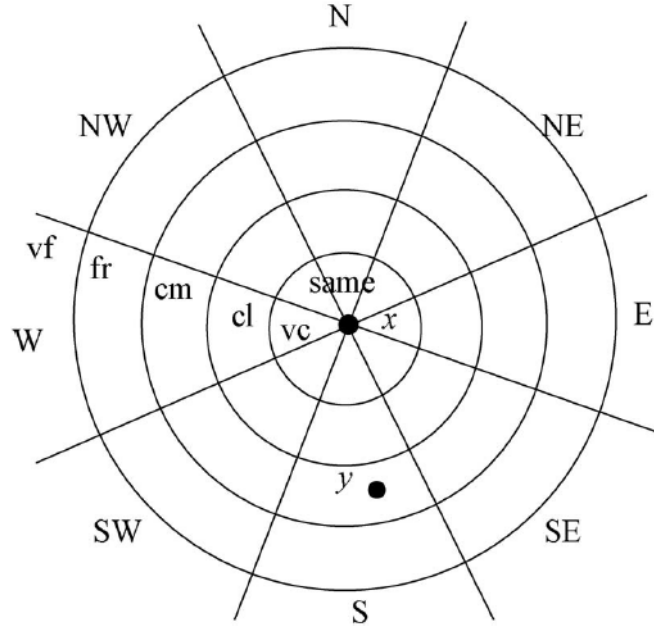


Figure 2.3: An representation of the combination of cone-shaped direction and absolute distance: very close(vc), close(cl), commensurate(cm), far(fr) and very far(vf), [10].

2.1.4 Moving object Representations

[7] : Topological representations, directional representations and distance representations describe relations between stationary objects, this limitation encouraged

the development of a moving object representation which can qualitatively represent moving objects and their trajectories. These representations effectively deal with both spatial and temporal data to describe valid relations among mobile objects, while these relations include some directional information they mainly describe the relative motion between two objects and not relative direction. The relative motion between two objects is described using oriented line segments which are approximations of the trajectory of the objects in motion. QTC, QRPC are the two prominent calculi that utilize moving object representations. Moving object representations and the calculi using these representations have been proven to have solved the problem of representing moving objects but since these relations lack any distance information, they are still prone to failure and often need a complimentary distance calculi to ensure that a mobile object(robot) can successfully move around in the given environment without collisions.

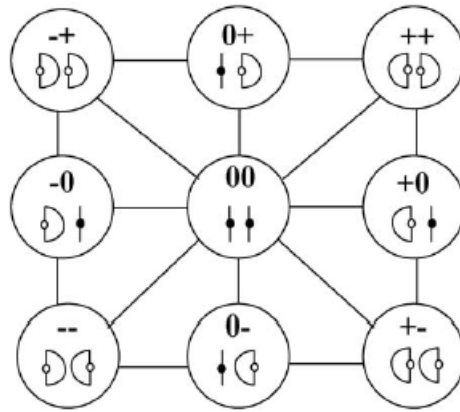


Figure 2.4: Basic relations of basic Qualitative Trajectory Calculus (QTCB) in a conceptual neighborhood diagram. The solid dots represent the stationary objects and the open dots represent the moving objects $[?]$, $[?]$.

2.1. Forms of qualitative spatial representations

Domain	Model Name	Type of objects	Number and granularity of relationships	Description
Temporal	Interval Algebra [3]	Time Intervals	13 relationships, Binary relationships	It does not consider time instants.
	Extended Interval Algebra [21]	Time intervals and extreme points of the intervals	29 (13 IA(Interval algebra) + 16 extremes), binary	It extends IA(Interval Algebra) model by considering new relationships including the extremes of the interval and it introduces the notion of conceptual neighborhood.
Spatial	Region Connection Calculus [34]	Sets	8 or 5 relationships, Binary Relationships	It uses the geometric properties associated to the connection between two sets to establish relationships that are no longer linear but planar, and which are invariant to translation, rotation and scaling.
	Cardinal Reference System(CRS) [20]	Generic objects	9 (8 cardinals + 1 neutral) relations, Binary Relationships	It describes the position of any object by using a cardinal orientation as reference system and by adding also a neutral region
	FFC (Flip Flop Calculus) [28]	Points	8 (6 + 1 double + 1 triple), Ternary Relations	It is based on the possible positions of a point C with respect to a segment AB defined by other two points, A and B.
	SCC (Single Cross Calculus) [21]	Points	11 (8 + B=C+1 double + 1 triple), Ternary Relations	Describes the possible positions of a point C with respect to a segment AB and the orthogonal line to segment AB on B.
	DCC (Double Cross Calculus) [22]	Points	17 (15 regions + 1 double + 1 triple), Ternary Relations	Describes the possible positions of a point C with respect to a segment AB and two orthogonal lines to segment AB on A and B.
	Oriented point based Reasoning [31]	Oriented Points	4, Binary Relations	It is based on the relative orientation between pairs of oriented points in terms of two qualitative spatial dichotomies: the frontback and leftright.
	DRA (Dipole Relation Algebra) [17], [18]	Dipoles (or oriented segments)	24, Binary Relations	It is based on the relative position of oriented segments.
	OPRA (Oriented Point Relation Algebra) [19]	Oriented points	Depends on the granularity, Binary Relations	As DRA model, it is also based on the relative position two oriented points, but it supports different levels of granularity.
Spatio-temporal	QTC (Qualitative Trajectory Calculus) [41]	Points	81, Binary Relations	It describes the possible relations among two moving points in terms of the frontback and leftright dichotomies.
	QRPC (Qualitative Rectilinear Projection Calculus) [24]	Oriented points	Depends on the chosen granularity (up to 48), Ternary Relations	It establishes the possible relations of an object with respect to the trajectory of another object depending on the cross-point of the trajectories and the relative position among them

Table 2.1: Key features of the more representative models(calculi) of qualitative representations of spatial or temporal domains in the existing literature [24].

2.1.5 Conclusion

From the above breakdown of the representations and the calculi, it is easy to summarize that distance representations and moving object representations are the most promising representations for our application in mobile robot navigation. Consequently the calculi associated with these representations will be the ones that are further scrutinized in the following section. The reasoning behind this conclusion is fairly simple moving object representations are basically spatio-temporal representations which take into account both the spatial and temporal data to create abstractions of the objects trajectory, this is crucial when dealing with mobile objects as this gives a more concrete representation of the objects in motion. In the case of distance representations although these representations deal only with spatial information, they provide explicit information on how close or far the objects under consideration are. Thus effectively capturing the possibility of a collision between the objects, this sort of information cannot be found in the direction and topological representations hence rendering them unfavorable for our application in mobile robot navigation. [7], [11], [12], [13], [44].

2.2 Analyzing qualitative calculi for navigation

This section aims to provide a through understanding at a selective group of qualitative calculi based on the conclusions drawn from the previous section. Namely we shall look at the qualitative calculi such as the QTC, QRPC and ARGD which use moving object representations and distance representations and function in the spatio-temporal and spatial domains respectively.

2.2.1 Qualitative Trajectory calculus

[40], [43], [42] The QTC calculus was developed to solve the problem of inadequate representation of mobile objects in the spatio-temporal domain, which until then were represented only in the spatial domain using either the RCC or the n-intersections calculi. The major drawbacks of those calculi was their failure to deal with temporal data. Hence mobile objects were often abstracted as stationary

regions using either 'disconnected from' relation (DC) in RCC or 'disjoint' relation in the 9-intersection model, with the exception of a few limiting cases where the two objects meet, such as a collision between two mobile robots. Thus, the limiting factor of these formalisms was that all the DC relations were non-differentiable, due to the ignorance of information regarding relative motion between the two objects.

The QTC calculus constitutes of two major variants the QTC_B and the QTC_C , with the major difference between the two being the inclusion of the directional information in the relationships (between two objects) of the QTC_C calculus. Both versions of the QTC are adept at dealing with qualitative movement of objects in one, two and three dimensions. In the QTC_B calculus, as the euclidean distance between two objects is taken as the only constraining dimension. The abstraction of movement is depicted using three qualitative values:

- 0: the object is stable with respect to the other object.
- -: the object is moving towards the other object.
- +: the object is moving away from the other object.

The assigning of these qualitative values to an object's movement depends upon the relative position (constrained by distance) and relative speed of the two objects with respect to each other. This can be illustrated by the following example, consider two objects 'j' and 'k', the possible values for 'j' :

- based on relative position at a time 't' are:
 1. 0 (stable): if there is no change in the relative position with respect to 'k' (no change in relative distance).
 2. - (moving towards): if there is a change in the relative position with respect to 'k', such that the relative distance between the objects decreases.
 3. + (moving away): if there is a change in the relative position with respect to 'k', such that the relative distance between the objects increases.
- based on relative speed at a time 't' are:

1. 0 (stable): if speed of 'j' is equal to the speed of 'k'.
2. - (moving towards): if speed of 'j' is lesser than the speed of 'k'.
3. + (moving away): if speed of 'j' is greater than the speed of 'k'.

Hence a valid QTC_B relation between qualitative trajectories of two objects is represented as such '-,+,-' (for object 1) and '+,-,+' (for object two). Wherein the value in the first position is the relative position of the object in consideration, the second value is the relative position of the other object and the third value is the relative speed of the current object with respect to the other object. The benefit of having a relation that includes both relative position and speed comes to light when dealing with the movement of objects in higher dimensions (2D, 3D) for instance in 2D, the value '0' (stable) may be interpreted as either the distance being stable or the speed being stable, this confusion during interpretation is avoided by using unique values for both the relative distance and speed and hence the size of the resulting relations is a set of three. Interpretation of these relations is pretty straight-forward when dealing with movements one dimension.

The QTC_C variation of the QTC calculus is often seen as an extension of the QTC_B calculus, since it uses the same qualitative values to represent the qualitative trajectories of the objects. The only difference between the two versions comes from the integration of directional information which denotes the direction of movement of the current object in relation to a line segment between the two objects. This version of the QTC calculus was inspired in part by the 'Double cross calculus' [45], hence the name. The QTC_C calculus is an improvement on the double cross calculus, as it can define qualitative trajectories and direction for single as well as multiple objects at once, whereas the double cross calculus can only deal with single objects at any given instance of time.

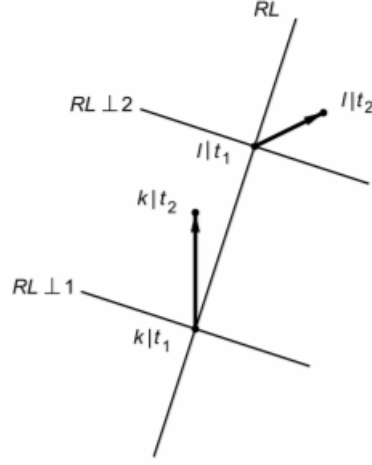


Figure 2.5: A graphical representation of the QTC_C calculus for a relation between two moving objects 'k' and 'l', where t_1 and t_2 are the two distinctive time instances and RL refers to the reference line and the double crosses ($RL \perp 1$, $RL \perp 2$) for the two objects [42] .

The relations of the QTC_C calculus, while following the same basic principles of the QTC_B , have been tweaked slightly to allow inferencing of the objects position in terms of the relative direction to the reference line. The assignment of the qualitative values to the object's movements can be illustrated using two objects 'k' and 'l', the possible values for 'l' at any given time interval are based on the following reasoning:

- based on movement relative to the respective perpendicular reference line:
 1. 0 (stable): if there is no change in the relative distance with respect to 'k' or with respect to the reference line.
 2. - (moving towards): if there is an increase in the relative distance between the objects.
 3. + (moving away): if there is an increase in the relative distance between the objects.
- based on movement relative to the directed perpendicular reference line(from 'l' to 'k'):

1. 0 (moving along the directed reference line): if the object moves along the line segment or if it was moving along the left/right and continues to do so in the given time interval.
2. - (moving to left side of the directed reference line): if the object moves from the right side of the line segment to the left side in the given time interval.
3. + (moving to right side of the directed reference line): if the object moves from the left side of the line segment to the right side in the given time interval.

Hence a valid QTC_C relation between qualitative trajectories of two objects is represented as such ‘-,+,-,0’(for object 1) and ‘+,-,-,0’(for object two). Wherein the value in the first position is the relative position of the object in consideration, the second value is the relative direction of its movement, the third value is the relative position of the other object and the fourth is it’s relative direction of movement.

Conclusion [40]In conclusion it is safe to say that the QTC_B calculi is more complete and robust in the sense that it can qualitatively and correctly represent all possible trajectories of the mobile object at a given instance of time, although due to it being developed to deal with mobile objects when they are in DC regions [43] it still cannot make a very robust or accurate relation regarding collision conditions, it provides a safer alternative to the QTC_C calculus as this calculus is still regarded as a work in progress [42]due to it’s inability to distinguish between the trajectories of a mobile object moving along the directed reference line and continuing to do so and a mobile object moving on either side of the directed reference line and continuing to do so. Thus this justifies the selection of QTC_B for our implementation, not only is it safer and simpler but it also allows easier integration with other complimentary calculi such as ARGD, RCC which may be used to deal with possible collision cases.

2.2.2 Qualitative Rectilinear Projection calculus

[24], [4], [14] The qualitative rectilinear projection calculus(QRPC) presents a innovative approach to qualitatively representing motion patterns based on planar trajectories. In comparison to the QTC calculus, this representation has a richer description of the motion exhibited by mobile objects. The basis of this claim lies in the oriented rectilinear projection used to represent the trajectories, which allows this calculus to represent rotational motions of an mobile object, something that was not possible in the existing calculi such as the QTC. The QRPC is specifically tailored towards obstacle avoidance and geometric relationships between two objects are generated using the front-back and the left-right dichotomies. The relationships encompassed in the QRPC abstract the objects as points and use their rectilinear projections to make qualitative distinctions such as front-back and left-right, these atomic relations and their base notations are illustrated below:

1. Notations:

- $P_i P_j$: is the relative disposition between the oriented rectilinear projection of the object O_i and the oriented rectilinear projection of O_j .
- $O_i O_j^{LR}$: The relative position of O_i with respect to the left-right dichotomy of O_j .
- $(CO_i^{FB})(CO_j^{FB})$: The relative position of the point of intersection('C') of the oriented rectilinear projections with respect to the frontback dichotomy of both objects.
- $O_i O_j^{FB}$: The relative position of O_i with respect to the front-back dichotomy of O_j when the trajectories are superimposed.

Note: 'i' and 'j' denote the two different objects.

2. Qualitative (atomic)relations in each of the notations :

- The relative disposition between two oriented rectilinear projections($P_i P_j$):
 - $\uparrow\uparrow$: Parellel in same direction
 - $\uparrow\downarrow$: Parellel in opposite direction

- \uparrow : Coincident in same direction
- \updownarrow : Coincident in opposite direction
- X : Crossed/Intersecting rectilinear projections
- The relative position of O_i with respect to the left-right dichotomy of O_j , $(O_i O_j^{LR})$:
 - ‘-’ : if O_i is on the left of P_j .
 - ‘0’ : if O_i is over P_j .
 - ‘+’ : if O_i is on the right of P_j .

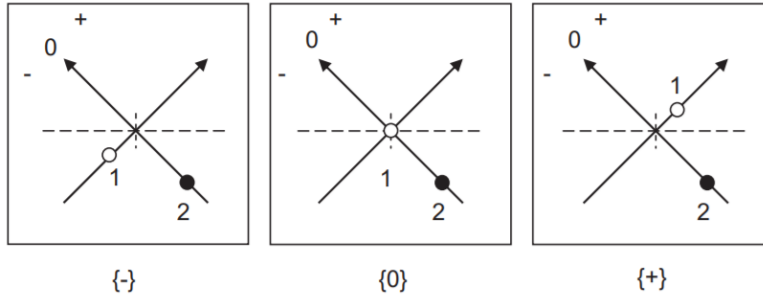


Figure 2.6: Relative position of O_i w.r.t the left-right dichotomy of O_j for crossed projections [24].

- The relative position of ‘C’ with respect to the front-back dichotomy of two objects $(CO_i^{FB})(CO_j^{FB})$:
 - $(+, +)$: if ‘C’ is in front of O_i and O_j .
 - $(0, +)$: if ‘C’ is at same position as O_i and in front of O_j .
 - $(+, -)$: if ‘C’ is in front of O_i and behind O_j .
 - $(0, -)$: if ‘C’ is at same position as O_i and behind O_j .
 - $(-, +)$: if ‘C’ is behind O_i and in front of O_j .
 - $(-, 0)$: if ‘C’ is behind O_i and in same position as O_j .
 - $(-, -)$: if ‘C’ is behind O_i and O_j .
 - $(+, 0)$: if ‘C’ is in front of O_i and at the same position as O_j .

In cases where the two projections do not intersect with each other ($\uparrow\uparrow$ or \updownarrow), this qualitative abstraction presents as conundrum

as the point of intersection ‘C’ may lie at either positive or negative infinity, hence in such cases the relation is abstracted to either $(+, +)$ or $(-, -)$.

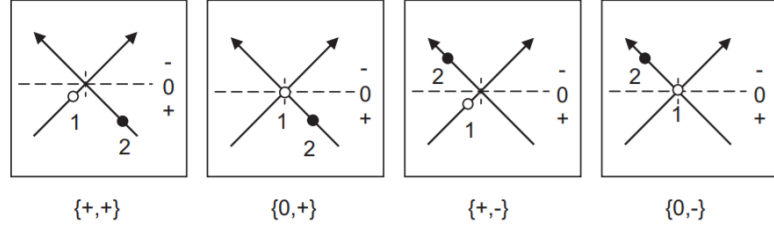
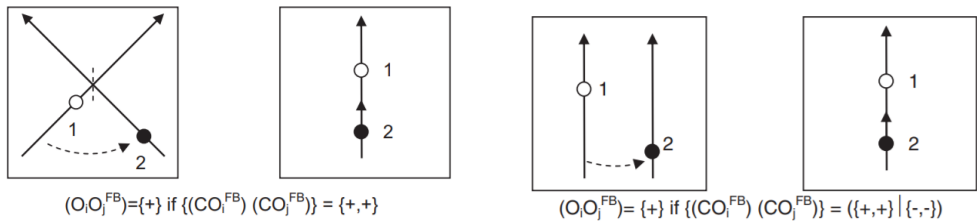


Figure 2.7: Some of the spatial configurations of the intersection point with respect to the front-back dichotomy of two objects for crossed projections $(CO_i^{FB})(CO_j^{FB})$, [24].

- The relative position of O_i with respect to the front-back dichotomy of O_j when the trajectories are superimposed($O_i O_j^{FB}$):
 - ‘+’ : if O_i is in front of O_j after P_i is superimposed on P_j .
 - ‘0’ : if O_i is at the same position as O_j after P_i is superimposed on P_j .
 - ‘-’ : if O_i is behind O_j after P_i is superimposed on P_j .

Note: The after the rectilinear projection of O_i is rotated (such that the objects are always facing in opposing directions) along ‘C’ if it exists, before being superimposed on the rectilinear projection of O_j .



(a) The $(O_i O_j^{FB})$ feature for crossed projections. [24]

(b) The $(O_i O_j^{FB})$ feature for parallel projections. [24]

Figure 2.8: The point based and projection based direction representations [?]

Conslusion Hence a complete valid QRPC relation comprising of the above mentioned atomic relations can be written as $[(P_i P_j)(O_i O_j^{LR})((CO_i^{FB})(CO_j^{FB}))(O_i O_j^{FB})]$, with the various values replacing their respective placeholders. Thus proving to be a richer representation of the movements of the mobile objects as it can effectively distinguish between front-back, left-right as well as same or opposing direction of heading. While this calculus does present a compact view of the movements of the objects, like it's predecessors it still requires a sequence of qualitative(QRPC) states(individual sets of relations) to effectively represent the movement of an object, besides a completely theoretical formulation of the calculi without the backing of suitable empirical data or implementation makes it hard to believe that this calculi would function reliably in a real time mobile robot scenario. These drawbacks dissuade us from further pursuing this calculi for our purpose of achieving qualitative perception and control in mobile robots [24].

2.2.3 Qualitative Distance calculus

[10], [45] The qualitative description of distance is based on three primary elements, a primary object, a reference object and a reference frame. When making a statement such as 'A is near B' the qualitative inference is ambiguous without taking into consideration spatial entities such as metric distance between the objects, their respective sizes and shapes, their relative positions, the positions of other objects as well as the frame of reference with respect to the objects itself. Furthermore the distance between two objects varies with perspective, for instance looking at a moving object from two different perspectives leads to two different interpretations of the distance to the object, with respect to observing entity. The distance calculi aims to summarize all these varying spatial quantities into a single coherent qualitative description which can be used to reason about space in terms of qualitative distances.

The ARGD or Delta calculus are some of the common names used for the qualitative distance calculus. These calculi partition the physical space into circular regions of varying granularity. Since there is no restriction on the number of granular divisions that can be applied to a given physical space we may define

this in a manner that is suitable for our application. Commonly the granularity varies from anywhere between 2-5, with the respective labels being very close, close, commensurate, far, and very far.

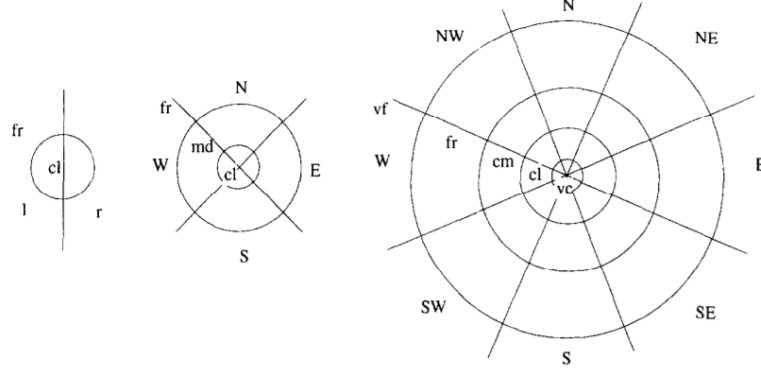


Figure 2.9: Various levels of distance and orientation distinctions. These figures show typical distance/orientation granularity configurations [10].

The various granular regions in the distance calculi are always centered around the object in consideration, these granularities are subject to an inherent ‘greater than’ order amongst themselves such that the granular region closest to the object has the lowest distance value and the one that is farthest has the highest order. Consider ‘ q_n ’ as the granularity of the distance representation, then the various instances are organized as such $[q_0 < q_1 < q_2 < \dots < q_n]$, with q_0 being the smallest distance to the object and q_n being the largest. By using this comparative approach for distance magnitudes the calculus effectively maps the granular symbols to one dimensional geometric intervals that represent the distance ranges.

Conclusion Since the applicability of the distance approach does not depend upon the number of distance relations, it allows the distance calculus to be highly adaptive to the users demands and hence provides a feasible alternative to collision free navigation in mobile objects. Also as mentioned previously the distance representation effectively divides the physical regions around the object into geometric intervals, hence making this approach suitable to define distance thresholds around the robot to avoid collisions with other objects as well as define a suitable safe

region around the robot, which in-turn ensures safe movement in the physical space. These benefits of the qualitative distance calculi make it favorable to our application, hence warranting its utilization [10], [29].

2.3 Implementations utilizing qualitative representations for navigation in robots

The goal of this section is to introduce the reader to the existing approaches that use qualitative spatial representations in some capacity to achieve efficient and collision free navigation in mobile robots. The merits and de-merits of each implementation is recognized and a brief summary is constructed based upon the same.

- [8], This approach relies heavily on the detection of tangible features in two sets of images one of which is a reference image that is taken during a teach phase (when the robot is taken manually through the desired path and allowed to take reference images through out its path traversal) and a second image that is taken during a replay phase during which the robot is allowed to navigate the desired path by itself, capturing new images all along. The features in both these images are detected and tracked using the Kanade-Lucas-Tomasi [6] feature tracker. The tracked features in the current image (taken during the replay phase) are compared with the features observed in the reference image (taken during the teach phase) and the difference in their positions and distance is used to make qualitative decisions regarding the corrections that have to be made to the robot's path with respect to the desired path. The underlying spatial entity that is compared is the corresponding distance between the tracked features (in both the reference and the current image and the reference image) with respect to a common principal point of the images. Based on this conditions the decisions are made as follows:
 - if the robot is moving from point A to B without deviating from the original path, then continue the current path until some deviation occurs.

2.3. Implementations utilizing qualitative representations for navigation in robots

- if the robot deviates laterally from the desired path and this is indicated in the signed distances between the features of the current and reference image, then:
 - * if the distance between the reference feature lying on the left/right of the image and the principle point is more than the distance between the current feature lying on the left/right of the image and the principle point then move left or right respectively.
 - * if the signed distance of the feature lying on the left/right of the image does not match with the sign of the feature lying on the left/right of the reference image then move right or left respectively.

Conclusion The merits of such an feature based approach seem to be apparent, yet this approach does not utilize any of the traditionally accepted qualitative calculi. Furthermore it's reliance on a teaching phase renders it invalid in cases where prior information about the environment is denied to the robot. The dependence on further factors such as lighting conditions, detection of features and inability to work efficiently in an outdoor environment (due to lack of contrast, the features are not detected) show that this is a highly constrained approach that can work only if a large amount of prerequisites are satisfied. The merit of this approach is still it's ability to function exceptionally well when the teach phase is executed properly, with the robot able to follow trajectories upto a 100 meters easily. The authors also mention the apparent improvement in efficiency (in terms of reduced cost and power consumption as well as increased robustness) when using such qualitative approaches, but fail to provide empirical proof for such statements.

- [9], The approach presented in this paper also utilizes detection of tangible features to extract pixel coordinates of these features and then compare these coordinates with the corresponding pixel coordinates of the feature in the reference frame. The resulting differences are then used to make decisions regarding the control of the robots trajectory, as previously introduced this approach also makes use of the teach-replay method. This paper extends the approach presented in [8] by combining the pixel coordinates with odometry

information to achieve a more robust navigation, also the use of the ‘funnel lane’ methodology is a novel concept that helps in localizing the robot. The underlying spatial entity uses in this approach is the relative positions of the features with respect to the principal point of the image, which yields signed (x,y) co-ordinate values. The distance between these reference points and the principal points is used to define a region called the ‘funnel lane’, while the robot lies in this region it is allowed to move directly towards the goal position, but if there are any violations such that the robot moves out of this ‘funnel lane’ then the controller updates the control commands to ensure the robot re-enters the ‘funnel lane’. Since the ‘funnel lane’ is oriented such that its origin is always at the goal position hence ensuring that the robot zeros in on the goal position.

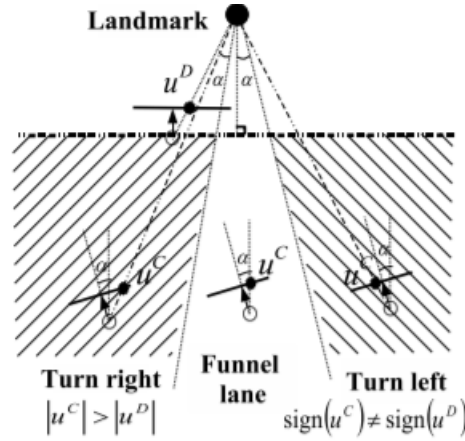


Figure 2.10: The funnel lane created by the two constraints (distance from the principal point and the relative signs of the distances), and when it has turned by an angle α , here μ^C and μ^D represent the horizontal pixel coordinates of the reference and the current frame.

Conclusion Being an extension of the approach specified in [8], this implementation suffers from very much the same over-reliance on the teach phase to correctly capture the reference features, while completely failing to utilize any of the traditionally accepted qualitative calculi. Furthermore the authors fail to indicate the maximum number of features that can be considered

2.3. Implementations utilizing qualitative representations for navigation in robots

when constructing this ‘funnel lane’ and do not provide details about what happens when no feature is detected, making this a promising yet incomplete implementation as not all details are disclosed. The implementation is more robust thanks to the introduction of the funnel lane concept and utilization of odometry information which enable the robot to follow trajectories of upto 380m and at a speed of 1m/s. Again the authors mention the improvement in efficiency in terms of power consumption and computational requirements yet they fail to provide any conclusive evidence to validate these claims.

- [32], The approach followed in this implementation is also based on a teach-replay method, but instead of using RGB cameras and images to extract and compare features it uses a sonar array to find the distances from the obstacle. Since this implementation is deployed on a wheelchair in a indoor corridor environment, the sonar array is used to measure the distance from the wall. The primary use of qualitative representations is for human robot interaction and is not used for the navigation task as a suitable update rate for the qualitative representations was not possible, hence although the use of qualitative calculi based on the directional and distance representations was hypothesized it was not put to test in a factual manner. As mentioned above the proposed approach used a sonar array and dead reckoning to record desired paths and then autonomously replay them. The base assumption being that any path in an indoor environment is basically a combination of following walls and making turns at the corners, based on this assumption path were described with as a sequence of distances and angles with specific triggers wherever a corner or an immovable object was encountered so that a suitable maneuver may be performed. Being a teach and replay approach this implementation also compared data obtained during the replay stage with the reference data obtained during the replay stage and made decisions based on the differences so that the wheelchair follows a path that is as close as possible to the original path as possible.

Conclusion Since this is another teach-replay approach it’s major drawback is the over-reliance on the teach phase, furthermore being a teach replay

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<close forward fast>  
<close right medium-speed>  
<close backward slow>  
<very-close left medium-speed>
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Figure 2.11: The hypothesized qualitative representation with the left most value being the distance, followed by the direction to move in and finally the speed with which to move [32].

approach that utilizes sonar distances, angles and dead reckoning to obtain trajectories, the system cannot deal with dynamic objects such as humans that may be encountered during autonomous replay as these objects did not exist during the teach phase and hence no information about them exists in the systems knowledge of the environment. The authors also fail to provide concrete information regarding how the control decisions are made instead choosing to only mention that this is done based on the differences in the represented trajectories. One clear merit of this implementation was the hypothesis of how qualitative distance and direction calculi can be combined to achieve navigation in robots, but this is also it's drawback as this was only hypothesized and not tested or implemented on the mobile platform. Again the authors assume better efficiency in terms of power consumption and computational requirements due to the usage of qualitative representations yet they fail to provide any conclusive evidence as validation.

- [36], The approach presented in this project makes use of a unique qualitative map based representation, which is inherently based on distance relations. The authors propose the 'Qmap' framework which accepts as a input a line segment representing the desired path and . This line segment is then quantized into rectangular cells that form a part of the grid. Since the robot is equipped with a sensor array of 8 sonar's each placed at 45 degrees (in a manner similar to the layout of the cardinal directions) and orientation sensors the data received from each of these sensors is stored in a qualitative manner within the cells of the grid. Sensors that are in close proximity of obstacle are marked as active and their respective relations are indicated using either of the three distance primitives [I(increasing), D(decreasing), S(stable)], this

2.3. Implementations utilizing qualitative representations for navigation in robots

is the qualitative data that is stored in each cell during the off-line planning phase. During the run-time the implementation takes as input the generated ‘Qmap’ and the starting and ending positions. Additionally, data stored in each cell is compared with the real-time data and the control decisions are made based on the differences between the two. In cases where the difference between the reference data (simulated during the planning stage) and the real-time data is large such that can be caused by the presence of moving obstacles the preference in the control algorithm is given to the real time data such that it ensures that the robot stops moving completely until further intervention by a human controller.

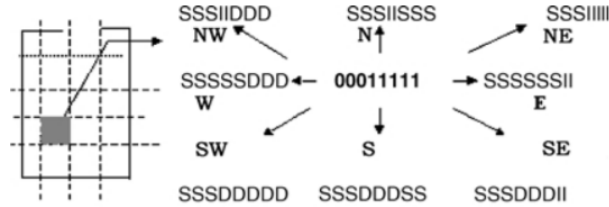


Figure 2.12: figure showing the ‘Qmap’ for a given line segment, the 0’s and 1’s indicate the inactive and active sensors while ‘S’, ‘I’, ‘D’ indicate the distance relations of each sensor w.r.t the obstacle(grey cell) [36].

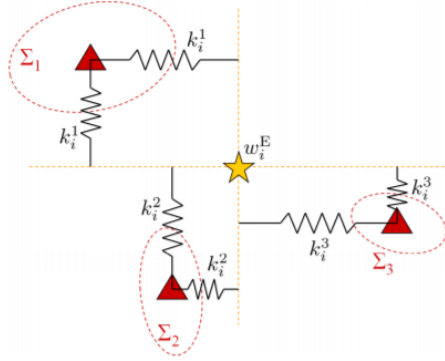
Conclusion The authors mention that the implementation deals with obstacles by marking those respective cells as blocked, but do not indicate how or when(planning or run-time) this information is provided to the map, also the stopping of the robot when dealing with moving objects is an obvious drawback when considering real world applications. The authors mention that a successful navigation was achieved in 60 percent of the cases out of a possible 15 experimental runs, with the causes of failure being the large size of the robot which in turn caused collisions when turning, the accumulation of errors in the orientation data due to inaccurate orientation sensors and errors in localizing the robot position on the ‘Qmap’ due to increasing uncertainty, especially when moving in large open spaces. Yet again the author’s mention the efficiency based benefits of the qualitative approach but do not provide

tangible proof for it and although this is a promising qualitative representation in relation to a global map of the environment it still does not use any of the traditionally accepted qualitative calculi.

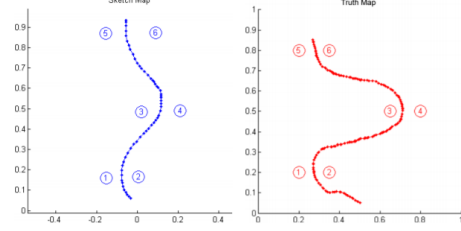
- [37], This implementation also provides reasonable cause to prove the utility of qualitative representations in global planners. It uses as an input a hand-drawn map containing the desired path to be followed and a set of landmarks that can be used as a reference, this qualitative map does not have to be accurate but should be able to represent the approximate positions of the landmarks in the physical space. The planning module used in this approach utilizes this approximate way-point positions and the corresponding landmark positions to plan a valid path that can be further fed to a path following module which in-turn executes it on a low level. The path planning is modeled as a quadratic optimization problem, wherein each way-point is influenced by it's surrounding landmarks, such that the closest landmark has a higher bearing on the placement of the way-point rather than a landmark that is farther away. The uncertainty in the position of the landmark is also taken into account when placing a way-point in the final trajectory that is to be executed. Furthermore when planning the final path the relative qualitative relations between the robot and the landmarks are maintained which makes it easier to localize the robot based on the available landmarks and in-turn reduce the uncertainty in the positions of the landmarks themselves. Additionally the EKF-SLAM algorithm is used to make the localization and way-point planning more robust.

Conclusion This implementation represents a more reliable approach to the utilization of qualitative representations in a global planning based approach. The preservations of qualitative relations between the way-points and the landmarks combined with a SLAM implementation provide a robust platform on which the robot can securely navigate a given environment. In it's current state this approach lacks the knowledge of obstacle avoidance for both stationary and mobile objects, also the authors do not elaborate on how the robot knows which observed landmark is to be associated with which

2.3. Implementations utilizing qualitative representations for navigation in robots



(a) Landmarks (shown as red triangles) represented with linear springs to the proposed waypoint location (shown as a star). For each landmark, the spring constant is calculated as a function of the distance between waypoint and landmark, and the uncertainty in the estimated location of the landmark (represented by red ellipses) [38].



(b) The sketched map (blue, on left) includes six landmarks and a trajectory that slaloms between pairs of landmarks. In the true environment (red, on right), the robot must slalom more aggressively to pass between the landmark pairs [37].

reference position in the given map, although during implementation on a robot this problem was solved using an overhead camera this does not suggest a feasible real-time implementation. Furthermore the authors suggest the advantage in efficiency that qualitative approaches have over quantitative approaches but do little to prove this as the truth.

- [5], This implementation features the use of the qualitative trajectory calculus to create abstractions of human movements and then use these abstractions to reason and execute the corresponding motions of the robot. QTC_B is the selected calculi for creating these abstractions, since it takes into account the relative motion between two mobile objects. The abstractions are described as such:

- ‘-’ (moving towards) : if the distance between the two objects is decreasing at a time instant t_{-1} and t_{+1} , where the current time instant is t .
- ‘+’ (moving away) : if the distance between the objects is increasing at a time instant t_{-1} and t_{+1} , where the current time instant is t .
- ‘0’ (stable) : for every other case.

Using the above mentioned abstractions the relative motion between the robot's and the human trajectory is encoded as a qualitative representation. A graph structure is used to build a situation graph tree where each node represents a particular scenario or agent's states and the edges indicate the transition to the next possible states. A depth first approach is used to traverse the whole tree and a fuzzy-logic based interpreter(F-Limette) is used to interpret the states and convert them to a low-level motion command. For the sake of simplicity the authors have only implemented this approach in a restricted limited manner, wherein the robot either follows the human or stops following it based on the described qualitative scenarios.

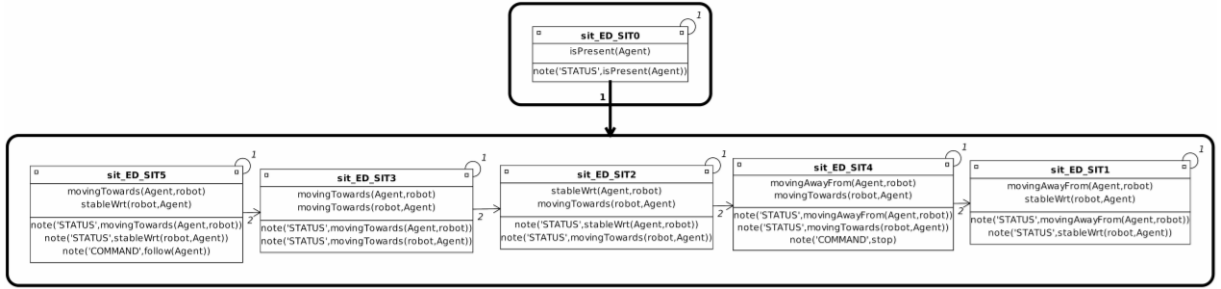


Figure 2.13: Situation Graph Tree of the human motion behaviour and relative robot actions [5].

Conclusion The above mentioned approach was successfully implemented on the robot platform using laser range finders to track human feet, and create suitable abstractions. Yet it presents only a limited view on the applicability of qualitative representations for robot navigation, furthermore when using such graph structures the space and time complexity increases exponentially with increase in the number of scenarios. Thus contradicting the base assumption that using qualitative representations allow improvement to the computational efficiency for a given task. The authors do suggest the improvement of the current approach by replacing the QTC_B representation with a QTC_C representation that allows a finer control paradigm since it includes directional information(left-right) to be represented in addition to the nature of the existing motion(moving away-towards). Although this im-

2.3. Implementations utilizing qualitative representations for navigation in robots

plementation shows the utilization of the QTC calculi, it cannot be considered a robust implementation due to the lack of extensive testing and the limited experimentation that was carried out for this purpose.

- [15], This approach makes use of the qualitative trajectory calculus to depict relative motion between a human and a robot, in a restricted environment which in this case is a corridor. The use of qualitative representations to achieve robot trajectories that are perceived as safe and intuitive by humans is the main aim of this project and to that effect the ‘pass-by’(human and robot cross each other in opposite directions) scenarios are evaluated. The authors use ‘velocity costmaps based on the qualitative descriptions to limit the sample space of the dynamic window approach local planner to generate trajectories’ [15], that are safe for the robot and human as well as intuitive for the human. The authors combine the QTC_B and QTC_C calculus into a single calculus called the QTC_{BC} which allows the representation to switch between the QTC_B and QTC_C depending upon a distance threshold. This distance threshold is defined such that when the robot is in close proximity to the human agent the representation switches to QTC_C as this provides a more informed representation of the relative trajectories, at farther distances since it is sufficient to know whether the two objects are approaching each other or not, the QTC_B representation is used.

Conclusion The approach was tested by both simulation and application on a robot and the qualitative representation velocity costmaps far outperformed(in terms of minimum number of collisions) the costmaps that utilized cartesian coordinates as well as a naive dynamic window approach. This approach provides a concrete argument to the utility of qualitative representations in robot navigation as well as human robot interaction, yet it does not clarify the claim stating that the use of qualitative representations is more efficient when compared to a quantitative representation. Also, it’s evaluation on a single test scenario makes it likely that this approach is highly tuned to achieve greater success on the described task with no indication of it’s performance on a more generalized task such as navigation through a

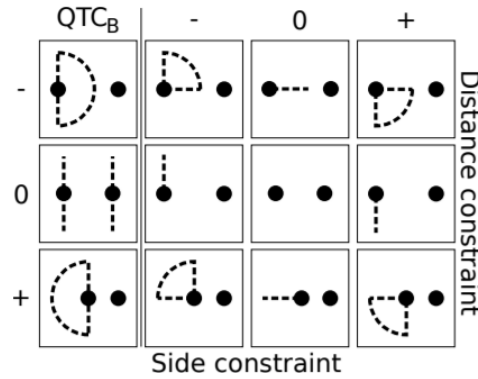


Figure 2.14: The velocity costmap prototypes. The area enclosed by the partial circle represents the low cost area, everything outside is assigned the highest cost value. The black dot on the right represents a human that can have any possible QTC state (except for QTC_B 0) [15].

corridor with or without multiple obstacles.

2.4 Limitations of previous work

The previous section brings to light a variety of implementations that utilize qualitative spatial representations in varying capacity to abstract spatial entities and relate them in a semantically cohesive manner. The concern that's highlighted immediately is that many of these approaches do not utilize the traditionally accepted qualitative calculi and hence often end up with provisional implementations that have been developed with reliance on a set of highly specific parameters, which if varied will most likely cause the developed algorithm to fail the given task. Thus showing that there is a lack of a generalized approach to the application of qualitative spatial representations in the domain of mobile robot navigation.

Furthermore all the approaches state the efficiency gain especially in terms of computation and power consumption as the motivation behind using qualitative spatial representations over quantitative ones, but none of them provide tangible proofs to establish the truth of this statement. There exists a lack of effort on this front as there are no comparative studies nor any empirical evidence to support this seemingly obvious claim.

Thus for the purpose of this project we will aim to address the above mentioned limitations, in the proposed approach.

Approach

The conclusions drawn in the previous chapter, allow us the liberty of focusing specifically on the two most promising qualitative calculi QTC_B and $ARGD$, for the purpose of developing an algorithm that centers around the utilization of either one or both of these calculi for the purpose of qualitatively representing physical space in our application of mobile robot navigation.

From the above analysis of the state of the art it is clear that the advantages of qualitative representations lie in the dealing with imprecise raw data, but it should be noted that these representations aren't a replacement for quantitative representation instead they are simply an alternative that can be harnessed to deal with scenarios where the need for crisp, precise data cannot be justified such as traversal in a fairly empty open spaces(halls, corridors etc.). Precise quantitative representations are still necessary when dealing with scenarios such as passing through a door.

3.1 Proposed approach

3.2 Implementation details

Methodology

This chapter aims to highlight both the hardware and software setup of the developed system. The integration of the software libraries and packages has been implemented and tested extensively on the ‘KUKA youBot’ which is the aforementioned hardware platform. The following sections briefly illustrate the applied hardware and explain the software packages and their integration with the QSRLib library, which allows us to express physical space qualitatively.

4.1 Hardware Setup

The applied robot platform for our application is the ‘KUKA youBot’. This is an omni-directional platform, equipped with a 5 Degree of freedom robotic arm, that features a two finger gripper. The robot base is equipped with two ‘Hokuyo URG-04LX’ laser range finders situated at the front and at the back respectively, this placement allows for robust localization and map-based navigation in known indoor environments [35]. Physically the dimensions of the robot are as follows length 58cm, width 38cm, height 14cm with a ground clearance of 2cm and a minimum and maximum velocity of 0.01m/s and 0.8m/s respectively [2]. The power to this applied platform comes from a 24 volt, 5 Ah lead-acid battery that has an approximate optimal runtime of 90 minutes, but this varies depending upon a multitude of factors such as the robot’s velocity, sensors used etc.



Figure 4.1: The youBot robot platform

The robotic arm plays host to a camera mounting which supports the ‘ASUS Xtion Pro Live’ RDB-D camera, which as the name suggests supports the perception of depth information in addition to the usual RGB or raw image data. This RGB-D camera has a detection range of 80cm - 3.5m with a field of view limited to 58° , 45° , 70° horizontally, vertically and diagonally respectively [39]. The image size for this camera is ‘320x240’ for a QVGA format at 60 frames per second, also being highly compatible with the ‘OpenNi development framework’ ensures it’s easy integration with the ROS packages by the ‘b-it-bots RoboCup@Work’ team, which has already developed scene segmentation and object detection applications centered around this sensor. The stock internal computer that comes issued with the youBot has been replaced with a ‘Intel Core i5’ processor that facilitates highly computational perception tasks to be run directly on the platform [35].

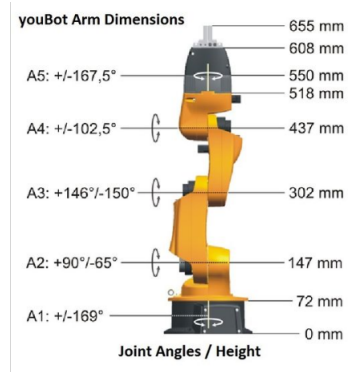


Figure 4.2: youBot arm at full extension

4.2 Software Framework

The software framework underpinning the applied robot platform has been developed by the ‘b-it bots @Work’ team and is based on ROS(Kinetic Kame version) or the robot operating system [33], which provides a modular and distributed structure to design a functional system based on the developer’s requirements. This modular architecture provides a rapid and robust communication infrastructure that is based on actions, services and clients to interchange data amongst the various different functional, software components of the applied platform. The framework provides an effective and efficient medium for interfacing various sensors and actuators such as laser scanners, cameras etc.

Another merit of the robot operating system is it’s provision of advanced tools for visualizing and testing various types of data and troubleshooting the entire system in cases of failures or errors. One such heavily utilized tool was ‘rosbag’, used particularly to capture data [25] and evaluate the developed implementation with varying parameters but always on the same set of captured data.

4.3 Integration of Qualitative representations

The current software framework, set-up on the robot consists of numerous packages that allow the control of it’s base as well as arm actuators while also providing an effective interface to it’s various sensors. This modular approach facilitates the use of these small components to develop a higher level task. In the instance of ‘Qualitative spatial representations’ we need to access the raw RGB image from the camera to detect features or objects and further extract their approximated pose in order to build a qualitative relation with respect to the robot. The nature of this relation depends upon the type of qualitative calculi that is being implemented in order to define these abstractions.

As the objective of this project is to show an generalized and efficient utilization of the existing qualitative calculi, we do not develop any of these calculi from scratch, instead deciding to exploit an existing qualitative spatial representations library called ‘QSRLib’ [23], this library contains ROS compatible python implementations of the various qualitative calculi, as discussed in the previous chapter.

Although this library can be used either as a standalone python package or a ROS catkin package, we use it primarily with ROS and hence shall focus on it's installation and integration with the same. The 'qsr_lib' package is the one that is being used in our implementation and has system dependencies on 'numpy' and 'matplotlib'. Installing the library is extremely easy as it involves directly cloning the repository(https://github.com/strands-project/strands_qsr_lib.git) from git, and moving the 'qsr_lib' package into the 'src' folder of our catkin workspace [1].

[1], [23]The pre-requisites for using any of the qualitative calculi implemented in the library is input data such as distinctive object id's or names for the various objects amongst which a qualitative relation is desired, a time-series of the states of the perceived objects and the Cartesian coordinates for each of the objects at every instance of the time series. This information is packaged into a custom input data object that is the default input data format of the library. Additional information such as the size of the object may also be included in the input data object, but it is mandatory to include the name of the qualitative calculi for which the qualitative spatial relations are to be computed. This input data structure is sent to a QSRLib service in the form of a request message, the server then computes the relationships and send the output in the form of a response message(client-service architecture in ROS) that details the qualitative relations between the objects constrained by their respective time stamps. The library comes built with the necessary functions that can be used to convert raw data into the data structure format required by the library. The output of the QSRLib can then be further inspected and employed to make decisions regarding the movement or path of the applied mobile platform.

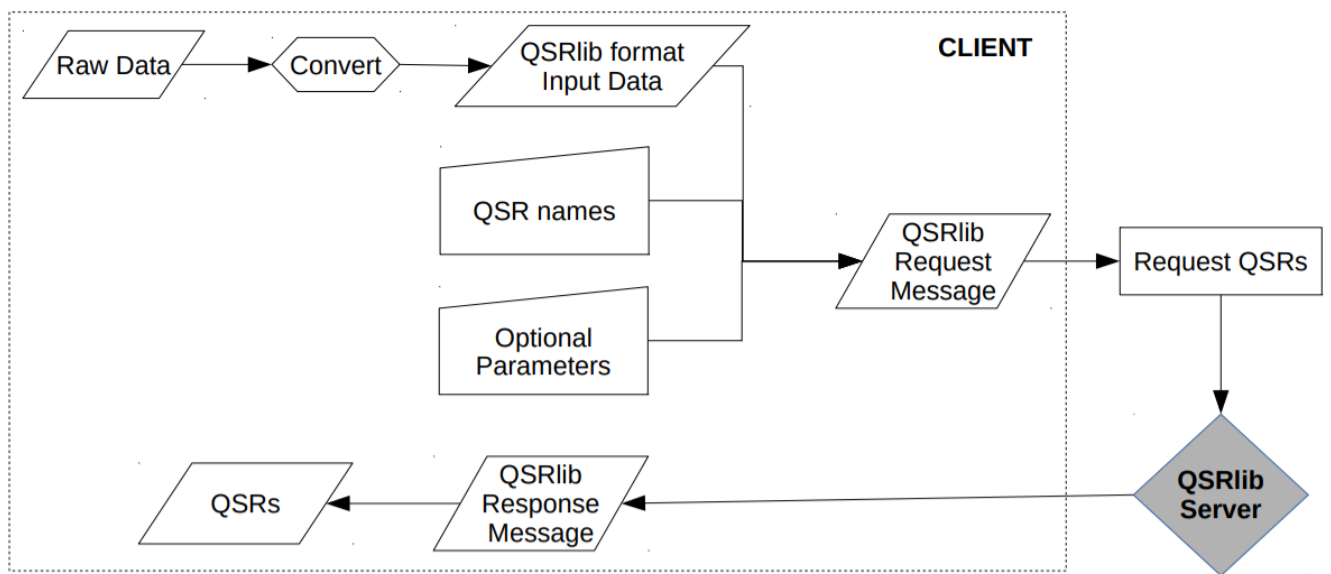


Figure 4.3: A flow chart detailing the inner workings of the QSRLib library [1], [23].

Experimental Evaluation

The primary goal of this chapter is to provide vital information regarding the empirical evaluation that was carried out to validate the proposed approach. The following sections will discuss the practical use cases for the developed system and give a brief overview of the general test setup of the performed experiments before diving into the details of the experiments themselves. A logical analysis of the obtained results will be performed to conclude the chapter.

5.1 Use Cases

The main aim of this project is to evaluate the efficiency paradigm of qualitative spatial representations for navigation in mobile robots, especially in closed indoor spaces where quantitative representations of the physical space are considered excessive and unnecessary. Therefore keeping in mind these preconditions we define the following possible use cases.

Use case: Navigating in a corridor environment

A mobile robot is tasked with navigating from point ‘A’ to point ‘B’ in a corridor environment such that it should avoid collision with the walls and any other static or dynamic obstacles if they exist in its path. Furthermore the robot’s movement should be such that it avoids any sudden motions that may seem unsafe or unintuitive to an human agent who might interact with the robot. Also chiefly,

the robot must achieve this path traversal in a manner that is as efficient as possible ,while dealing with imprecise information about the environment or in extreme cases lack of complete information about the environment.

Resulting Requirements

Ideally it is desired that any new functionality that is being implemented must be highly generalizable, but keeping in mind the given problem it is unrealistic to expect a ‘one size fit’s all’ implementation that works impeccably for all imaginable situations without any restrictions or compromises. Hence a list of requirements resulting from the problem statement and the above described use case is presented below:

- The starting position should be irrelevant when navigating the corridor.
- The detection of the markers or features should be robust with respect to a reasonable speed of the robot.
- The number of markers or features should not adversely affect the robot’s behavior.
- The camera used should have a reasonable field of view so that it can see both the walls and their respective features at any given point of time.
- The camera should be able to capture the features reasonably well, irrespective of the lighting conditions.
- The motion profile of the robot should be a smooth and not disruptive.
- It should be able to navigate any corridor irrespective of it’s size or the color of it’s walls.

5.2 Data collection

During the development stage of the algorithm it was tested continuously against a set of collected data that served as a simulation for corresponding real world situations. This method served as a good test to ensure robustness of the individual

software components as well as the entire system once it was combined together. The data was collected by manually driving around the robot in a corridor and recording the output of the camera video stream(RGB) after markers had been attached to the walls of the corridor. This simulated data served as a backbone for understanding some of the constraints of the developed algorithm such as the minimum number of markers required, the field of view of the camera, the position of the camera, the velocity of the robot and the orientation of the robot to ensure that both the walls and their respective markers are visible. The collected data simulated conditions such as,

- The robot moving along the center of the corridor.
- The robot moving along the left/right wall.
- The robot moving diagonally across the corridor.
- The robot following a zig-zag pattern along the corridor.

In all these collected videos a set of two markers was placed on the opposing walls such that both the markers lie on the same axis that is perpendicular to the walls, also the markers were placed at equidistant intervals.

5.3 General Test Setup

The testing of the developed algorithm was carried out in a two step manner wherein during the first step we evaluated the performance of the two implemented calculi for the task of corridor navigation. The performance is evaluated based on three criteria, the effect of the starting positions, the effect of the marker positions and the number of markers. The evaluation was judged based on the number of possible control paradigms that ensued in a crash with either of the walls. This led to the selection of the calculi with the least number of crashes, the selected calculi was then compared against the existing map based navigation approach which uses quantitative spatial representations and has been implemented on the applied robot platform by the ‘b-it bots’ team. This comparison yields a evaluation of the efficiency paradigms for both the approaches.

A general setup of the performed experiments is presented below, with the specifics of each experiment discussed in a later section.

Experiment Variables:

- Initial position and orientation of the robot.
- Field of View of the camera.
- Lighting conditions of the corridor.
- Initial Position of the camera.
- Position of the markers relative to the fixed camera position.
- Position of the markers relative to each other.
- Battery voltage.
- Range of the wireless network.

Software Requirements:

- ROS Kinetic
- Python 2.7 or higher
- Qsr_lib package
- Qsr_nav package
- Mir_bringup package
- Mir_moveit_youbot_brsu_4 package
- Moveit_commander package

Hardware Requirements:

- Kuka Youbot
- PC capable of running ROS
- Remote joystick
- Power supply
- Aruco markers
- Asus Xtion Pro camera

5.4 Experiments

5.4.1 Experiments for QTCB calculi

Testing the navigational capabilities of the QTCB calculus in a indoor corridor environment

The individual experiments and their respective analysis have been presented in a tabular format in the figures 5.1, 5.2 and 5.3.

Evaluation

From the experiment tables presented in the following figures(5.1,5.2,5.3) it is clear to see that the main reason for failure of the QTCB calculus is the limited FOV of the camera used. Also the tabular structure makes it clear to understand that the the algorithm is robust enough to function with an arbitrary number and placement of the markers with the only failure occurring when it cannot detect atleast two markers placed on opposite walls. Additionally out of all the test scenarios the only clear failure(irrespective of starting position) of the algorithm was when the markers were placed in a staggered manner along the walls, this was also due to the fact that the camera's FOV is limited and prevented it from detecting both the markers at all instances of time. All the experiments were carried out such that they travel from point 'A' to 'B' and back from 'B' to 'A' this was done to ensure

that the detection component isn't favorable to any one side or travel and is robust enough to function even if the markers on the opposing walls were interchanged. Out of a set of 12 experiments conducted the QTCB representation was able to perform collision free navigation in all but 1 set of experiments giving it a success rate of 83.3 percent.

5.4.2 Experiments for ARGD calculi

Testing the navigational capabilities of the ARGD calculus in a indoor corridor environment

The individual experiments and their respective analysis have been presented in a tabular format in the figures 5.4, 5.5 and 5.6. For the ARGD calculus the distance thresholds used for discretizing continuous space are an additional experiment variable that affects the representation of physical space.

Evaluation

From the experiment tables presented in the following figures(5.4, 5.5, 5.6) it is clear to see that there are two main reasons for failure of the ARGD calculus, the first is the limited FOV of the camera used and the second is the inability of the calculi to distinguish between two objects that lie in the same distance threshold due to this the number of failure cases is higher for the ARGD when compared to the QTC_B . Also the tabular structure makes it clear to understand that the the algorithm isn't robust enough to function with any arbitrary number and placement of the markers with collisions occurring regularly in nearly all the test cases. One of the clearest cases of failure was when the markers were placed in a staggered manner along the walls, this was a clear illustration of the ARGD being an insufficient calculi when it comes to dealing with mobile objects, with the need for fine distinctions between the objects lying in the same distance threshold being clearly highlighted in this case. All the experiments were carried out such that they travel from point 'A' to 'B' and back from 'B' to 'A' this was done to ensure that the detection component isn't favorable to any one side or travel and is robust enough to function even if the markers on the opposing walls were interchanged. Out of a set of 12 experiments

conducted the ARGD representation was able to perform collision free navigation in all but 4 sets of experiments giving it a success rate of 66.6 percent.

5.4.3 Common Observations

- All the movements observed during the experiments are gradual and there is no sudden change to the robot's velocity or speed.
- The algorithm can be made more robust if the *ARGD* and the *QTC_B* calculus can be combined, this is possible with the current implementation but is complicated as the number of rulesets would increase exponentially with respect to the objects in consideration.
- In the current setup the algorithm is inherently dependent on the perception module and any changes to this module would likely warrant changes to the entire setup especially in the case of the distance based *ARGD* calculus, the *QTC_B* calculus on the other hand would only require that the number of objects in consideration be changed to the desired number.
- The current setup uses small velocity values to control the robot with the maximum value being 0.1 m/s and the lowest being 0.02 m/s.
- Improvements to the current algorithm can also be made using different setup of the cameras where two cameras facing the opposite wall may be used.
- The current implementation also uses a time based filter to build relations only when two or more markers are detected simultaneously at similar timesteps, in cases where only a single object is used to build the relation with the robot this filtering must be removed to ensure successful navigation.
- Also if more than two objects are to be used when calculating the motion updates then, filtering has to be done to ensure that there is no repetition when building the relations that are consequently used for the decision making process.

5.4.4 Conclusion

From the above breakdown of the results it is easy to see that the QTC_B calculi outperforms the $ARGD$ calculi when it comes to the task of collision free robot navigation. As discussed above this is attributed to the fact that the distance calculi lacks the tools to distinguish between markers or features that lie in the same distance thresholds, furthermore due to the limited representation capabilities there exist very few instances where a clear distinction between the markers can be made hence resulting in a fewer number of instances where suitable control commands can be exercised. Beyond this, both the calculi suffered failures due to the limited FOV of the camera as it prevented the detection of the markers lying on the opposing walls whenever the robot moved close to either of the walls(it remains crucial to the algorithm that atleast two markers are detected simultaneously, when placed along the same axis or otherwise). To compliment the validity of the results it is worth mentioning that the $ARGD$ calculus works on abstractions of spatial distances and was developed for representing and reasoning about static objects whereas the QTC_B calculi works on abstractions of relative trajectories between two objects and was developed representing and reasoning about mobile objects, hence it is obvious that it should perform better than the $ARGD$ calculus for the given task. Thus based on this empirical evidence we select the QTC_B calculi to compare and evaluate the efficiency paradigms against a quantitative map based representation.

5.5 Evaluation of the efficiency of qualitative representations

Based on the above validation efficiency of the QTC_B calculi was compared against the map based navigation technique that utilized quantitative spatial representations, on the task of navigating from point 'A' to 'B' in the corridor. The starting positions were kept approximately same for the purpose of this testing and the velocity values were ensured to be same. Furthermore since we would like to evaluate the battery consumption a fully charged battery was used during the tests for each representation. The experiment was repeated thrice for each of

the representations so as to obtain any variance in the values and ensure accurate resulting values. For the purpose of this evaluation the QTC_B experiment was setup so that the markers always lay on the same perpendicular axis to the wall and the number of markers on both the walls was the same, the starting position was always along the center of the corridor.

Need to add the battery values here

5.6 Conclusion

From the above evaluation it is obvious(or not ?) that the qualitative representations are more efficient in comparison to quantitative representations. This satisfies our initial aim of providing conclusive proof to show the improved efficiency of qualitative representations and evaluating it's utility for the same.

5.6. Conclusion

Placement of markers	Pattern of the marker placements	Expected results	Obtained results and analysis
Along a common axis perpendicular to the opposing walls.	Equal number of markers on both the walls	<ul style="list-style-type: none"> * Successful navigation of the corridor while avoiding collision with the walls. * A highly discontinuous motion profile with jerky motion. * A video log of the performed experiment. 	<ul style="list-style-type: none"> * The robot managed to successfully navigate the corridor. * The motion profile is smooth and not jerky as previously thought. * The robot maintains a path that is along the center of the corridor. * No collision cases were observed. * It remains crucial to the algorithm that atleast two markers are detected simultaneously, when placed along the same axis.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> * Successful navigation of the corridor while avoiding collision with the walls. * A highly discontinuous motion profile with jerky motion. * A video log of the performed experiment. * A collision case due to uneven number of markers are placed on the opposing walls. 	<ul style="list-style-type: none"> * The robot is able to successfully navigate through the corridor despite of the uneven placement of the markers on the opposing walls. * The motion profile is smooth and not jerky as previously thought. * The robot tries to move along the center of the corridor. * Collision occurs when the robot gets too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	Staggered along the wall	<ul style="list-style-type: none"> * A highly discontinuous motion profile with jerky motion. * A video log of the performed experiment. * A collision case when moving too close to the walls. * A collision case due to staggered placement of the markers 	<ul style="list-style-type: none"> * The robot almost always fails. The failure can be attributed to the irregular placement of the markers on the wall. * The motion profile is smooth and not jerky as previously thought. * The robot tries to move along the center of the corridor, but due to lack of any motion updates ends up moving diagonally towards either wall and collides with it. * Collision occurs when the robot gets too close to either wall as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	Equal number of markers on both the walls	<ul style="list-style-type: none"> * A highly discontinuous motion profile with jerky motion. * A zig-zag pattern to the robot's motion. * A video log of the performed experiment. * A collision case due to staggered and uneven placement of the markers. 	<ul style="list-style-type: none"> * The robot is able to successfully navigate through the corridor despite of the staggered, uneven placement of the markers on the opposing walls. * The motion profile is smooth and not jerky as previously thought. * The motion pattern is moderately zig-zag as previously assumed. * The robot tries to move along the center of the corridor. * Collision occurs when the robot gets too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> * A highly discontinuous motion profile with jerky motion. * A zig-zag pattern to the robot's motion. * A video log of the performed experiment. * A collision case due to staggered and uneven placement of the markers. 	<ul style="list-style-type: none"> * The robot is able to successfully navigate through the corridor despite of the staggered, uneven placement of the markers on the opposing walls. * The motion profile is smooth and not jerky as previously thought. * The motion pattern is moderately zig-zag as previously assumed. * The robot tries to move along the center of the corridor. * Collision occurs when the robot gets too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.

Figure 5.1: Table of conducted experiments for QTC_B and their respective analysis for a starting position that is along the center of the corridor.

Placement of markers	Pattern of the marker placements	Expected results	Obtained results and analysis
Along a common axis perpendicular to the opposing walls	Equal number of markers on both the walls	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case when moving too close to the walls 	<ul style="list-style-type: none"> *The robot managed to successfully navigate the corridor, only if the starting position still allowed the camera to detect both the markers. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case when moving too close to the wall. 	<ul style="list-style-type: none"> *The robot managed to successfully navigate the corridor as long as there were atleast two observable markers on the opposite walls. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor in a diagonal fashion. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
Staggered along the wall	Equal number of markers on both the walls	<ul style="list-style-type: none"> *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case when moving too close to the walls. *A collision case due to staggered placement of the markers 	<ul style="list-style-type: none"> *The robot almost always fails. The failure can be attributed to the irregular placement of the markers on the wall. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor, but due to lack of any motion updates ends up moving diagonally towards the opposite wall and collides with it. *Collision occurs when the robot is too close to the wall as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case due to staggered and uneven placement of the markers. *A diagonal zig-zag path towards the center of the corridor. 	<ul style="list-style-type: none"> *The robot is able to successfully navigate through the corridor as long as it can see atleast two markers on the opposite walls. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor in zig-zag fashion. *Collision occurs when the robot gets too close to the wall as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.

Figure 5.2: Table of conducted experiments for QTC_B and their respective analysis for a starting position that is along the right wall of the corridor.

Placement of markers	Pattern of the marker placements	Expected results	Obtained results and analysis
Along a common axis perpendicular to the opposing walls.	Equal number of markers on both the walls	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case when moving too close to the walls 	<ul style="list-style-type: none"> *The robot managed to successfully navigate the corridor only if the starting position still allowed the camera to detect both the markers. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case when moving too close to the wall 	<ul style="list-style-type: none"> *The robot managed to successfully navigate the corridor as long as there were atleast two observable markers on the opposite walls. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor in a diagonal manner. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
Staggered along the wall	Equal number of markers on both the walls	<ul style="list-style-type: none"> *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case when moving too close to the walls. *A collision case due to staggered placement of the markers 	<ul style="list-style-type: none"> *The robot almost always fails. The failure can be attributed to the irregular placement of the markers on the wall *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor, but due to lack of any motion updates ends up moving diagonally towards the opposite wall and collides with it. *Collision occurs when the robot is too close to the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *A highly discontinuous motion profile with jerky motion. *A video log of the performed experiment. *A collision case due to staggered and uneven placement of the markers. *A diagonal zig-zag path towards the center of the corridor. 	<ul style="list-style-type: none"> *The robot is able to successfully navigate through the corridor as long as it can see atleast two markers on the opposite walls. *The motion profile is smooth and not jerky as previously thought. *The robot tries to move towards the center of the corridor in zig-zag fashion. *Collision occurs when the robot gets too close to the wall as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.

Figure 5.3: Table of conducted experiments for QTC_B and their respective analysis for a starting position that is along the left wall of the corridor.

Chapter 5. Experimental Evaluation

Placement of markers	Pattern of the marker placements	Expected results	Obtained results and analysis
Along a common axis perpendicular to the opposing walls.	Equal number of markers on both the walls	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly smooth motion profile without discontinuous jerky motion. *A video log of the performed experiment. 	<ul style="list-style-type: none"> *When starting from a central position along the walls, the robot managed to successfully navigate the corridor. *The motion profile is smooth as previously theorized. *The robot tries to move along the center of the corridor.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly smooth motion profile without any jerky motion. *A video log of the performed experiment. *A collision case when robot gets too close to the walls *A collision case when uneven number of markers are placed on the opposing walls. 	<ul style="list-style-type: none"> *When starting along the center of the corridor, the algorithm almost always fails as the numerous markers always lie in the same distance range and hence no tangible update to the robots motion can be made also another factor contributing to the failure is that the markers are not detected as they move out of the FOV of the camera as the robot moves forward or diagonally. *The motion profile is smooth as previously thought. *Collision occurs when the robot gets too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
Staggered along the wall	Equal number of markers on both the walls	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly smooth motion profile without any jerky motion. *A video log of the performed experiment. *A collision case when robot gets too close to the wall *A collision case when markers are placed in a staggered manner on the opposing walls. 	<ul style="list-style-type: none"> *The collision is unavoidable in this scenario, this failure is attributed to the lack of extremely fine values for the distance thresholds and also to the limited FOV of the camera, which often loses track of the markers on the opposing wall as the robot moves along the corridor(diagonally). *The motion profile is smooth as previously thought. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *A highly smooth motion profile without jerky motion. *A video log of the performed experiment. *A collision case due to staggered and uneven placement of the markers. *A zig-zag path along the center of the corridor. 	<ul style="list-style-type: none"> *When starting from a position along the center of the corridor the robot moves along the center. *The motion profile is smooth as previously thought. *Collision almost never occurs as there is always atleast one marker on the opposite wall that is detected at the same instance of time.

Figure 5.4: Table of conducted experiments for *ARGD* and their respective analysis for a starting position that is along the center of the corridor.

Placement of markers	Pattern of the marker placements	Expected results	Obtained results and analysis
Along a common axis perpendicular to the opposing walls.	Equal number of markers on both the walls	<p>*Successful navigation of the corridor while avoiding collision with the walls.</p> <p>*A highly smooth motion profile without any jerky motion.</p> <p>*A video log of the performed experiment.</p> <p>*A collision case when moving or starting from a position too close to the wall</p>	<p>*When starting from a position close to the right wall the robot moves diagonally towards the opposite wall and will crash as the markers go out of the FOV. In cases where the markers are detected simultaneously along the same axis the robot showed a tendency to move along the center of the corridor and the ability to recover from possible collision cases.</p> <p>*The motion profile is smooth as previously thought.</p> <p>*Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made</p>
	More number of markers on one of the walls in comparison to the other wall	<p>*Successful navigation of the corridor while avoiding collision with the walls.</p> <p>*A highly smooth motion profile without any jerky motion.</p> <p>*A video log of the performed experiment.</p> <p>*A collision case when moving or starting from too close to the wall</p> <p>*A collision case when uneven number of markers are placed on the opposing walls.</p>	<p>*When starting from a position close to the right wall the robot moves along the wall or collides, this depends on whether the FOV of the camera if the markers are detected simultaneously in the same frame then collision can be avoided otherwise no motion updates are performed and the robot will crash as the markers go out of the FOV.</p> <p>*The motion profile is smooth as previously thought.</p> <p>*Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made</p>
Staggered along the wall	Equal number of markers on both the walls	<p>*Successful navigation of the corridor while avoiding collision with the walls.</p> <p>*A highly smooth motion profile without any jerky motion.</p> <p>*A video log of the performed experiment.</p> <p>*A collision case when starting or moving too close to the wall</p> <p>*A collision case when markers are placed in a staggered manner on the opposing walls.</p>	<p>The collision is unavoidable in this scenario , this failure is attributed to the lack of extremely fine values for the distance thresholds and also to the limited FOV of the camera, which often loses track of the markers on the opposing wall as the robot moves along the corridor(diagonally).</p> <p>*The motion profile is smooth as previously thought.</p> <p>*Collision occurs when the robot is too close to the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.</p>
	More number of markers on one of the walls in comparison to the other wall	<p>*A highly smooth motion profile without jerky motion.</p> <p>*A video log of the performed experiment.</p> <p>*A collision case due to staggered and uneven placement of the markers.</p> <p>*A diagonal zig-zag path towards the center of the corridor.</p>	<p>*When starting from a position close to the right wall the robot moves along the wall or diagonally towards the opposite wall, this depends on the FOV of the camera and on detection of the opposing set of markers.</p> <p>*The motion profile is smooth as previously thought.</p> <p>*Collision almost never occurs as there is always atleast one marker on the opposite wall that is detected at the same instance of time</p>

Figure 5.5: Table of conducted experiments for *ARGD* and their respective analysis for a starting position that is along the right wall of the corridor.

Chapter 5. Experimental Evaluation

Placement of markers	Pattern of the marker placements	Expected results	Obtained results and analysis
Along a common axis perpendicular to the opposing walls.	Equal number of markers on both the walls	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly smooth motion profile without any jerky motion. *A video log of the performed experiment. *A collision case when moving or starting from a position too close to the wall 	<ul style="list-style-type: none"> *When starting from a position close to the left wall the robot moves diagonally towards the opposite wall and will crash as the markers go out of the FOV. In cases where the markers are detected simultaneously along the same axis the robot showed a tendency to move along the center of the corridor and the ability to recover from possible collision cases. *The motion profile is smooth as previously thought. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly smooth motion profile without any jerky motion. *A video log of the performed experiment. *A collision case when moving or starting from too close to the wall *A collision case when uneven number of markers are placed on the opposing walls. 	<ul style="list-style-type: none"> *When starting from a position close to the left wall the robot moves along the wall or collides, this depends on whether the FOV of the camera if the markers are detected simultaneously in the same frame then collision can be avoided otherwise no motion updates are performed and the robot will crash as the markers go out of the FOV. *The motion profile is smooth as previously thought. *Collision occurs when the robot is too close to either of the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
Staggered along the wall	Equal number of markers on both the walls	<ul style="list-style-type: none"> *Successful navigation of the corridor while avoiding collision with the walls. *A highly smooth motion profile without any jerky motion. *A video log of the performed experiment. *A collision case when starting or moving too close to the wall *A collision case when markers are placed in a staggered manner on the opposing walls. 	<p>The collision is unavoidable in this scenario, this failure is attributed to the lack of extremely fine values for the distance thresholds and also to the limited FOV of the camera, which often loses track of the markers on the opposing wall as the robot moves along the corridor(diagonally).</p> <ul style="list-style-type: none"> *The motion profile is smooth as previously thought. *Collision occurs when the robot is too close to the walls as the opposite set of markers goes out of the FOV of the camera and hence no update to the robot's motion can be made.
	More number of markers on one of the walls in comparison to the other wall	<ul style="list-style-type: none"> *A highly smooth motion profile without jerky motion. *A video log of the performed experiment. *A collision case due to staggered and uneven placement of the markers. *A diagonal zig-zag path towards the center of the corridor. 	<ul style="list-style-type: none"> *When starting from a position close to the left wall the robot moves along the wall or diagonally towards the opposite wall, this depends on the FOV of the camera and on detection of the opposing set of markers. *The motion profile is smooth as previously thought. *Collision almost never occurs as there is always atleast one marker on the opposite wall that is detected at the same instance of time.

Figure 5.6: Table of conducted experiments for *ARCD* and their respective analysis for a starting position that is along the left wall of the corridor.

6

Conclusions

6.1 Contributions

6.2 Lessons learned

6.3 Future work

A

Design Details

Your first appendix

B

Parameters

Your second chapter appendix

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