

⑨ Kinematics of cm^n



$$\theta_c = \theta_1 + \theta_2 + \theta_3$$

$$x_c = L_1 \cos \theta_1 + L_2 \cos(\theta_2 + \theta_1) + L_3 \cos(\theta_1 + \theta_2 + \theta_3)$$

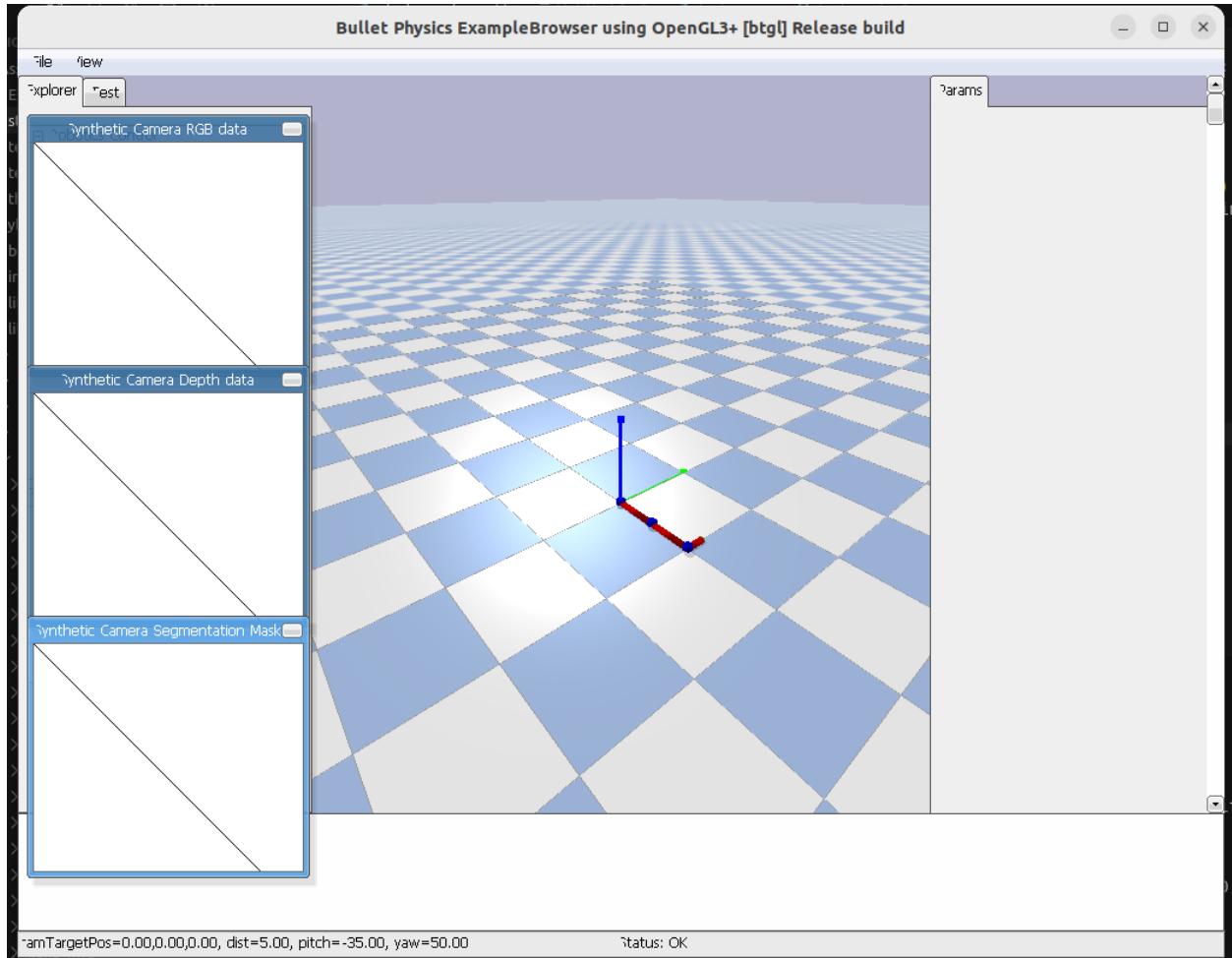
$$y_c = L_1 \sin \theta_1 + L_2 \sin(\theta_2 + \theta_1) + L_3 \sin(\theta_1 + \theta_2 + \theta_3)$$

While running the code set variable

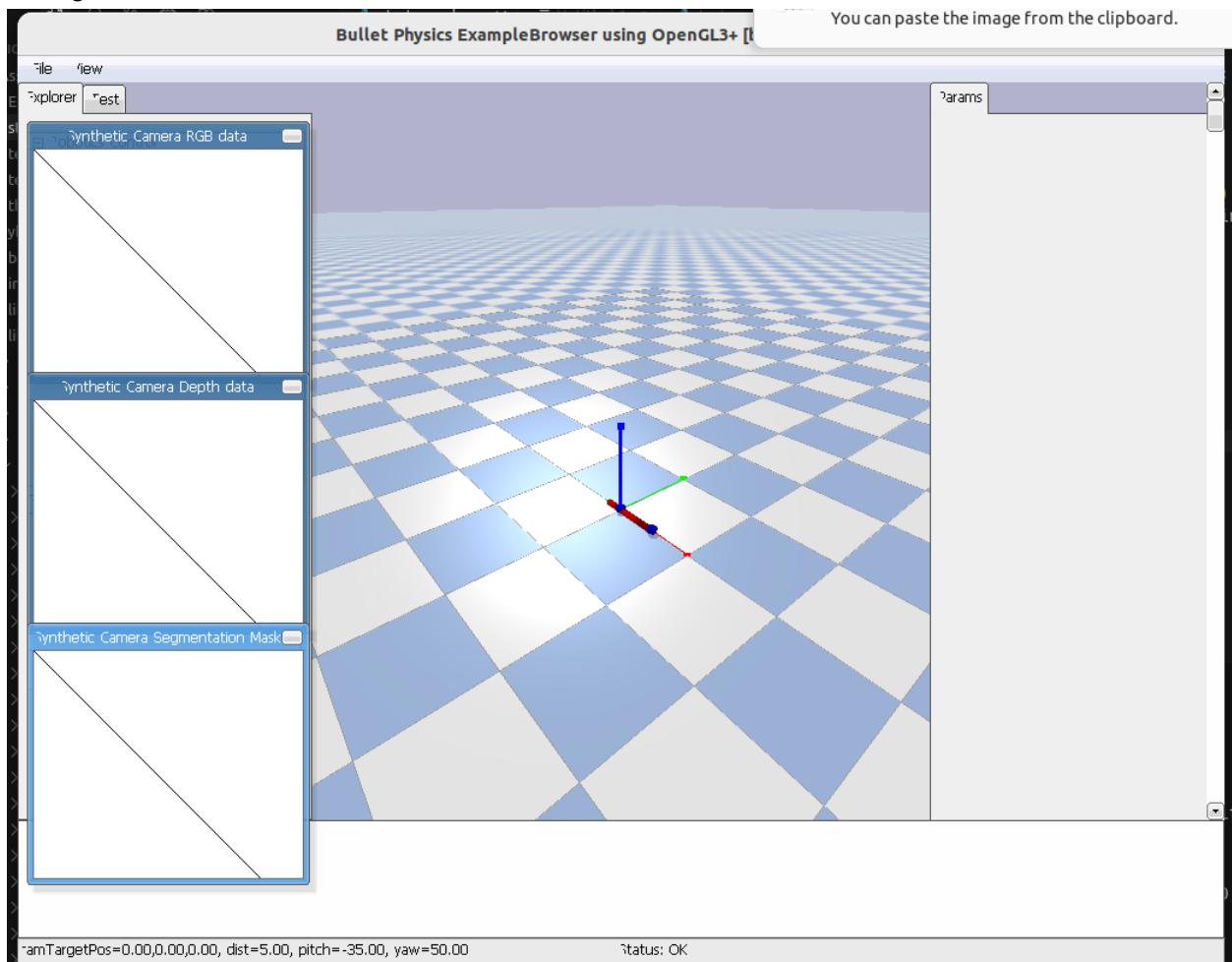
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run_part_no = None # 1 for open loop, 2 for closed loop, 3 for null space  
control
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Q3)

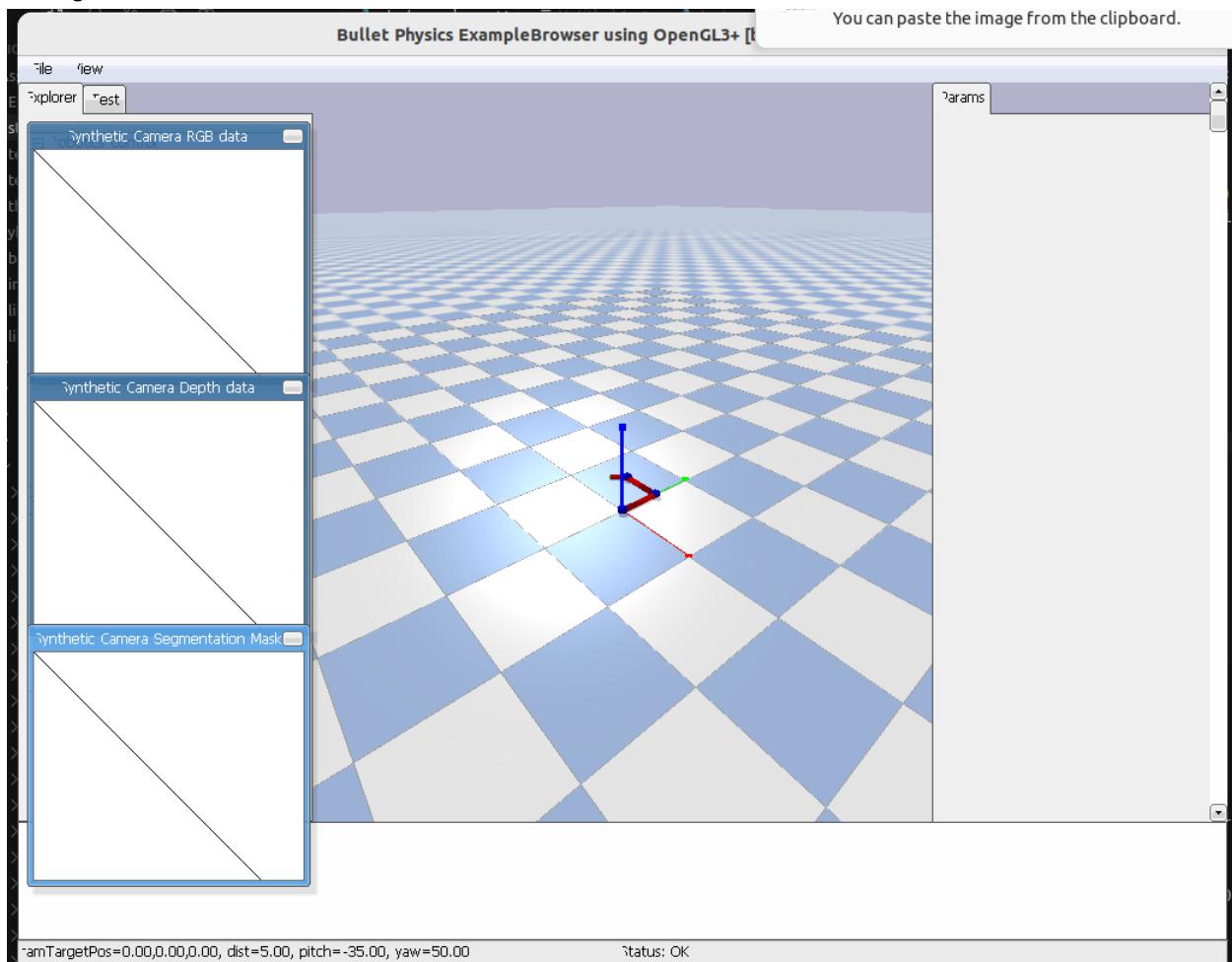
Config1



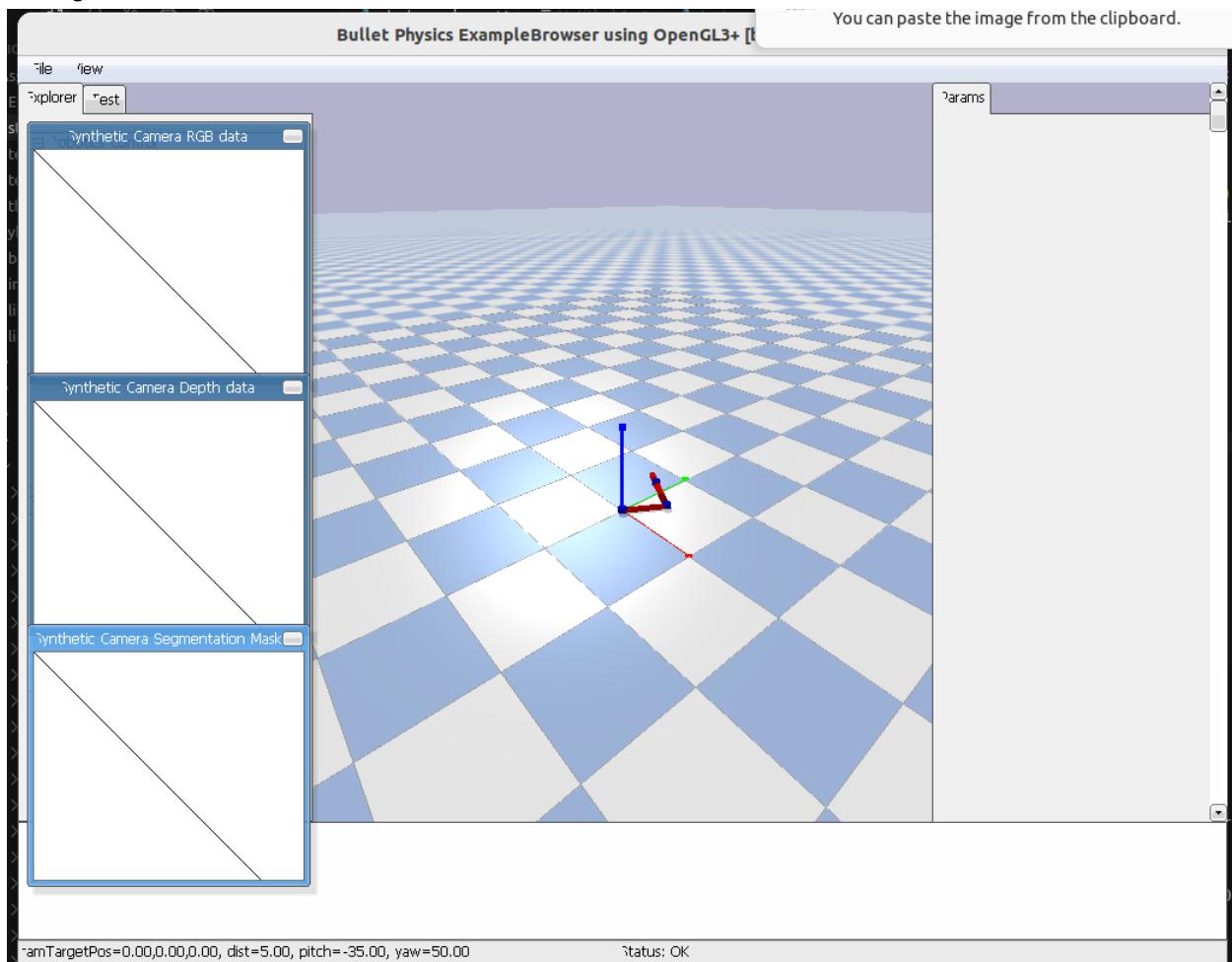
Config2



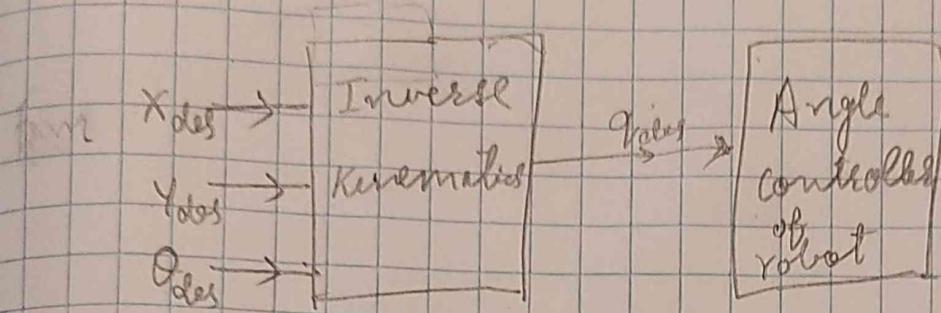
Config3



Config4



open Loop

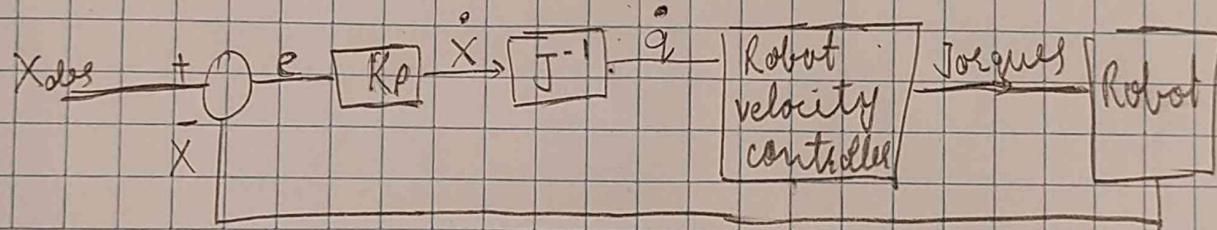


$q_{des} \rightarrow$ joint angle commands.

Closed loop

$X_{des} = (x_{des}, y_{des}, \theta_{des}) \rightarrow$ desired state

$X = (x, y, \theta) \rightarrow$ current state



$$e = X_{des} - X$$

$$\dot{X} = K_p e$$

$\dot{q} = J^{-1} K_p e \rightarrow$ velocity commands for joints

(5)

$$x_{\text{des}} = at^3 + bt^2 + ct + d$$

$$\begin{matrix} \psi \\ 0 \end{matrix} \begin{matrix} k \\ n \end{matrix}$$

at

$$x(0) = n_0$$

$$x(t) = n_1$$

$$\dot{x}(0) = 0$$

$$\ddot{x}(1) = 0$$

$$\begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 \\ 3 & 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} n_0 \\ n_1 \\ 0 \\ 0 \end{bmatrix}$$

$$k = \frac{y_1 - y_0}{n_1 - n_0}$$

6) closed loop

$$\theta_{\text{des}} = 0 = \theta_1 + \theta_2 + \theta_3$$

$$X_{\text{des}} = \begin{bmatrix} n_{\text{des}} \\ f_{\text{des}} \\ \theta_{\text{des}} \end{bmatrix}$$

$$c = X_{\text{des}} - X$$

$$q_{\text{des}} = J^{-1} K_p e \quad \leftarrow \text{where } J^{-1} = J^T [JJ^T + \lambda^2 I]$$

⑥ For null space

cost function

$$J(\theta) = \theta_2^2 + \theta_3^2 \rightarrow \text{Minimise}$$

$\theta_2 \rightarrow 0, \theta_3 \rightarrow 0$ ensures links are far apart

$$\nabla J(\theta) = \begin{bmatrix} 0 \\ 2\theta_2 \\ 2\theta_3 \end{bmatrix} \quad \begin{array}{l} \text{Minimise } J(\theta) \text{ for} \\ \text{max separations} \end{array}$$

$$\dot{q}_{\text{null}} = - (I - J^{-1}J) \nabla J(\theta) * k$$

tuning

Parameter

$$\dot{q}_i = \dot{q}_{\text{des}} + \dot{q}_{\text{null}}$$

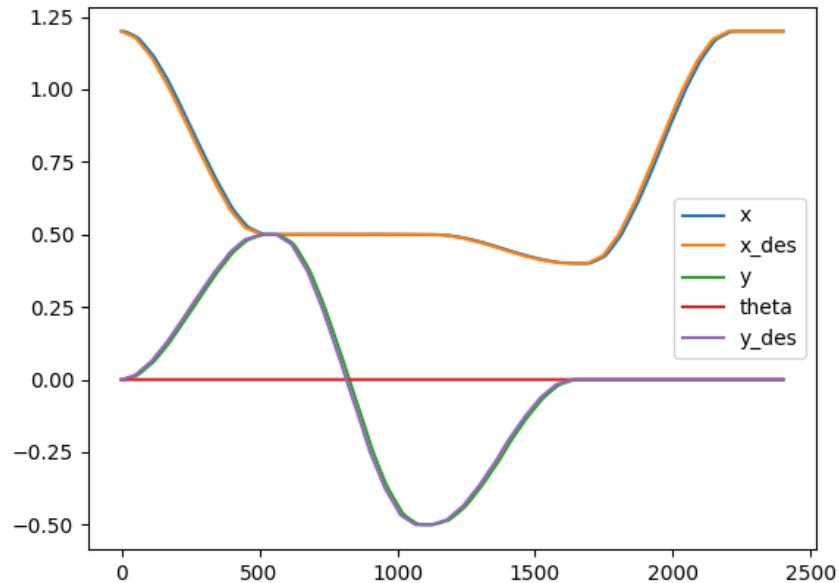
↑
closed
loop

↑
Null space

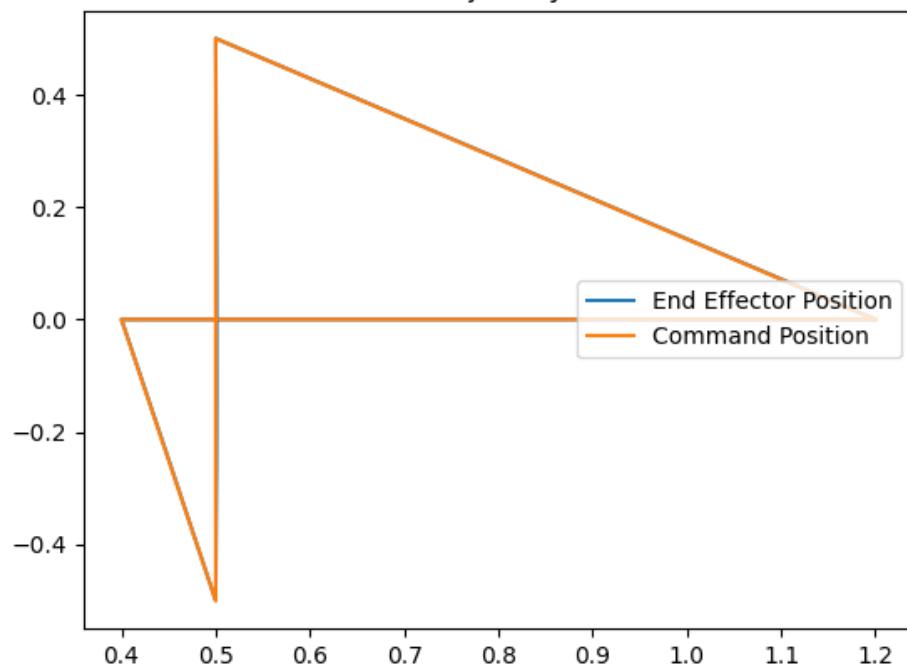
Q5) Open loop control

While running the code set variable

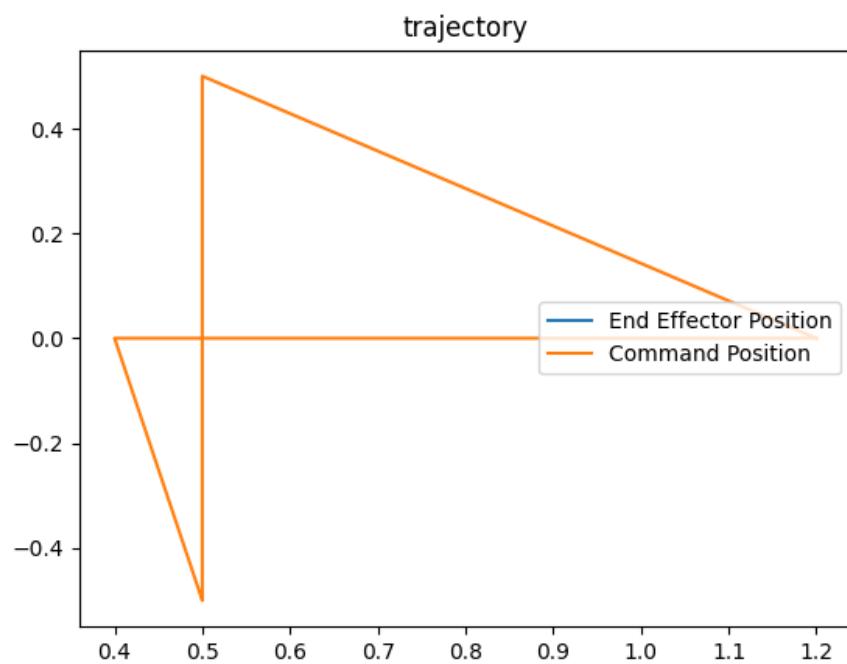
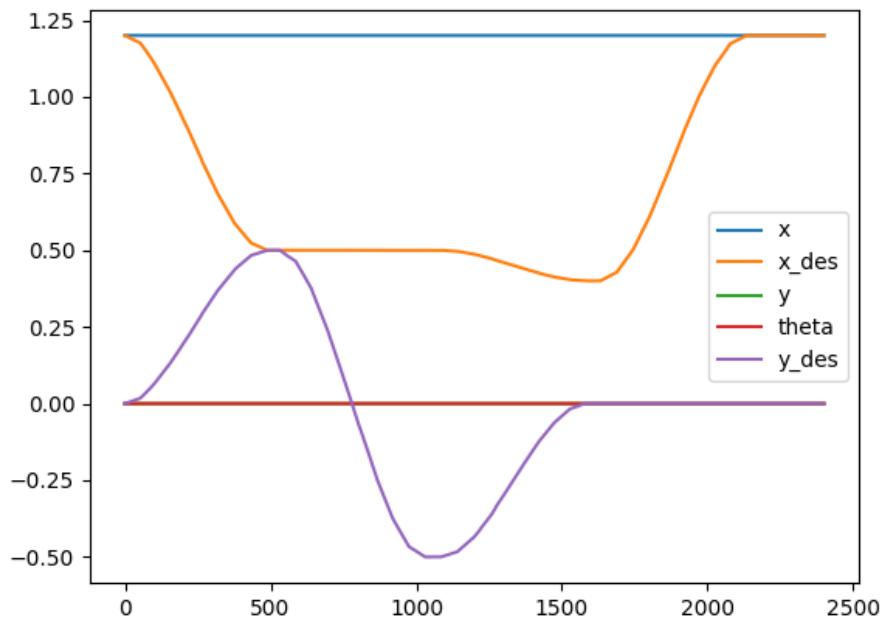
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```



trajectory



Q6) a) Closed loop control



Q6) b) Null space control

