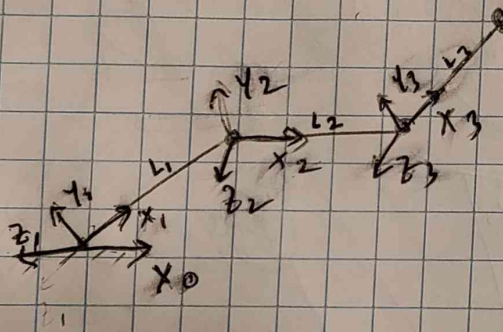
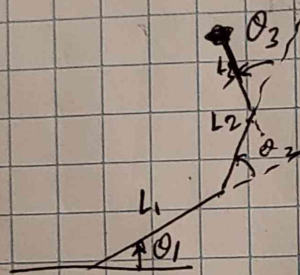


①



\*  $z$  axis is coming out of plane

② Kinematics of  $m$



$$\theta_e = \theta_1 + \theta_2 + \theta_3$$

$$x_e = L_1 \cos \theta_1 + L_2 \cos(\theta_1 + \theta_2) + L_3 \cos(\theta_1 + \theta_2 + \theta_3)$$

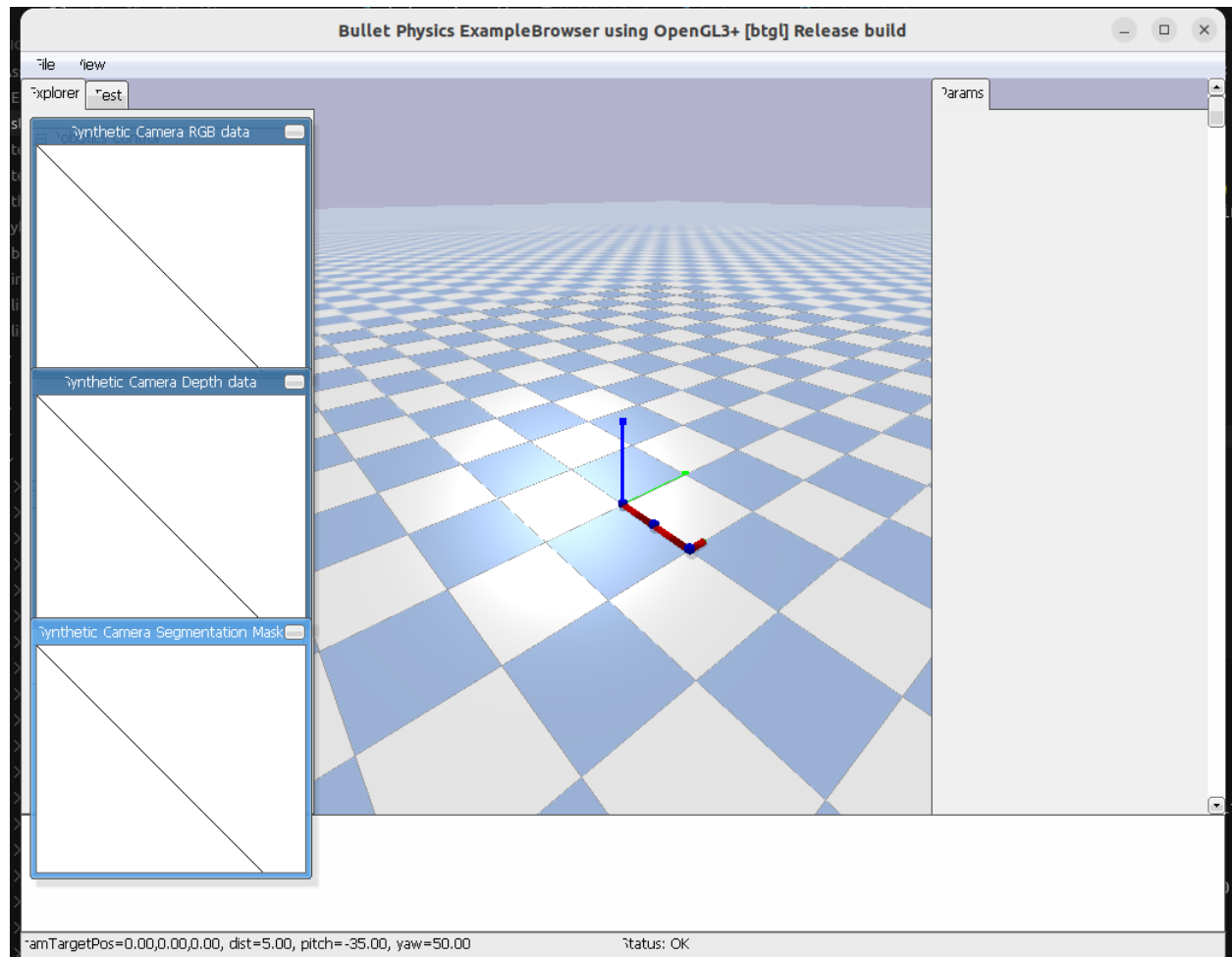
$$y_e = L_1 \sin \theta_1 + L_2 \sin(\theta_1 + \theta_2) + L_3 \sin(\theta_1 + \theta_2 + \theta_3)$$

While running the code set variable

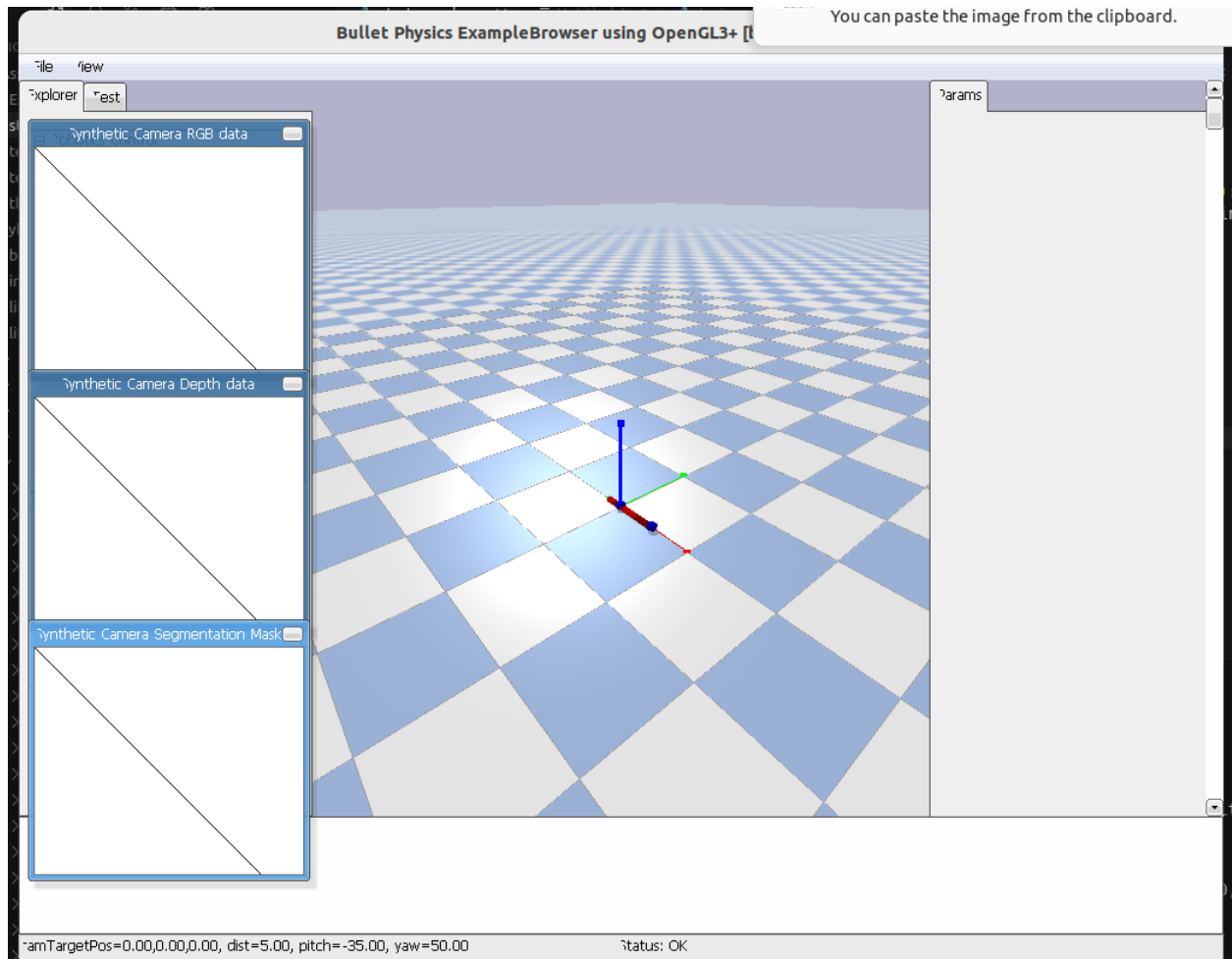
`run_part_no = None` # 1 for open loop, 2 for closed loop, 3 for null space control

Q3)

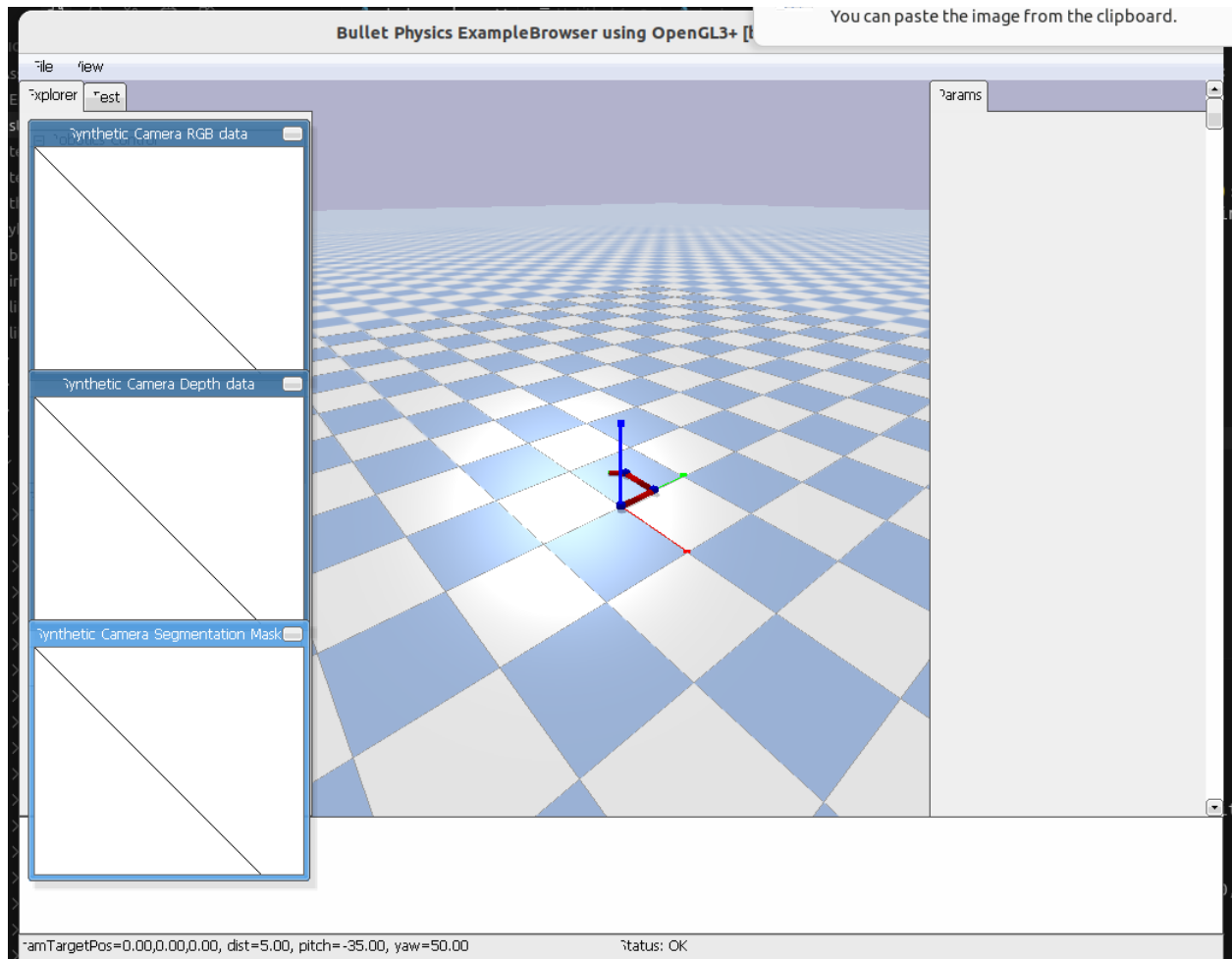
Config1



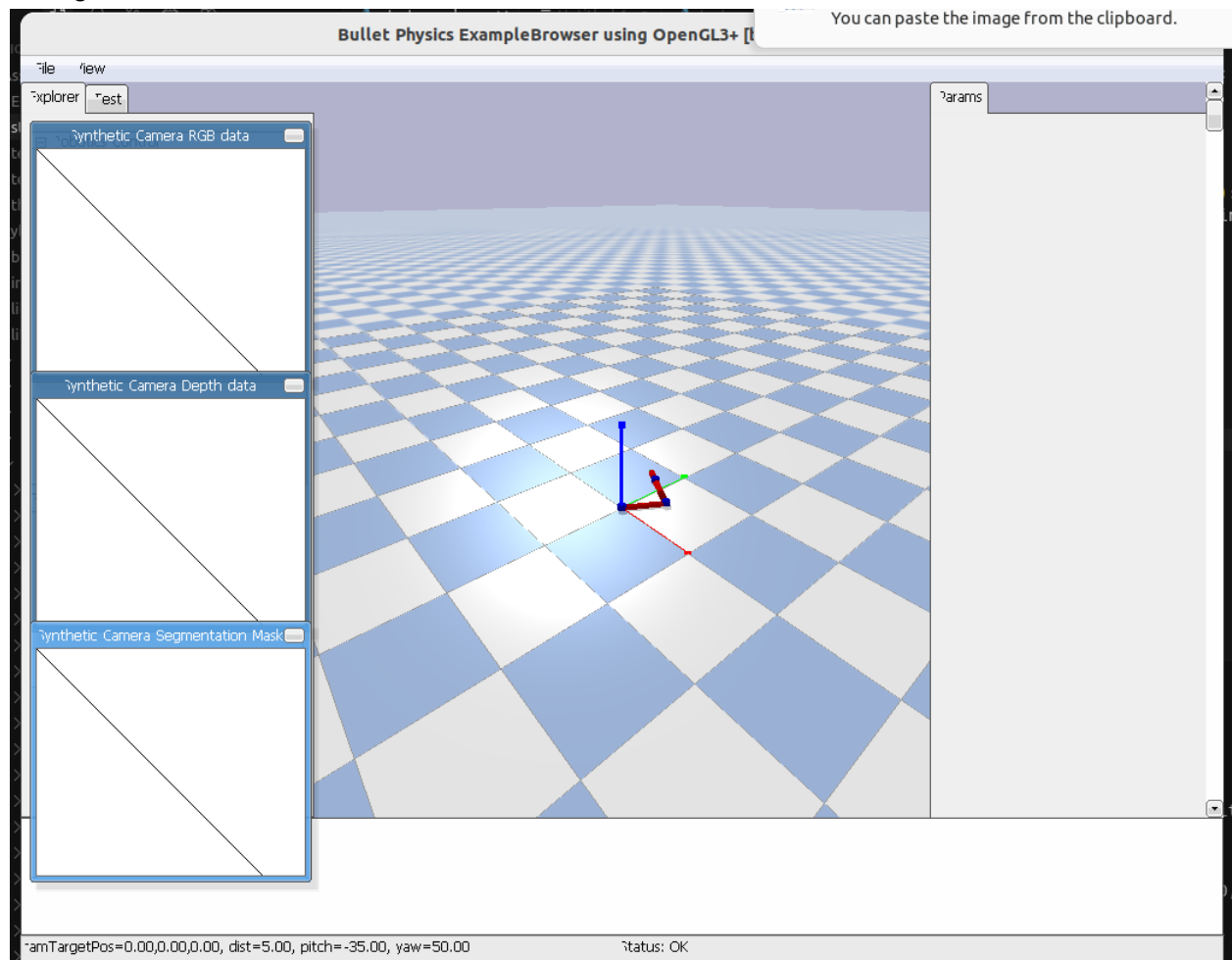
## Config2



### Config3

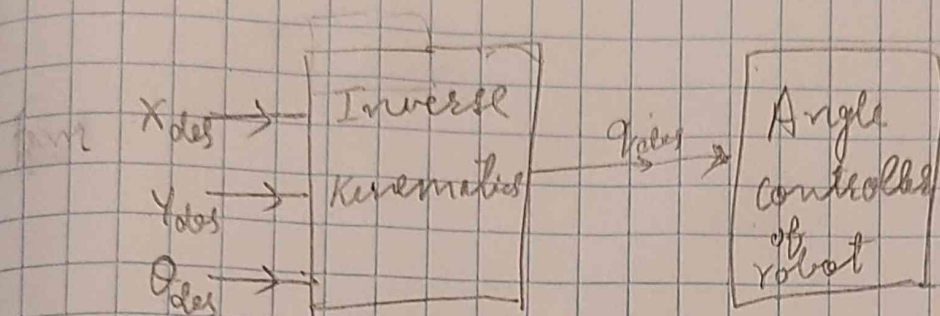


## Config4





open Loop.

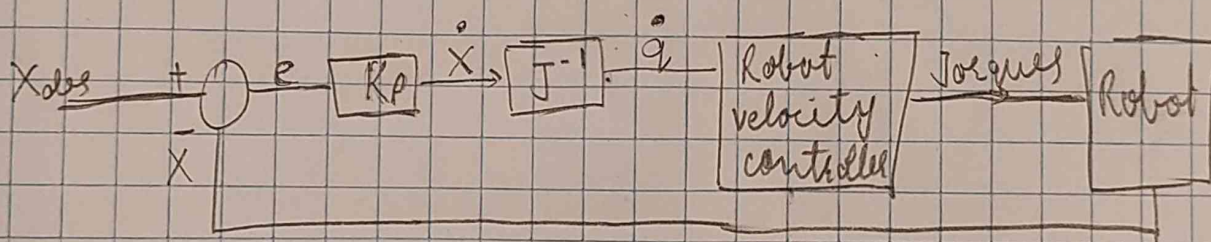


$q_{des} \rightarrow$  joint angle commands.

closed loop

$X_{des} = (x_{des}, y_{des}, \theta_{des}) \rightarrow$  desired state

$X = (x, y, \theta) \rightarrow$  current state



$$e = X_{des} - X$$

$$\dot{x} = K_p e$$

$$\dot{q} = J^{-1} K_p e \rightarrow \text{velocity commands for joints}$$

5)

$$x_{\text{des}} = at^3 + bt^2 + ct + d$$

$$y_{\text{des}} = kx$$

s.t

$$x(0) = x_0$$

$$\dot{x}(0) = 0$$

$$x(1) = x_1$$

$$\dot{x}(1) = 0$$

$$\begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 \\ 3 & 2 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix} = \begin{bmatrix} x_0 \\ x_1 \\ 0 \\ 0 \end{bmatrix}$$

$$k = \frac{y_1 - y_0}{x_1 - x_0}$$

6) closed loop

$$\ddot{\theta}_{\text{des}} = 0 = \ddot{\theta}_1 + \ddot{\theta}_2 + \ddot{\theta}_3$$

$$X_{\text{des}} = \begin{bmatrix} x_{\text{des}} \\ y_{\text{des}} \\ \theta_{\text{des}} \end{bmatrix}$$

$$e = X_{\text{des}} - x$$

$$\ddot{\theta}_{\text{des}} = J^{-1} K_P e \quad \leftarrow \quad \text{where } J^{-1} = J^T [JJ^T + \lambda^2 I]^{-1}$$



⑥ For null space  
cost function

$$J(\theta) = \theta_2^2 + \theta_3^2 \rightarrow \text{Minimise}$$

$\theta_2 \rightarrow 0, \theta_3 \rightarrow 0$   
ensures links are far apart

$$\nabla J(\theta) = \begin{bmatrix} 0 \\ 2\theta_2 \\ 2\theta_3 \end{bmatrix}$$

Minimise  $J(\theta)$  for  
max separation

$$\dot{q}_{\text{null}} = -(\mathbf{I} - \mathbf{J}^{-1}\mathbf{J}) \nabla J(\theta) * k$$

$\uparrow$   
tuning  
Parameter

$$\dot{q} = \dot{q}_{\text{des}} + \dot{q}_{\text{null}}$$

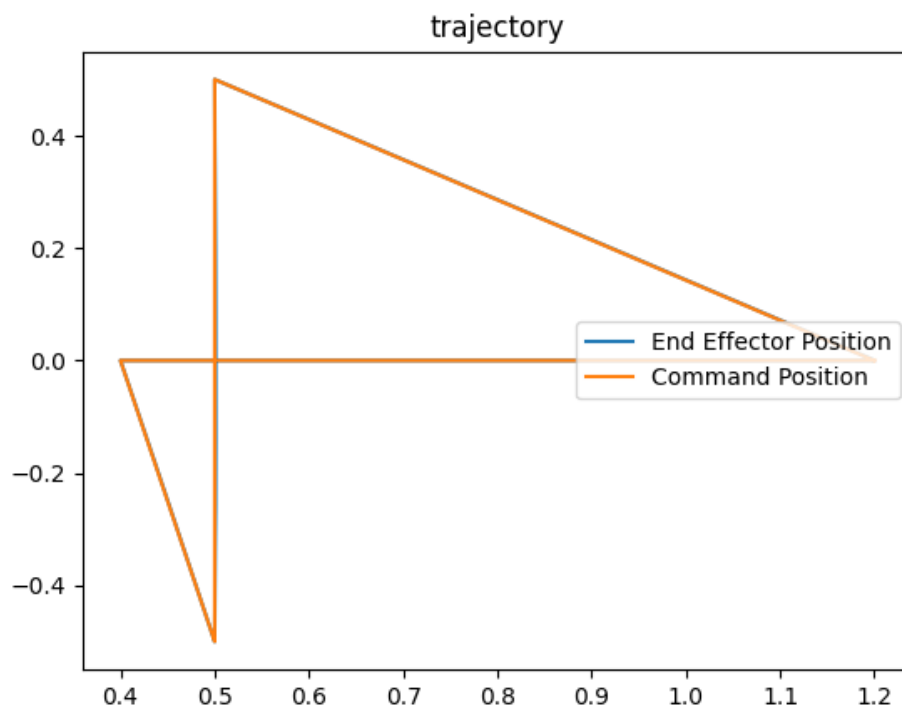
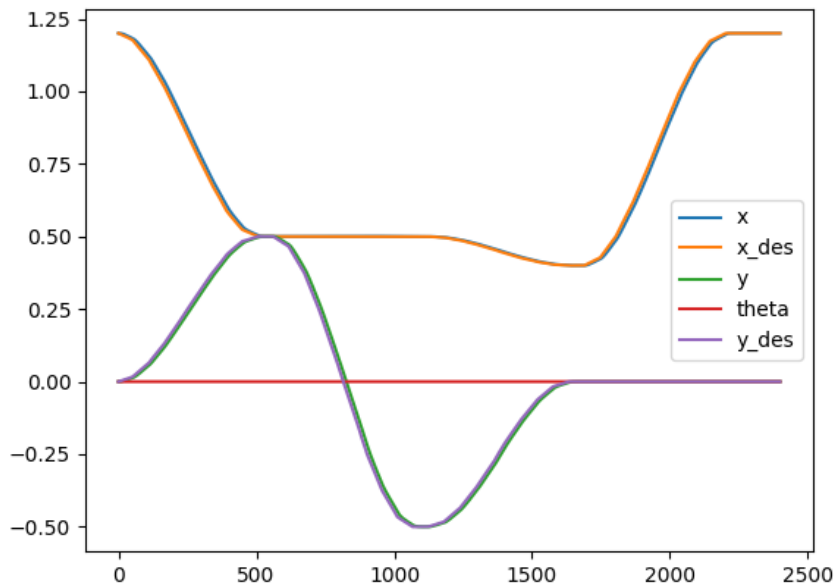
$\uparrow$   
desired  
loop

$\uparrow$   
null space

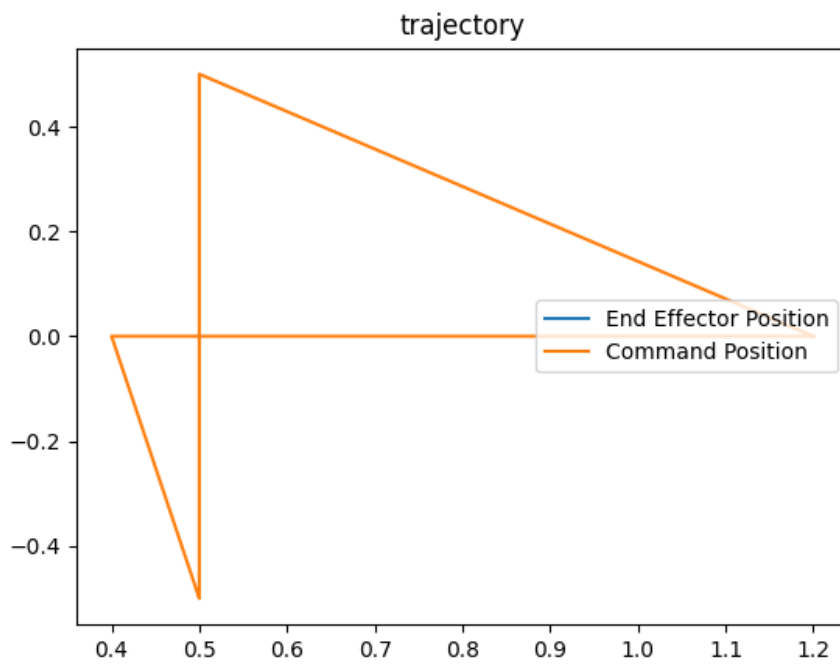
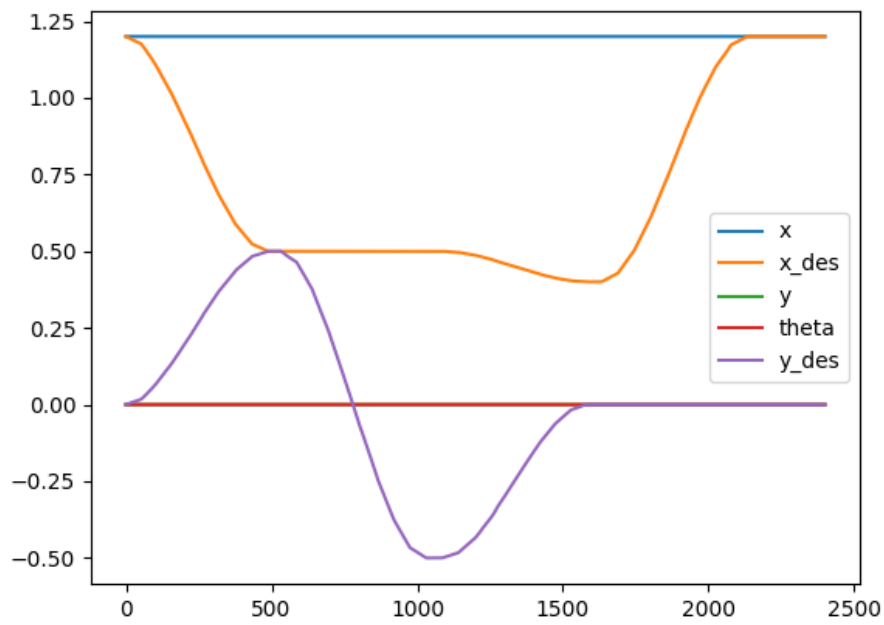
### Q5) Open loop control

While running the code set variable

`run_part_no = None` # 1 for open loop, 2 for closed loop, 3 for null space control



Q6) a) Closed loop control



Q6) b) Null space control

