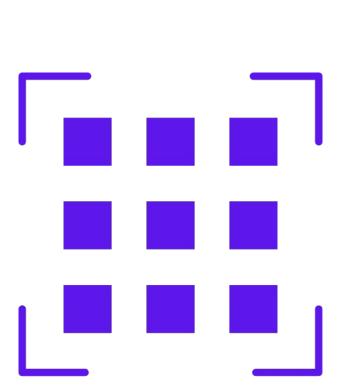
Array/Lists And Matrices







Pre-requisites

- Basic Python Knowledge
- Time and Space Complexity
- Willingness to learn







What are Data Structures?







- Particular way of organizing, and storing the data
- Tools to build efficient algorithms
- The right one depends on the task
- Common Data Structures:
 - Arrays
 - Linked Lists
 - Stacks
 - Queues

- Trees
- Maps(dictionaries)
- Sets
- Tries, etc...





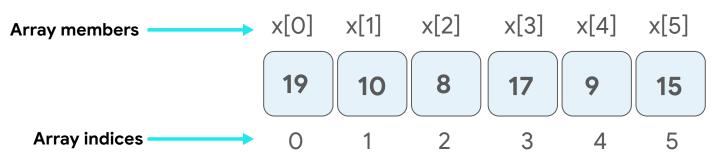


Arrays





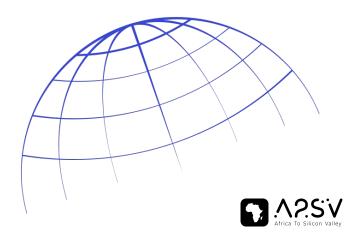
- Collection of items stored at contiguous memory locations.
- Storing multiple items of the same type together.
- Easier to calculate the position of each element by simply adding an offset to a base value.







Static Arrays



Static Arrays



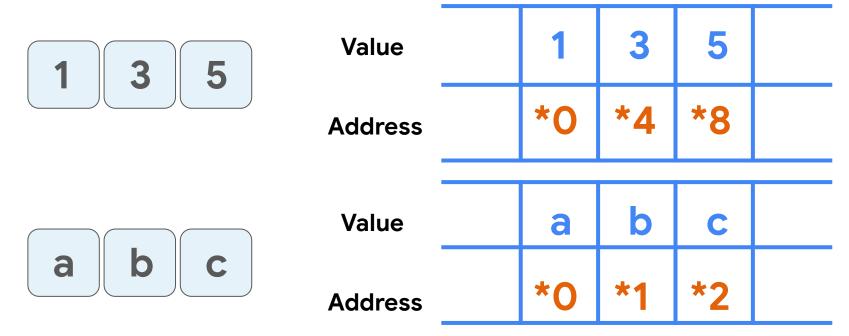
• A type of array in which the size or length is determined when the array is created and/or allocated.

7	3	6	
*0	*4	*8	





Static Arrays





Static Arrays - Reading

- Reading is Very fast : O(1)
- Why?

print(my_array[4])

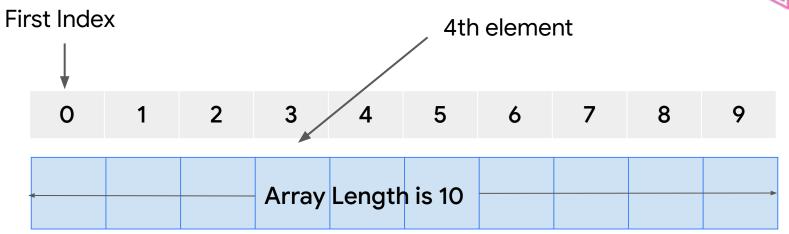








Static Arrays - Reading



Each integer occupies 4 bytes, so let us say the 0th index is at memory location 1400





Static Arrays - Writing

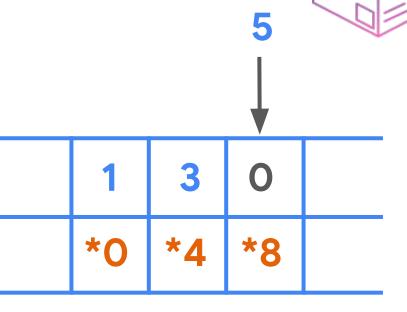
Writing is an instant operation

1 3

1

Value

Address







Static Arrays - Writing

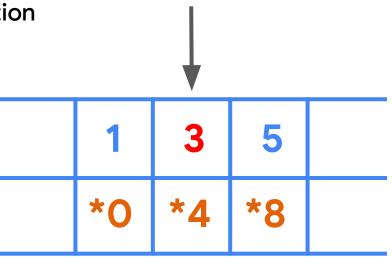
• Overwriting is an instant operation

Value

Address

1 3 5

4



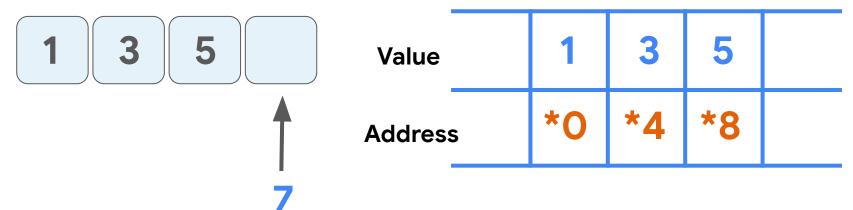








 What happens when we want to add an element to our array but don't have any empty spots?











- The operating system might be using this part of the memory for some other purpose.
- So we are not necessarily allowed to put our seven there.

1 3 5	Value	1	3	5	0
	Address	*0	*4	*8	
7					









Operation	Big-O Time
Read i-th Element	O(1)
Write i-th Element	O(1)





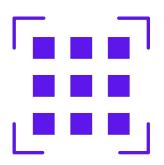
Dynamic Arrays





Dynamic Arrays

- A Dynamic array has the ability to resize itself automatically when an element is inserted or deleted.
- Double the size when it reaches capacity, cut by half when it's down to quarter







Does Python list allow the storage of different types?







Dynamic Arrays

No way to find out arr[3] without traversing the full list

$$arr = [3, 0.5, 'a', "1"]$$

Value	3	0.5	a	"1"	
Address	*0	*4	*12	*13	





Dynamic Arrays

- A list in Python is implemented as an array of references.
- That is that you are actually creating an array of references like so:

```
0 1 2 3
[Oxa3d25342, Ox635423fa, Oxff243546, Ox2545fade]
```







 Each element is a reference that "points" to the respective objects in memory

	*0	*1	*2	*3	
Reference	*10	*14	*22	*23	
Value	3	0.5	a	"1"	





Dynamic Arrays

• This works because the all references are of the same size unlike the actual values they point to.

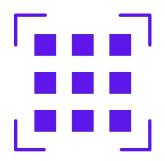
	*0	*1	*2	*3	
Reference	*10	*14	*22	*23	
Value	3	0.5	a	"1"	





Common Terminologies

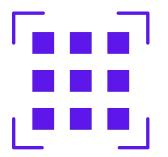
- Pushing/Appending: inserting an element at the next empty spot
- Popping: removing the element from the end of the list







- Whenever we reach our array's capacity, our interpreter allocates another memory which is double our original capacity and copies over all the old elements with now more space.
- Isn't this operation costly?

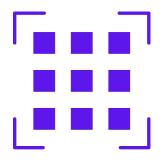








• It takes amortized O(1) time! Let's see why



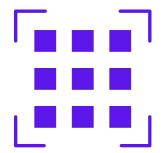






- Our goal is to push 8 elements to a dynamic array.
- Assumption: Our initial capacity is of size one.

 5
 6
 7
 8
 9
 1
 2
 3







After pushing 5, no place for 6

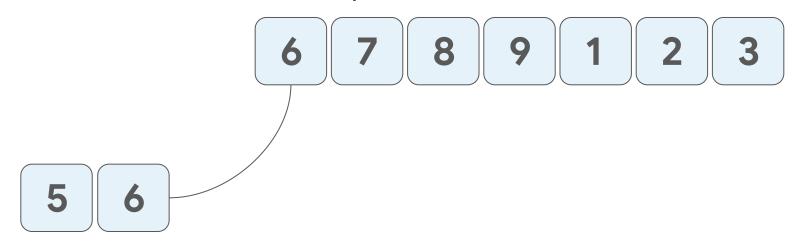


Operation count: 1





• Copy the original array ([5]) to the new allocated memory which is double the old size and push 6 onto it



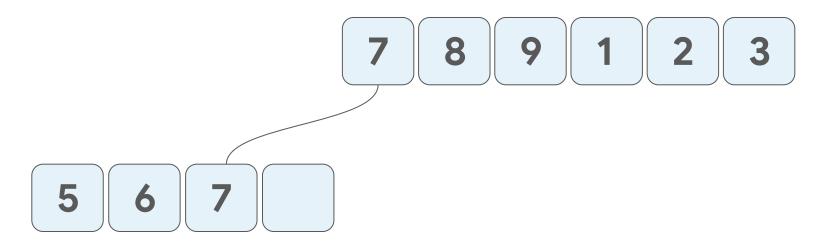
Operation count: 1 + 2







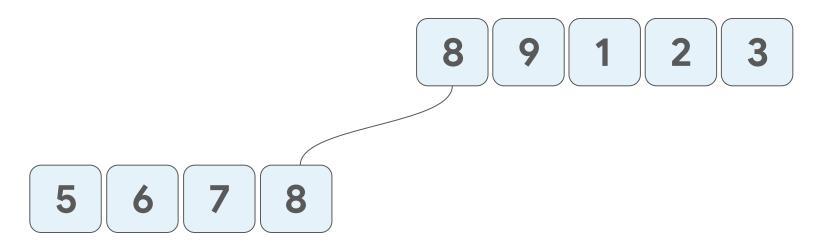
 Allocate a new array of size 4 and copy over all the old elements and then we append 7







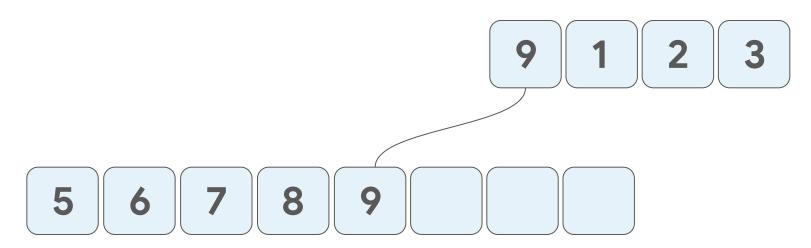
• Push 8 onto the array. Now we have run out of space for the next elements.







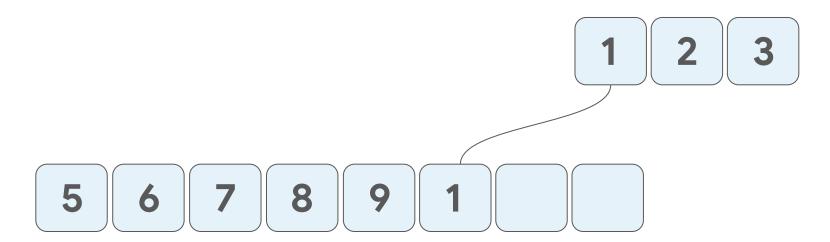
 Allocate a new array of size 8 and copy over all the old elements and then we append the element 9







Push/append 1 into the array







Push/append 2 into the array





• Push/append 3 into the array







Pushing- Power Series

- For a length of 8, it took us 1 + 2 + 4 + 8 operations. The last summand always dominates the sum.













Pushing - Power Series

- For a length of 8, it took us 1 + 2 + 4 + 8 operations.
- The last summand always dominates the sum.

```
2 \ge 1

4 \ge 1 + 2

8 \ge 1 + 2 + 4

.

.

2*N \ge 1 + 2 + 4 + 8 + ... + N
```

 Thus to push N elements, it will take us no more than 2N operations, making the time complexity O(N).



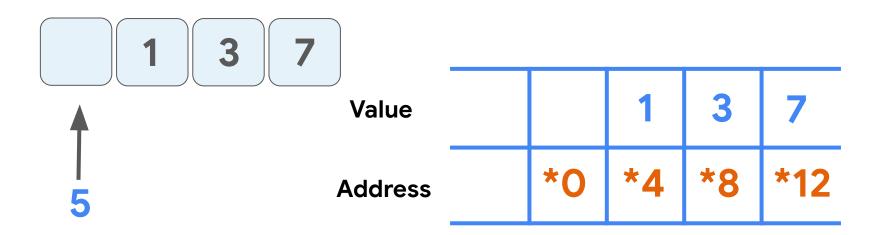
Pushing - Power Series

- This means, to push a single element onto an array, on average, we say it is an instant O(1) operation.
- Because after a while, the copying operation becomes very infrequent.
- Hence, pushing an element onto an array is Amortized O(1) operation.



Dynamic Arrays - Insertion

 Inserting an element in an arbitrary position is, in the worst case, an O(n) operation.

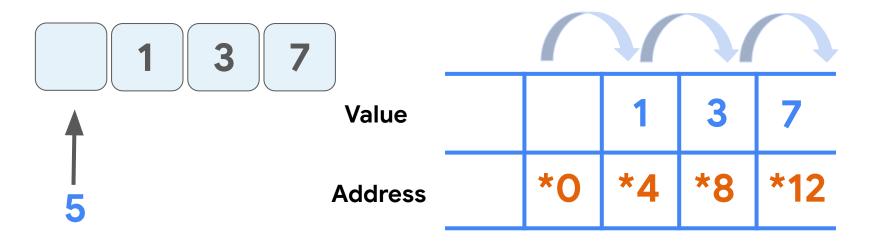








 We need to shift all elements to the right of the new element, to not lose data, and create the empty space needed.





Dynamic Arrays - Insertion

• The shifting is what costs us time.

5 | 1 | 3 | 7

Value

Address

5	1	3	7
*0	*4	*8	*12





Dynamic Arrays - Removal

What about removing an element?

 5
 1
 3
 7

 Address
 *0
 *4
 *8
 *12



Dynamic Arrays - Removal



• It is O(n) at worst.

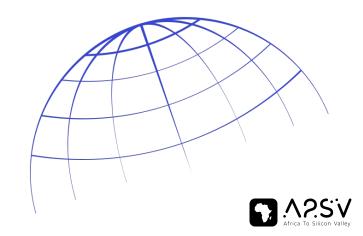
1 3 7

Value 1 3 7
Address *0 *4 *8





Checkpoint



Traversing Lists



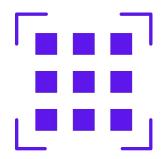


Traversing Lists - Reverse Traversal

Approach

- Start from the last index
- Decrement by 1 until -1

```
for index in range(len(array)-1, -1, -1):
    print(array[index])
```





Traversing Lists - Even/Odd Indices Traversal

Approach

- Start from the first even/odd index
- Increment by 2

```
step = 2 # incremental value
# even indices traversal
size = len(array)
for index in range(0, size, step):
    print(array[index])
```



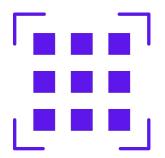


Traversing Lists - Circular Traversal

Approach

- Start from first index to size*2
- Incrementally go 1 step but modulo index by size

```
size = len(array)
for index in range(0, 2 * size):
    value = array[index % size]
    print(value)
```





Pair Programming
Find the winner of the circular

game



Swapping Elements







Approach

- Approach 1
 - Store first element in a variable
 - Change first element with second element
 - Change second element with stored value
- Approach 2: Use tuple unpacking to swap

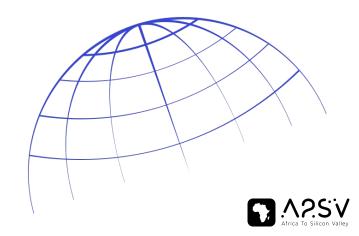
```
# approach 1
temp = arr[i]
arr[i] = arr[j]
arr[j] = temp

# approach 2
arr[i], arr[j] = arr[j], arr[i]
```



Pair Programming Reverse string

Storing letter and Numbers



Storing - Using Arrays as Dictionaries

- For Letters
 - Character's ASCII value can be the index by correcting the offset by 65 ('A') for uppercase letters and 97 ('a') for lower case letters
- For Numbers
 - The number itself is the key
- Note: the advantage of this approach is that you can use built in functions like sum, sort, max, min on the frequency list whereas maps don't give you this flexibilities.



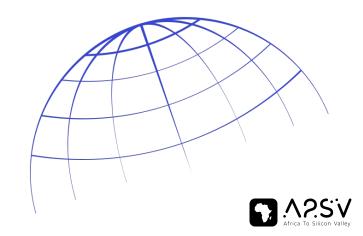


Storing - Implementation

```
word = "abceabce"
arrayDictionary = [0]*26
offset = ord('a') # 'a' has ASCII value of 97
for char in word:
  ascii = ord(char)
  arrayDictionary[ascii - offset] += 1
print(arrayDictionary)
#abcdefghijklmn,opqrstuvwxyz
```



Read and Write Indices





Read and Write and Indices

Approach

- Set your read index accordingly to your need
- Set your write index accordingly to your need
- Your read should always move
- Your write only moves after write operation

Implementation (Question Link)

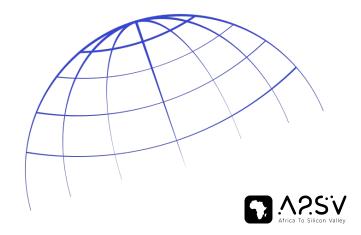
```
def moveZeroes(self, nums: List[int])
    write = 0
    read = 0
    while read < len(nums):</pre>
        if nums[read] != 0:
            temp = nums[read]
            nums[read] = nums[write]
            nums[write] = temp
            write = write + 1
        read = read + 1
```



Pair Programming

Apply operations to an array

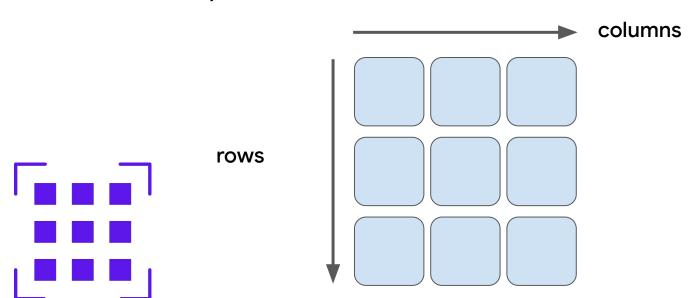
Matrices







- Two-dimensional arrays can be defined as arrays within an array.
- 2D arrays erected as matrices, which is a collection of rows and columns.

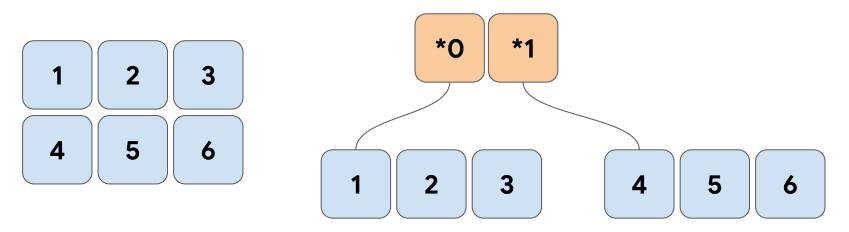




Matrices



- You should think two dimensional arrays as matrices. In reality, they are arrays holding references to other arrays





Common Approaches



Traversing Matrices

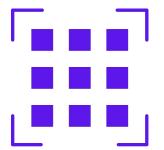


Traversing - from Top-left to Bottom-right

Approach

- Start from (0, 0)
- Increment column index by one for each row you visit

```
for row_idx in range(len(matrix)):
    for col_idx in range(len(matrix[0])):
        print(matrix[row_idx][col_idx])
```



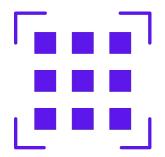


Traversing - From Bottom-right to Top-left

Approach

- Start from (last_row 1, last_col - 1)
- Decrement column index by one for each row you visit.

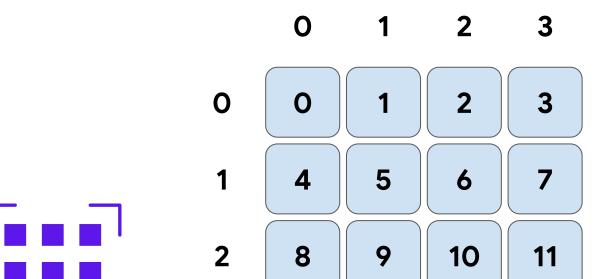
```
for row_idx in range(len(matrix) - 1, -1, -1):
    for col_idx in range(len(matrix[0]) - 1, -1, -1):
        print(matrix[row_idx][col_idx])
```





Enumerating Cells/ 2D - 1D Mapping

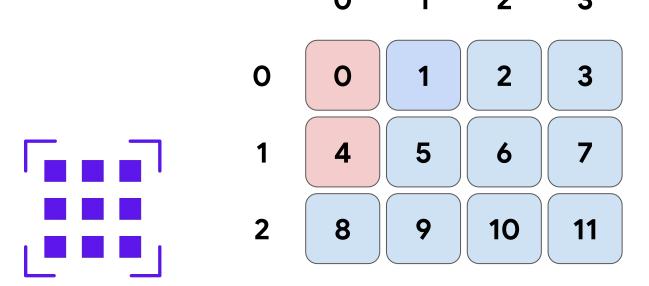








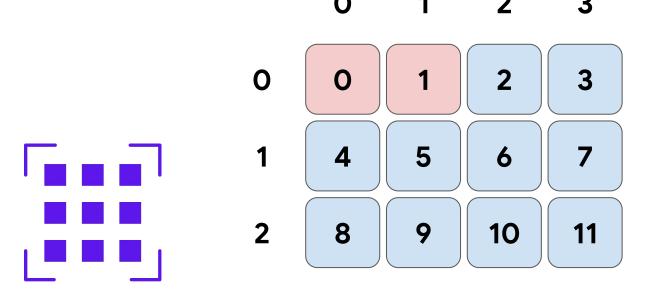
Consecutive elements in a column differ by the number of columns







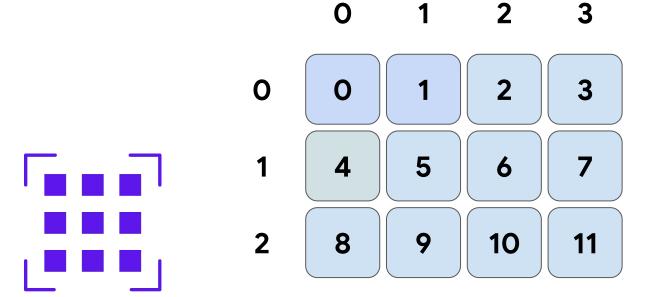
Consecutive elements in a row differ by 1







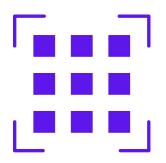
Therefore the 1D number of a cell is row_number*n_columns + column_number





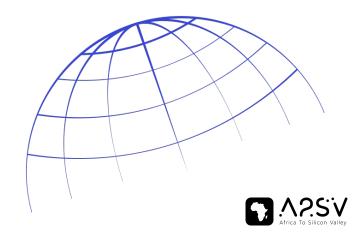
Enumerating Cells - Remainder Theorem

```
cell_number = row_number*n_columns + column_number
row_number = cell_number // n_columns
column_number = cell_number % n_columns
```





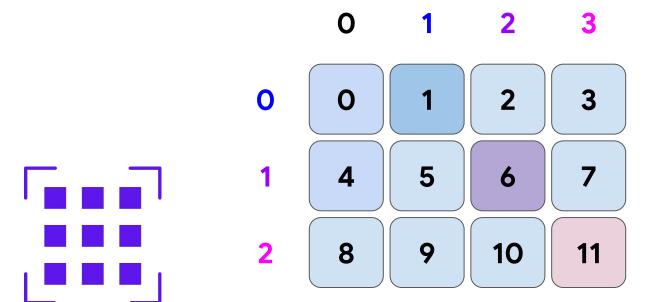
Diagonal Keys







What is common about the highlighted column and row numbers?

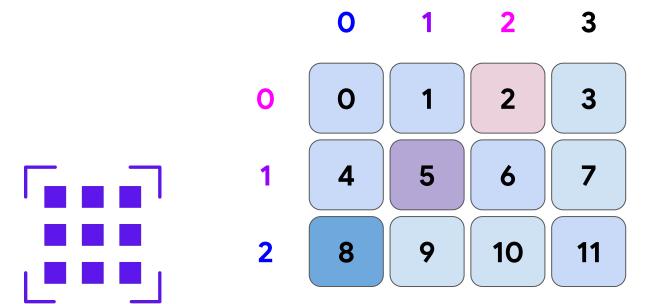








What is common about the highlighted column and row numbers?





Common Pitfalls



Common Pitfalls - Index Out of Bound

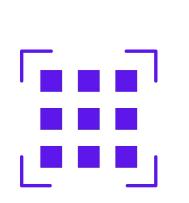
• Trying to access elements using indices that are greater (or equal to) than the size of our array will result in this exception.





Common Pitfalls - Negative Indexing

 Because we may use negative indices in Python, it is a typical problem to use negative indices accidently, which can result in a highly troublesome misunderstanding if no exception is triggered.



Negative indices: -4 -3 -2 -1

Positive indices: 0 1 2 3

Values: [1, 2, 3, 4]

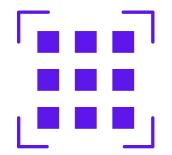




Common Pitfalls - Copying lists

 A list is a reference. Take care when you want to you want to pass only the content of the list.

```
nums[::]
nums.copy()
```





Common Pitfalls - Initializing with *

- The * operator can be used as [object] *n where n is the number of elements in the array.
- In the case of 2D arrays, this will result in shallow lists
- Hence using list comprehensions is a safer way to create 2D lists.

```
row = len(matrix)
col = len(matrix[0])

transposed = [[0]*rows for _ in range(cols)]
```



Common Pitfalls - Using insert, pop and in

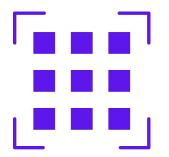
- insert inserts a given element at a given index
 - o insert(i, value) :O(N)
- pop returns the value at a given index and removes it from the list where the default is the last index
 - o pop:O(1)
 o pop(i):O(n)
- The in operator is returns a boolean denoting whether an element is present in the iterable data structure we use it on.
- Lists O(N)
- Map, Set ○(1)⊺



Common Pitfalls - Mistaking Row Iterators with Column iterators

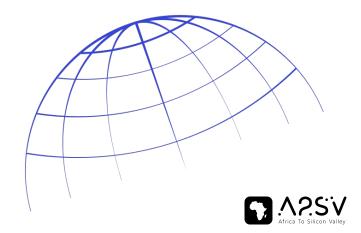
• It is pretty common to mistake your i and j's representing rows and columns. And sometimes, especially when the matrix is a square one, it does not throw an exception but hours of confusion

```
for col_idx in range(len(matrix[0])):
    for row_idx in range(len(matrix)):
        print(matrix[col_idx][row_idx])
```





Checkpoint



Practice Question Image smoother

Practice Questions Reverse string

Count Equal and Divisible Pairs in an..

All Divisions With the Highest Score...

Transpose matrix

Diagonal traverse

Rotate image



Resources

- https://neetcode.io/courses/dsa-for-beginners/0: useful on laying out the fundamentals
- https://www.geeksforgeeks.org/python-arrays/: covers large range of topics for python
- Python List pop() Method GeeksforGeeks: good examples
- <u>Python List insert() Method With Examples GeeksforGeeks</u>: good examples
- <u>Python | Which is faster to initialize lists? GeeksforGeeks</u>: good article on list initialization



Quote of the Day

If you want to enjoy the rainbow, be prepared to endure the storm

Warren W. Wiersbe

