1.	. If $x$ and $y$ are real numbers and $5x = 5y$ , then $x = y$ . True . Sets $\mathbb{Z}$ and $\mathbb{N}$ . Not a statement
	. Sets $\mathbb Z$ and $\mathbb N$ are infinite. True . Some sets are finite. True
	8 $\mathbb{N} \notin P(\mathbb{N})$ . True 1 The integer $x$ is a multiple of 7. Not a statement
13	2 If the integer x is a multiple of 7, then it is divisible by 7. <b>True</b> 3 Either x is a multiple of 7, or it is not. <b>True</b>
	tercises for Section 3.2
1.	The number 8 is both even and a power of 2.  p = The number 8 is even  q = The number 8 is a power of 2
2.	$p \wedge q$ . The matrix A is not invertible. $p = \text{matrix A is invertible}$
3.	$   \begin{array}{l}                                     $
5	$   \begin{array}{l}                                     $
7	$p \lor q$ 7 The number $x$ equals zero, but the number $y$ does not. $p = \text{The number } x \text{ equals zero}$
8	q = The number $y$ equals zero $p \wedge \neg q$ 8 At least one of the numbers $x$ and $y$ equals 0. $p$ = The number $x$ equals zero
9	q = The number $y$ equals zero $p \lor q$ $x \in A - B$
	$p = x \in A$ $q = x \in B$ $r = x \in A \cap B$ $p \land \neg q \land \neg r$
10	$   \begin{array}{l}     x \in A \cup B \\     p = x \in A \\     q = x \in B   \end{array} $
13	$p \lor q$ B Human beings want to be good, but not too good, and not all the time. $p = \text{Human beings want to be good}$ $q = \text{Human beings want to be too good}$
14	r = Human beings want to be good all the time $p \wedge \neg q \wedge \neg r$ 4 A man should look for what is, and not for what he thinks should be.
	p = A man should look for what is $q = A$ man should look for what he thinks should be $p \wedge \neg q$
	tercises for Section 3.3  . A matrix is invertible provided that its determinant is not zero.
	If a matrix determinant is not zero, then it's invertible.  For a function to be continuous, it is sufficient that it is differenciable.  If a function is differenciable, then it's continuous.
	<ul> <li>For a function to be integrable, it is necessary that it is continuous.</li> <li>If a function is continuous, then it's integrable.</li> <li>A function is rational if it is a polynomial</li> </ul>
	If a function is a polynomial, then it's rational.  An integer is divisible by 8 only if it is divisible by 4 If an integer is divisible by 4, then it's divisible by 8.
	. Whenever a surface has only one side, it is non-orientable If a surface is non-orientable, then it only has one side.
	<ul> <li>A series converges whenever it converges absolutely If a series converges absolutely, then it converges.</li> <li>A geometric series with ratio r converges if  r  &lt; 1 If the ratio r of a geometric series is  r  &lt; 1, then it converges.</li> </ul>
9.	A function is integrable provided the function is continuous  If a function is continuous, then it's integrable.
	The discriminant is negative only if the quadratic equation has no real solutions.  If the quadratic equation has no real solutions, then the discriminant is negative.  You fail only if you stop writing. (Ray Bradbury)
12.	If you stop writing, then you fail.  People will generally accept facts as truth only if the facts agree with what they already believe. (Andy Rooney)  If the facts agree with what people already believe, then they'll generally accept facts as truth.
13.	. Whenever people agree with me I feel I must be wrong. (Oscar Wilde)  If I feel I must be wrong, then people agree with me.
	tercises for Section 3.4  For matrix A to be invertible, it is necessary and sufficient that $\det(A) \neq 0$ .
2.	A matrix A is invertible if and only if $det(A) \neq 0$ . If a function has a constant derivative then it is linear, and conversely. A function is linear, if and only if it has a constant derivative, and conversely.
	. If $xy = 0$ then $x = 0$ or $y = 0$ , and conversely. $x = 0$ or $y = 0$ if and only if $xy = 0$ . . If $a \in \mathbb{Q}$ then $5a \in \mathbb{Q}$ , and if $5a \in \mathbb{Q}$ then $a \in \mathbb{Q}$ .
5.	$5a \in \mathbb{Q}$ if and only if $a \in \mathbb{Q}$ , and $a \in \mathbb{Q}$ if and only if $5a \in \mathbb{Q}$ . For an occurrence to become an adventure, it is necessary and sufficient for one to recount it. An occurrence becomes an adventure if and only if one can recount it.
	tercises for Section 3.5 $P \lor (Q \Rightarrow R)$
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	T         F         F         T         T           F         T         T         T         T           F         T         F         F         F           F         F         T         T         T
2.	F F F T T
	T         T         T         T           T         T         F         F           T         F         T         F         F           T         F         F         T
	F   T   T   T   T         T           F   T   F   T   F         F           F   F   T   T   F   F         F           F   F   F   F   F   T         T
7	$7 (P \land \neg P) \Rightarrow Q$
10	$\begin{array}{c c c c c c c c c c c c c c c c c c c $
	T         T         F         T           T         F         F         T           F         T         T         F         T           F         F         T         T
11	T T F F F T T T F T T T T T T T T T T T
	T T F F F T T T F T T T T T T T T T T T
Ex	T T F F F T T T F T T F T T T F T T T T
Ex	T T F F F T T T T T T T T T T T T T T T
Ex	T T F F F T T T F T T T T T T T T T T T
<b>E</b> x	T T F F F T T T F F T T T T T T T T T T
<b>Ex</b> :  1	T T F F F T T T F T T T T T T T T T T T
<b>E</b> x	T T F F F T T T F T T T T T T T T T T T
<b>Ex</b> :  1	T T F F F F T T T F F F T T T F F F F F
<b>Ex</b> 1	T T F F F T T T F T T F T T T F T T T T
<b>Ex</b> 1	T T F F F T T T F T T F T T T F T T T F T T T F T T T T F T
Ex. 1	The propose the statement $((P \land Q) \lor R) \Rightarrow (R \lor S)$ is false. Find the truth values of $P, Q, R, S$ Refalse, Sefalse, Petrue, Qetrue 1 Suppose P is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q)$ is true. Find the truth values of R and S. Retrue, Sefalse  **Recreases for Section 3.6*  1 $P \land (Q \lor R) \equiv (P \land Q) \lor (P \land R)$ Property Representation of Property Representat
Ex. 1 3	T T F F F T T T F T T F T T T F T T T T
Ex. 1  3  7	T T F F F T T F T F T T F T T T T T T T
Ex. 1  3  5	T T F F F T T F T T F T T F T T F F T T T F F T T F T T F T T F T T F T T F T T F T T F T T F T T F T T F T T F T T T F T T T F T T T F T T T T F T
Ex. 1 3 4 B	$\begin{array}{c c c c c c c c c c c c c c c c c c c $
Ex. 1 3 4 B Ex. 1.	$\begin{array}{c c c c c c c c c c c c c c c c c c c $
Ex. 1 3 3 5 7 4 B Ex. 1. 2.	The property of the statement $(P \land Q) \lor R \Rightarrow (R \lor S)$ is false. Find the truth values of $P, Q, R, S$ Refalse, Serialse, Perme, $Q = \text{true}$ Suppose the statement $(P \land Q) \lor R \Rightarrow (R \lor S)$ is false. Find the truth values of $P, Q, R, S$ Refalse, Serialse and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q)$ is true. Find the truth values of $R$ and $S$ Recroises for Section 3.6 $P \land Q \lor R) = (P \land Q) \lor (P \land R)$ $P \mid Q \mid R \mid (Q \lor R) \mid (P \land Q) \mid (P \land R) \mid P \land (Q \lor R) \mid (P \land Q) \lor (P \land R)$ $P \mid Q \mid R \mid (Q \lor R) \mid (P \land Q) \mid (P \land R) \mid P \land (Q \lor R) \mid (P \land Q) \lor (P \land R)$ $P \mid Q \mid R \mid (Q \lor R) \mid (P \land Q) \mid (P \land R) \mid P \land (Q \lor R) \mid (P \land Q) \lor (P \land R)$ $P \mid Q \mid R \mid (Q \lor R) \mid (P \land Q) \mid (P \land R) \mid P \land (Q \lor R) \mid (P \land Q) \lor (P \land R)$ $P \mid Q \mid (Q \land R) \mid (P \land Q) \mid (P \land R) \mid P \land (Q \lor R) \mid (P \land Q) \lor (P \land R)$ $P \mid P \mid$
Ex. 1 3 3 5 7 9 11 13 A B Ex. 1. 2. 3.	The propose the statement $((P \land Q) \lor R) \Rightarrow (R \lor S)$ is false. Find the truth values of $P,Q,R,S$ Reflace, Selates, $P = \text{true}, Q = \text{true}$ .  Suppose P is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q)$ is true. Find the truth values of $R$ and $S$ .  Reflections for Section 3.6.  Reflections for Section 3.6. $P \land (Q \lor R) = (P \land Q) \lor (P \land R)$ The propose $P \lor Q \land R$ is $P \land Q \lor R$ in $P \lor Q \lor R$ in $P \lor$
Ex. 1  3  5  7  9  11  13  A  B  Ex. 1.  2.  3.  4.  5.	$ \begin{array}{ c c c c c }\hline T & F & F & F & T \\\hline F & T & T & F & F & T \\\hline F & T & T & F & F & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline F & T & T & F & T & T \\\hline R & islae, S & lake, F & true, Q & true \\\hline Stappes F & islae and that the statement (R > S) \hookrightarrow (P \land Q) is true. Find the truth values of R and S.  \begin{array}{ c c c c c c c c c c c c c c c c c c c$
Ex. 1  3  5  7  9  11  13  A  B  Ex. 1. 2. 3. 4. 5. 6.	$ \begin{array}{ c c c c c }\hline T & F & F & F & T \\ F & T & T & F & F & T \\ F & T & T & F & F & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ F & T & T & F & T & T \\ Suppose & Is false, N = false, N = true, Q = true \\ S. Suppose & Is false and that the statement (R \Rightarrow S) \Leftrightarrow (P \land Q) is true. Find the truth values of R, and S. R = true, S = false. \\ \hline Cercises for Section 3.6 \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land R) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \lor (P \land Q) \\ \hline P \land (Q \lor R) = (P \land Q) \Rightarrow (Q \land Q) \\ \hline P \land (Q \lor R) \Rightarrow (P \land Q) \Rightarrow (P \land R) \\ \hline P \Rightarrow Q \Rightarrow (P \land A \lor Q) \Rightarrow (P \land R) \Rightarrow (P \lor Q) \land (P \land Q) \Rightarrow (P \land$
Ex. 1  3  5  7  9  11  13  A  B  Ex. 1. 2. 3. 4. 5. 6. 7.	T T F F F F T T F F F F F F F F F F F F
Ex. 1 3 4 4 5 6 7 8 9	The property of the statement $(P \land Q) \lor R) \Rightarrow (R \lor S)$ is false. Fixed the trath values of $P, Q, R, S$ Recalls. Suppose the statement $(P \land Q) \lor R) \Rightarrow (P \land Q)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q) \lor (P \land R)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q) \lor (P \land R)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q) \lor (P \land R)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q) \lor (P \land R)$ is true. Find the truth values of $R$ and $S$ .  Recalls. Suppose $P$ is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q) \lor (P \land R)$ is true. Find the truth values of $R$ and $R$

Logic Homework

Michael Padilla

 $\mathrm{June}\ 4,\ 2024$ 

Exercises for Section 3.1

1. Every real number is an even integer. False

There's at least one Natural number n, that |x| < n for every subset X of P, that n > n. There's at least one Natural number n, that |x| < n for every subset X of the Natural numbers, there's at least one integer n, that |x| = n. False n > n. For every subset X of the Natural numbers, that the cardinatity of X is equal to n. Thue n > n. For every integer n, there's at least one subset X of the Natural numbers, that the cardinatity of X is equal to n. Thue n > n. For every integer n, there's at least one integer m, that m = n - 5. Thue n > n. There's at least one integer n, that m = n + 5 for every integer n. Thue n > n is equal to n > n. There's at least one integer n, that n = n + 5 for every integer n. Thue n > n is equal to n > n. There's at least one integer n > n integer n > n. Thue n > n is equal to n > n. There's at least one integer n > n integer n > n. Thue n > n > n integer n > n integer n > n. Thue n > n > n integer n > n integer n > n integer n > n. Thue n > n > n integer n > n. Thue n > n > n integer n >