 Even Even If x Sets 	June 3, 2024 ises for Section 3.1
3. If x4. Sets	ry real number is an even integer. False
6. Som	ry even number is a real number. True and y are real numbers and $5x = 5y$, then $x = y$. True \mathbb{Z} and \mathbb{N} . Not a statement \mathbb{Z} and \mathbb{N} are infinite. True he sets are finite. True
8 N ∉ 11 The 12 If th	$P(\mathbb{N})$. True integer x is a multiple of 7. Not a statement ne integer x is a multiple of 7, then it is divisible by 7. True
14 Call	ises for Section 3.2
$p = q = p \land q$ $2. The p = q$	number 8 is both even and a power of 2. The number 8 is even The number 8 is a power of 2 q matrix A is not invertible. matrix A is invertible
$\neg p$ $5 \ y \ge$	(x = y)
$q = p \lor c$ 7 The p =	(y > x) q number x equals zero, but the number y does not. The number x equals zero The number y equals zero
$ 8 \text{ At l} \\ q = \\ p \lor c $ $ 9 x \in $	east one of the numbers x and y equals 0. $p = The number x equals zero. The number y equals zero$
$r = p \land 10 x \in p = q = q = q = q$	$x \in A \\ x \in B$
p = q = r = r = r	nan beings want to be good, but not too good, and not all the time. Human beings want to be good Human beings want to be too good Human beings want to be good all the time $\neg q \wedge \neg r$
$p = q = p \land q$	nan should look for what is, and not for what he thinks should be. A man should look for what is A man should look for what he thinks should be ¬q ises for Section 3.3
 A m If a For 	natrix is invertible provided that its determinant is not zero. matrix determinant is not zero, then it's invertible. a function to be continuous, it is sufficient that it is differenciable. function is differenciable, then it's continuous.
If a 4. A fu If a 5. An i	a function to be integrable, it is necessary that it is continuous. function is continuous, then it's integrable. unction is rational if it is a polynomial function is a polynomial, then it's rational. integer is divisible by 8 only if it is divisible by 4
6. Who If a7. A see	enever a surface has only one side, it is non-orientable surface is non-orientable, then it only has one side. eries converges whenever it converges absolutely series converges absolutely, then it converges.
9. A furth of the state of the	eometric series with ratio r converges if $ r < 1$ ne ratio r of a geometric series is $ r < 1$, then it converges. Inction is integrable provided the function is continuous function is continuous, then it's integrable. Indicate the discriminant is negative only if the quadratic equation has no real solutions.
11. You If you12. Peop Roo	fail only if you stop writing. (Ray Bradbury) ou stop writing, then you fail. ple will generally accept facts as truth only if the facts agree with what they already believe. (And oney)
13. Whe	ne facts agree with what people already believe, then they'll generally accept facts as truth. enever people agree with me I feel I must be wrong. (Oscar Wilde) feel I must be wrong, then people agree with me. ises for Section 3.4
A m 2. If a A fu	matrix A to be invertible, it is necessary and sufficient that $\det(A) \neq 0$. natrix A is invertible if and only if $\det(A) \neq 0$ function has a constant derivative then it is linear, and conversely. natrix A is invertible if and only if it has a constant derivative, and conversely. $y = 0$ then $x = 0$ or $y = 0$, and conversely.
$x = 4. \text{ If } a$ $5a \in 5. \text{ For } a$	0 or $y = 0$ if and only if $xy = 0$. $\in \mathbb{Q}$ then $5a \in \mathbb{Q}$, and if $5a \in \mathbb{Q}$ then $a \in \mathbb{Q}$. $\in \mathbb{Q}$ if and only if $a \in \mathbb{Q}$, and $a \in \mathbb{Q}$ if and only if $5a \in \mathbb{Q}$ an occurrence to become an adventure, it is necessary and sufficient for one to recount it.
1. $\frac{P \vee \overline{P}}{T}$	ises for Section 3.5
T T F F F	T F T F T T F F T T T T T F F F T T F F T
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
F F F 7 (P/	$ \begin{array}{ c c c c c c }\hline T & T & T & T & T \\ T & F & T & F & F \\ F & T & T & F & F \\ F & F & F & F & T \\\hline\hline \hline Q & (\neg P) & (P \land \neg P) & (P \neg P) \Rightarrow Q \\\hline \hline \end{array} $
T T F F T Sup	T F F T T T T F T T T T T F T T T T F T T T T F T T T T F T T T T F T
11 Supp S. R =	pose P is false and that the statement $(R \Rightarrow S) \Leftrightarrow (P \land Q)$ is true. Find the truth values of R and true, S = false ises for Section 3.6
$ \begin{array}{c} 1 \ \underline{P \wedge} \\ \underline{P} \\ T \\ T \\ T \\ T \end{array} $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
F F F	$ \begin{array}{ c c c c c c }\hline T & T & T & F & F & F & F \\\hline T & F & T & F & F & F & F \\\hline F & T & T & F & F & F & F \\\hline F & F & F & F & F & F \\\hline\hline Q & (\neg P) & (\neg P \lor Q) & (P \Rightarrow Q) \\\hline\hline \end{array} $
$ \begin{array}{c} T \\ T \\ F \\ F \end{array} $ $ 5 \underline{\neg(P)}{P} $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
T T T F F	T T F F F T F F F T F F F F T F F F F F F T T F F F T T F F T T F F T T F
$ \begin{array}{c} F \\ 7 P \Rightarrow \\ \hline P \\ T \\ T \end{array} $	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\equiv \neg$ The	$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
	$P(P) \land (P \Rightarrow Q) \text{ and } \neg (Q \Rightarrow P)$ $\land (\neg P \lor Q) \neq \neg P \land Q$ $\land (\neg P \lor Q) \neq \neg P \land Q$ $\land (Q \land R) \text{ and } (P \lor Q) \land R$ $\land (Q \land R) \neq (R \land P) \lor (R \land Q)$ $\land (P \lor R) \neq (R \land P) \lor (R \land Q)$
The	y are not logically equivalent.