Minimum Spanning Tree Comparison

By Mikaela Montaos Prepared under the direction of Professor Henry Chang

School of Engineering Northwestern Polytechnic University 117 Fourier Ave, Fremont, CA 94539 April 2021

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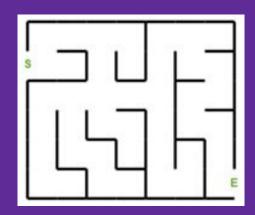
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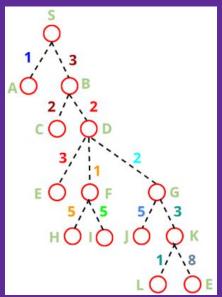
Introduction

- A Minimum Spanning Tree (MST) is finding the minimum weight in a spanning tree. A spanning tree is both a tree (connected) and spanning (includes all vertices).
- This document compares two MST algorithms:
 - Prim's MST
 - Kruskal's MST

Design

The problem is a maze. The goal is to start on letter S and reach the end on letter E while using the minimum weight/fastest path.



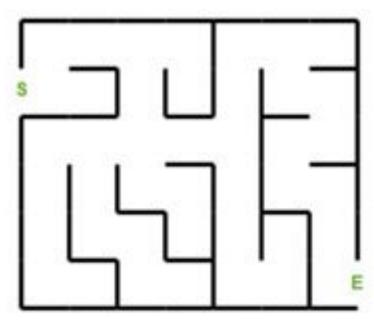


Implementation: Prim's MST

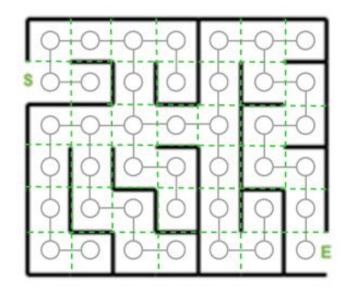
- 1. Add 0 next to the starting node and mark it as visited
- 2. Add the weight value next to the nodes connected to the starting node
- 3. The next node to visit is the node with the lowest weight value
- 4. Continue until all nodes are visited
 - a. If there is more than one weight on a node, choose the lowest value

Test: Maze Problem

1. Problem

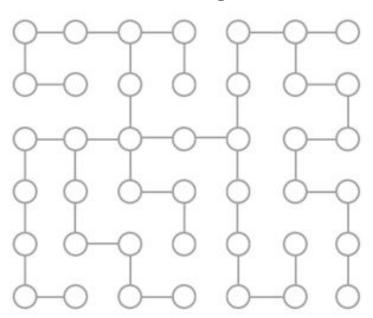


2. Create a graph over the maze and add nodes and edges

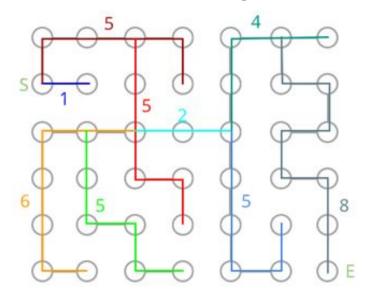


Test: Maze Problem

3. Extract the nodes and edges from the maze

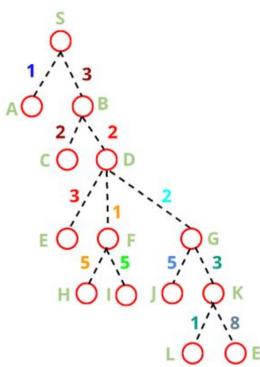


4. Count the number of nodes until it reaches a vertice. That will be the edge value

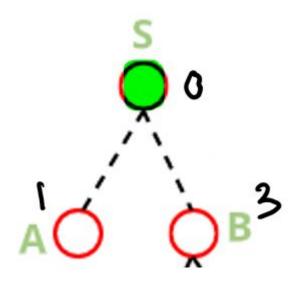


Test: Maze Problem

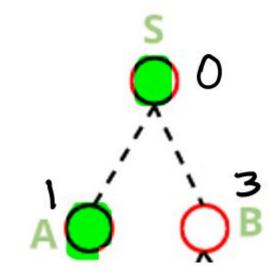
5. Convert into a tree



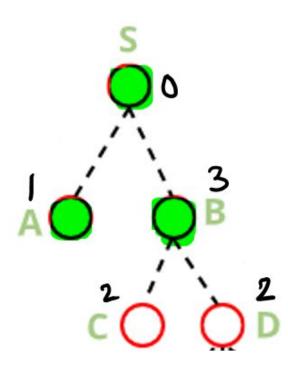
Node Start



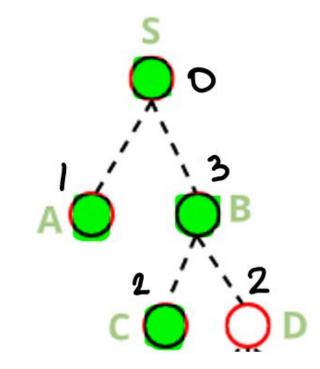
2. Node A



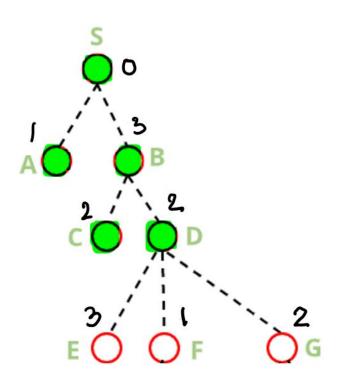
3. Node B



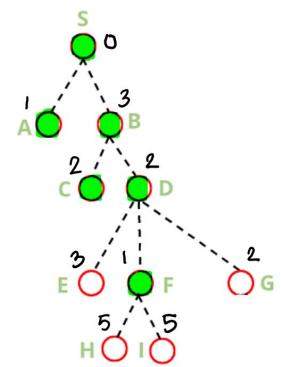
4. Node C



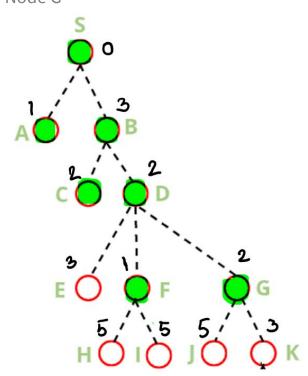
5. Node D



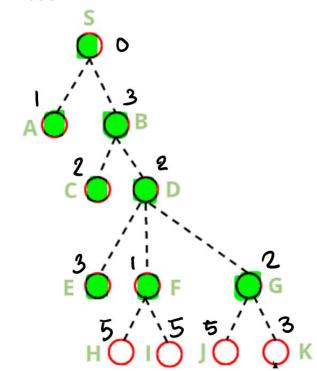
6. Node F



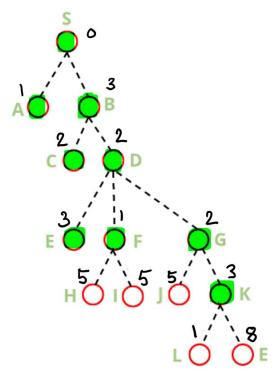
7. Node G



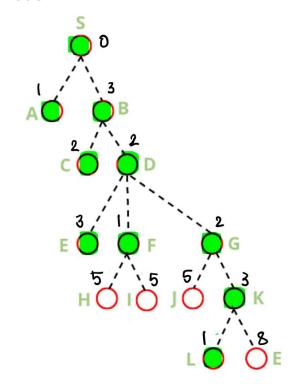
8. Node E



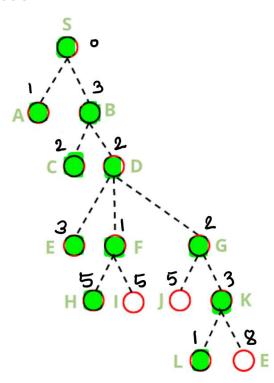
9. Node K



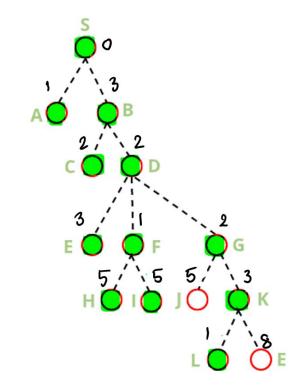
10. Node L



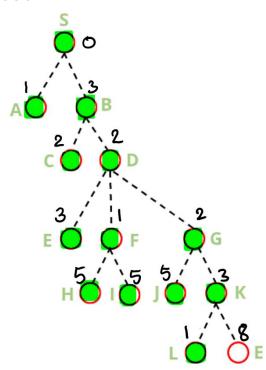
11. Node H



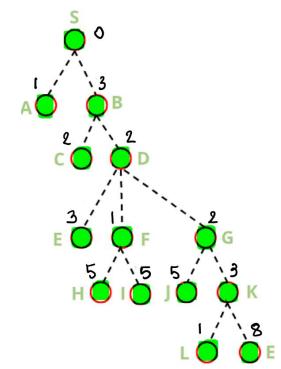
12. Node I



13. Node J



14. Node End

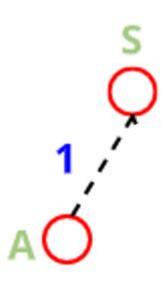


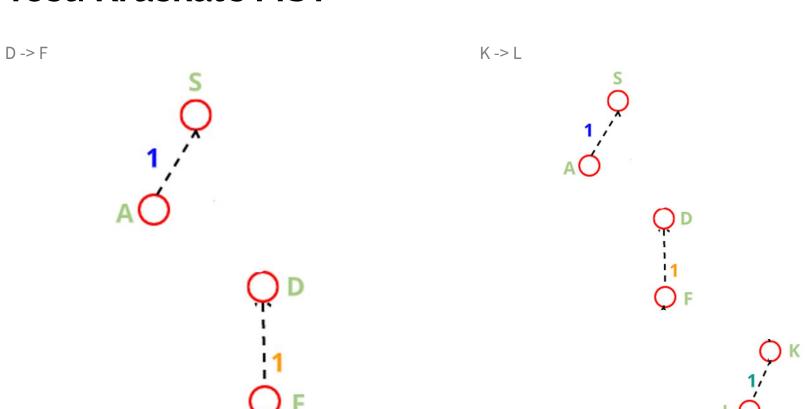
Implementation: Kruskal's MST

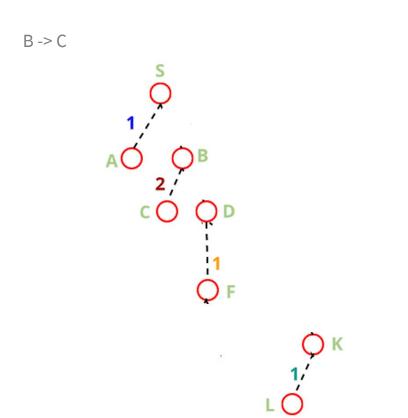
- 1. Sort the edges in an increasing order according to weight
- 2. Start with the smallest edge
- 3. Continue until all edges are visited
 - a. If a cycle/loop is formed, do not include the edge
 - b. If there is an edge already connected to the node, disregard. Only keep the smaller edge.

Weight	Source -> Destination
1	S -> A
1	D -> F
1	K -> L
2	B -> C
2	B -> D
2	D -> G
3	S -> B
3	D -> E
3	G -> K
5	F -> H
5	F -> I
5	G -> J
8	K -> E (End)

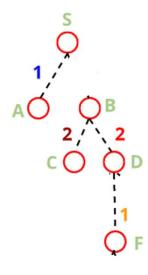




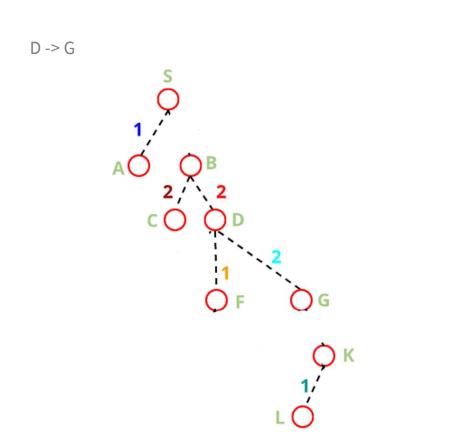


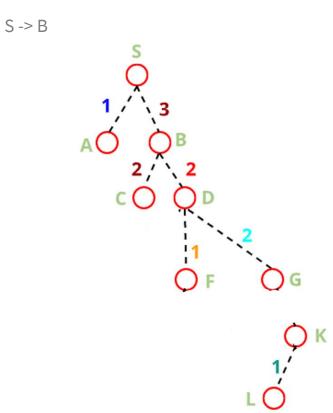


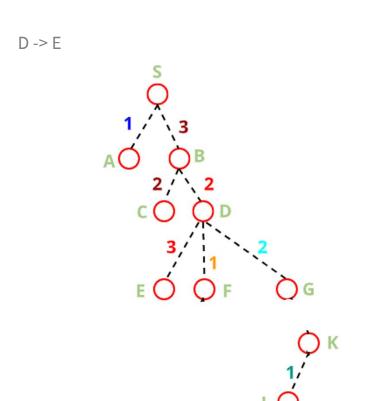
B -> D



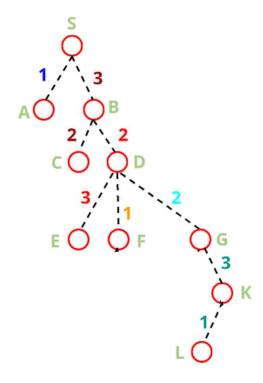


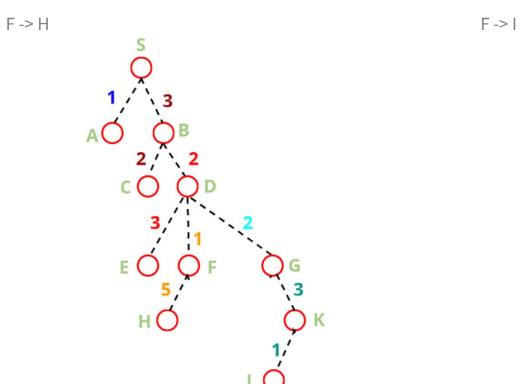


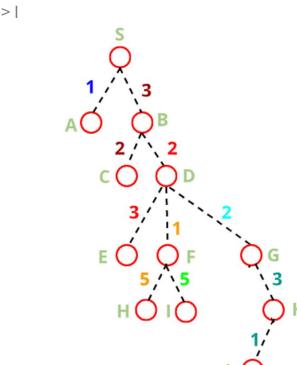


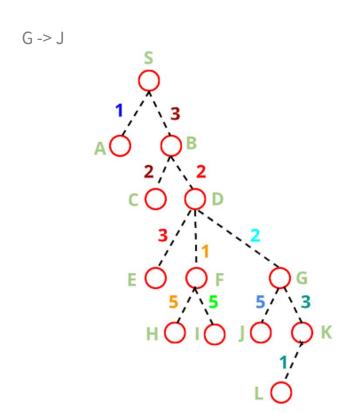


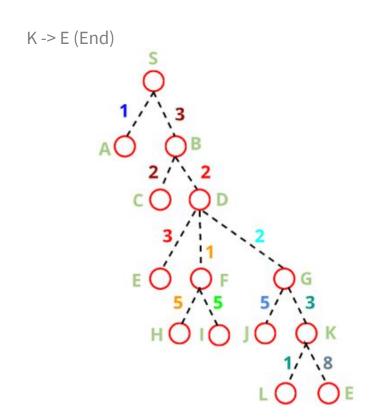
G -> K











Enhancement ideas

- Real-life application of the algorithms
 - o Prim's MST
 - Al pathfinding
 - Kruskal's MST
 - Gas piping

Conclusion

Prim's MST

- Big-O is O(E + log V)
 - E = Edges, V = Vertex
- Same performance for the maze problem
- Runs faster in dense graphs (several edges)

Kruskal's MST

- Big-O is O(E log V)
 - E = Edges, V = Vertex
- Same performance for the maze problem
- Runs faster in sparse graphs (few edges)

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