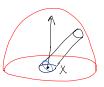


A unit area on the surface gives a cross sectional area of coso = n.l in the tube. (Only a slice through areas are shown.)

Irradiance E(x)



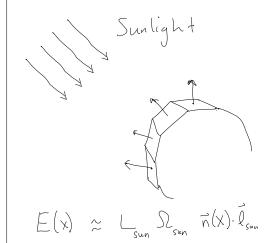




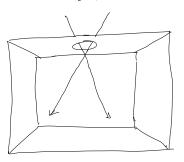
 $dE = L(x, \vec{e}) \vec{n}(x) \cdot \vec{l} d\Omega$ $E(x) = \int L(x, \vec{\ell}) \vec{n}(x) \cdot \vec{\ell} d\Omega$ Example - Sunlight

 $\lfloor (z, 0) \rfloor$ is very high in a small range of directions

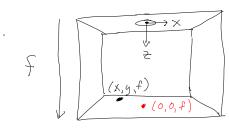
$$E(X) = \int L(X, \vec{\ell}) \vec{n}(X) \cdot \vec{\ell} d\Omega$$



Example: skylight (disk) window



What is the irradiance E(x)on the floor?

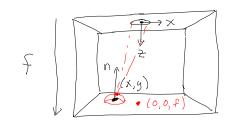


radience from sky is constant Lo as on an overcast (cloudy) day

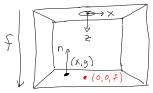
· center of disk skylight is (0,0,0)

· height of room is f

What is E(x,y) on the floor?



 $: E(x,y) = \int L(x,y,\vec{\ell}) \vec{n}(x,y) \cdot \vec{\ell}(x,y) d\Omega$ \approx Lo $n(x,y) \cdot \vec{\ell}(x,y) \Omega$



$$l(x,y) = \frac{(-x,-y,-f)}{\sqrt{x^2+y^2+f^2}}$$

$$l(x,y) = \frac{(0,0,-1)}{(0,0,-1)}$$

$$N(x,y) = \frac{f}{\sqrt{x^2 + y^2 + f^2}}$$

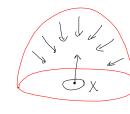
$$E(x,y) \approx L_0 n(x,y) \cdot \hat{I}(x,y) \Omega$$

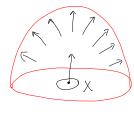
$$\Omega = \frac{A_{disk}}{\sum_{x=1}^{2} y_{x}^{2} + y_{x}^{2} + f_{x}^{2}}$$
Vecall def foreshorten of solid the angle of a source cone disk

Thus,

$$E(x,y) \sim L_0 A_{dusk} \frac{(n \cdot \vec{e})^4}{f^2}$$

incoming outgoing (incident) (exitant)













eather

velvet

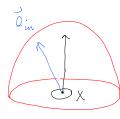
skin

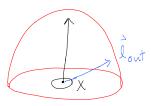
polish the apple (change its reflectance)





Modelling Surface Reflectance





How does light reflected in direction Don't depend on light arriving from direction In?



 $E(X) = \int L(X_1\vec{\ell}) \vec{n}(X) \cdot \vec{\ell} d\Omega$

 $L\left(\alpha,\, L_{out}\right) = \int \rho\left(x, \vec{\ell}_{in}, \vec{\ell}_{out}\right) \; L\left(x, \vec{\ell}_{in}\right) \, \vec{n}(x) \cdot \vec{\ell}_{in} \; d\, \vec{\ell}_{in}$

called "bidirection reflectance BRDF distribution function"

* property of surface material only

http://www.merl.com/brdf/

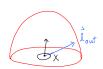
BRDF's are heavily used in computer graphics

- Phong model (early 1970's)
- Ward model (early 1990's)
- BSS, RDF (2001)

subsurface scattering in skin, marble

Special Case: Lambertian surface (matte)





 $L(x, l_{n+}) = \int p(x, l_{in}, l_{out}) L(x, \vec{l}_{in}) \vec{n}(\vec{x}) \cdot \vec{l}_{in} dl_{in}$ $= \int \rho(x) L(x, lin) \vec{n}(x) \cdot \vec{l}_{in} d\vec{l}_{in}$

Special Case

· Sunlight · Lambertian reflectance



 $L(x, l_{out}) \approx c \cdot p(x) n(x) \cdot \vec{l}_{sun}$