

$$\frac{z}{z} = f$$

$$(x,y) = \left(f \frac{x}{z}, f \frac{y}{z}\right)$$



$$ax + by + cz = d$$

$$Multiply by \frac{f}{z}.$$

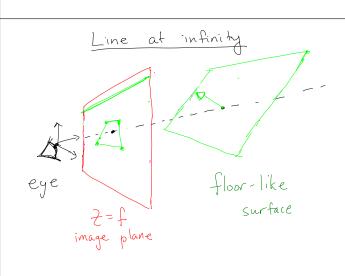
$$a\frac{fx}{z} + b\frac{fy}{z} + c\frac{fz}{z} = \frac{fd}{z}$$

$$ax + by + cf = \frac{fd}{z}$$

Example: a plane

ax + by + cf =
$$\frac{fd}{z}$$

het $z \Rightarrow \infty$ gives
 $ax + by + cf = 0$
"line at infinity"

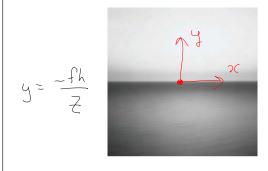




Example: ground plane

$$y = -h$$
 $y = f \frac{y}{Z}$ When $Z \rightarrow \infty$
 $y \rightarrow 0$
 $y \rightarrow 0$

When $Z \rightarrow \infty$
 $y \rightarrow 0$



Ground plane
$$y=-h$$

$$y=-\frac{fh}{z}$$

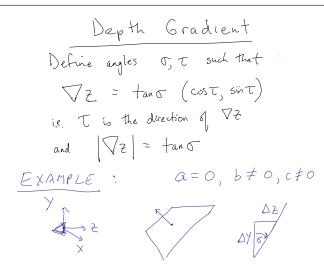
$$\Delta y = \frac{fh}{z^2} \Delta z \quad \Delta y = \frac{h}{z} \quad \text{foreshortening of tiles}$$

$$\lambda = \frac{f}{z} \quad \Delta y = \frac{h}{z} \quad \text{on position}$$

Depth Gradient
$$\frac{\partial z}{\partial x} = -\frac{a}{c} \qquad \frac{\partial z}{\partial y} = -\frac{b}{c}$$

$$| \nabla z | = \left(-\frac{a}{c}, -\frac{b}{c}\right)$$

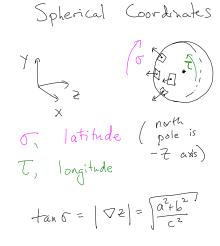
$$| \nabla z | = \left(\frac{a^2 + b^2}{c^2}\right)$$

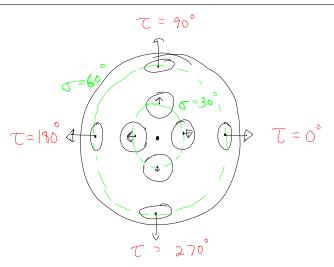


Note: The following few slides were changed to conform better to the lecture notes.

 $\Delta x = \frac{f}{2} \Delta X$

Surface Normal aX + bY + cZ = dnormal vector to plane is (a,b,c) (a,b,c)



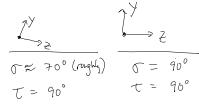


slant & tilt





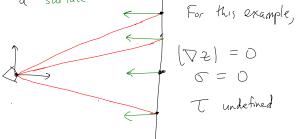


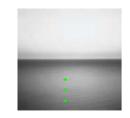




WARNING (POSSIBLE CONFWION)

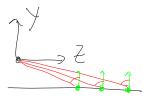
The definition of slant and tilt applies to a (global) plane, not to the angles between the line of sight to a point and a surface normal.





(g'lobal) slant is constant (0=0). But "local slant" varies. ie angle between

In this example,



line of sight and normal vector,