

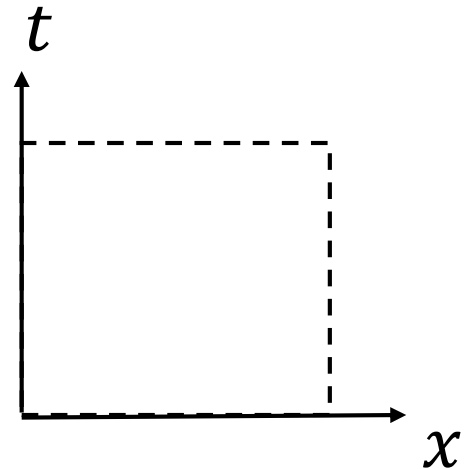
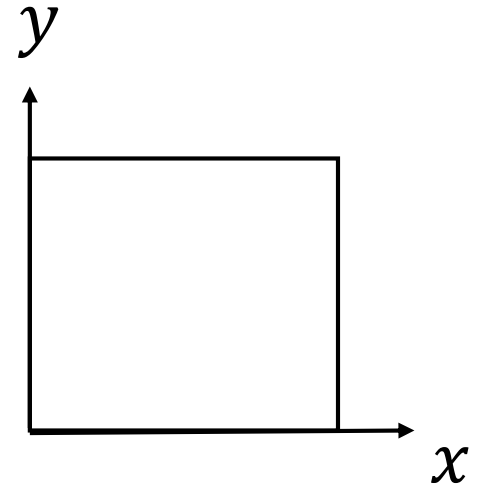
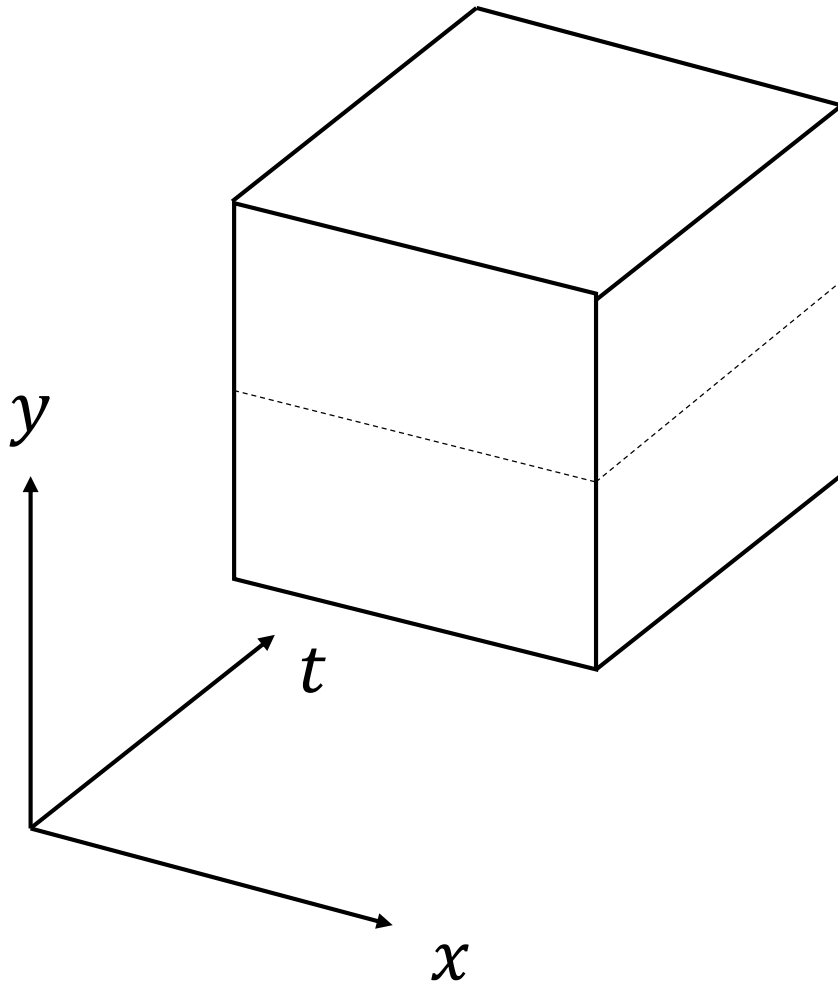
COMP 546

Lecture 7

image motion

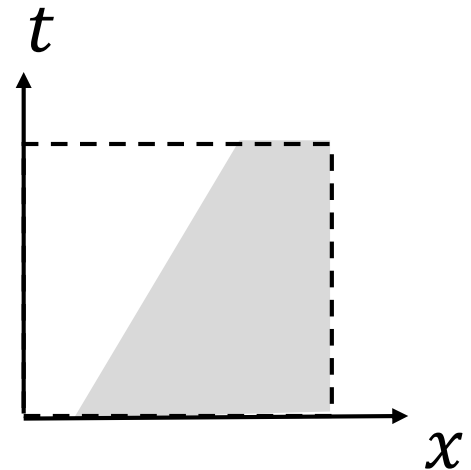
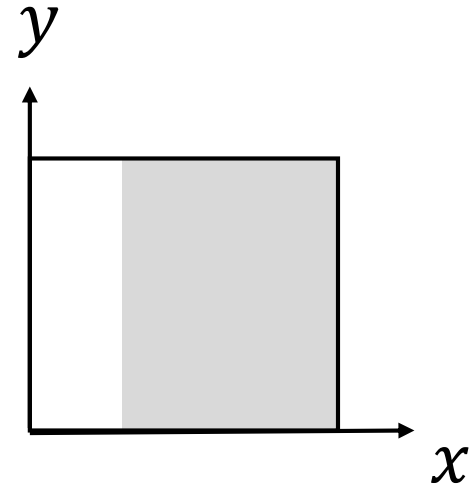
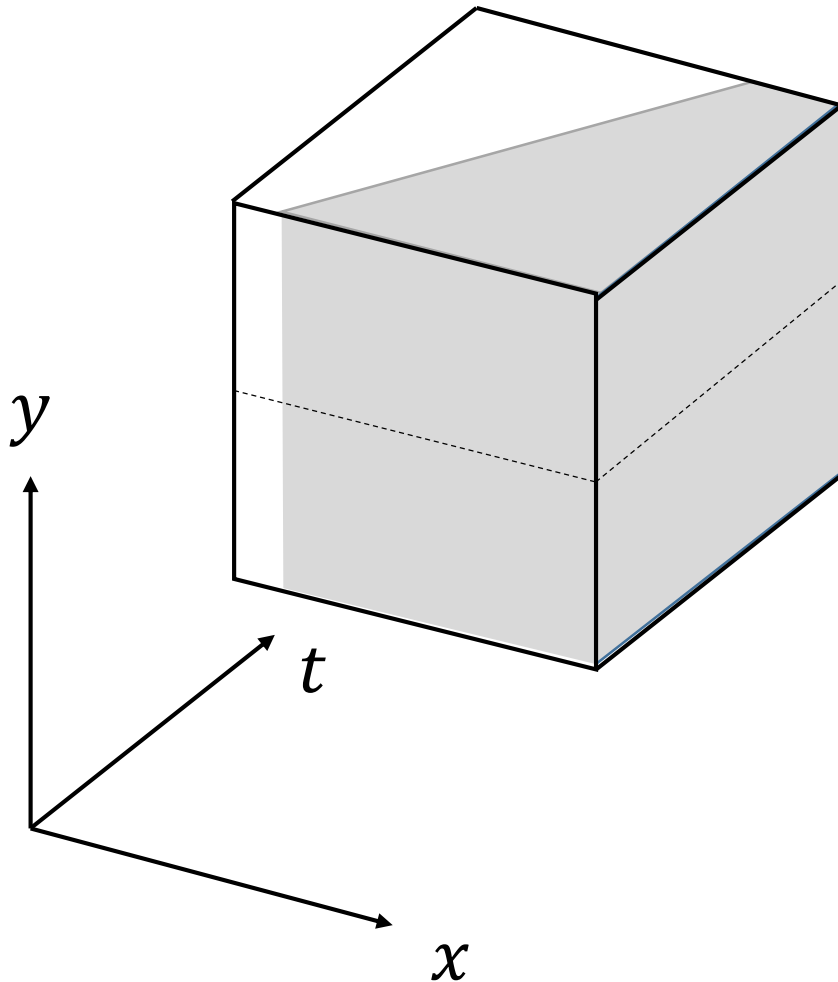
Thurs. Jan. 31, 2018

Time varying images (XYT)



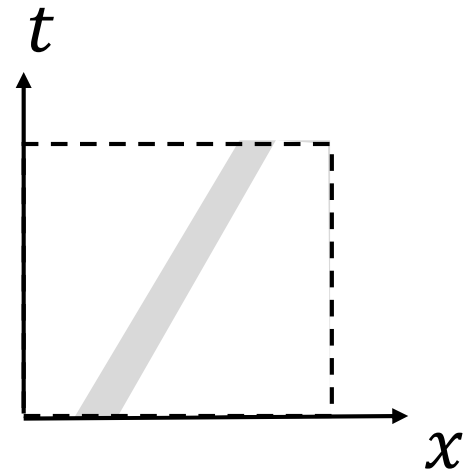
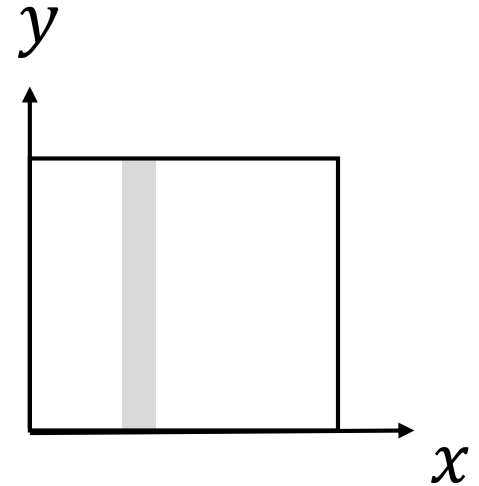
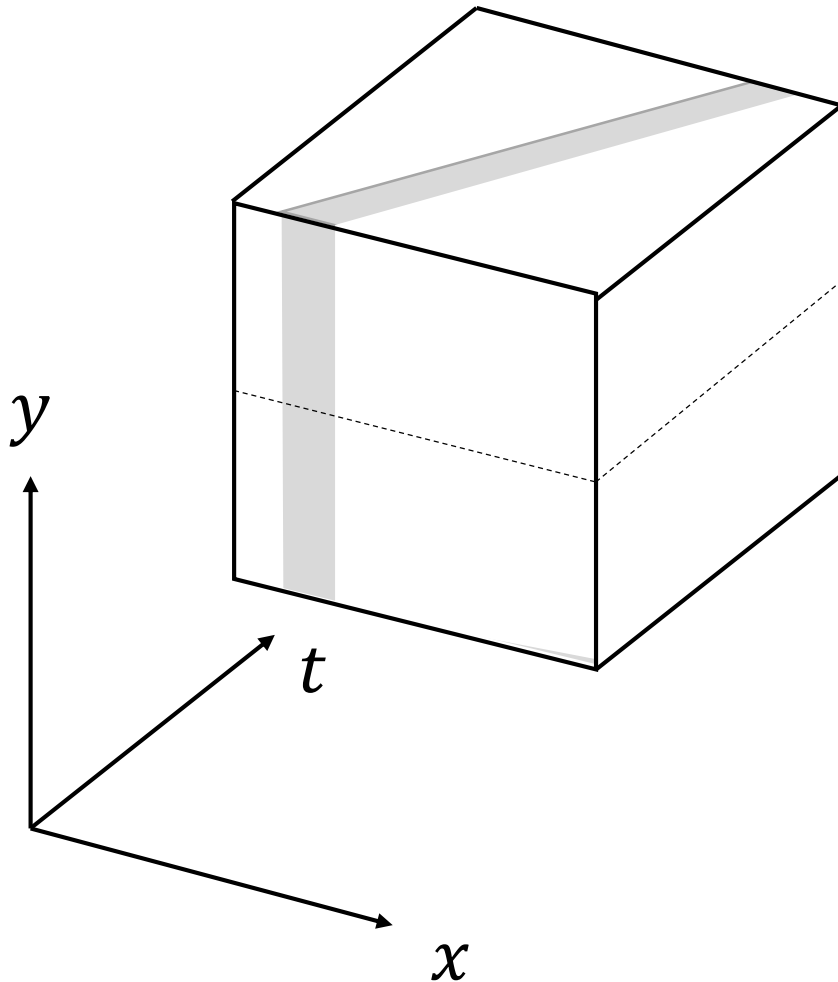
Motion in XYT

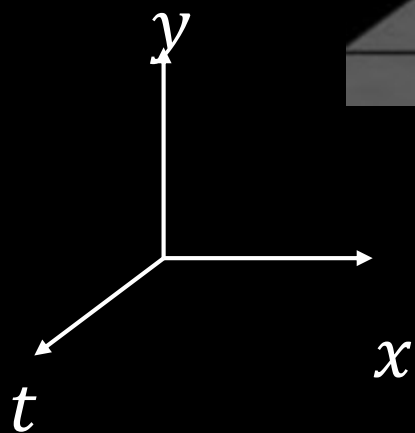
e.g. translating vertical edge



Motion in XYT

e.g. translating vertical bar

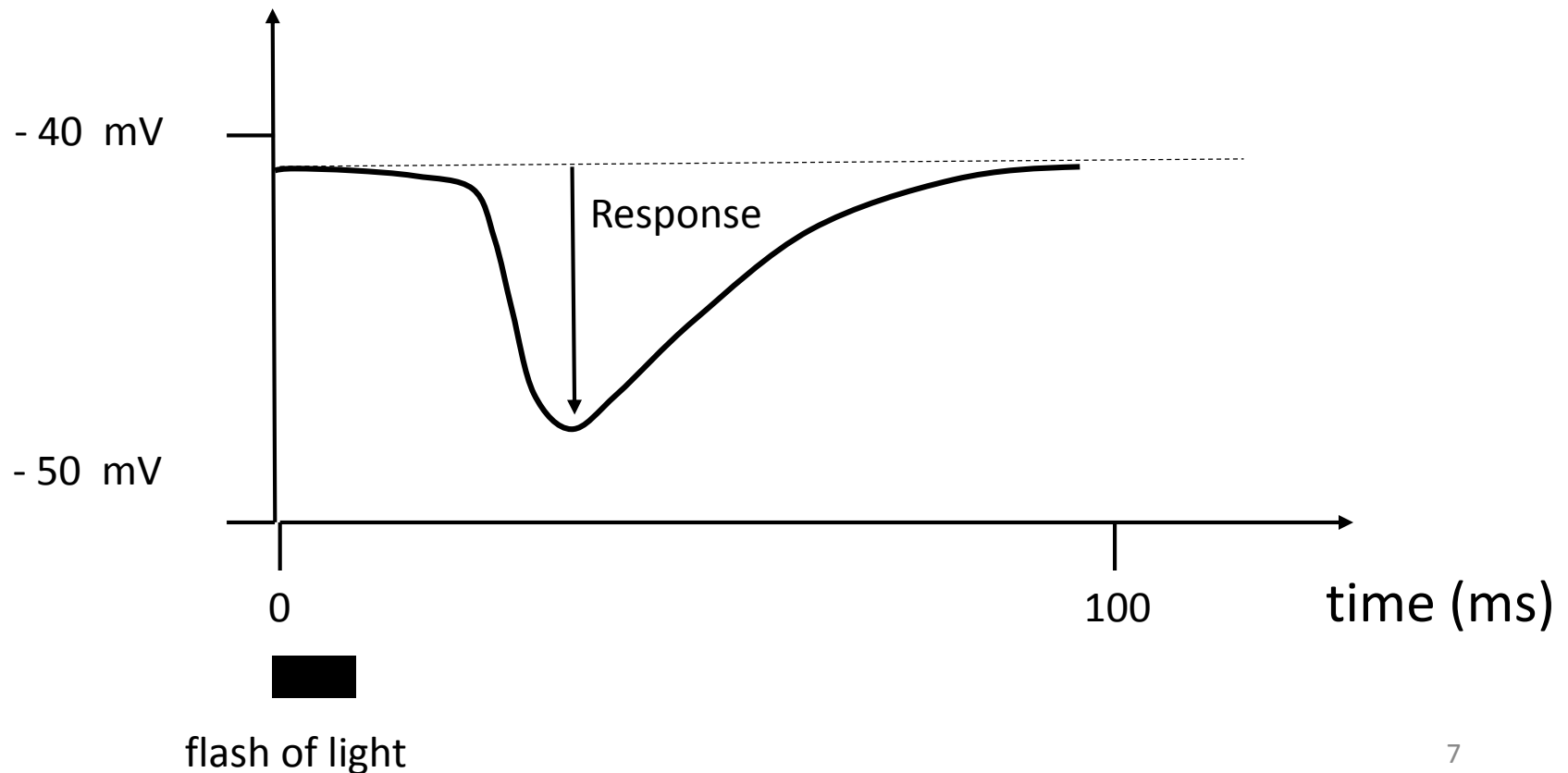




How do the eye and brain
(retina, LGN, V1)
measure image motion?

Photoreceptor response to a *brief flash of light*

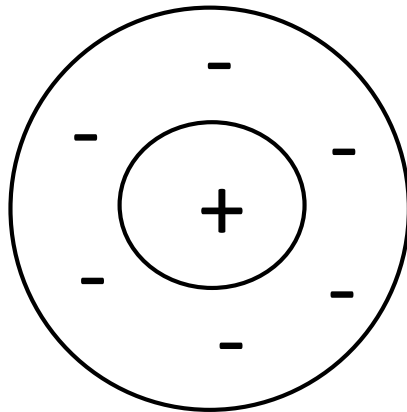
(recall from lecture 3)



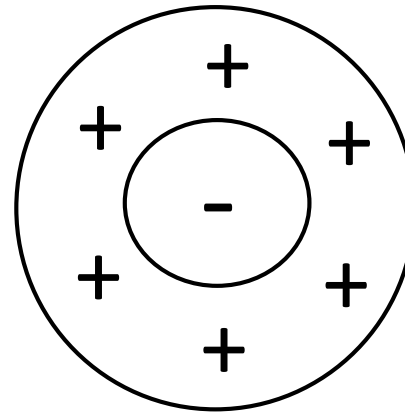
Retinal Ganglion and LGN cells

Our models up to now have been static only.

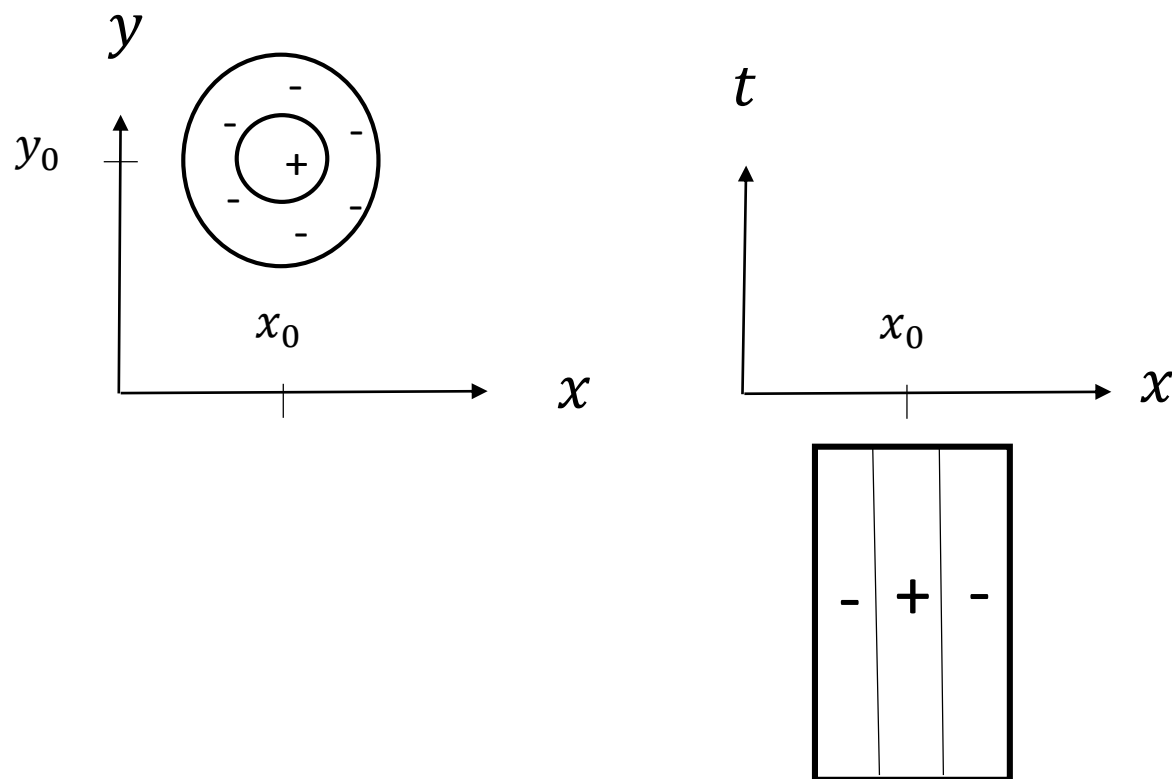
ON center,
OFF surround



OFF center,
ON surround



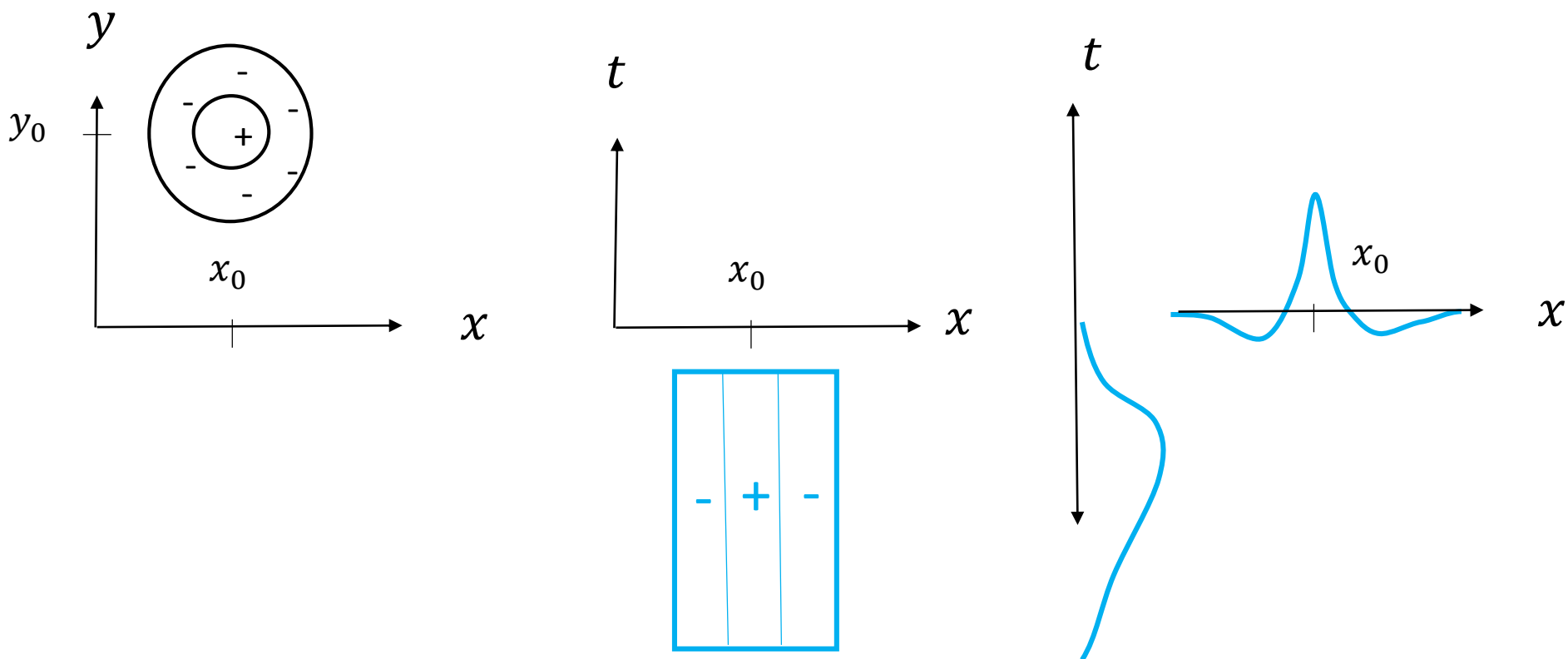
XY and XT slices through DOG(x,y,t)



The response at $t = 0$
depends on the image
intensities in the past ($t < 0$).

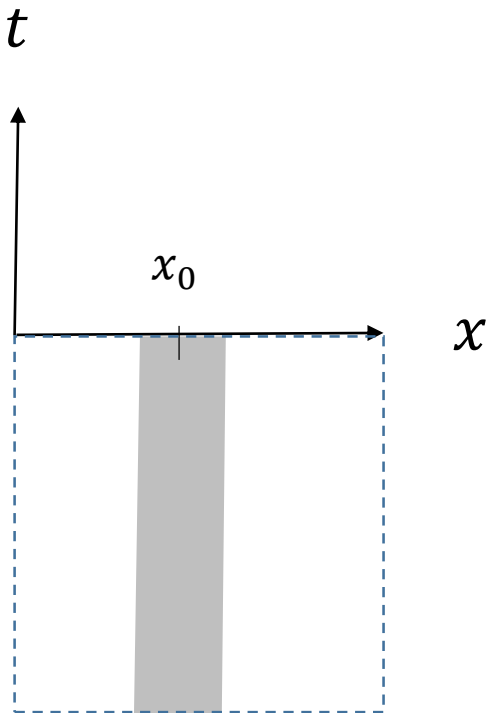
Space-time separable model

$$g(x, y, t) = DOG(x, y)f(t)$$

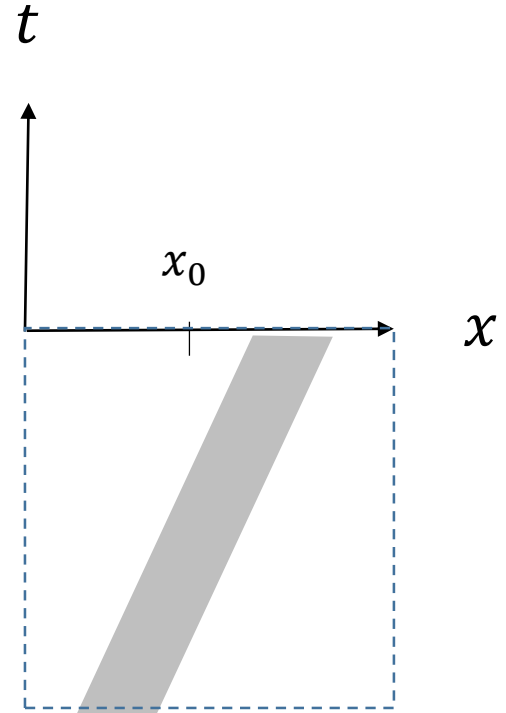
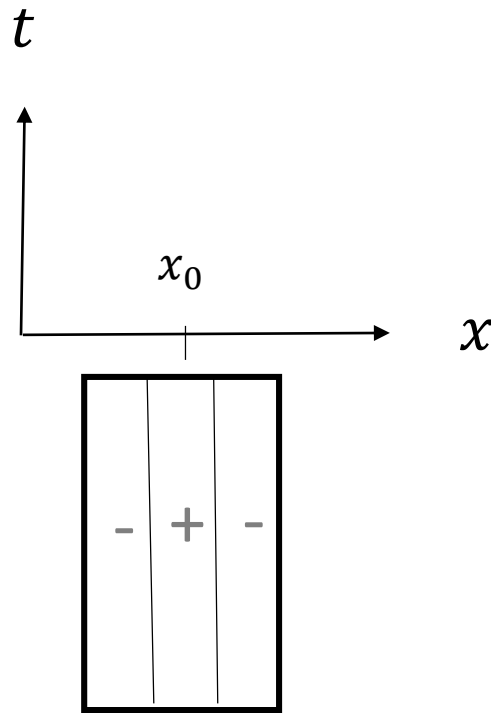


The response at $t = 0$
depends on the image
intensities in the past ($t < 0$).

This cell would
respond better to
the static image.

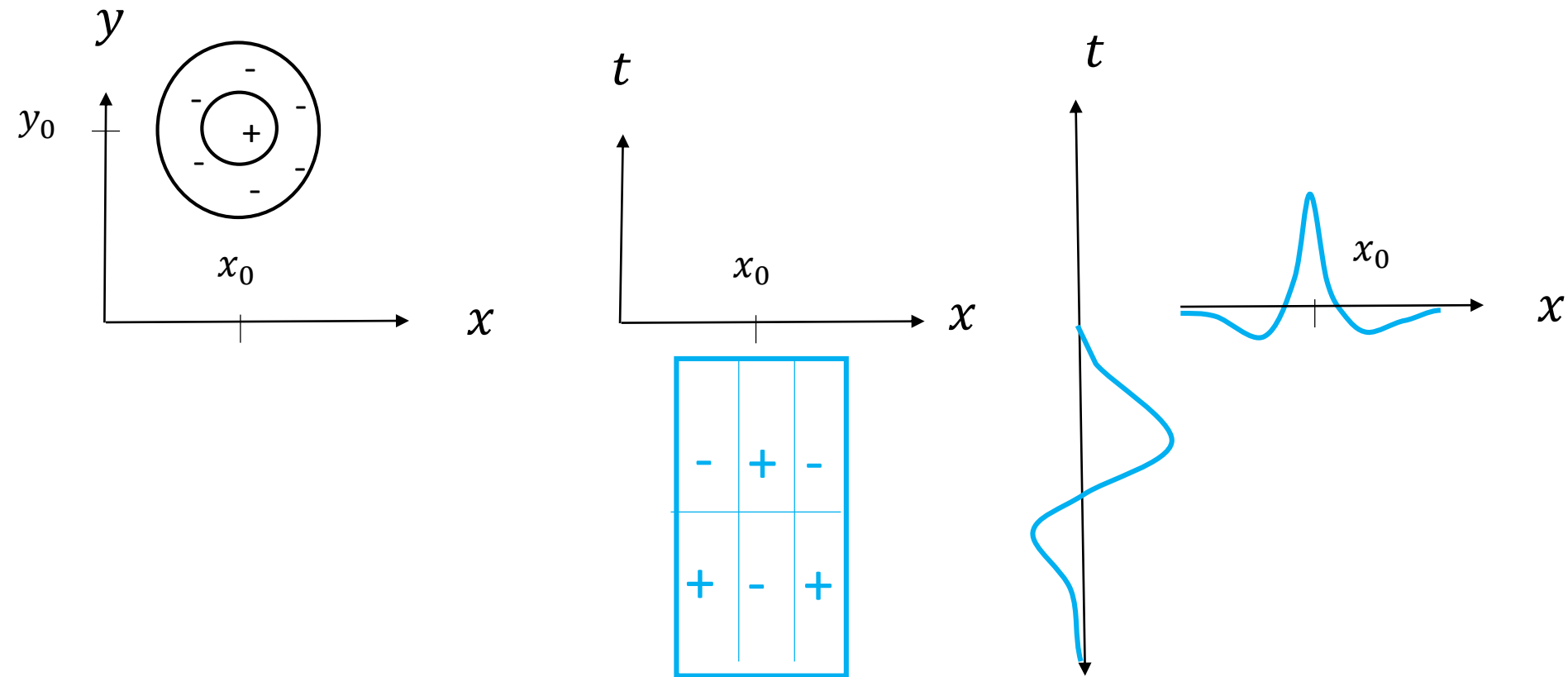


static

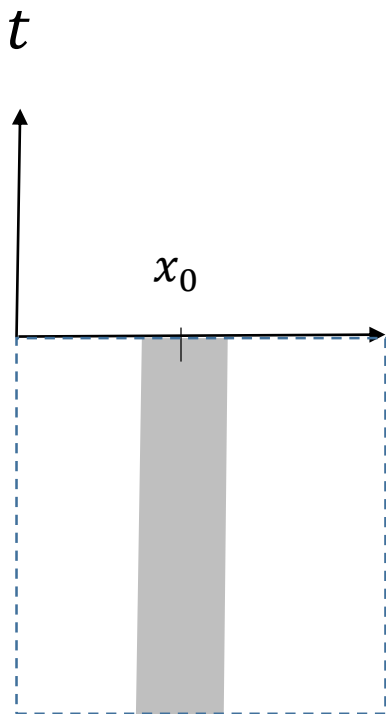


moving

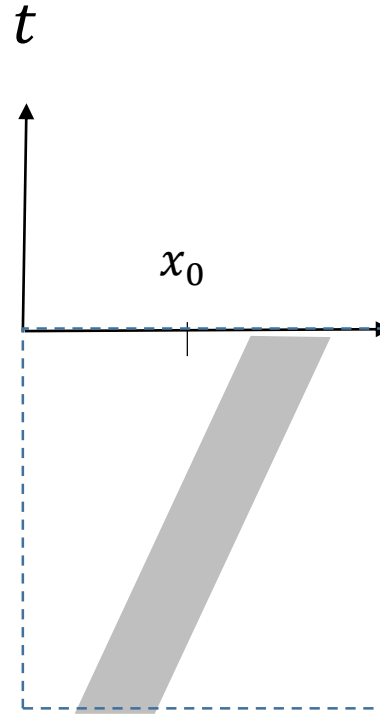
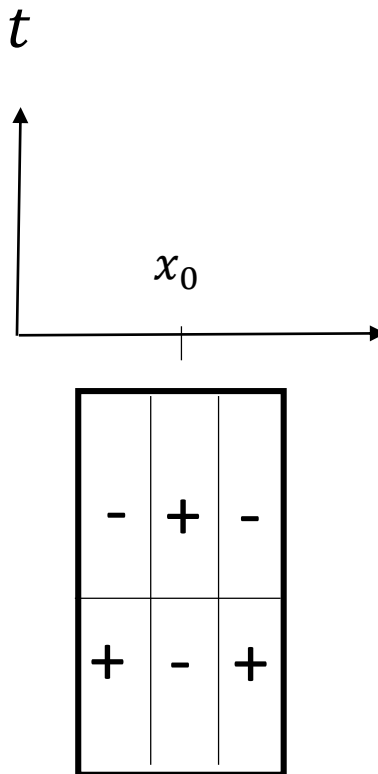
Space-time separable model (with temporal sensitivity)



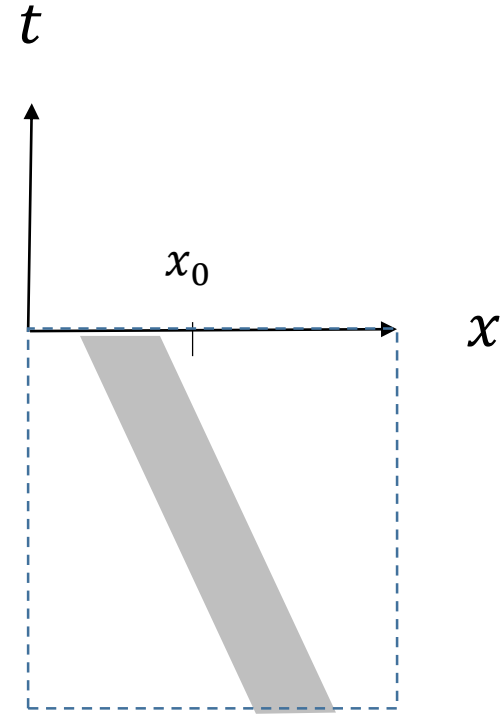
This cell would
respond better
to motion than
to static image.



static

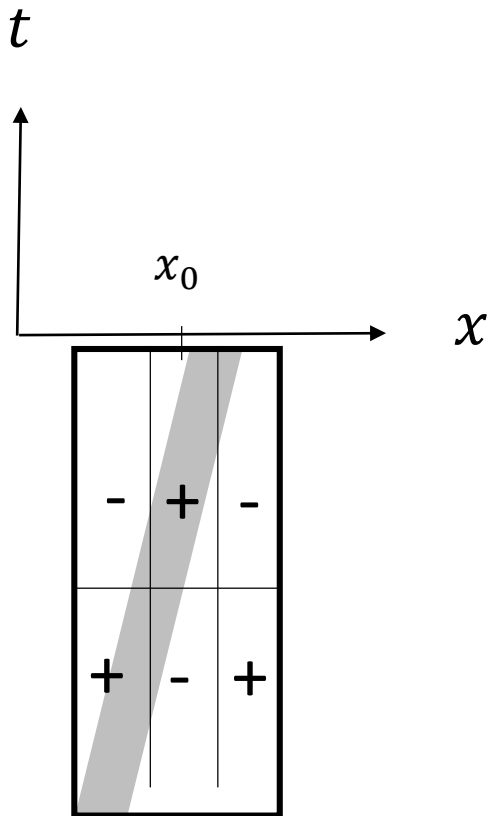


moving

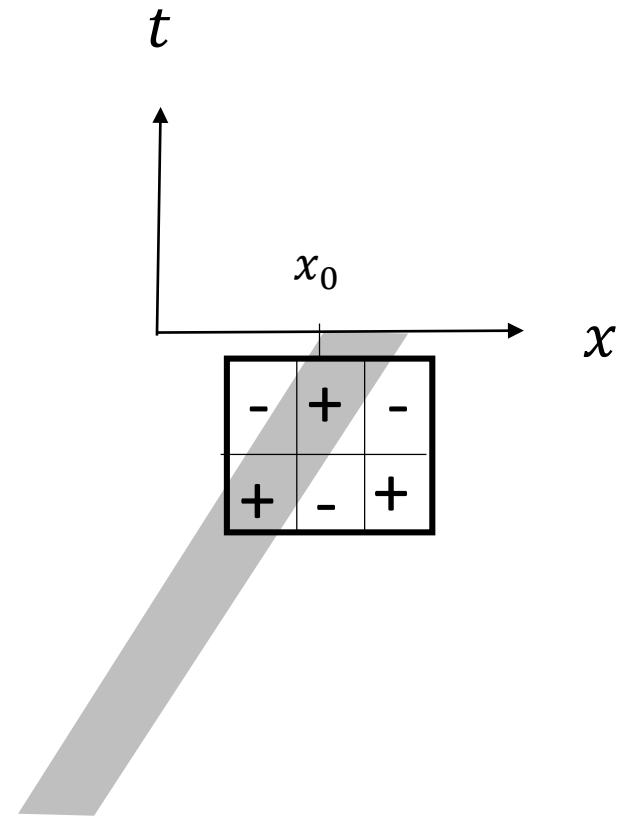


moving

This cell would respond better to *slow* motion.

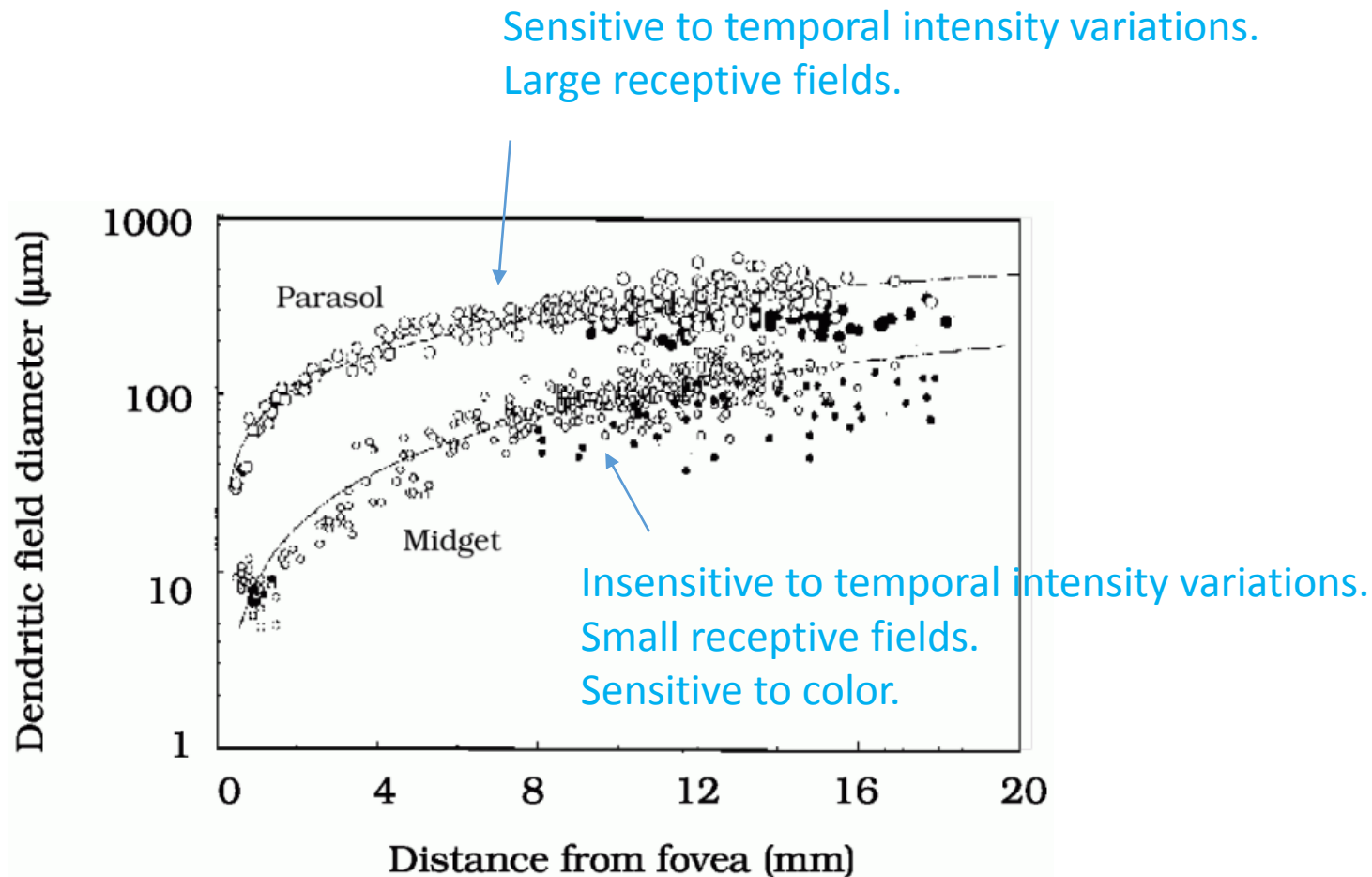


This cell would respond better to *fast* motion.

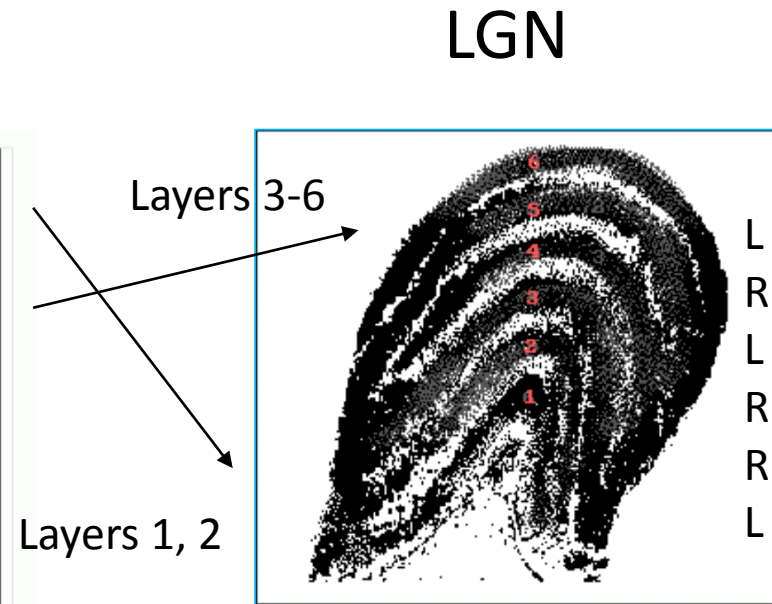
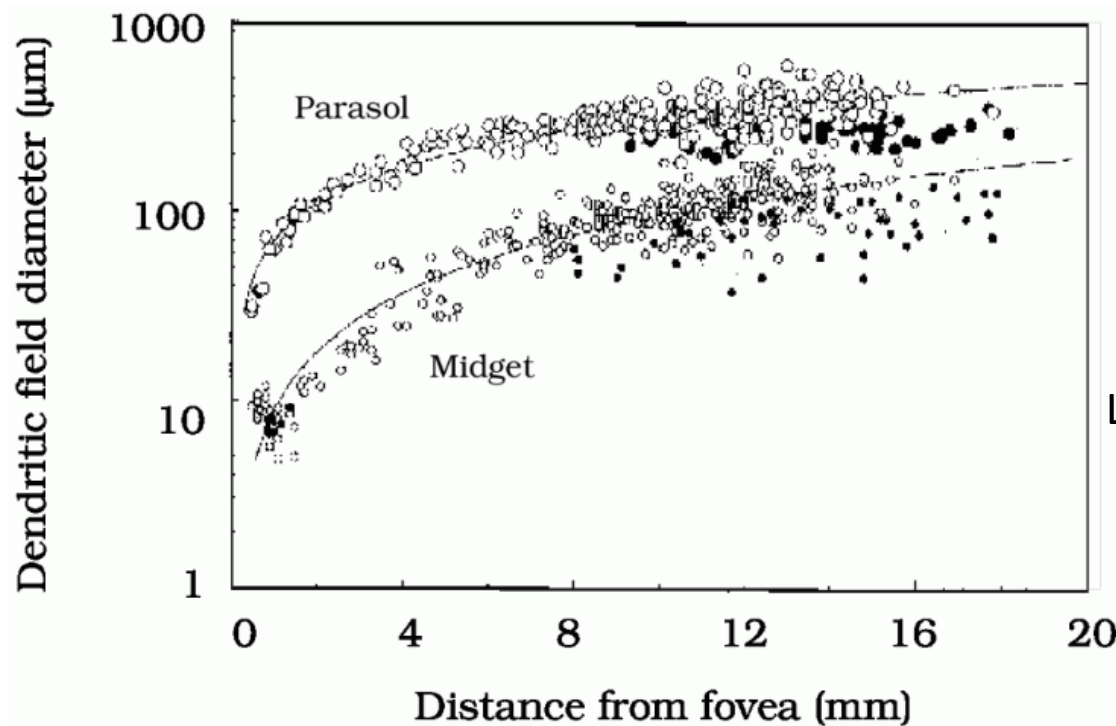


For your interest... (not on exam)

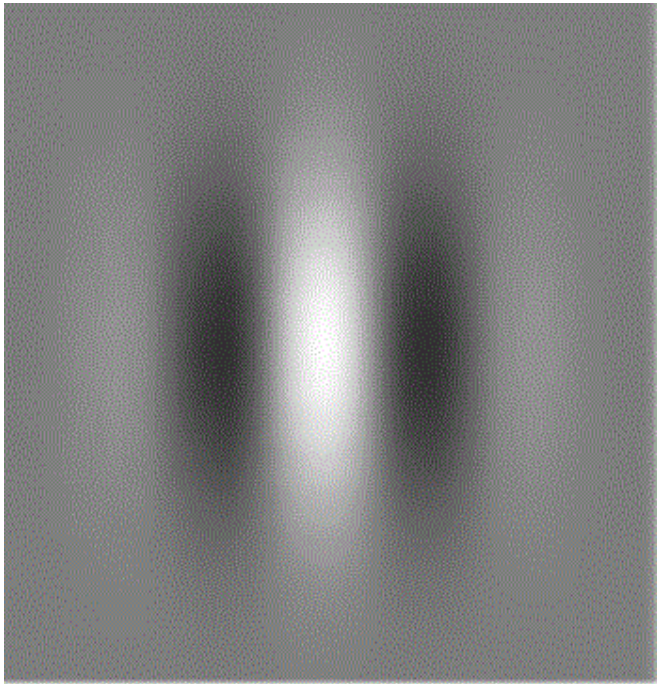
There are two classes of retinal ganglion cells...



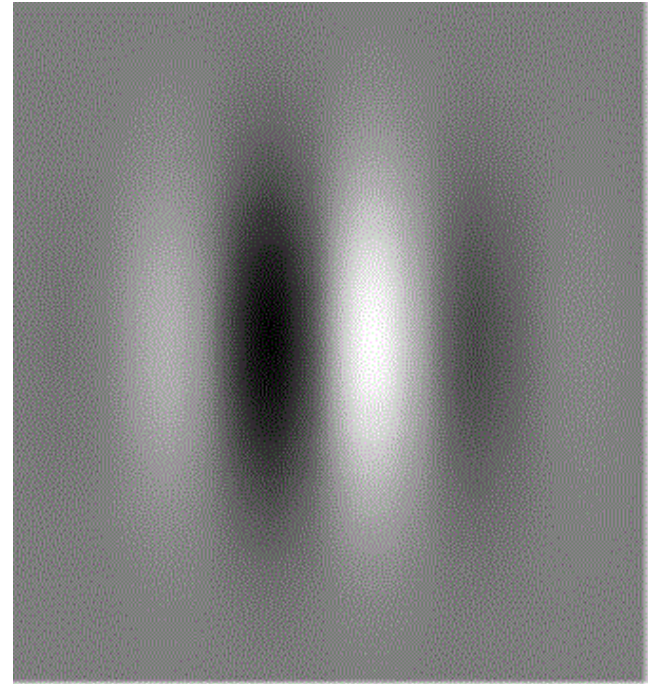
... and these two classes map to distinct layers in the LGN.



V1 cells can detect oriented structure in XY.
What about XT and YT ?

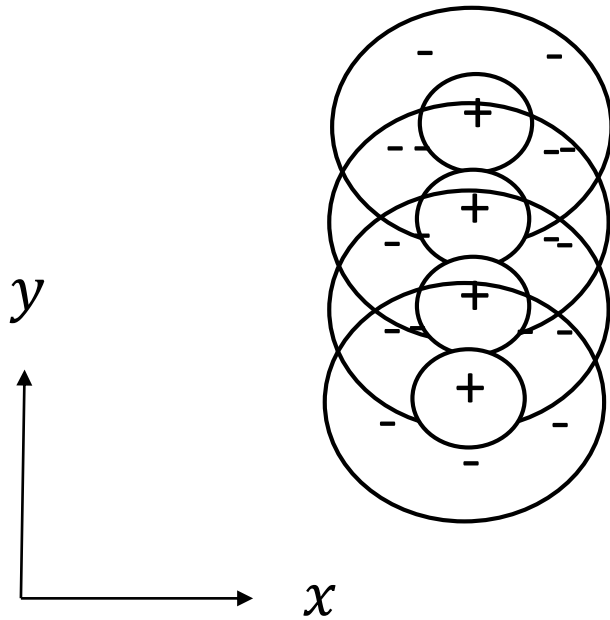


$\cos\text{Gabor}(x,y)$

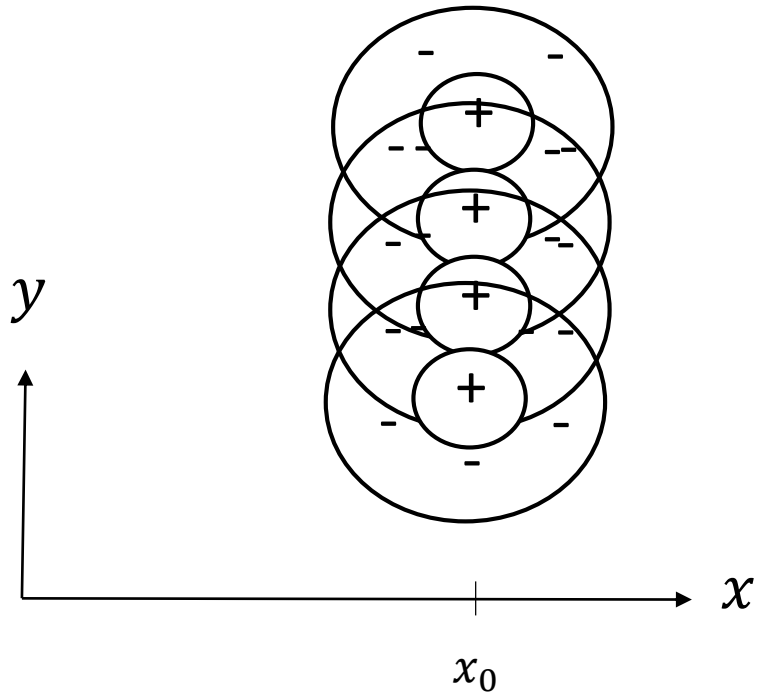


$\sin\text{Gabor}(x,y)$

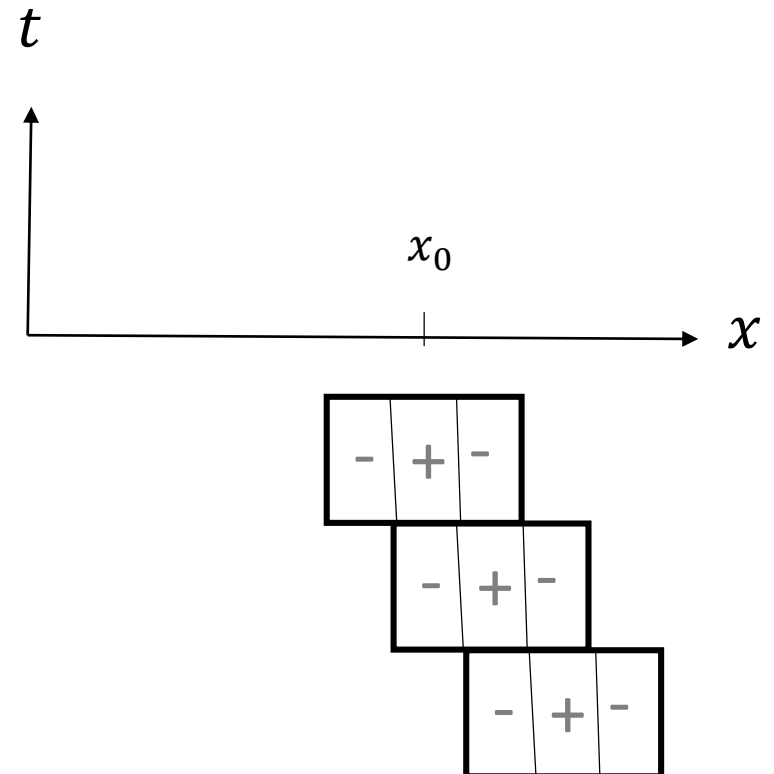
Hubel and Wiesel's idea for
a simple cell (line detector).

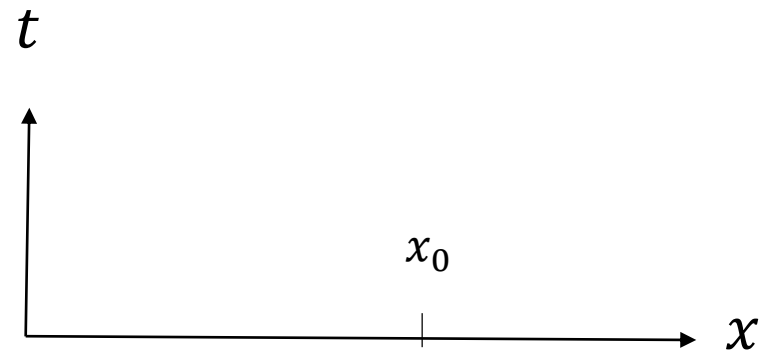


Hubel and Wiesel's idea for
a simple cell (line detector).



Reichardt (1950's):
Temporal delays
combined with spatial
shifts could produce
motion direction
sensitivity.



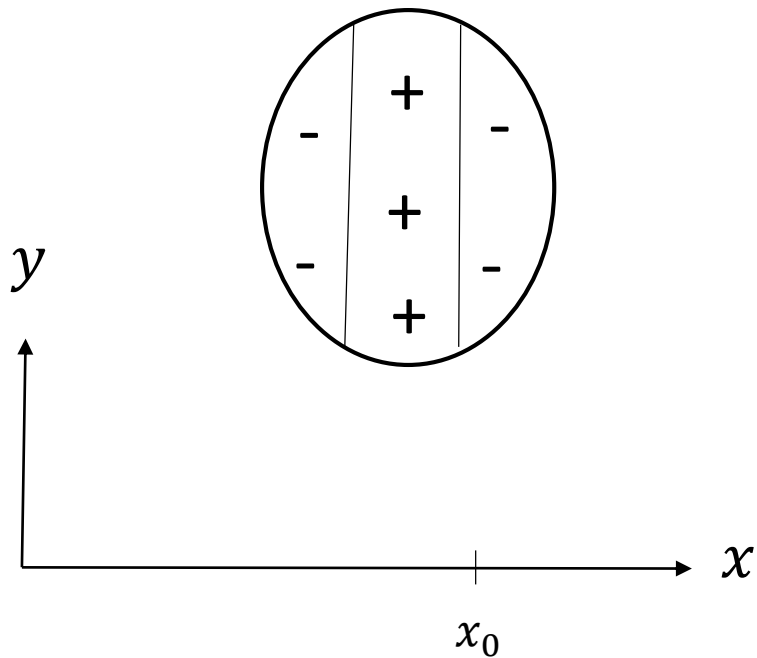


Alternatively, using time
varying DOGs:

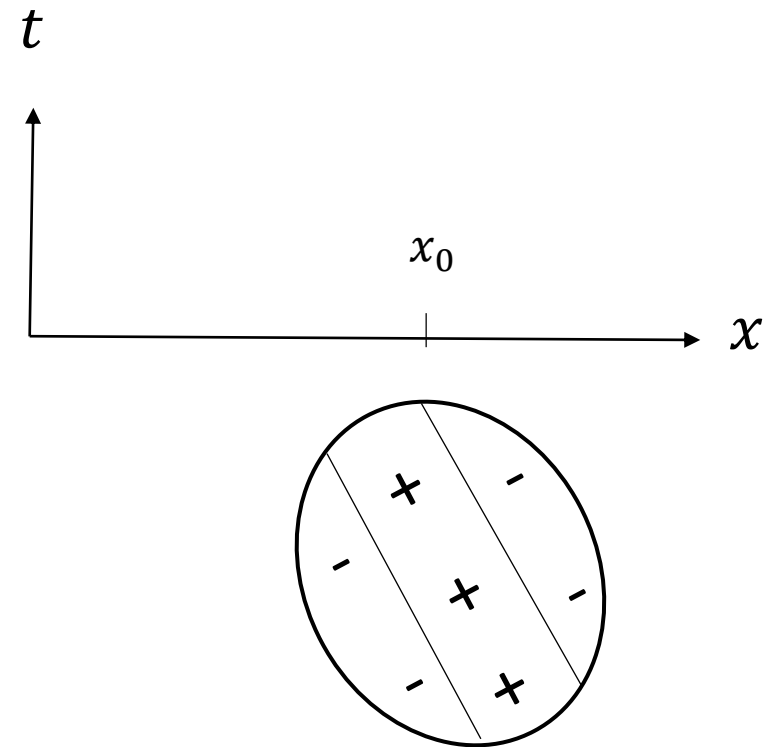
-	+	-
+	-	+

-	+	-		
+	-	+	-	
	+	-	+	-
		+	-	+
			+	-

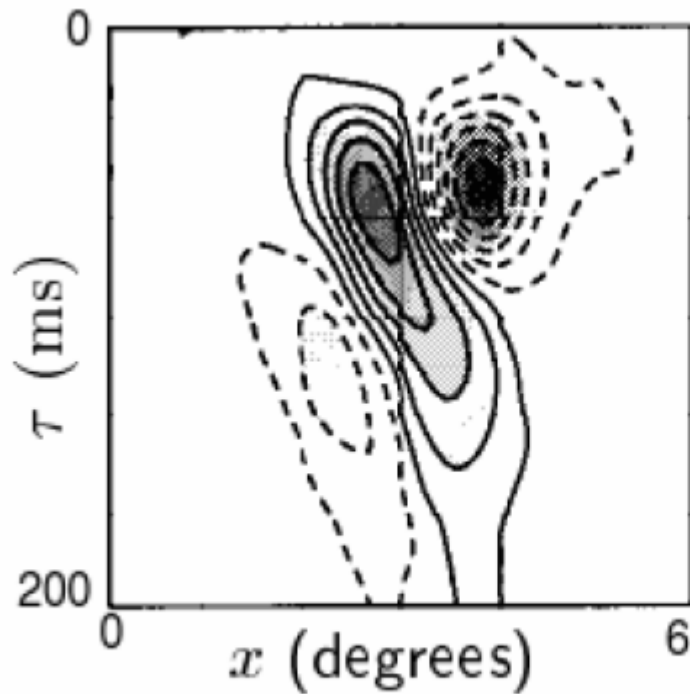
Orientation and direction tuning in V1



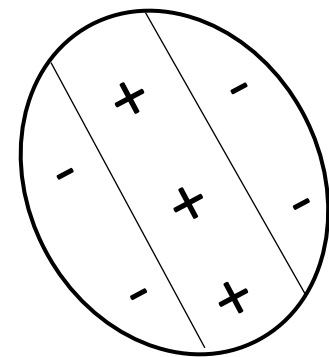
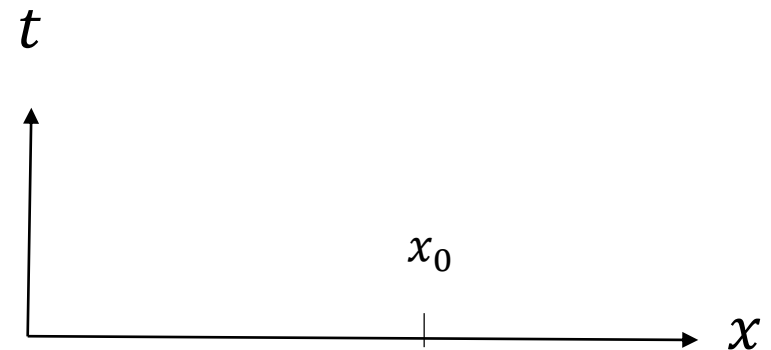
Cell is selective for
vertically line
moving to the left.



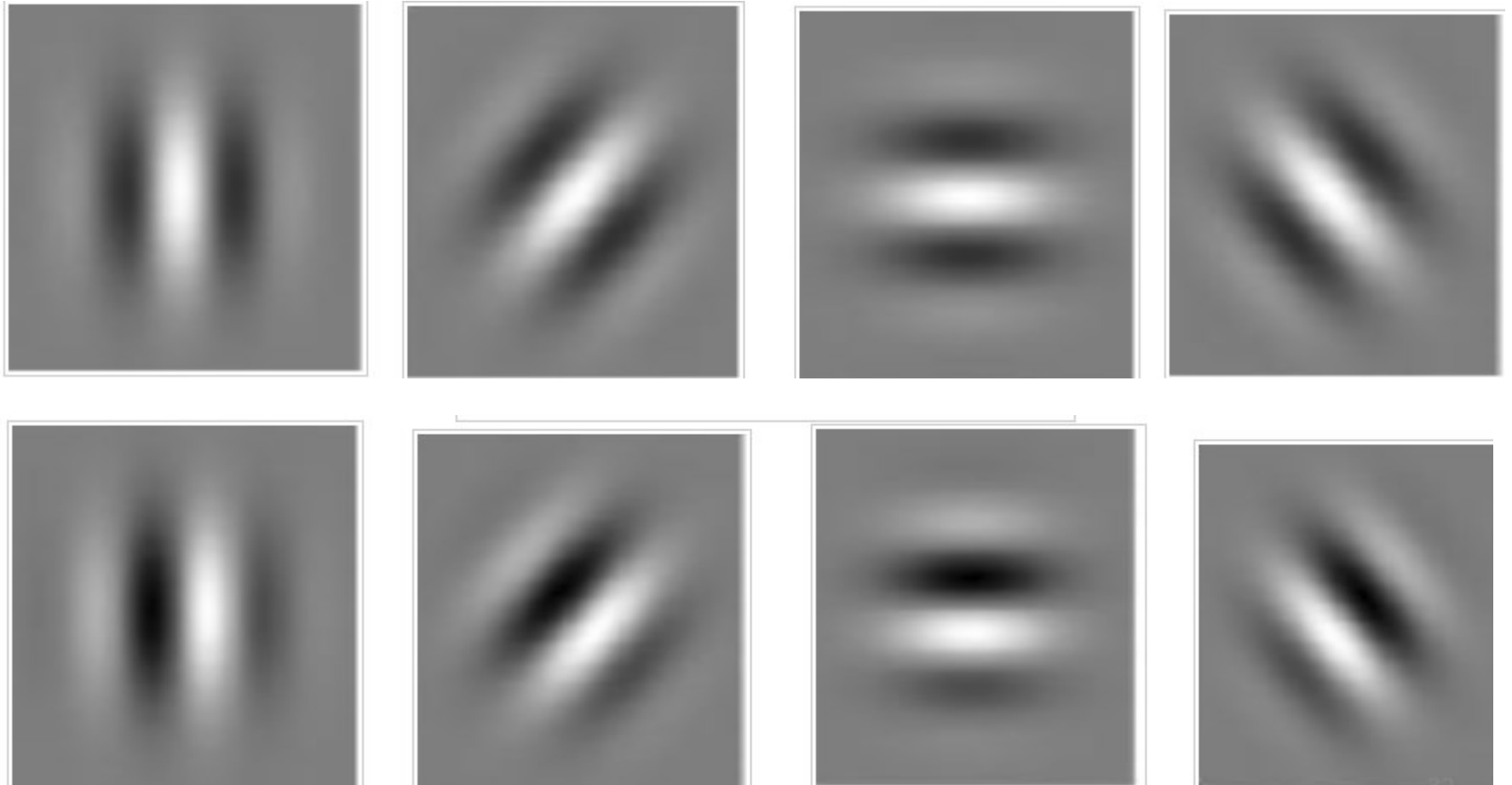
XT slice through receptive field profile of V1 cell



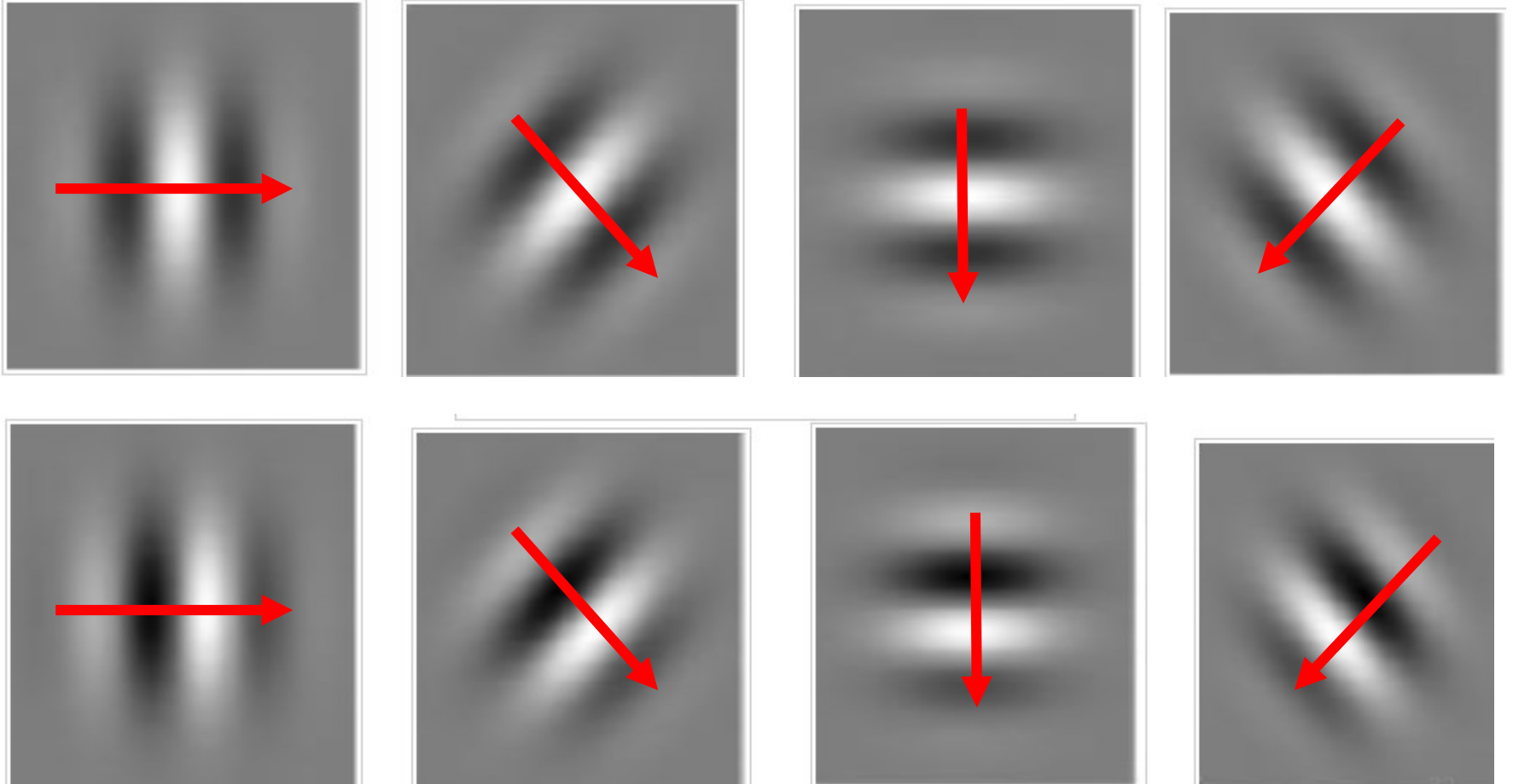
\mathcal{X}



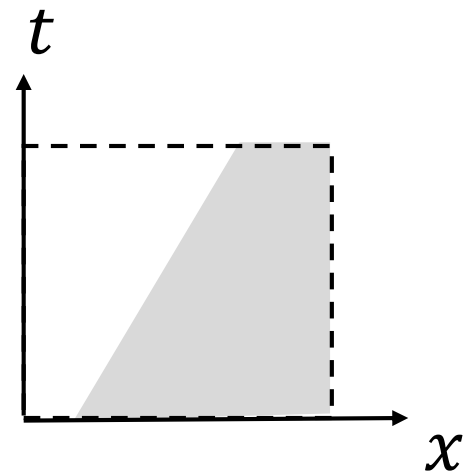
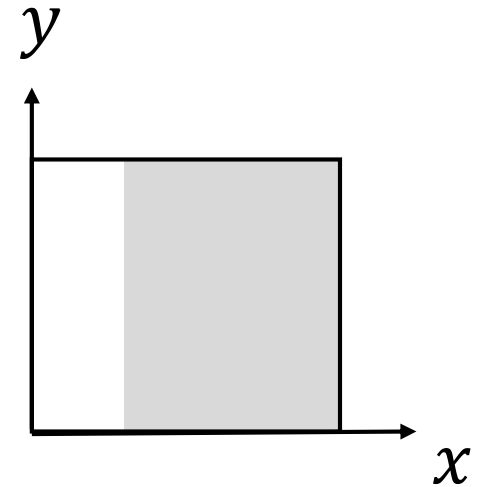
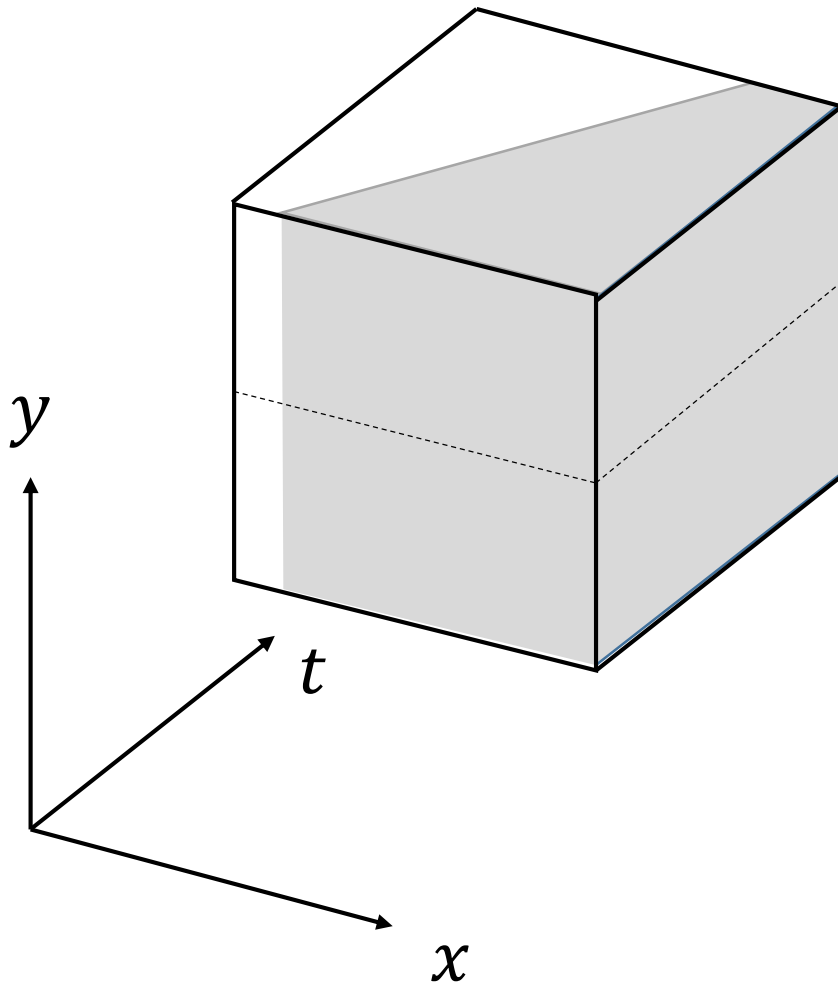
Simple and Complex Cells are *Orientation Tuned* (XY slice)
and many are binocularly disparity tuned.



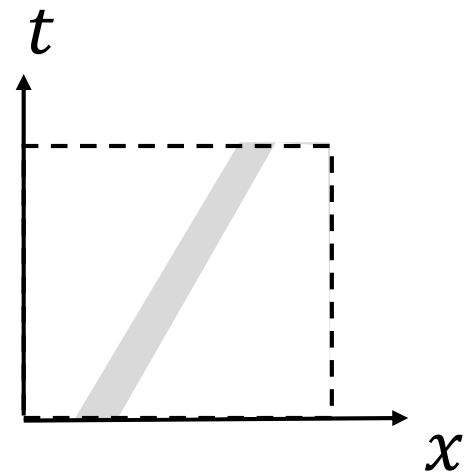
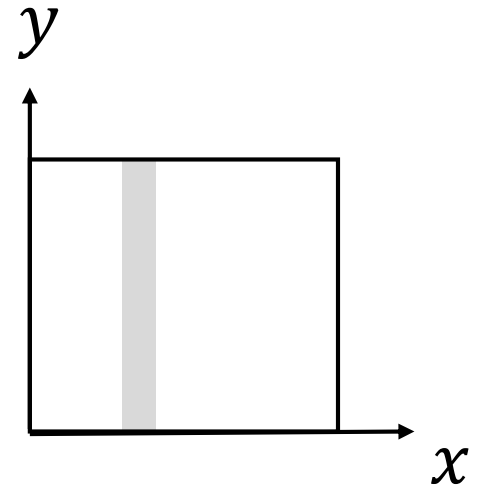
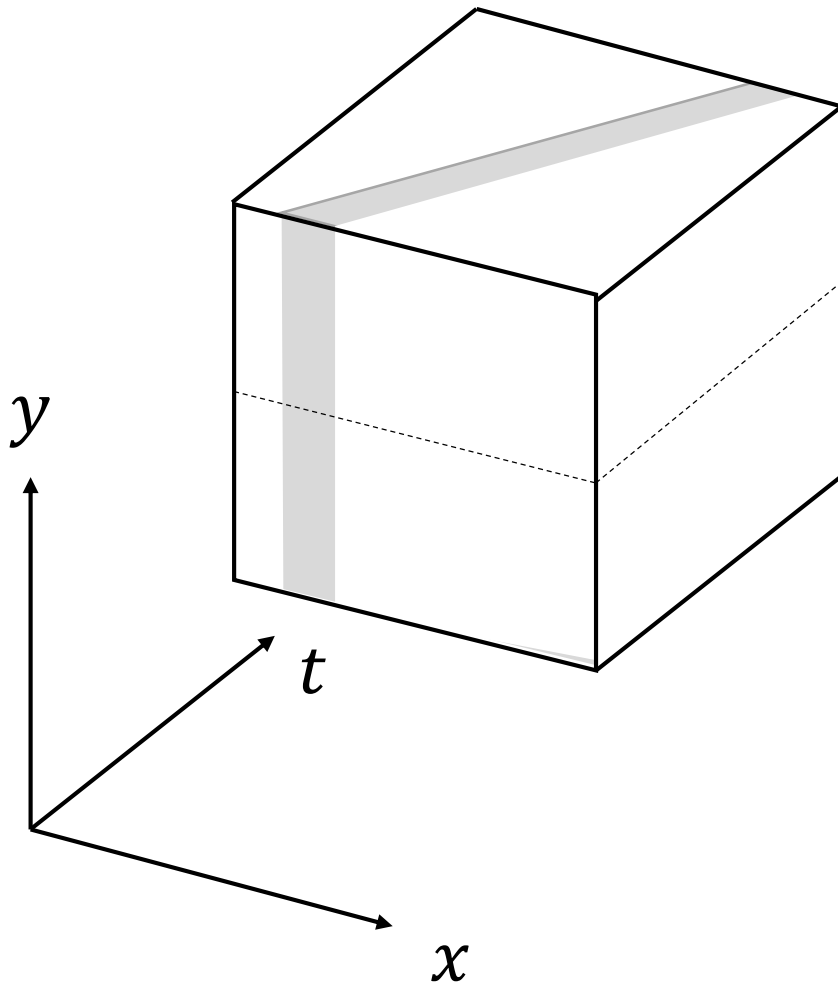
Many are also *motion direction and speed tuned*.



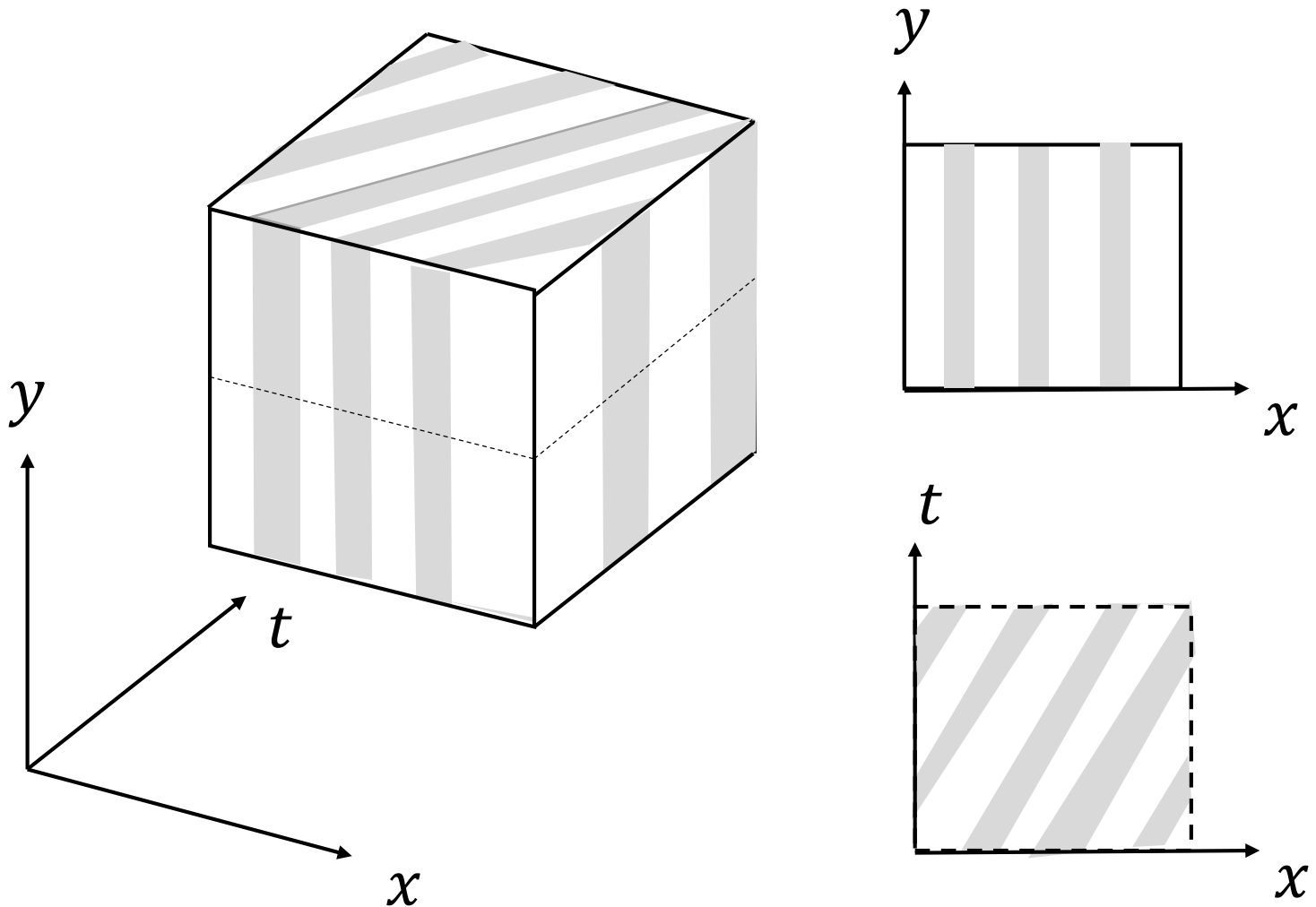
Vertical edge moving to the right



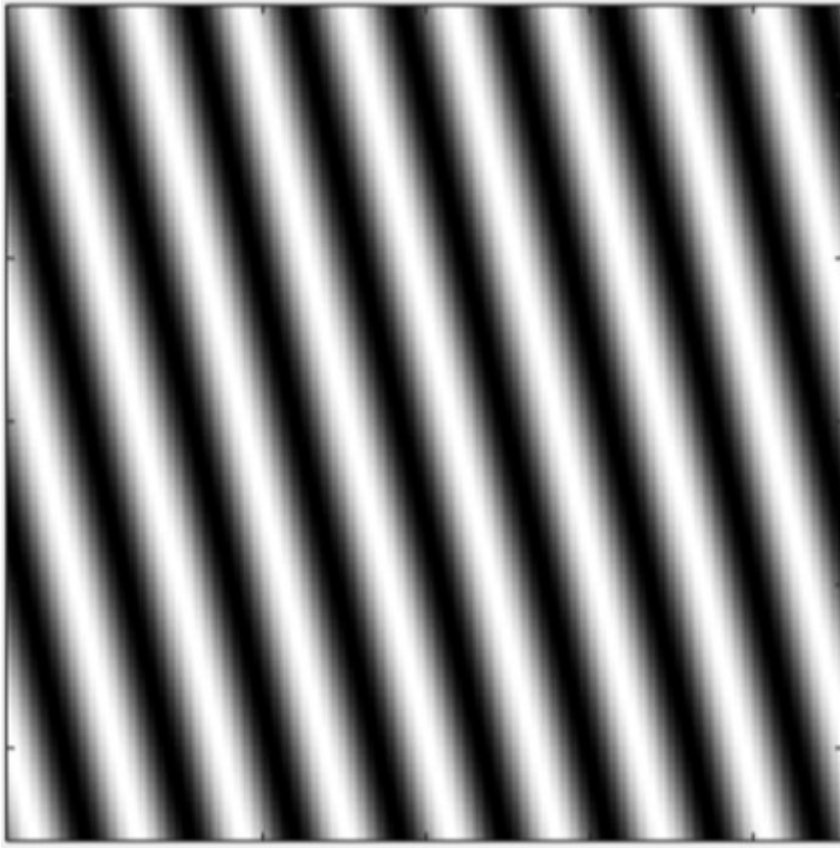
Vertical bar moving to the right



Vertically 2D sine moving to the right (wave)



Recall: 2D sine



$$\sin\left(\frac{2\pi}{N}(k_x x + k_y y)\right)$$

$$e.g. \quad k_x = 8$$

$$k_y = 2$$

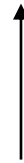
$$N = 256$$

sine wave in XYT

$$\sin \left(\frac{2\pi}{N} (k_x x + k_y y) + \frac{2\pi}{T} \omega t \right)$$



Spatial frequency
(cycles per N pixels)



Temporal frequency
(cycles per T frames)

Exercise: what is the speed of the wave?

3D sine in XYT

$$\sin \left(\frac{2\pi}{N} (k_x x + k_y y) + \frac{2\pi}{T} \omega t \right)$$

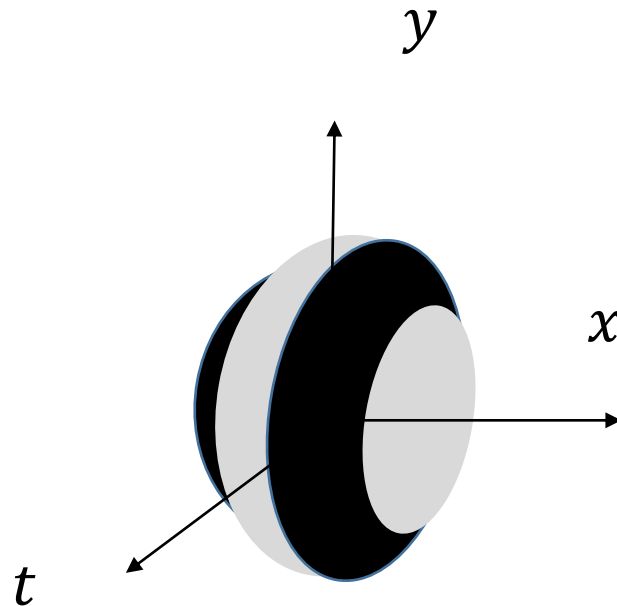
$$\frac{2\pi}{N} (k_x x + k_y y) + \frac{2\pi}{T} \omega t = c$$

is the equation of a plane in XYT.

$$\left(\frac{2\pi}{N} k_x, \frac{2\pi}{N} k_y, \frac{2\pi}{T} \omega \right) \cdot (x, y, t) = c$$

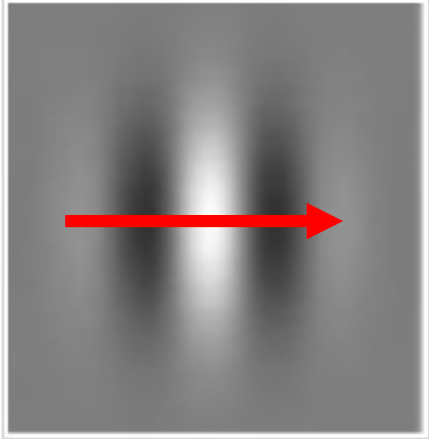
3D vector normal to the plane

3D sine Gabor

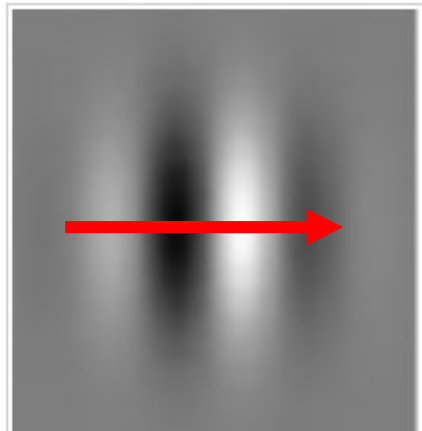


$$\sin \left(\frac{2\pi}{N} (k_x x + k_y y) + \frac{2\pi}{T} \omega t \right) G(x, y, t, \sigma_x, \sigma_y, \sigma_t)$$

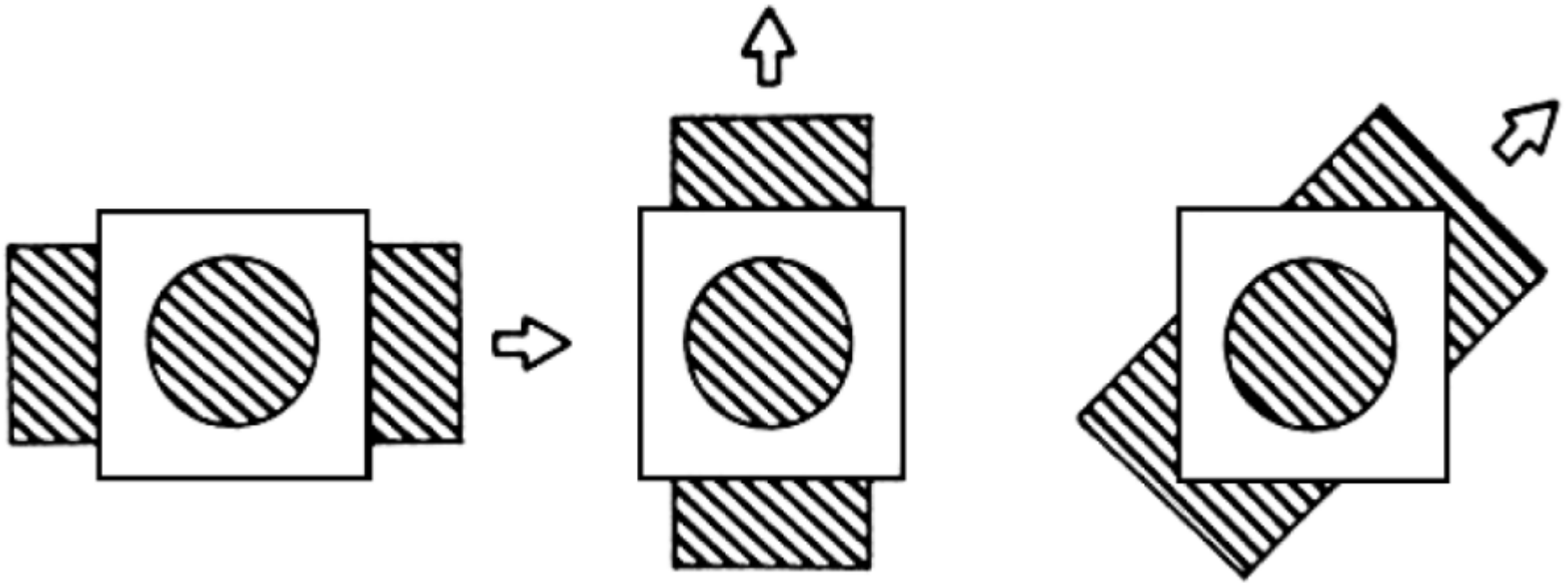
Normal Velocity



V1 cells only respond to the motion component that is normal (perpendicular) to their preferred orientation.



V1 : “Aperture Problem”



<http://www.opticalillusion.net/optical-illusions/the-barber-pole-illusion/>

The same issue arises with single bar, edge, or constant gradient.

To estimating image *velocity* (v_x, v_y) at (x, y) , the visual system needs to combine the responses of many V1 (normal velocity) cells.

