

COMP 546

Lecture 10

depth from X: defocus blur
and binocular disparity

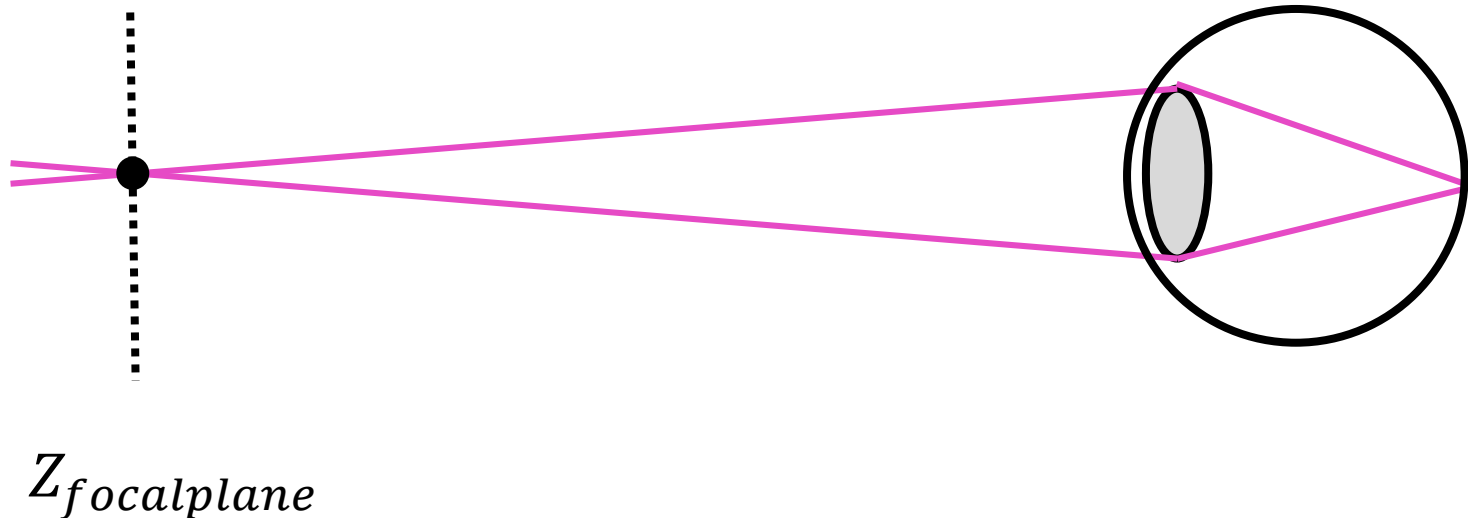
Tues. Feb. 13, 2018

Depth from defocus blur

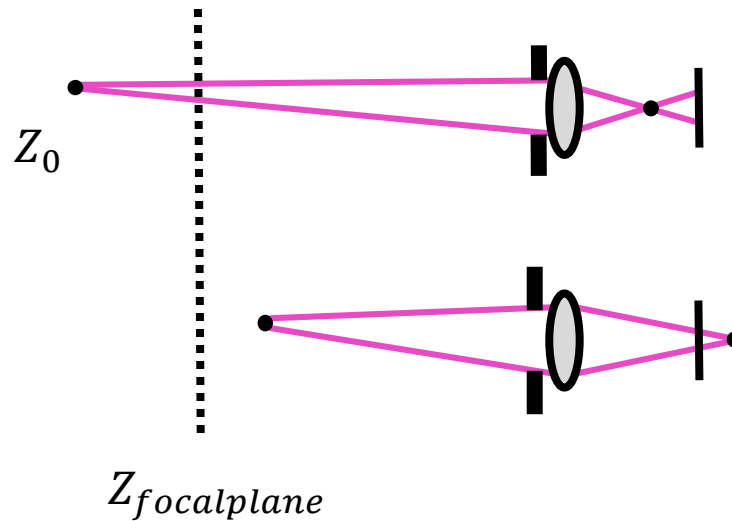


The eye controls f_{lens} , so it “knows” $Z_{focalplane}$.

$$\frac{1}{f_{cornea}} + \frac{1}{f_{lens}} = \frac{1}{Z_{focalplane}} + \frac{1}{Z_{sensor}}$$



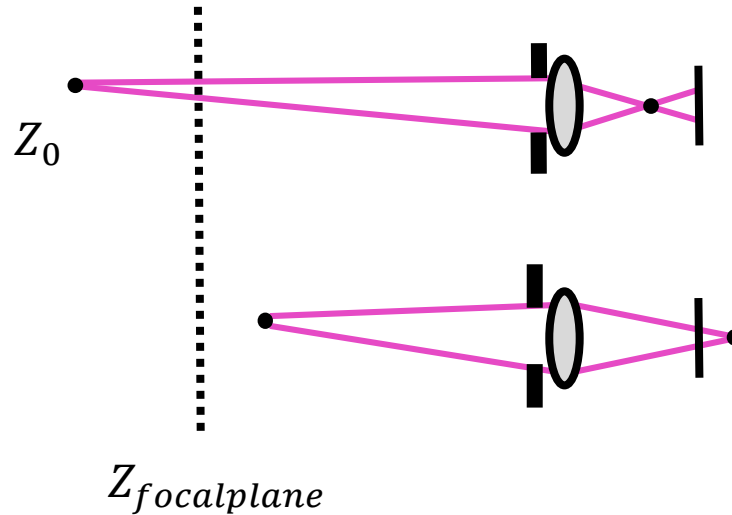
Recall: Depth and Defocus Blur



$$\text{blur width} = \text{aperture} \left| \frac{1}{Z_{focalplane}} - \frac{1}{Z_0} \right|$$

(See Exercise 2 Q 6 & Assignment 1)

Estimating Depth from Defocus Blur



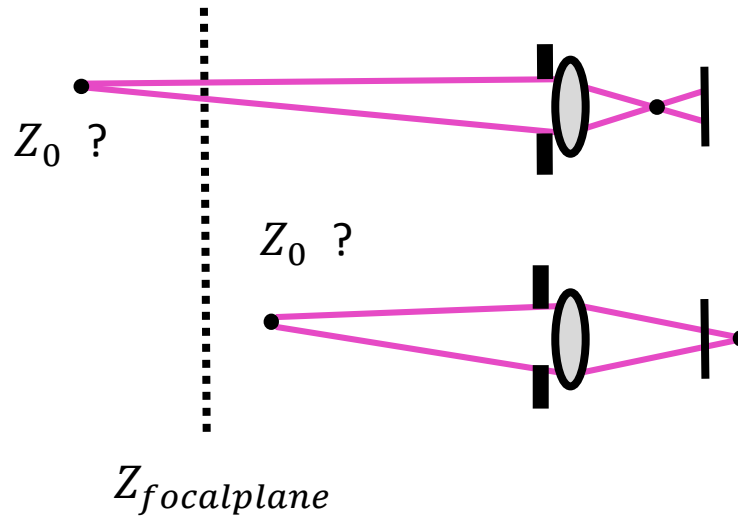
$$\text{blur width} = \text{aperture} \left| \frac{1}{Z_{focalplane}} - \frac{1}{Z_0} \right|$$

2.) measured
(details omitted)

1.) known
(controlled by vision system)

3.) estimated ⁵

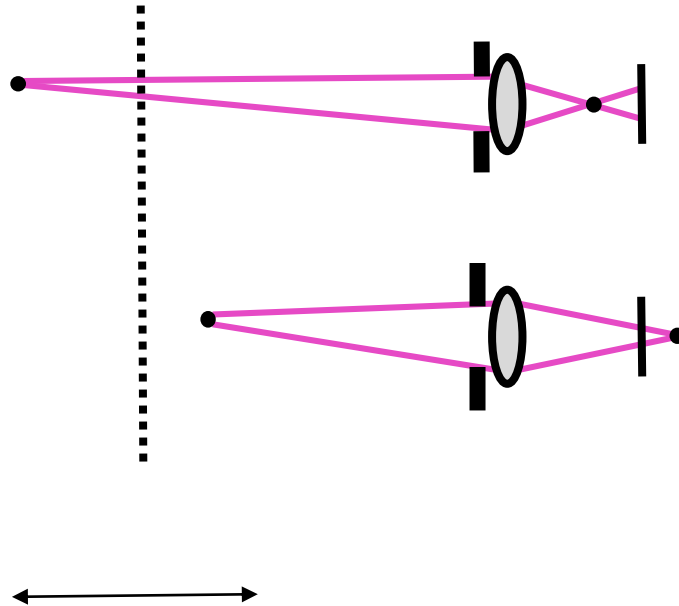
Estimating Depth from Defocus Blur



$$\text{blur width} = \text{aperture} \left| \frac{1}{Z_{focalplane}} - \frac{1}{Z_0} \right|$$

There is a two-fold depth ambiguity.

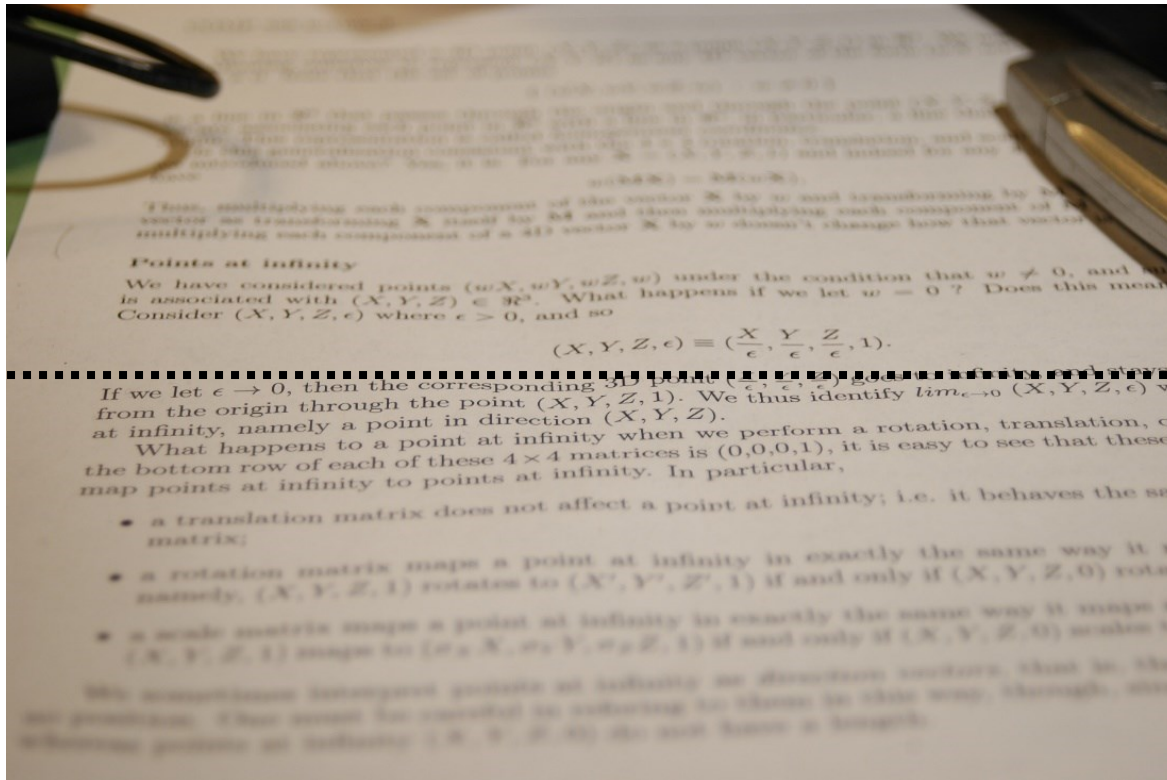
Estimating Depth from Defocus Blur



Varying accommodation resolves the two-fold ambiguity.

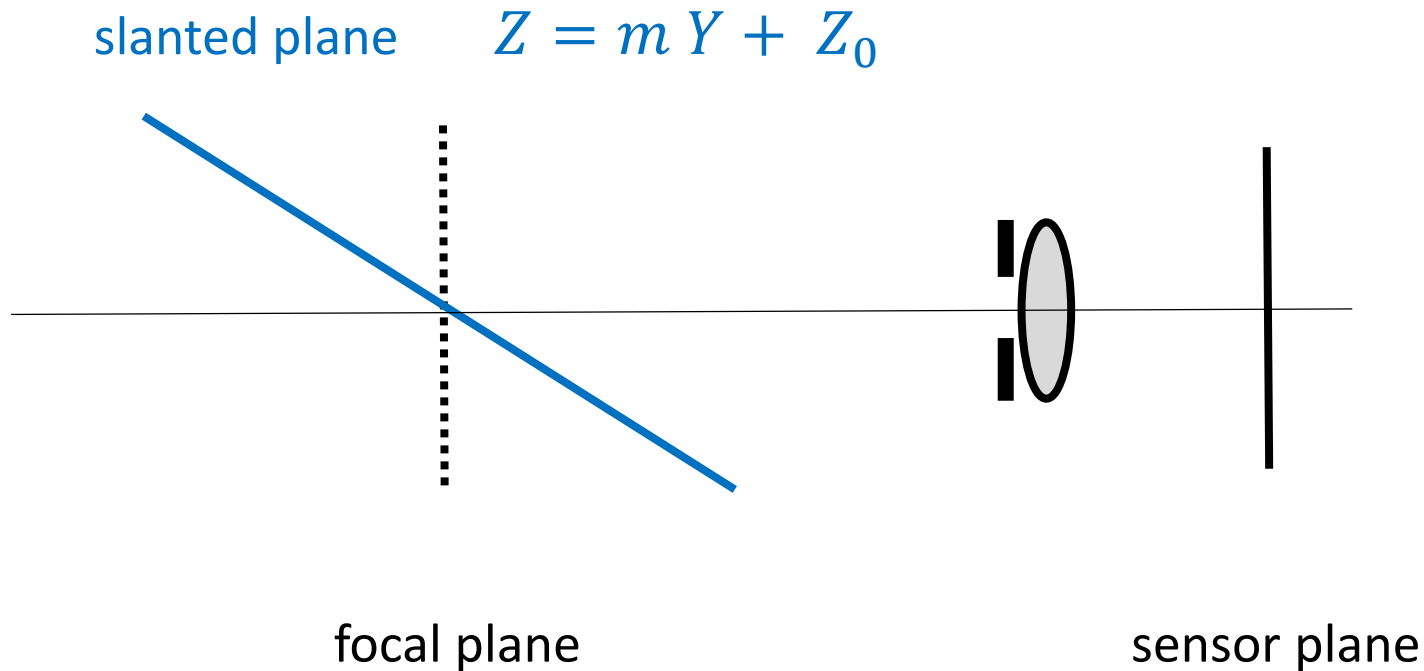
Blur on a slanted plane

focal plane
intersection

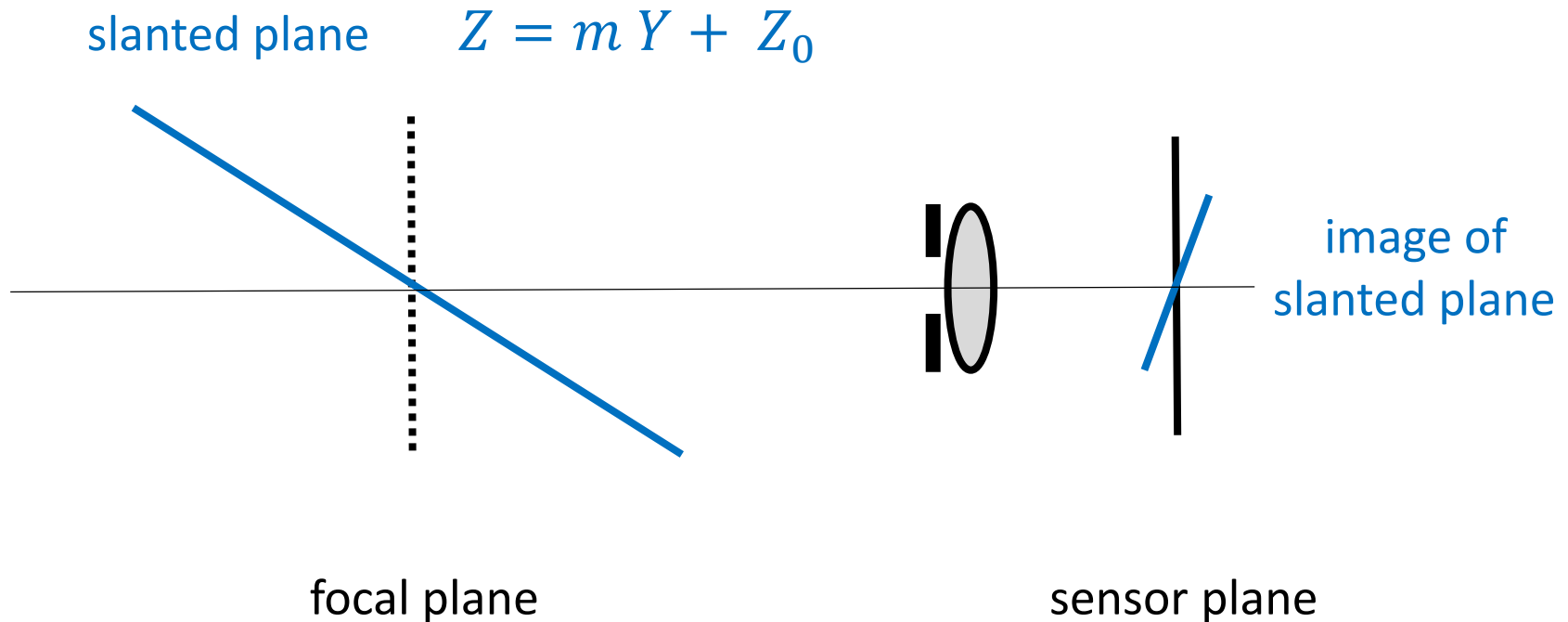


blur
gradient

Blur on a slanted plane

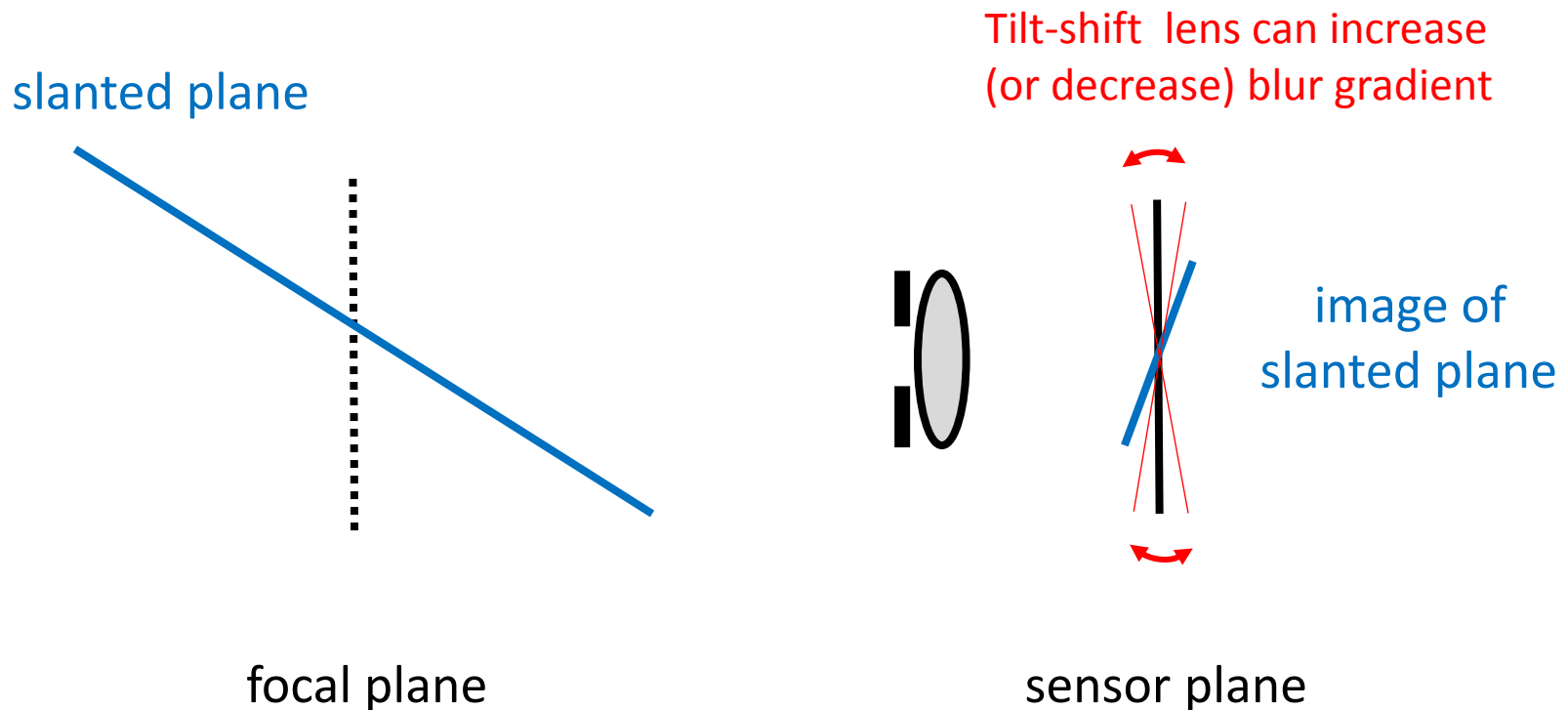


Blur on a slanted plane



See lecture notes: $\text{blur width (radians)} = A \frac{m}{Z_0} \left| \frac{y}{f} \right|$

ASIDE: tricks with a tilt-shift lens in photography

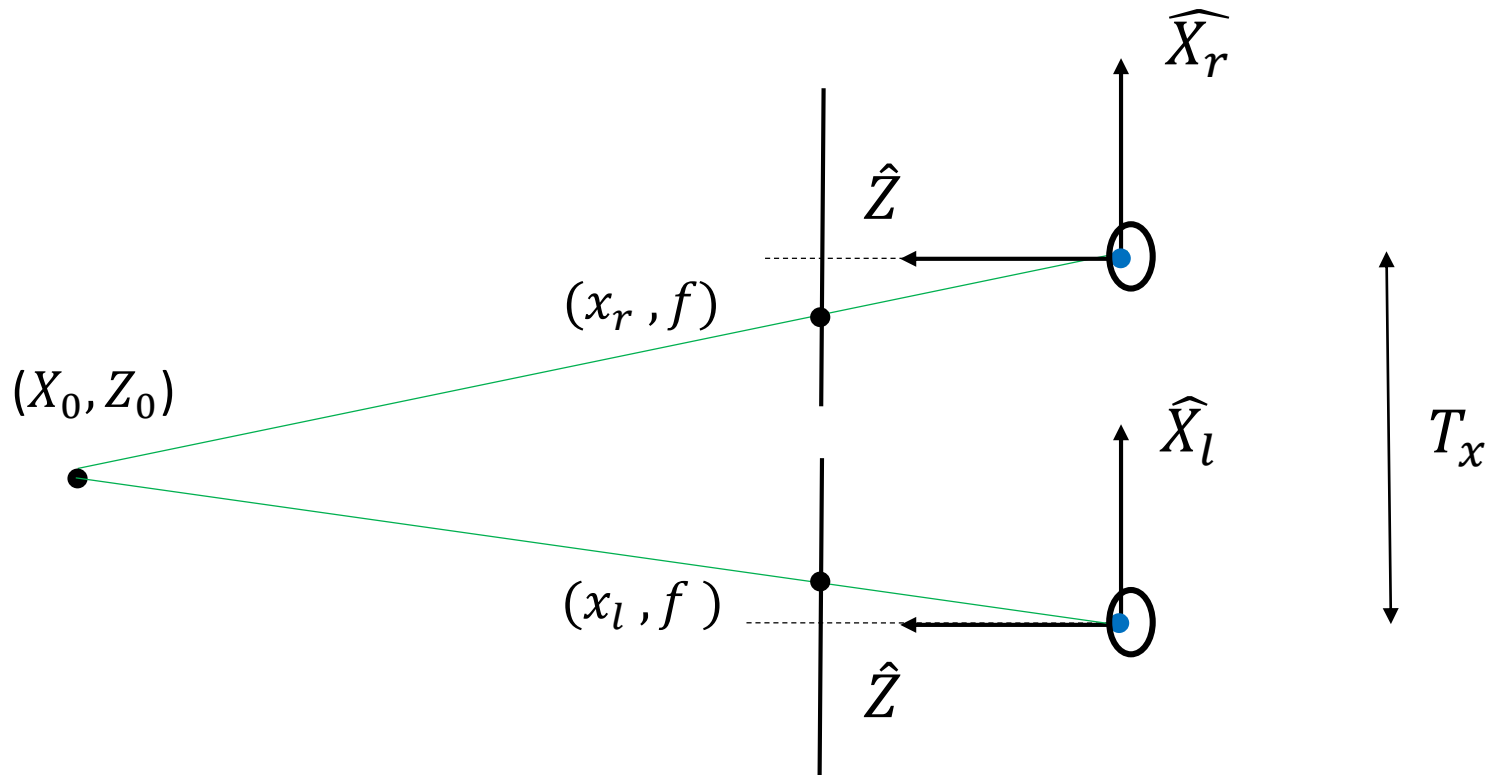






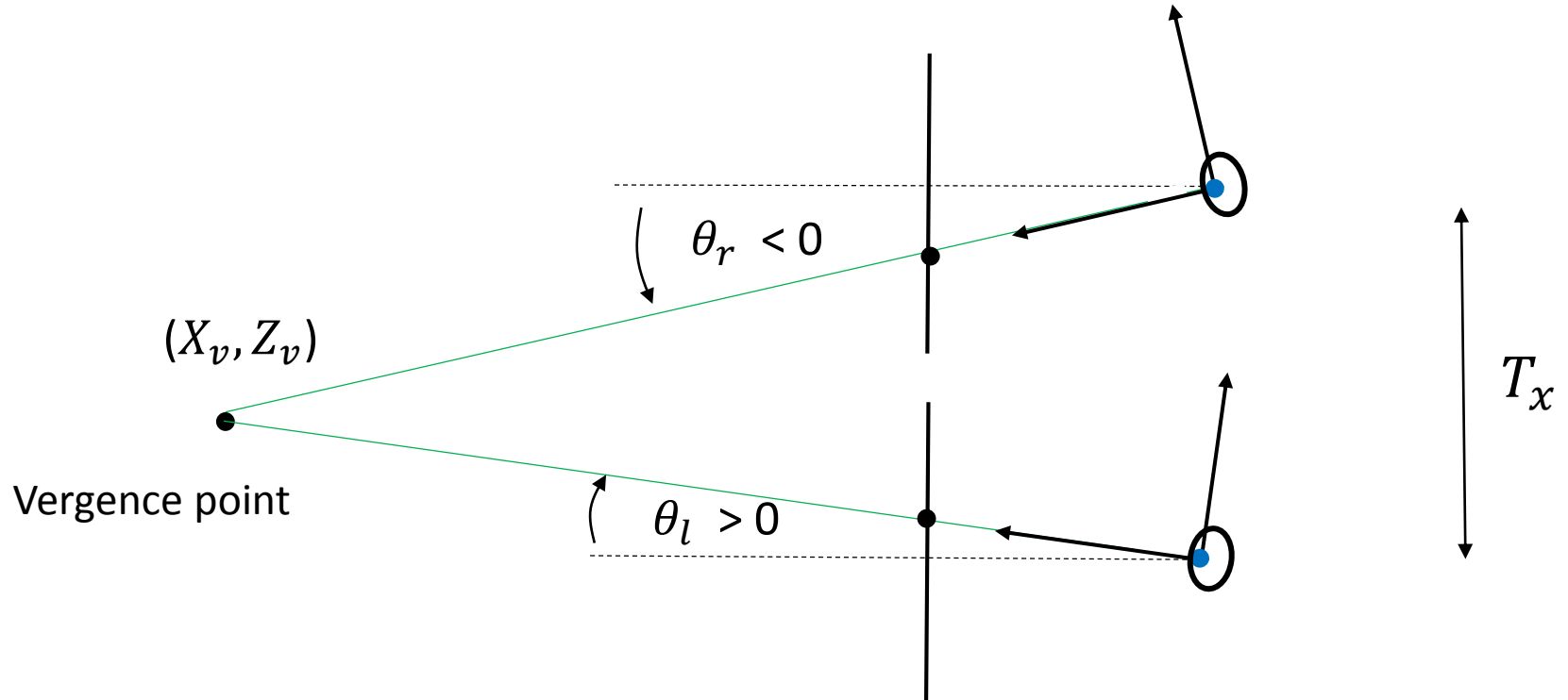
We next examine how defocus blur is related to binocular disparity.

Recall: Binocular disparity and depth

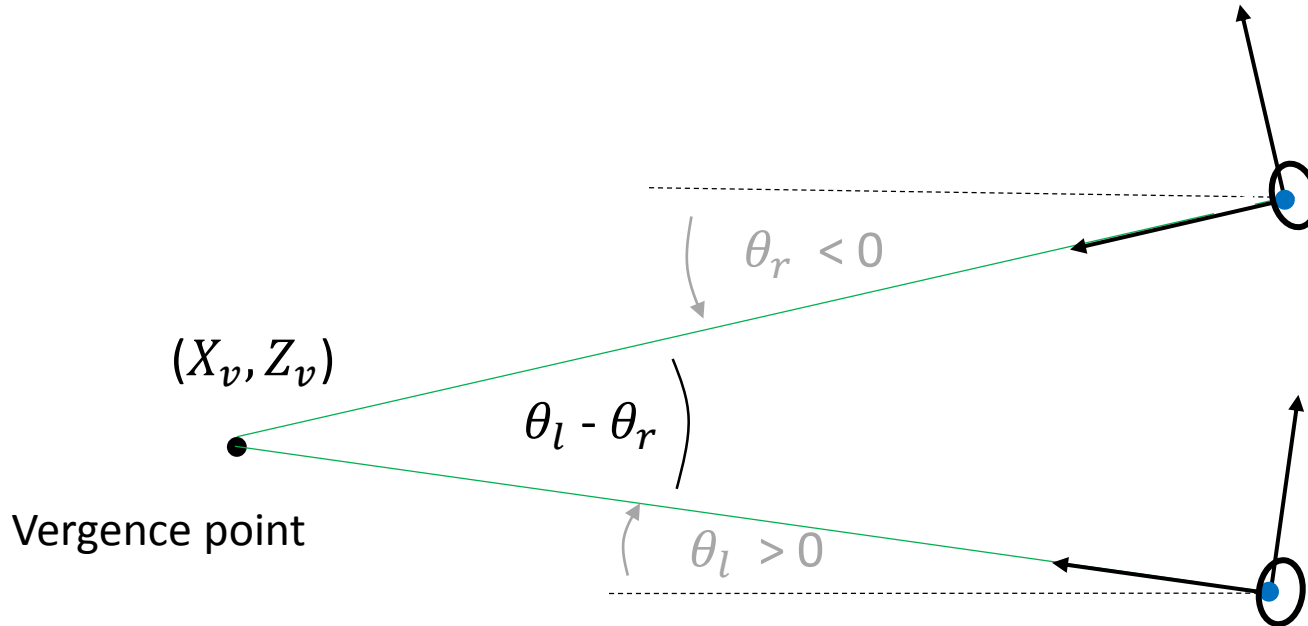


$$\text{disparity} \equiv \frac{x_l}{f} - \frac{x_r}{f} = \frac{T_x}{Z_0}$$

Recall: Binocular vergence

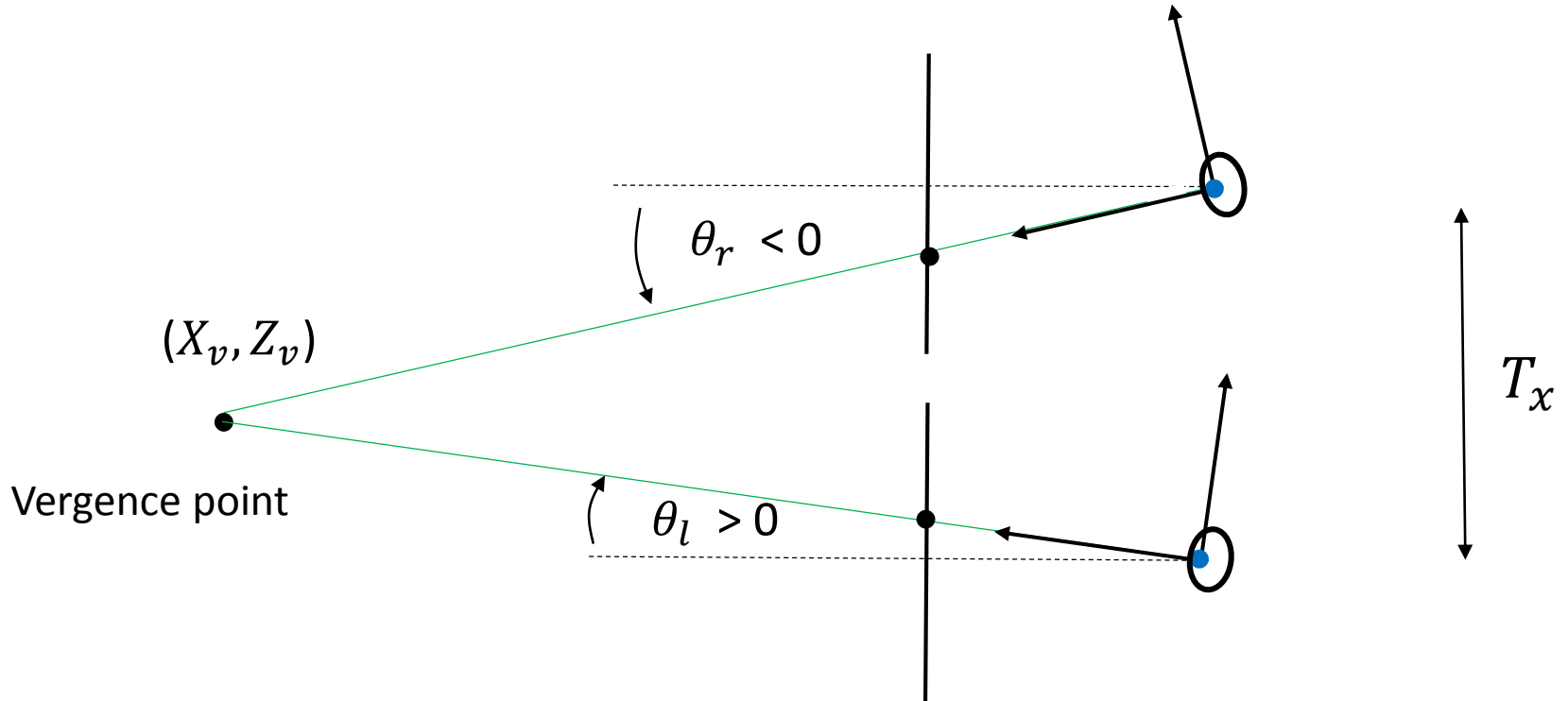


Vergence angle θ_v determines depth



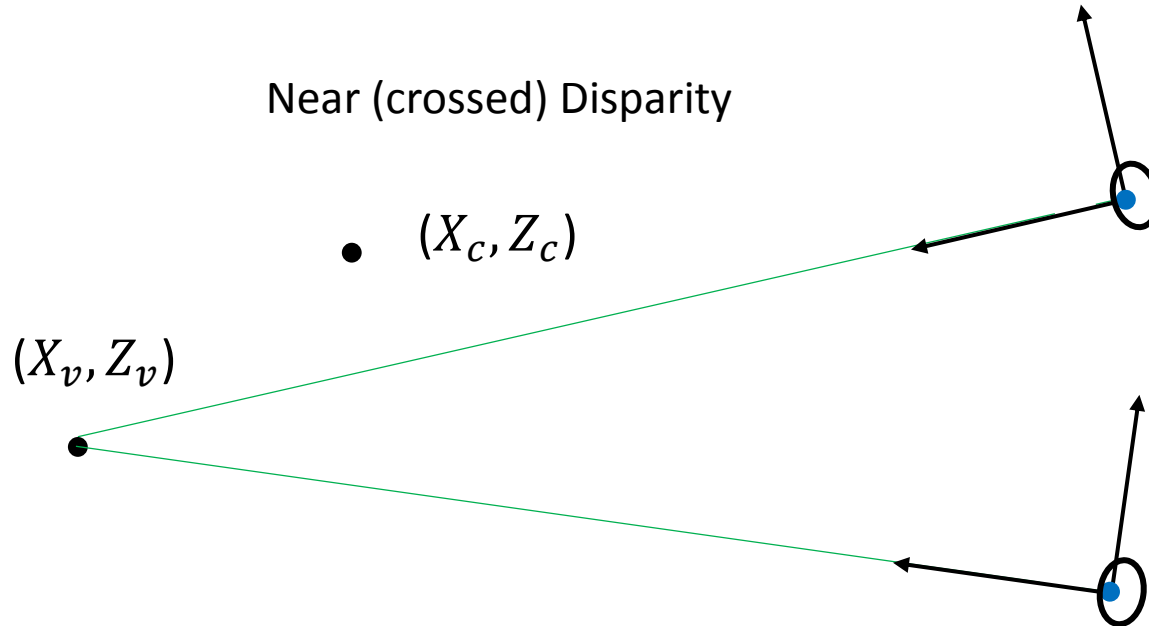
$$\theta_v \equiv \theta_l - \theta_r \approx \frac{x_l}{f} - \frac{x_r}{f} = \frac{T_x}{Z_v}$$

Binocular disparity of vergence point is 0 (obvious).



$$\left(\frac{x_l}{f} - \theta_l\right) - \left(\frac{x_r}{f} - \theta_r\right) = 0 - 0 = 0$$

Binocular disparity depends on distance (diopeters) from vergence depth.



$$disparity = T_x \left(\frac{1}{Z_c} - \frac{1}{Z_v} \right) > 0$$

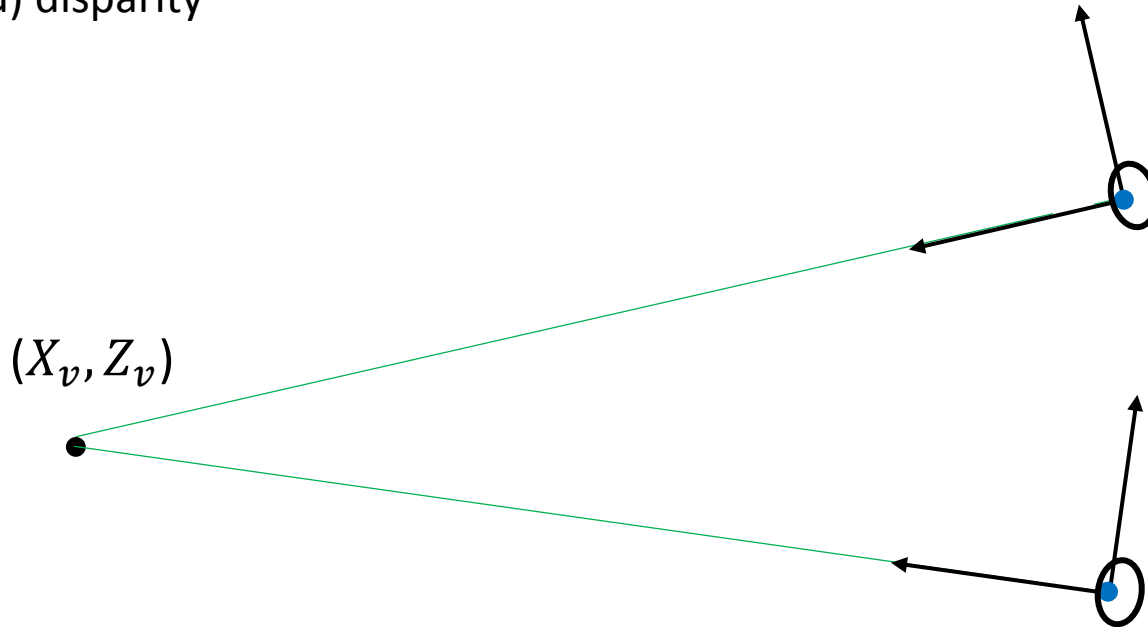
Binocular disparity depends on distance (diopters) from vergence depth.

Far (uncrossed) disparity

(X_u, Z_u)



(X_v, Z_v)



$$disparity = T_x \left(\frac{1}{Z_u} - \frac{1}{Z_v} \right) < 0$$

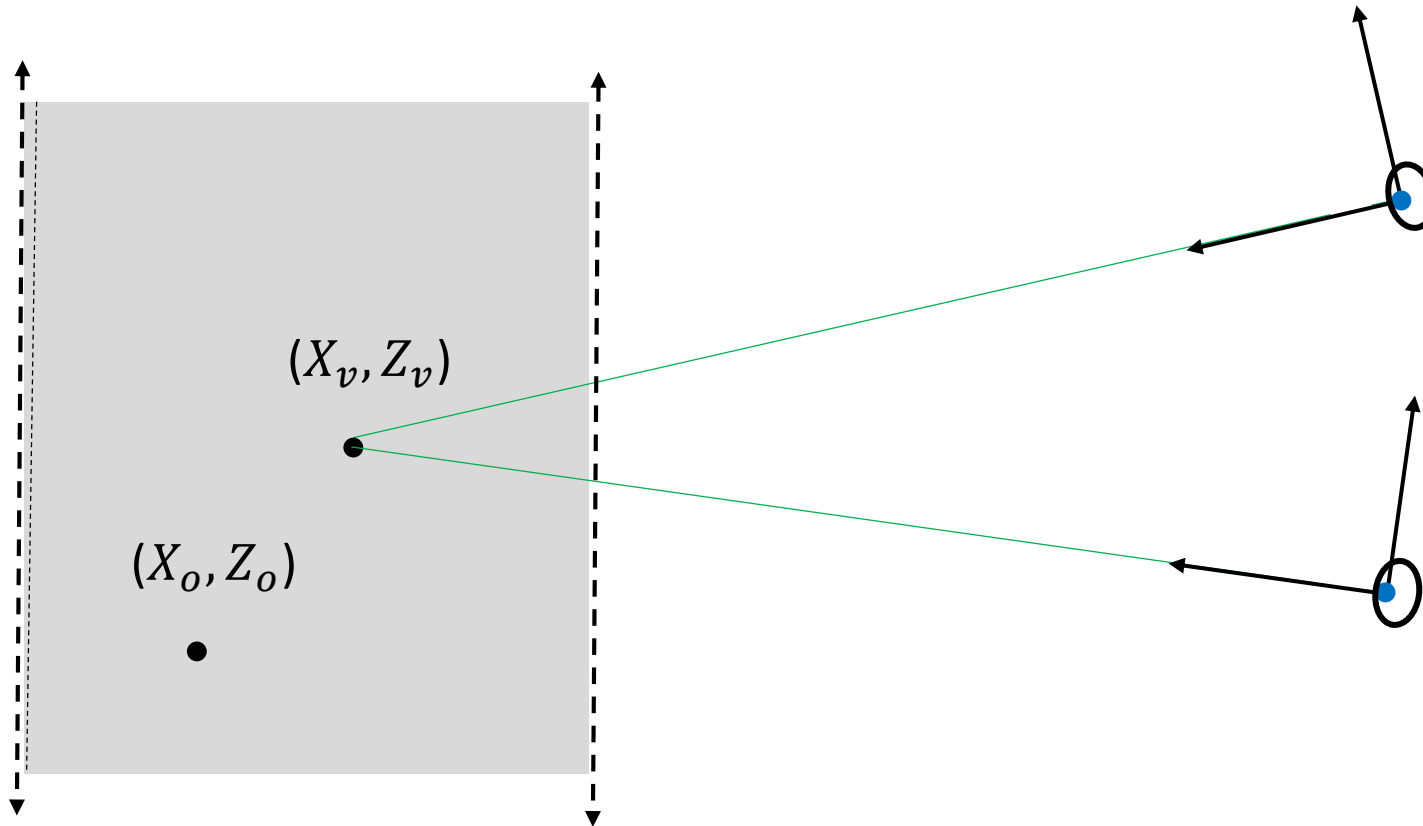
Binocular Fusion (“Cyclopean Vision”)

If disparity is *sufficiently* small, then we fuse the left and right eye images.

Otherwise, we perceive two images (“diplopia”).

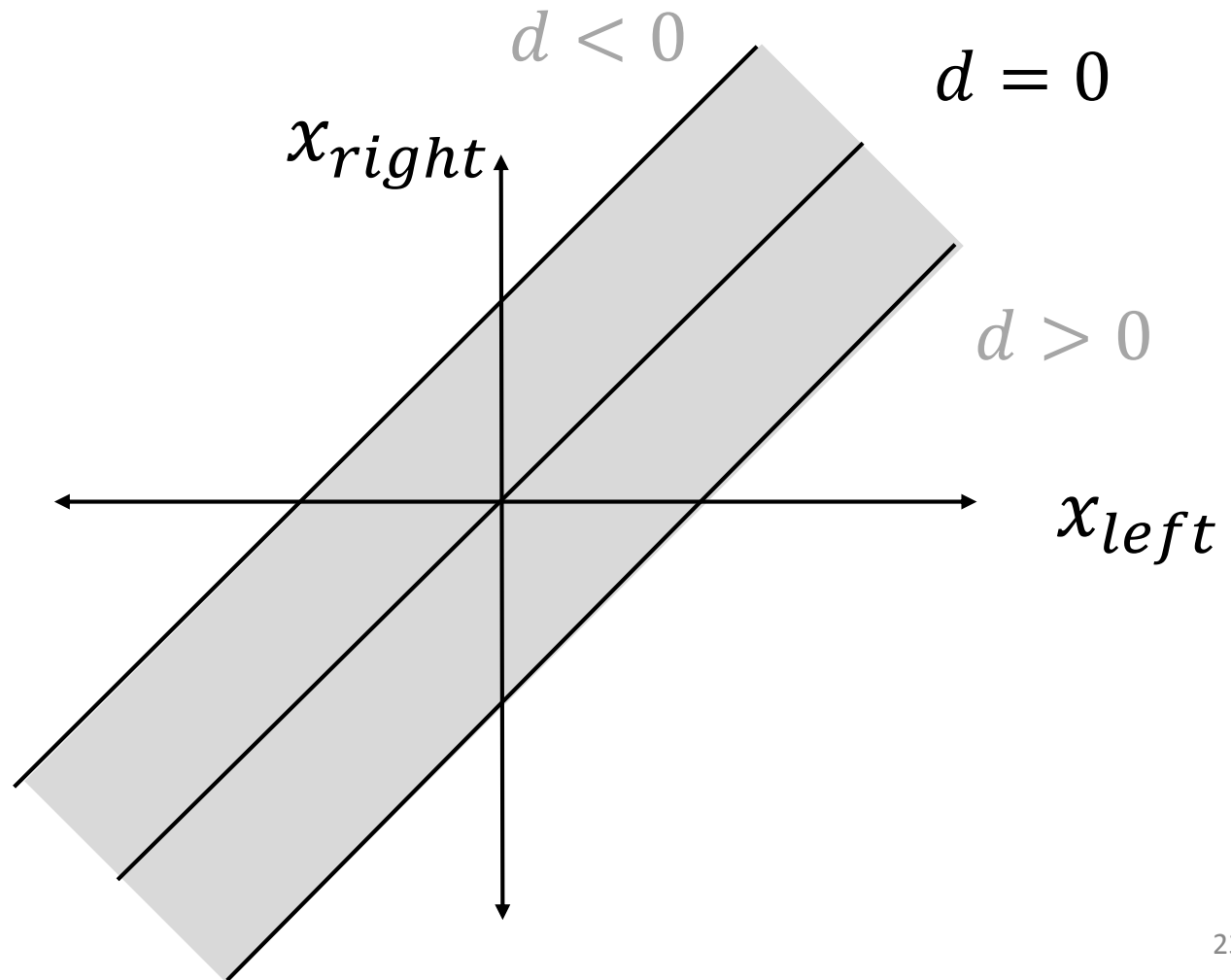


Panum's fusional area



$$\text{disparity} \approx T_x \left| \frac{1}{Z_o} - \frac{1}{Z_v} \right| < d_{max}$$

Panum's fusional area in disparity space



Binocular disparity and blur

$$\text{disparity} = \text{IOD} \left(\frac{1}{\text{object dist}} - \frac{1}{\text{vergence dist}} \right)$$

interocular distance or T_X

$$\text{blur width} = \text{aperture} \left| \frac{1}{\text{object dist}} - \frac{1}{\text{focal dist}} \right|$$

Binocular disparity and blur

$$\text{disparity} = \text{IOD} \left(\frac{1}{\text{object dist}} - \frac{1}{\text{vergence dist}} \right)$$

$$\text{blur width} = \text{aperture} \left| \frac{1}{\text{object dist}} - \frac{1}{\text{focal dist}} \right|$$

If vergence distance = focal distance then

$$\frac{|\text{disparity}|}{\text{blur}} = \frac{\text{IOD}}{\text{aperture}} \approx 10$$

Vergence and accommodation systems are coupled.

We verge at the same depth as we focus
(even if one eye is closed)
and vice-versa.

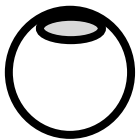
Monocular



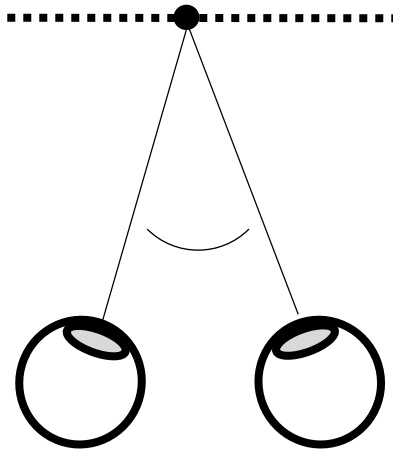
focal plane



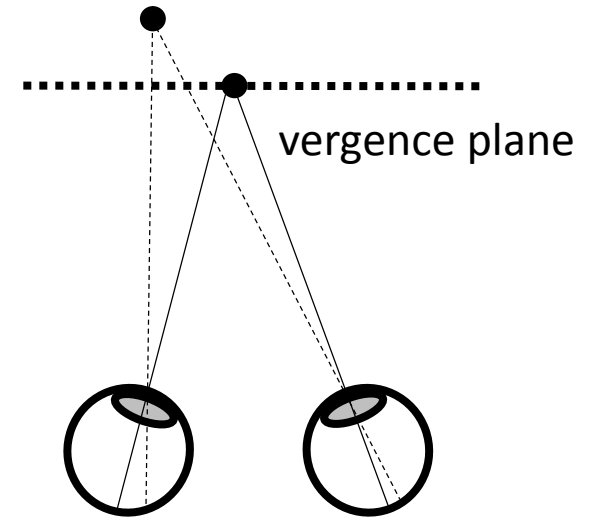
vergence plane



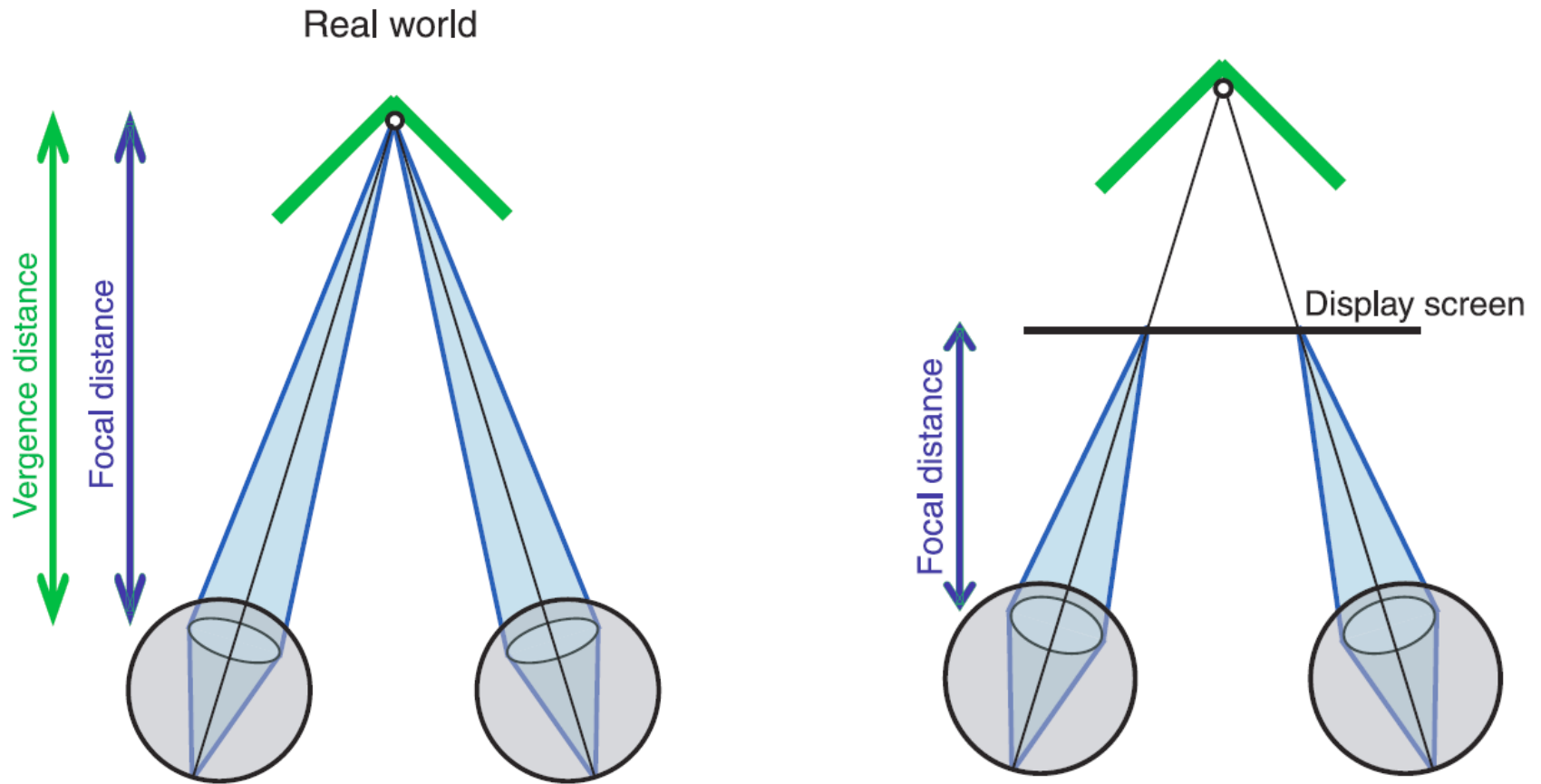
Binocular



Limitations on 3D cinema



3D stereo displays can create accommodation-vergence conflict



How to study binocular stereo vision ?

Neuroscience

- Show cats or monkeys different images to the left and right eyes and measure brain activity.

Computational modelling

- Write a computer program that finds matching points in left and right images, in a biologically plausible way

Psychology

- Show people different images to the left and right eyes and measure how well the people judge depth.

Random Dot Stereogram

Bela Julesz, “Binocular depth perception *without familiarity cues*” *Science* 1964.





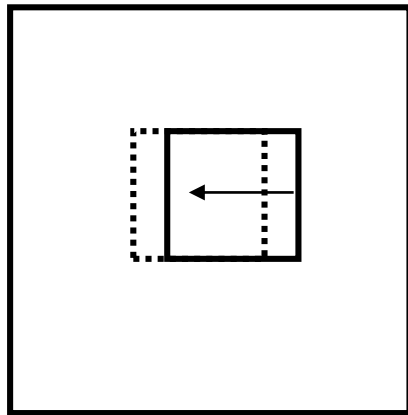


How to make a random dot stereogram?

image for
left eye



1.) shift
patch left



2.) Fill
empty
patch



image for
right eye

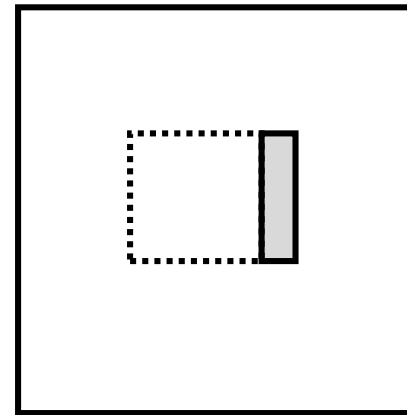
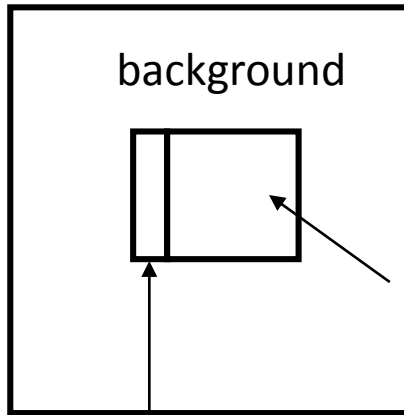


image for
left eye

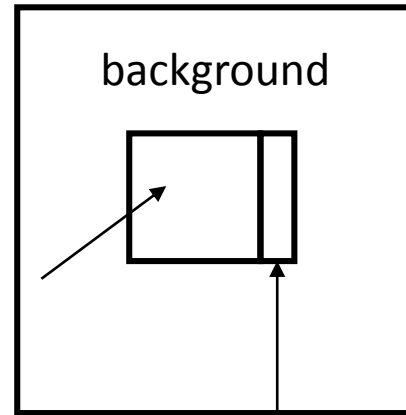


image for
right eye



left eye only

foreground
square



right eye only

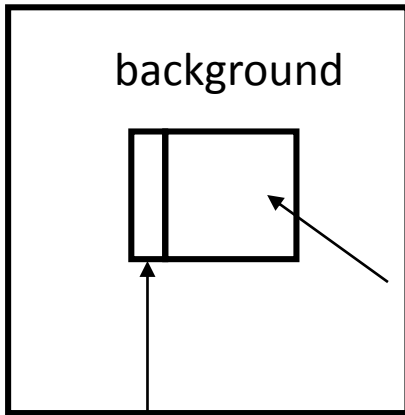
image for
left eye



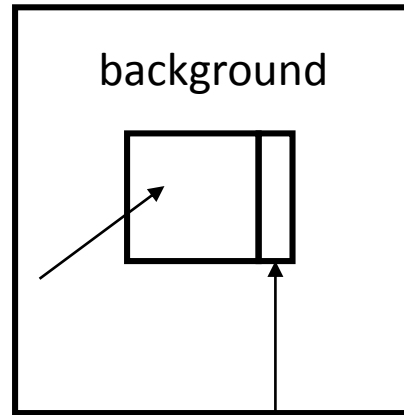
image for
right eye



perceived depths

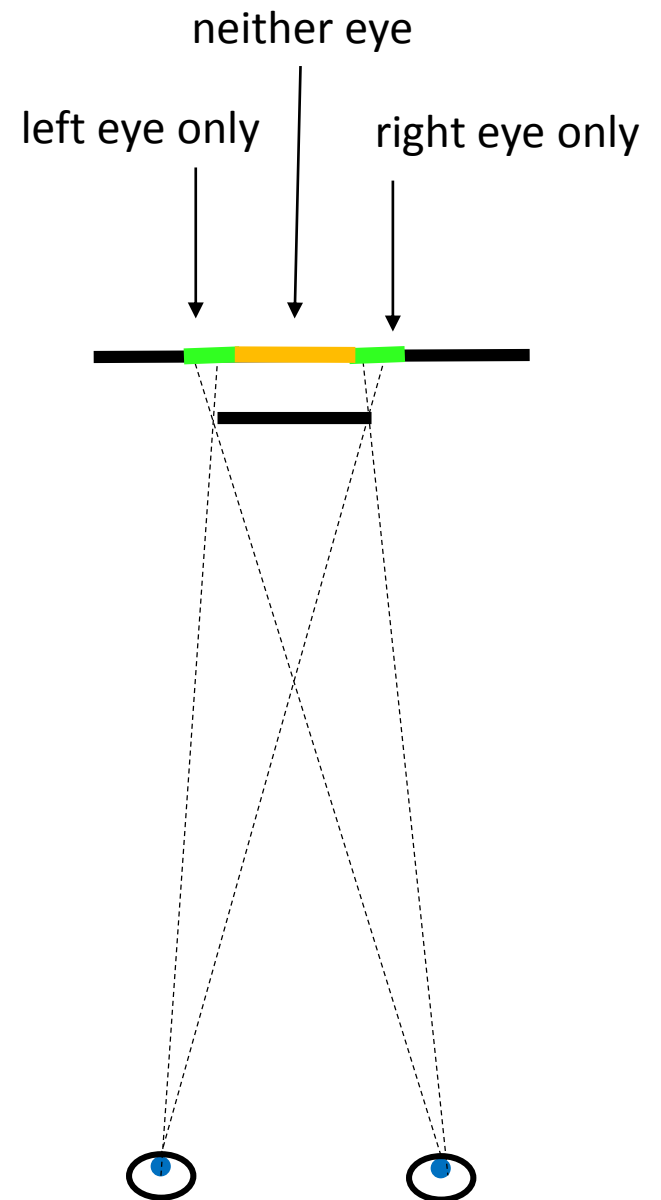


left eye only

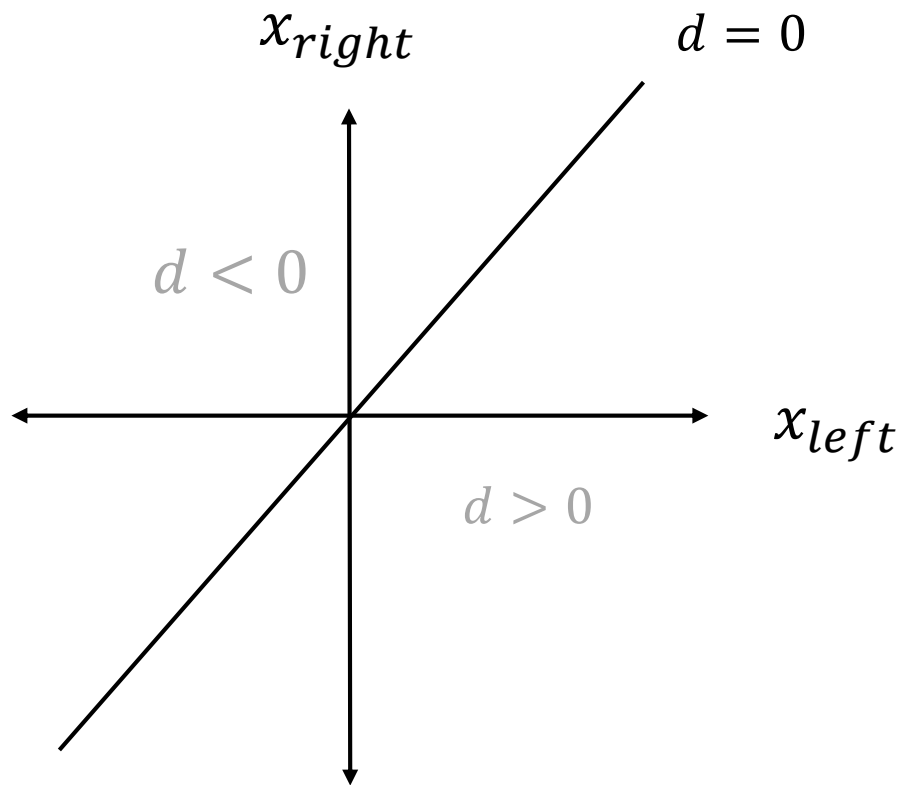


right eye only

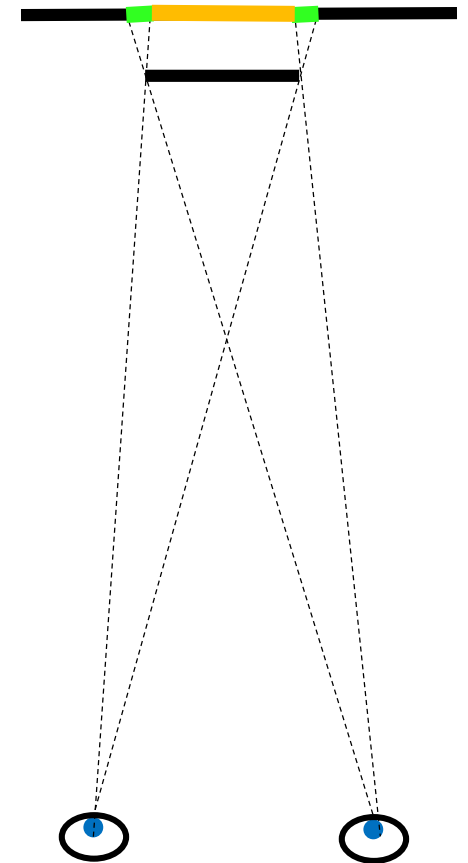
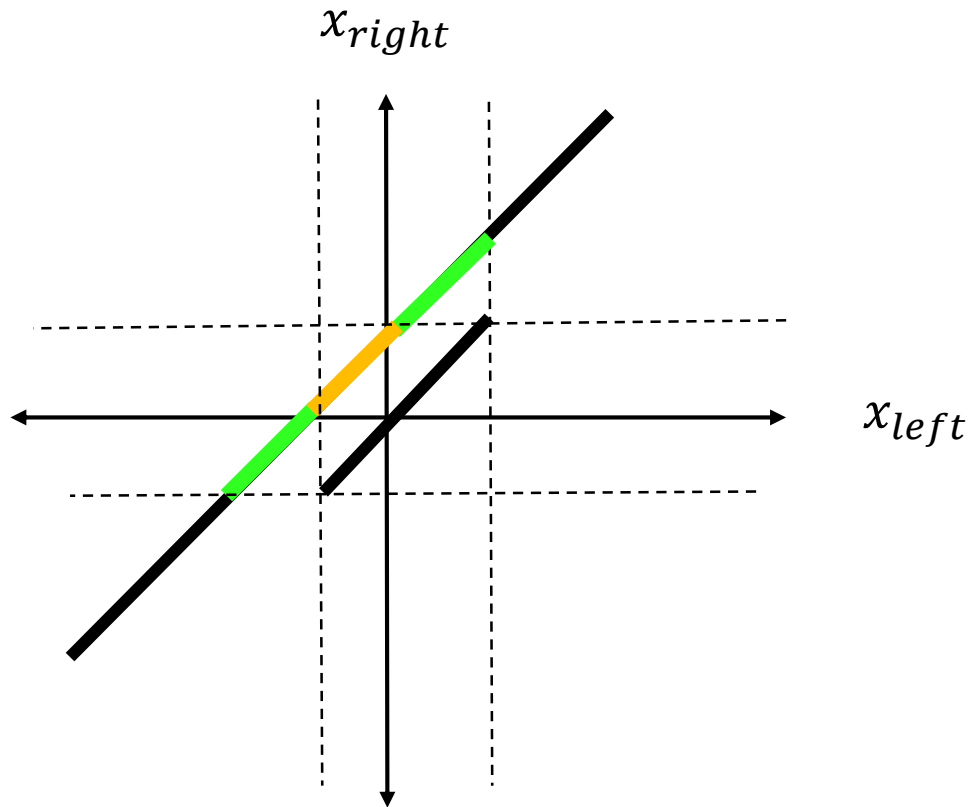




Disparity Space



Disparity Space



Q: where are the eyes verging?