

DEMO CAMERA TRANSLATION

$$\begin{pmatrix} X(t) \\ Y(t) \\ Z(t) \end{pmatrix} = \begin{pmatrix} X_{\circ} - T_{\times} t \\ Y_{\circ} - T_{Y} t \\ Z_{\circ} - T_{Z} t \end{pmatrix}$$

Recall
$$(x,y) = \left(\frac{X_o}{7}, \frac{Y_o}{2}\right) f$$

I mage Velocity at
$$t = 0$$

$$(x(t), y(t)) = \left(\frac{Y_0 - T_x t}{Z_t - T_x t}, \frac{Y_s - T_s t}{Z_s - T_x t}\right) f$$

$$(V_x, V_y) = \frac{d}{dt} \left(x(t), y(t)\right) \Big|_{t=0}$$

$$V_x = \frac{dx}{dt}\Big|_{t=0} = \frac{-T_x Z_0 + T_x X_0}{Z_0^2} \cdot f$$

$$V_y = \frac{dy}{dt}\Big|_{t=0} = \frac{-T_y Z_0 + T_x X_0}{Z_0^2} \cdot f$$

Special Cux:
$$T_z = 0$$
 (lateral motion)

$$V_x = \frac{dx}{dt}\Big|_{t=0} = -\frac{T_x}{2} + \frac{T_x}{2} \times 0 \cdot f = -\frac{f}{T_x} \times \frac{T_x}{2} \cdot 0 \cdot f$$

Lateral motion + Ground Plane

Recall
$$y = -\frac{fh}{2}$$

$$T_{y} = T_{z} = 0$$

$$\Rightarrow v_{x} = \frac{-T_{x}f}{Z_{0}} = \frac{T_{x}y}{Y} \qquad \Rightarrow \Rightarrow 1$$

Special Case: forward translation
$$T_{\chi} = T_{\gamma} = 0, \quad T_{Z} \neq 0$$

$$V_{\chi} = \frac{dx}{dt}\Big|_{t=0} = \frac{-T_{\chi}Z_{0} + T_{\chi}X_{0}}{Z_{0}^{2}} \cdot f = \frac{T_{\chi}X_{0}f}{Z_{0}^{2}} =$$

$$V_{x} = -\frac{T_{z}}{z_{o}} \times -\frac{T_{z}}{fh} \times y$$

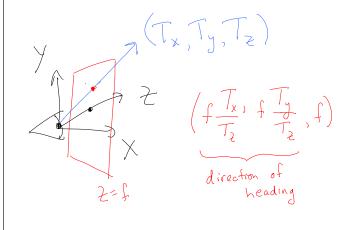
$$V_{y} = -\frac{T_{z}}{z_{o}} y = \frac{T_{z}}{fh} y^{2}$$

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General Translation
$$(T_2 \neq 0)$$

$$V_x = \frac{-T_x z_0 + T_z x_0}{z_0^2} \cdot f = \frac{T_z}{z_0} x - \frac{T_x f}{z_0} = \frac{T_z}{z_0} \left(x - \frac{T_x}{T_z} f\right)$$

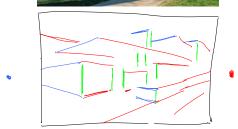
$$V_y = \frac{-T_y z_0 + T_z x_0}{z_0^2} \cdot f = \frac{T_z}{z_0} y - \frac{T_y}{z_0} f = \frac{T_z}{z_0} \left(y - \frac{T_y}{T_z} f\right)$$

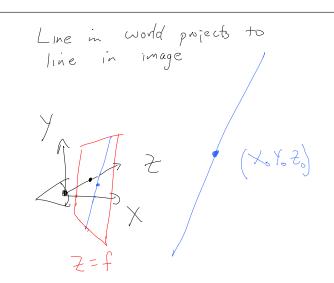


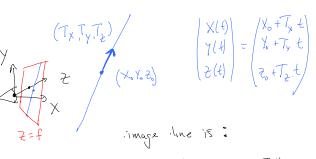


Parallel lines in 3D project (typically) to non-parallel lines in the image.









$$\left(\chi(t), y(t)\right) = \left(\frac{\chi_{o} - \chi_{t}}{\xi_{o} - \chi_{t}}, \frac{\chi_{o} - \chi_{t}}{\xi_{o} - \chi_{t}}\right) f$$

$$(7x, 7y, 7z)$$

$$(x(t)) = \begin{pmatrix} x(t) \\ y(t) \\ z(t) \end{pmatrix} = \begin{pmatrix} x_0 + 7x + t \\ y_0 + 7y + t \\ z_0 + 7z + t \end{pmatrix}$$

$$(x(t), y(t)) = \begin{pmatrix} x_0 - 7x + t \\ z_0 - 7z + t \end{pmatrix}$$

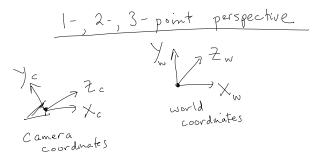
$$(x(t), y(t)) = \begin{pmatrix} x_0 - 7x + t \\ z_0 - 7z + t \end{pmatrix}$$

Corresponding image line is:

$$(\chi(4), y(4)) = \left(\frac{V_o - T_x t}{Z_o - T_x t}, \frac{V_o - T_x t}{Z_o - T_x t}\right) f$$

Let
$$t \Rightarrow \infty$$
 gives
$$(x(0), y(0)) = \left(\frac{T_x}{T_z}, \frac{T_y}{T_z}\right) \cdot f$$
vanishing point $(T_z \neq 0)$

- · Vanishing point is independent of (XoYo. Zo).
- If Tz = 0, then letting t→ ∞ gives a point at infinity and in direction (-Tx,-Ty)



- · X, Y, Z axes of world coordinates each define a vanishing point.
- · n point perspective means there are n finite vanishing points

1-point perspective



2-point perspective



3-point perspective

