

Jacobi and Gauss Seidel 1D Example Codes

Jacobi Example: 1D hot-cold rod SERIAL

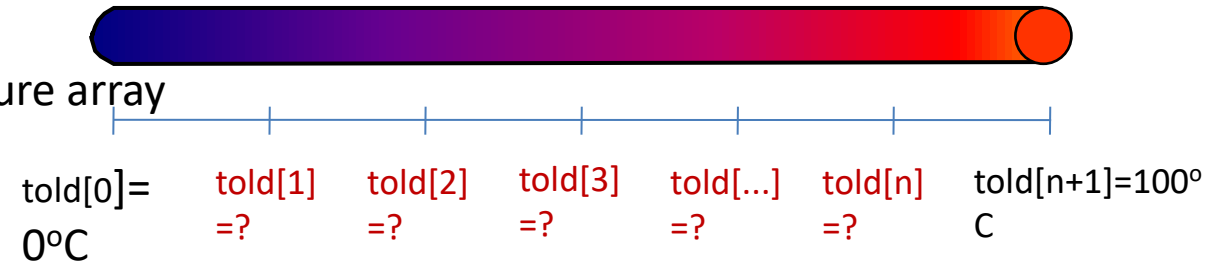
```
#include <stdio.h>
#include <math.h>
```

```
int max_size=1000001;
```

```
int main(int argc, char *argv[])
{
    double told[max_size], t[max_size], tol, diff, difmax;
    int i, iter, n;
    printf("enter the problem size (n) and the convergence
           tolerance\n");
    scanf("%d %lf", &n, &tol);
```

```
// initialise temperature array
```

```
for (i=1; i <= n; i++) {
    told[i] = 20.0;
}
```



```
// fix end points as cold and hot
```

```
told[0] = 0.0;
```

```
told[n+1] = 100.0;
```



Jacobi Example: 1D hot-cold rod SERIAL

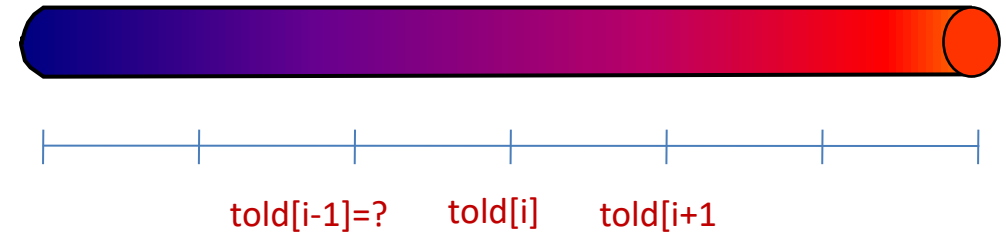
```
iter = 0;

difmax = 1000000.0;
while (difmax > tol) {
    iter=iter+1;
    // update temperature for next iteration
    for (i=1; i <= n; i++) {
        t[i] = (told[i-1]+told[i+1])/2.0;
    }
    // work out maximum difference between old and new temperatures
    difmax=0.0;
    for (i=1; i <= n; i++) {
        diff = fabs(t[i]-told[i]);
        if (diff > difmax) {
            difmax = diff;
        }
        told[i] = t[i];
    }
}

//while (difmax>tol)
for (i=1; i <= n; i++) {
    printf("told[%d] = %-5.7lf \n", i, t[i]);
}

printf("iterations = %d maximum difference = %-5.7lf \n", iter, difmax)
}
```

using a simple average of two temperatures from neighbouring points.



redefine temperatures from new (t) to old (told) in preparation for the next iteration of the solution (JACOBI algorithm)



Jacobi Example: 1D hot-cold rod OMP v1

```
#include <omp.h>
#include <stdio.h>
#include <math.h>
#include <stdlib.h>

int max_size=400000;

int main(int argc, char *argv[]) {
    double told[max_size], t[max_size], tol, diff, difmax, priv_difmax;
    double tstart, tstop;
    int i, iter, n, nthreads;
    printf("enter the problem size (n) and the convergence tolerance\n");
    scanf("%d %lf", &n, &tol);
    printf("Enter the number of threads (max 10) ");
    scanf("%d",&nthreads);

    /* define the number of threads to be used */
    omp_set_num_threads(nthreads);
```



Jacobi Example: 1D hot-cold rod OMP v1

```
tstart = omp_get_wtime ();
```

```
// initialise temperature array
```

```
#pragma omp parallel for schedule(static) \
```

```
default(shared) private(i)
```

loop iterations distributed amongst available threads

```
for (i=1; i <= n; i++) {
```

```
    told[i] = 20.0;
```

```
}
```

```
// fix end points as cold and hot
```

```
told[0] = 0.0;
```

```
told[n+1] = 100.0;
```

```
iter = 0;
```

```
difmax = 1000000.0;
```

```
while (difmax > tol) {
```

```
    iter=iter+1;
```

```
    // update temperature for next iteration
```

```
#pragma omp parallel for schedule(static) \
```

```
default(shared) private(i)
```

loop iterations distributed amongst available threads

```
for (i=1; i <= n; i++) {
```

```
    t[i] = (told[i-1]+told[i+1])/2.0;
```

```
}
```

Jacobi Example: 1D hot-cold rod OMP v1

```
// work out maximum difference between old and new temperatures
```

```
difmax = 0.0;
```

```
#pragma omp parallel default(shared) private(i, diff, priv_difmax)
```

```
{
```

```
    priv_difmax = 0.0;
```

```
    #pragma omp for schedule(static)
```

```
    for (i=1; i <= n; i++) {
```

```
        diff = fabs(t[i]-told[i]);
```

```
        if (diff > priv_difmax) {
```

```
            priv_difmax = diff;
```

```
        }
```

```
        told[i] = t[i];
```

```
    }
```

```
    #pragma omp critical
```

```
    if (priv_difmax > difmax) {
```

```
        difmax = priv_difmax;
```

```
    }
```

```
}
```

```
}//while (difmax>tol)
```

create parallel region with more than one directive being used here. NOTE priv_difmax variable

not a standard reduction operation so need to use less elegant (but practical) solution using local private difmax for each thread

critical region ensures only one local priv_difmax is compared at a time in order to create the global difmax value

Jacobi Example: 1D hot-cold rod OMP v1

```
tstop = omp_get_wtime ();
```

```
for (i=1; i <= n; i++) {  
    printf("told[%d] = %-5.7lf \n", i, t[i]);  
}  
printf("iterations = %d  maximum difference = %-5.7lf \n",  
    iter, difmax);
```

```
printf("time taken is %4.3lf\n", (tstop-tstart));  
}
```



Example – 1D hot-cold rod OMP v1

maximum difference tolerance = 0.001

Machine : cms-grid-03

Compile: -fopenmp -O3

Grid points (n) = 100000 serial time :151.27

# of threads	Wall clock time (s)	Speedup
1	147.62	-
2	106.33	1.388
4	87.09	1.695
8	96.83	1.525

Grid points (n) = 1000000 serial time :5399.53

# of threads	Wall clock time (s)	Speedup
1	5256.73	-
2	2997.04	1.754
4	1425.78	3.687
8	893.36	5.884



Gauss Seidel

Example: 1D hot-cold rod

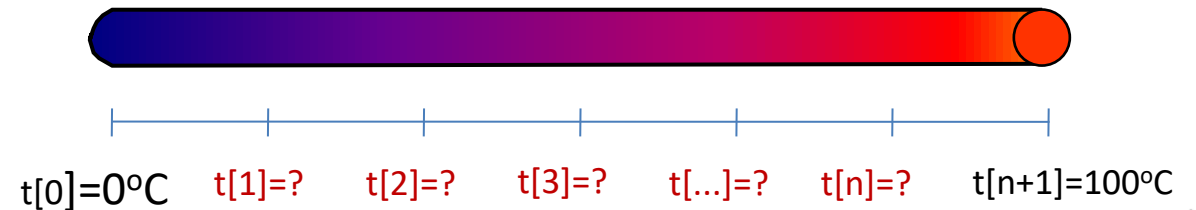
SERIAL

```
#include <stdio.h>
#include <math.h>

int max_size=100000;

int main(int argc, char *argv[])
{
    double t[max_size], told[max_size], tol, diff, difmax;
    int i, iter, n;
    printf("enter the problem size (n) and the convergence
           tolerance\n");
    scanf("%d %lf", &n, &tol);

    // initialise temperature array
    for (i=1; i <= n; i++) {
        t[i] = 20.0;
    }
    // fix end points as cold and hot
    t[0] = 0.0;
    t[n+1] = 100.0;
```



Gauss Seidel

Example: 1D hot-cold rod

SERIAL

```
iter = 0;
difmax = 1000000.0;
while (difmax > tol) {
    iter=iter+1;
    //populate tnew array to keep old values for calculating residual
    for (i=1; i <= n ; i++ )
    {
        told[i]= t[i];
    }
    // update temperature for next iteration
    for (i=1; i <= n; i++) {
        t[i] = (t[i-1]+t[i+1])/2.0;
    }
    // work out maximum difference between old and new temperatures
    difmax=0.0;
    for (i=1; i <= n; i++) {
        diff = fabs(t[i]-told[i]);
        if (diff > difmax) {
            difmax = diff;
        }
    }
} //while (difmax > tol)
for (i=1; i <= n; i++) {
    printf("t[%d] = %-5.7lf \n", i, told[i]);
}
printf("iterations = %d  maximum difference = %-5.7lf \n", iter, difmax);
}
```

redefine temperatures from new (t) to old (told) in preparation for calculating the residual

using a simple average of two temperatures from neighbouring points.

