

Correction devoir 1 A 19

①

Recherche $(\pi_1, \pi_2, \pi_3) \sqsubset$

$\pi_1 \leftarrow 1$
Répéter $\pi_2 \downarrow \text{div}$ \sqsubset

$\pi_3 \leftarrow \text{Premier}(\pi_1)$

$\pi_6 \leftarrow \text{Exp}(\pi_3, \pi_2)$

$\pi_7 \leftarrow \text{non}(\text{mod}(\pi_1, \pi_6))$ ($p_1^{\frac{1}{2}}$ divise π_1 ?)

$\pi_8 \leftarrow \text{mod}(\text{div}(\pi_1, \pi_6) \pi_5)$ (p_1 ne divise pas π_1/p_6)

Si Et $(\pi_7, \pi_8) \sqsubset$

$\pi_0 \leftarrow \pi_4$
 \sqsubset

\sqsupset

Si non $(\pi_0) \sqsubset$

$\pi_0 \leftarrow \pi_2 + 1$

\sqsupset
 \sqsupset

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$$a) \forall i \geq 1, \forall x \geq 0 \quad B_i(x) \geq x+1$$

cas de base $i=1$

$$B(x) = A(x, x) \geq A(0, x) = x+1$$

induction: on a que $B_{i-1}(x) \geq x+1, \forall x \geq 0$

$$\begin{aligned} B_i(x) &= B_{i-1}^{<x>}(1) = B_{i-1}(B_{i-1}^{<x-1>}(1)) \\ &\geq B_{i-1}^{<x-1>}(1) + 1 \geq B_{i-1}^{<x-1>}(1) + 2 \end{aligned}$$

donc $x+1$

$$b) B_i(x+1) > B_i(x)$$

Soit $i \geq 1$

$$\begin{aligned} B_i(x+1) &= B_i^{<x+1>}(1) = B_{i-1}(B_{i-1}^{<x>}(1)) \\ &\geq B_i^{<x>}(1) \end{aligned}$$