

Example 10. (Page 68). let  $C := \mathbb{R}$ ,  $m=1$  and  $p:=0$ :

$$1 \quad (P) \begin{cases} f(x) = x + 2010 \rightarrow \min \\ g(x) = \frac{1}{2} x^2 \leq 0 \end{cases}$$

the only feasible region is  $x=0$ ,  $f(0)=2010$

$$L(x, \lambda) = f(x) + \lambda g(x) = x + 2010 + \frac{\lambda}{2} x^2 \quad (\lambda \geq 0, x \in \mathbb{R})$$

$$\frac{\partial L(x, \lambda)}{\partial x} = 1 + \lambda x = 0 \Rightarrow x = -\frac{1}{\lambda}$$

$$\begin{aligned} \rightarrow \varphi(\lambda) &= \min_x L(x, \lambda) = -\frac{1}{\lambda} + 2010 + \underbrace{\left(\frac{\lambda}{2}\right) \left(\frac{1}{\lambda^2}\right)}_{\frac{1}{2\lambda}} \\ &= 2010 - \frac{1}{2\lambda} \end{aligned}$$

$$2 \quad (P) \begin{cases} f(x) = \exp(-x) \rightarrow \min \\ g(x) = -x \leq 0 \end{cases}$$

$$L(x, \lambda) = f(x) + \lambda g(x) = \exp(-x) - \lambda x \quad (\lambda \geq 0)$$

$$\begin{aligned} & \min_{x \in F_u} f(x) \\ & \varphi(\lambda_3) \\ & \varphi(\lambda_1) \\ & \varphi(\lambda_2) \end{aligned}$$