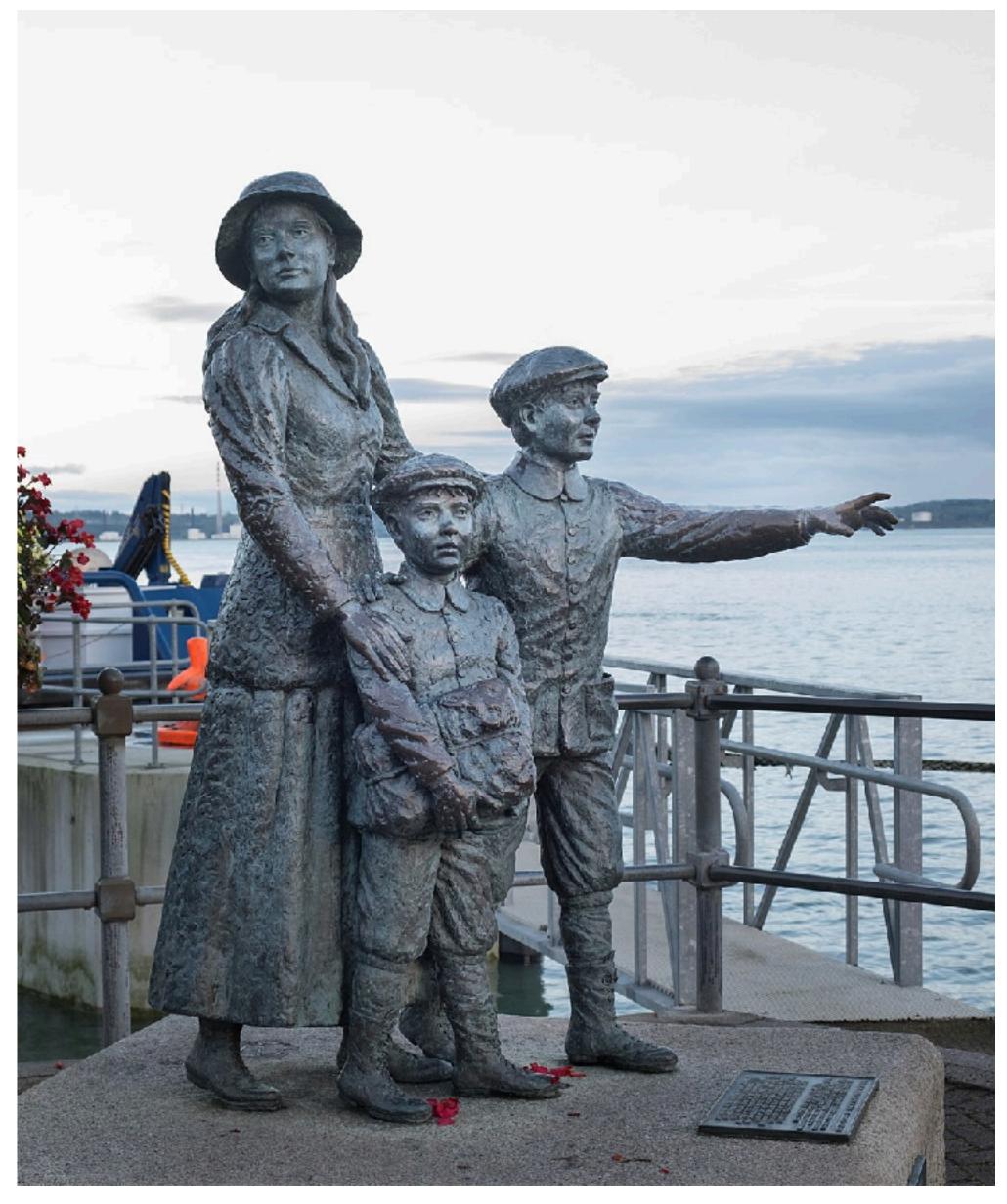
Say Goodbye to the For Loop with High Order Functions by Mike Harris





Pop Quiz

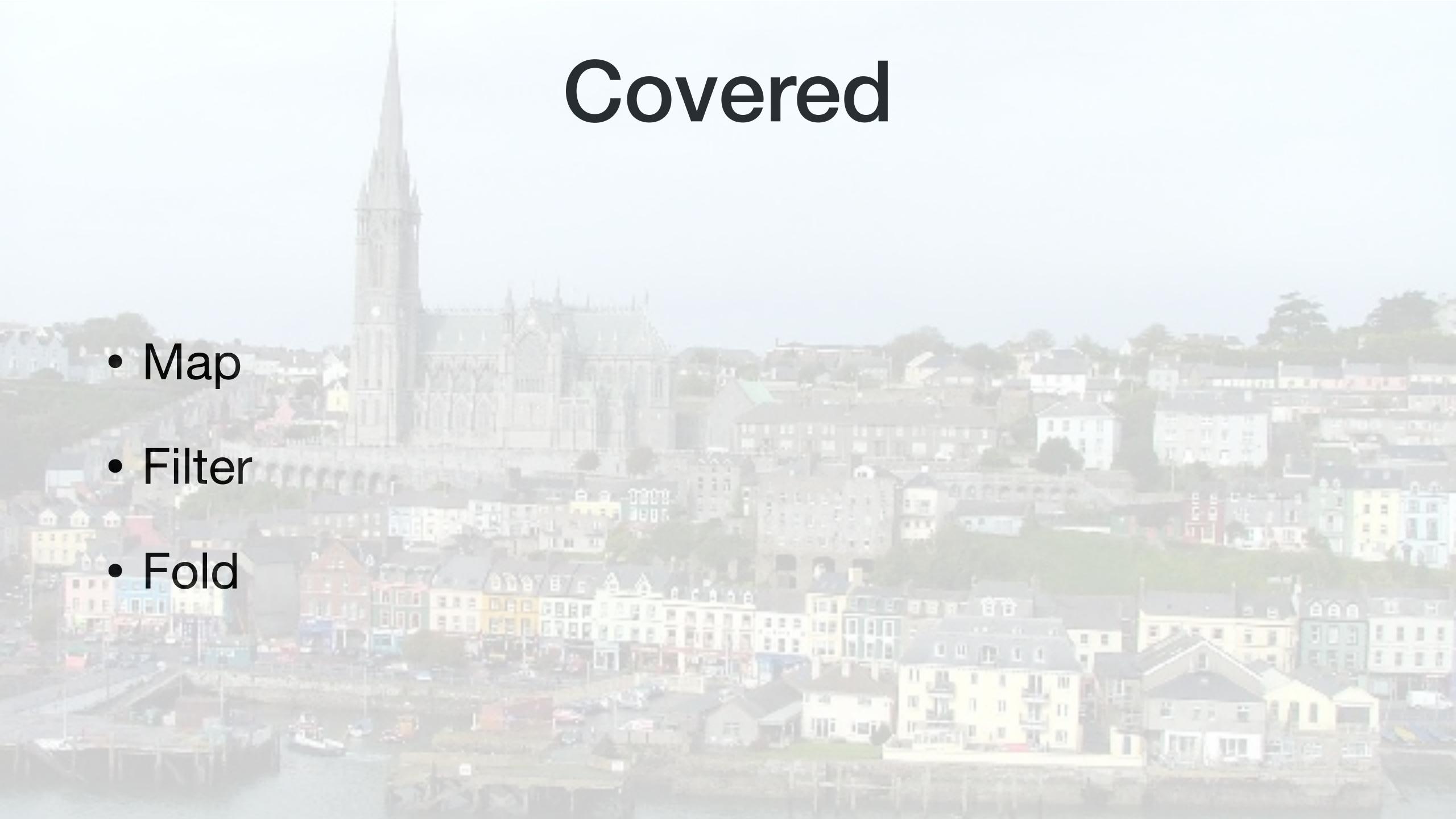
What do these do?

```
main ()
  int i, j, k, l;
  float x[8][2][8][2];
  for (i = 0; i < 8; i++)
    for (j = i; j < 8; j++)
      for (k = 0; k < 2; k++)
  for (l = 0; l < 2; l++)
      if ((i == j) \&\& (k == l))
        x[i][k][j][l] = 0.8;
      else
        x[i][k][j][l] = 0.8;
      if (x[i][k][j][l] < 0.0)
        abort ();
  exit (0);
```

```
int f(void)
{
    static _Complex double t;
    int i, j;
    for(i = 0;i<2;i++)
        for(j = 0;j<2;j++)
        t = .5 * 1.0;
    return t;
}</pre>
```

```
int n;
void foo (int i)
  int a, b;
  if (!i)
    for (a = 1; a < 4; a++)
      if (a)
  for (b = 1; b < 3; b++)
    foo (b);
  n++;
```

I have no idea either.



Problem Statment

Realistic Data

```
IList<(int Zip, double Price, int Quantity)> orders =
  new List<(int Zip, double Price, int Quantity)> {
        (53202, 1.89, 3),
        (60191, 1.99, 2),
        (60060, 0.99, 7),
        (53202, 1.29, 8),
        (60191, 1.89, 2),
        (53202, 0.99, 3)
};
```

Find the total for 53202?

For Loop

```
var total = 0.0;
for (int i = 0; i < orders.Count(); i++)
{
    if (orders[i].Zip == 53202)
        total += orders[i].Price * orders[i].Quantity;
}</pre>
```

```
var total = 0.0;
foreach (var order in orders)
{
    if (order.Zip == 53202)
        total += order.Price * order.Quantity;
}
```

Parts of the For Loop

```
var total = 0.0;
foreach (var order in orders)
{
    if (order.Zip == 53202)
        total += order.Price * order.Quantity;
}
```

```
var total = 0.0;
foreach (var order in orders)
{
    if (Predicate)
        total += order.Price * order.Quantity;
}
```

```
var total = 0.0;
foreach (var order in orders)
{
    if (Predicate)
        total += Mapping;
}
```

```
var total = 0.0;
foreach (var order in orders)
{
    if (Predicate)
        Accumulate += Mapping;
}
```



```
var Initial
foreach (var order in orders)
{
    if (Predicate)
        Accumulate += Mapping;
}
```

```
var total = orders
.Where(order => order.Zip == 53202)
.Select(order => order.Price * order.Quantity)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

```
var total = orders
.Where(Predicate)
.Select(order => order.Price * order.Quantity)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

```
var total = orders
.Where(Predicate)
.Select(Mapping)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

```
var total = orders
.Where(Predicate)
.Select(Mapping)
.Aggregate(0.0, Accumulate);
```

```
var total = orders
.Where(Predicate)
.Select(Mapping)
.Aggregate(Initial, Accumulate);
```

Compare

Compare

```
var total = orders
.Where(Predicate)
.Select(Mapping)
.Aggregate(Initial, Accumulate);
```

```
var Initial
foreach (var order in orders)
{
    if (Predicate)
        Accumulate += Mapping;
}
```



FIOW

FIOW

orders

```
Filter
var total = orders predicate
    .Where(Predicate)
    . Select (Mapping)
    - Aggregate (Ini mapping
                                   Map
                     accumulate
            initial
                                   Fold
                                             total
```

FIOW

```
orders
                                  Filter
                      predicate
var total
    . Where (Predicate)
    .Select (Mapping)
    . Aggregate (Ini
                     mapping
                                   Map
            initial
                    accumulate
                                   Fold
```

Flow

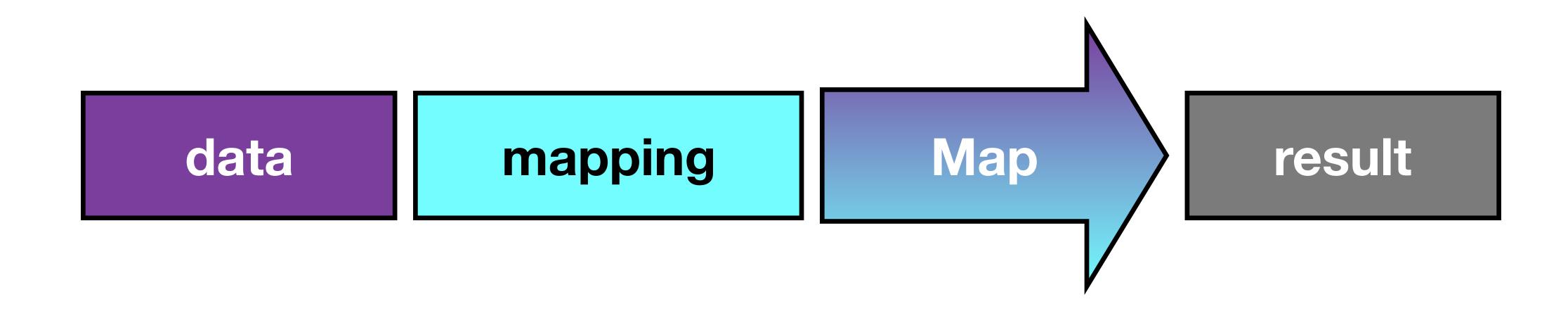
```
Filter
var total = orders predicate
    .Where(Predicate)
    . Select (Mapping)
    -Aggre orders
                     mapping
                                  Map
            initial
                    accumulate
                                  Fold
```

Flow

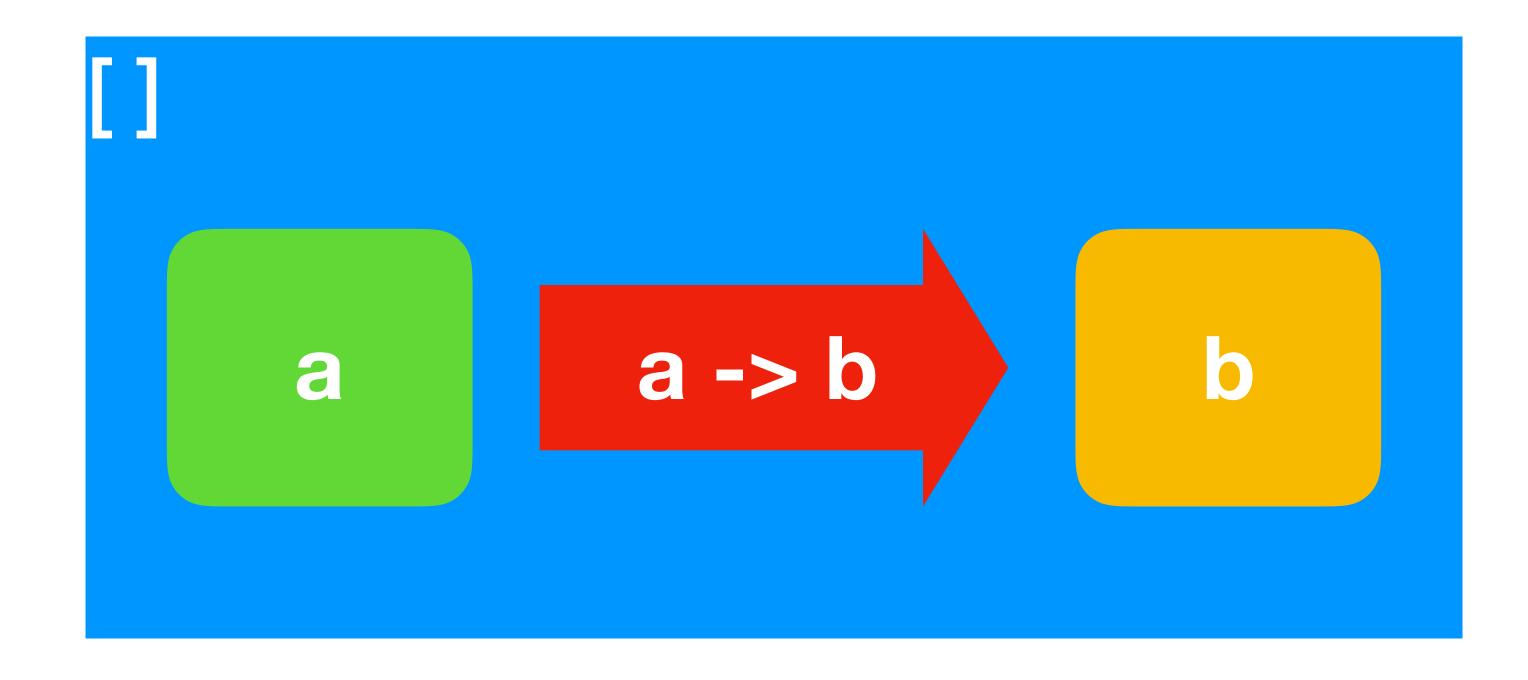
```
Filter
var total = orders predicate
    .Where(Predicate)
    . Select (Mapping)
    - Aggregate (Ini mapping
                                   Map
            initial
 orders
                     accumulate
                                   Fold
                                             total
```

Higher Order Functions

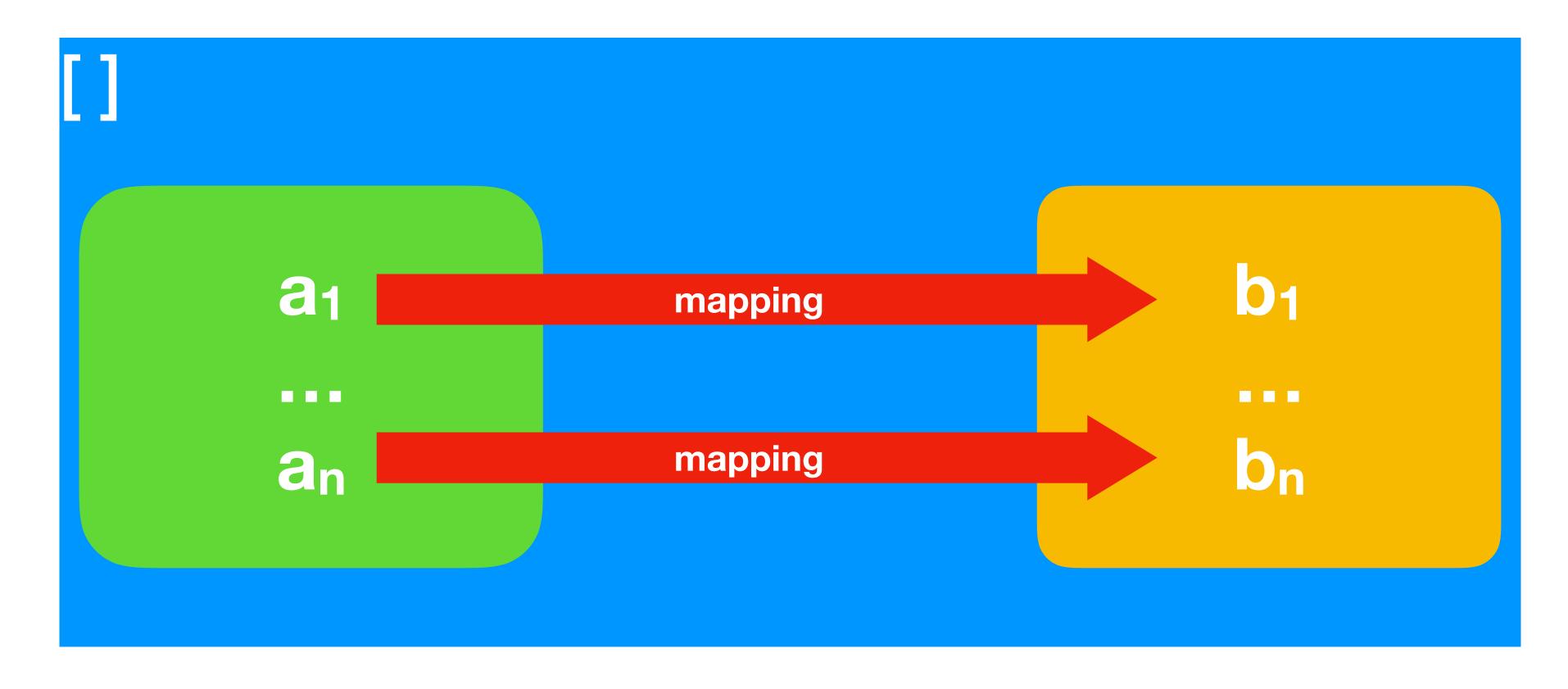
Map



Map

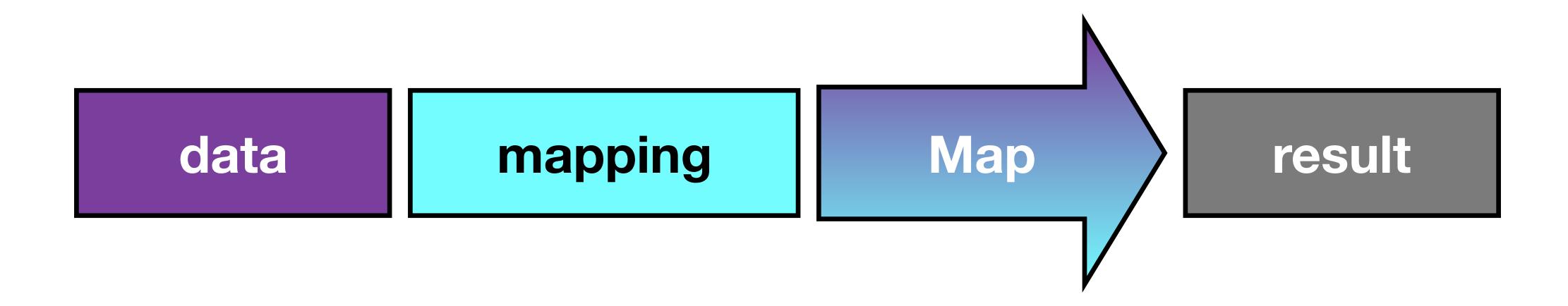


Map

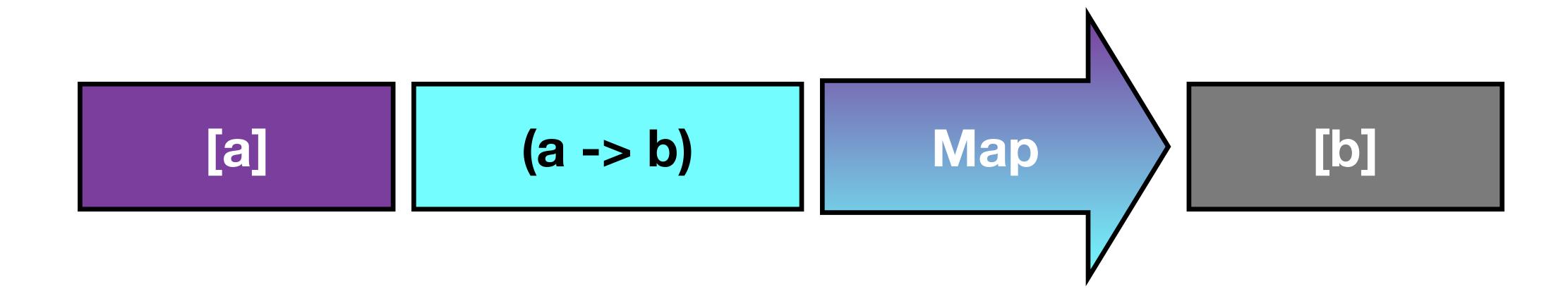


mapping

Map

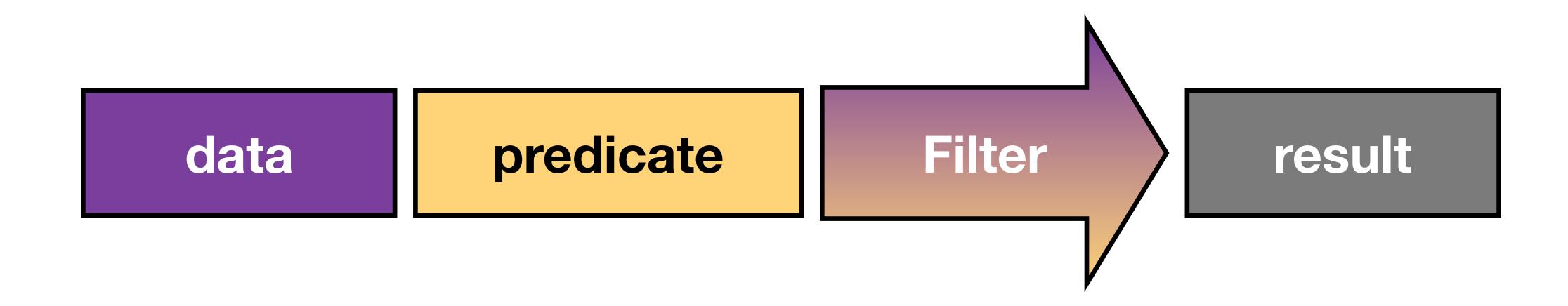


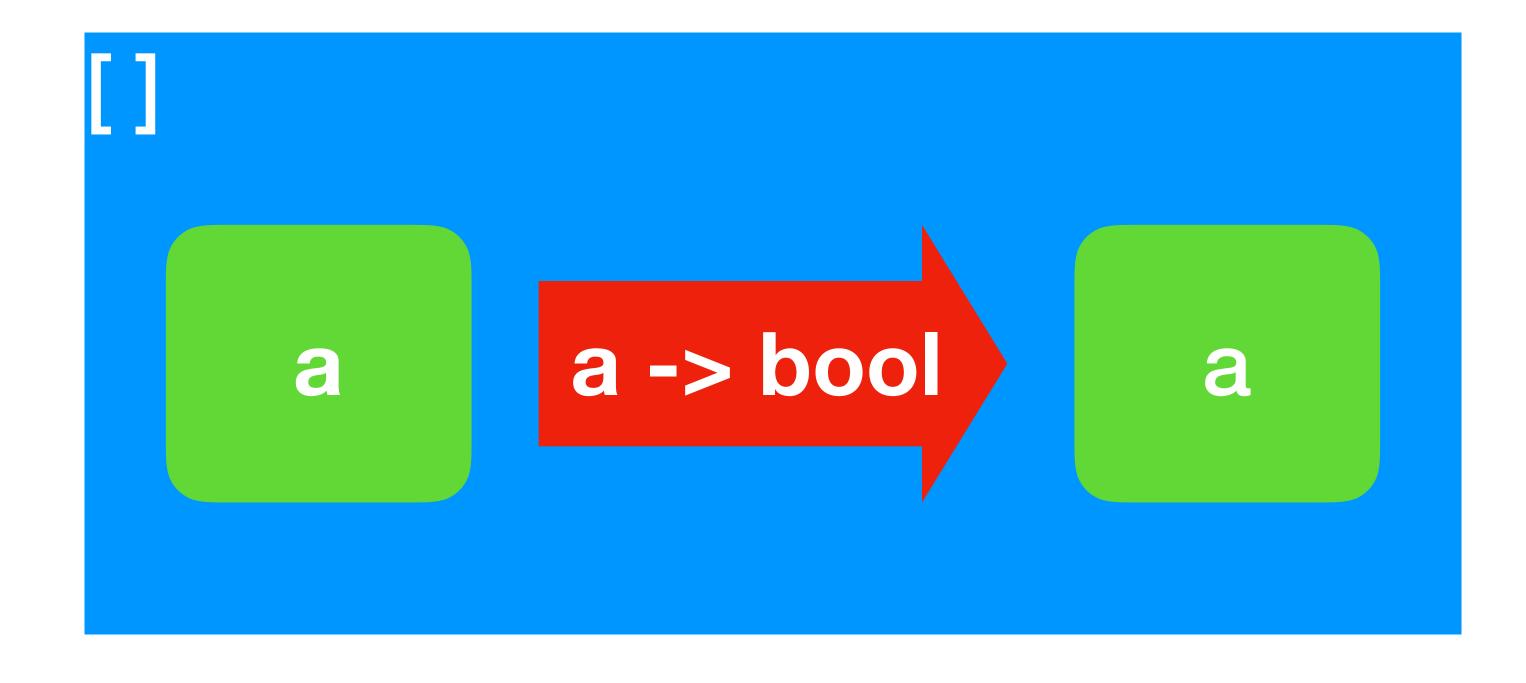
Map



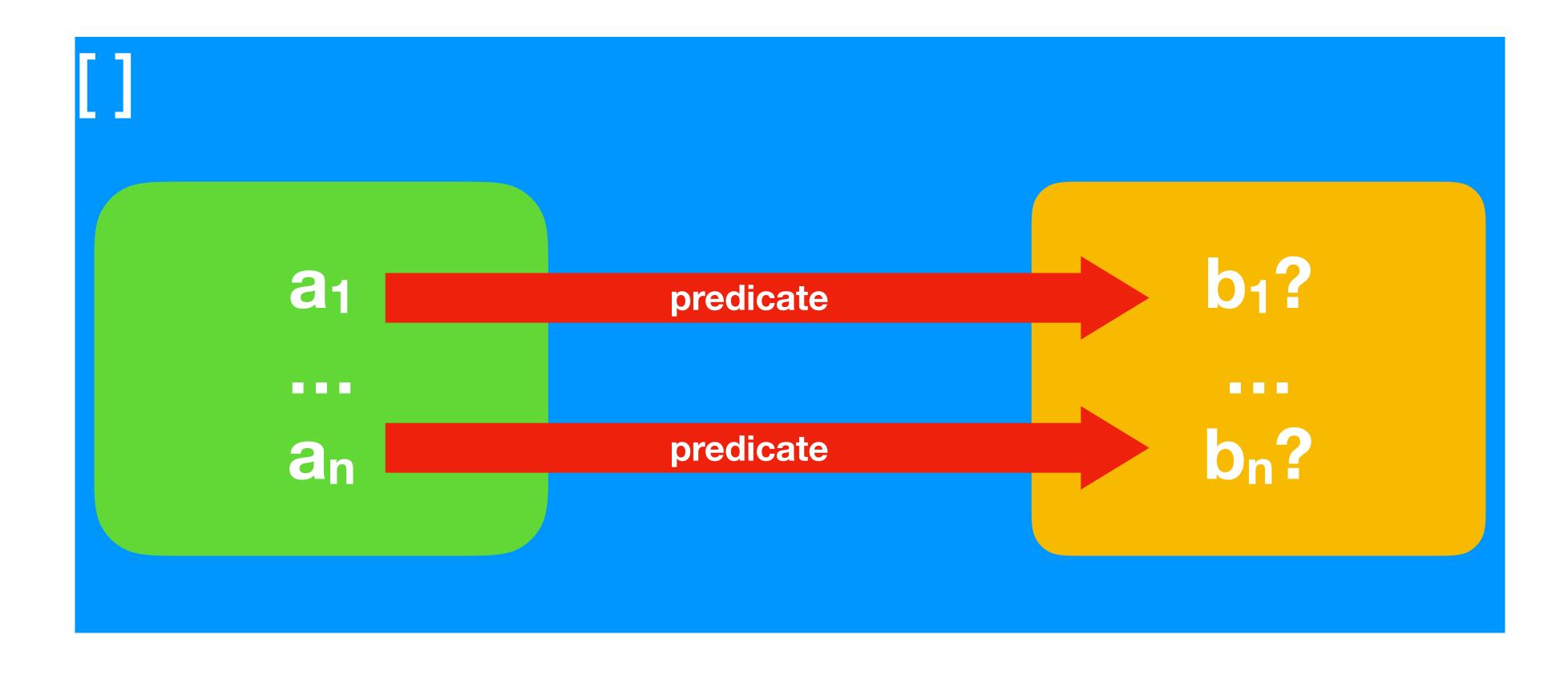
```
public static IEnumerable<U> Map<T, U>(
   this IEnumerable<T> source, Func<T, U> mapping)
   var result = new List<U>();
   foreach(var item in source)
        result.Add(mapping(item));
    return result;
```

```
var result = new List<U>();
foreach(var item in source)
{
    result.Add(Mapping);
}
```

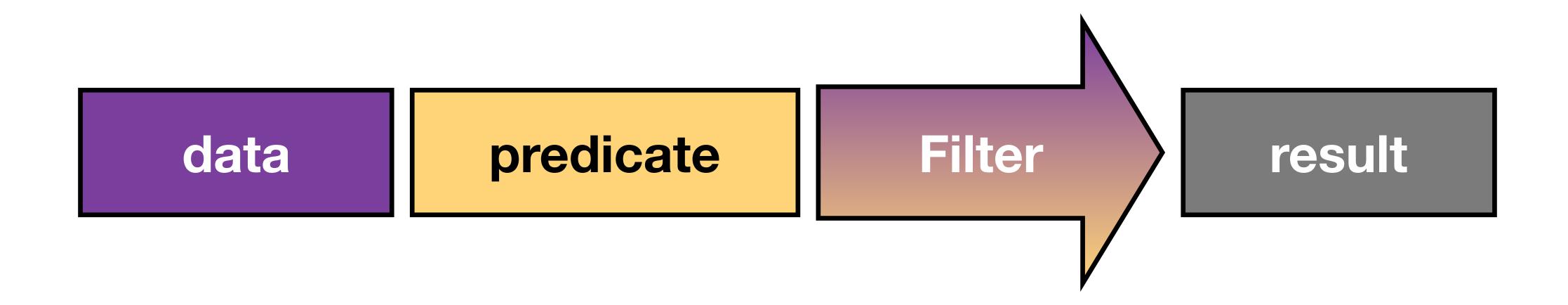




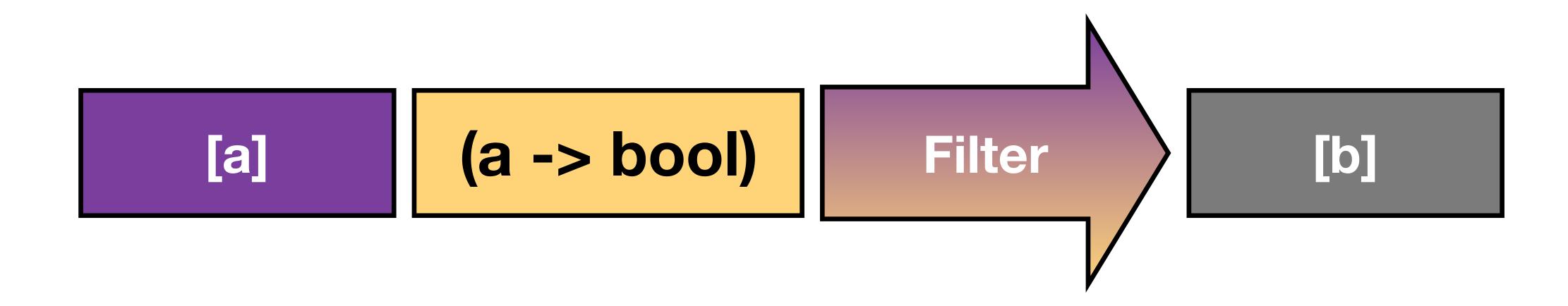
[a] ->
$$(a -> bool) -> [a]$$



n + m predicate



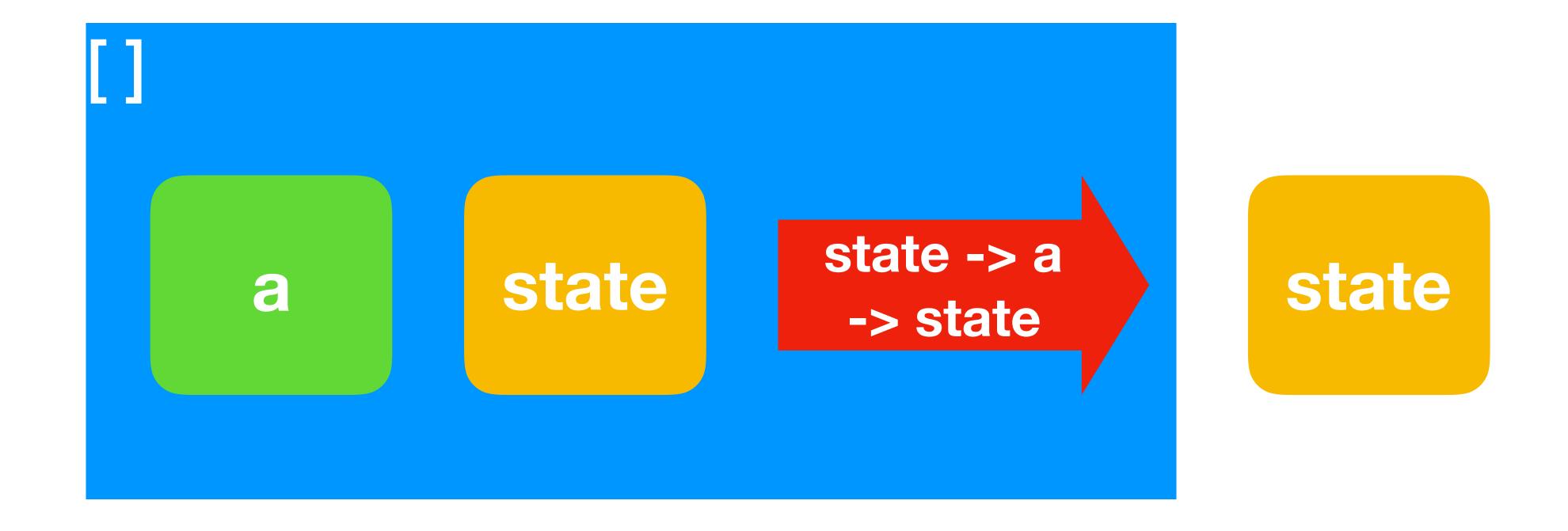
[a] -> (a -> bool) -> [a]



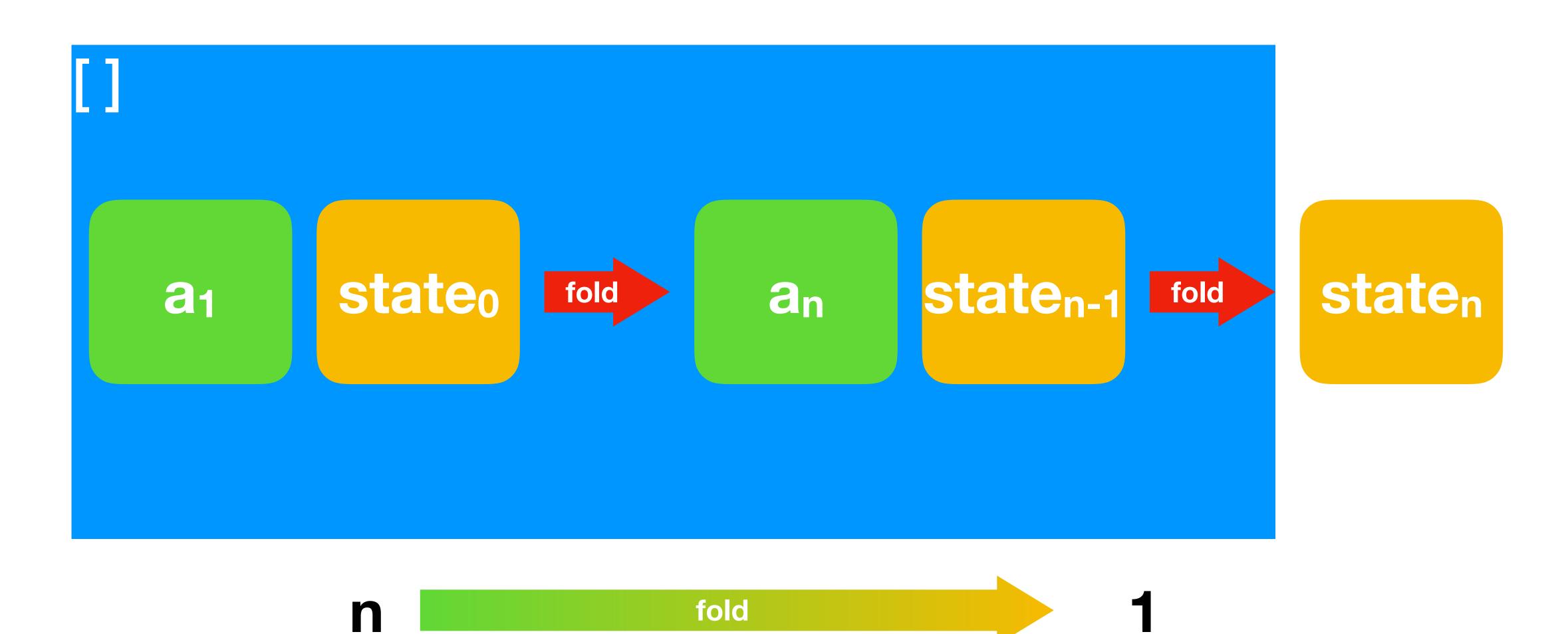
```
public static IEnumerable<T> Filter<T>(
    this IEnumerable<T> source, Func<T, bool> predicate)
    var result = new List<T>();
    foreach(var item in source)
        if (predicate(item))
        result.Add(item);
    return result;
```

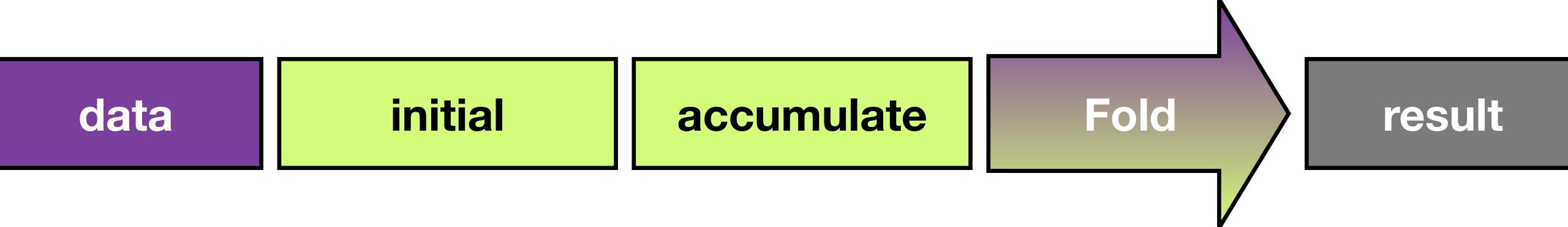
```
var result = new List<T>();
foreach(var item in source)
{
    if (Predicate)
       result.Add(item);
}
```

data initial accumulate Fold result

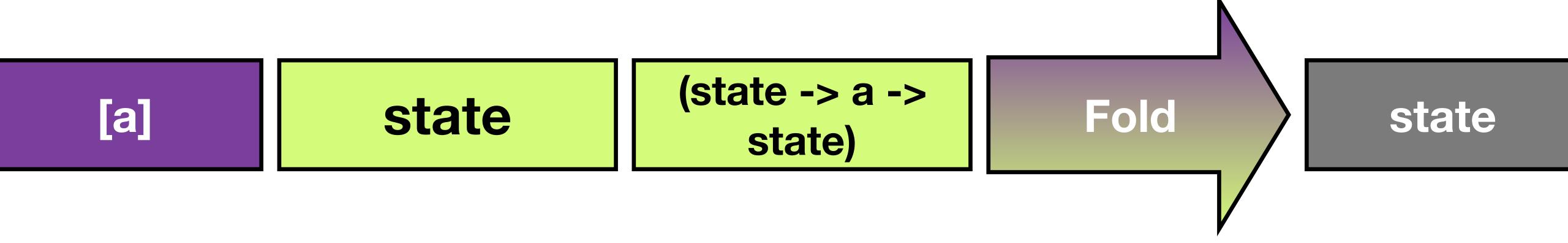


[a] -> state -> (state -> a -> state) -> state





[a] -> state -> (state -> a -> state) -> state

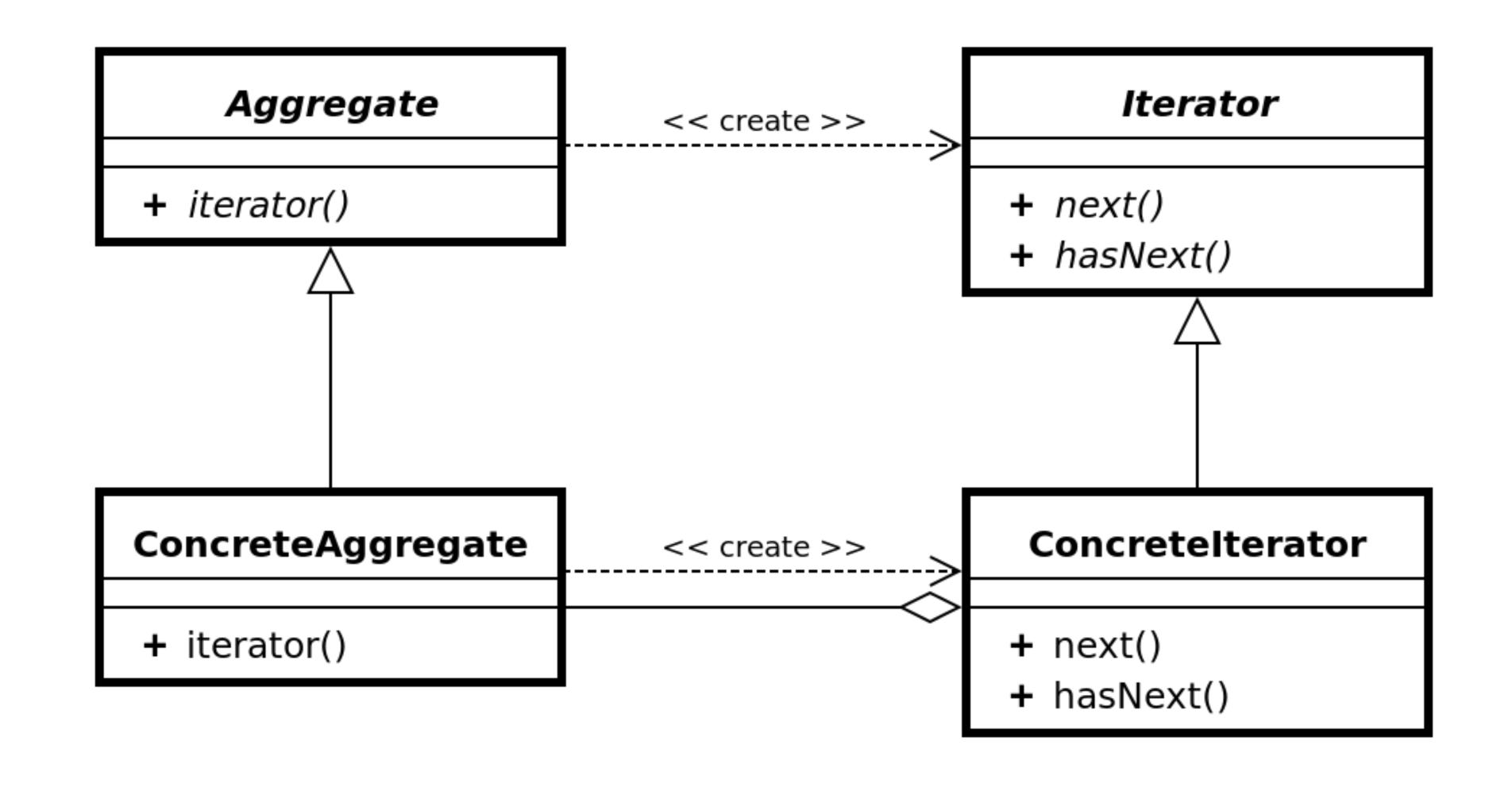


```
public static U Fold<T, U>(
    this IEnumerable<T> source,
    U initial,
    Func<U, T, U> accumulate)
    var result = initial;
    foreach(var item in source)
        result = accumulate(result, item);
    return result;
```

```
var result = Initial;
foreach(var item in source)
{
    result = Accumulate;
}
```

Higher Order Functions in C#

Iterator Pattern



IEnumerator

+ Current

- + MoveNext()
- + Reset()

IEnumerator

Next

+ Current

HasNext

- + MoveNext()
 + Reset()

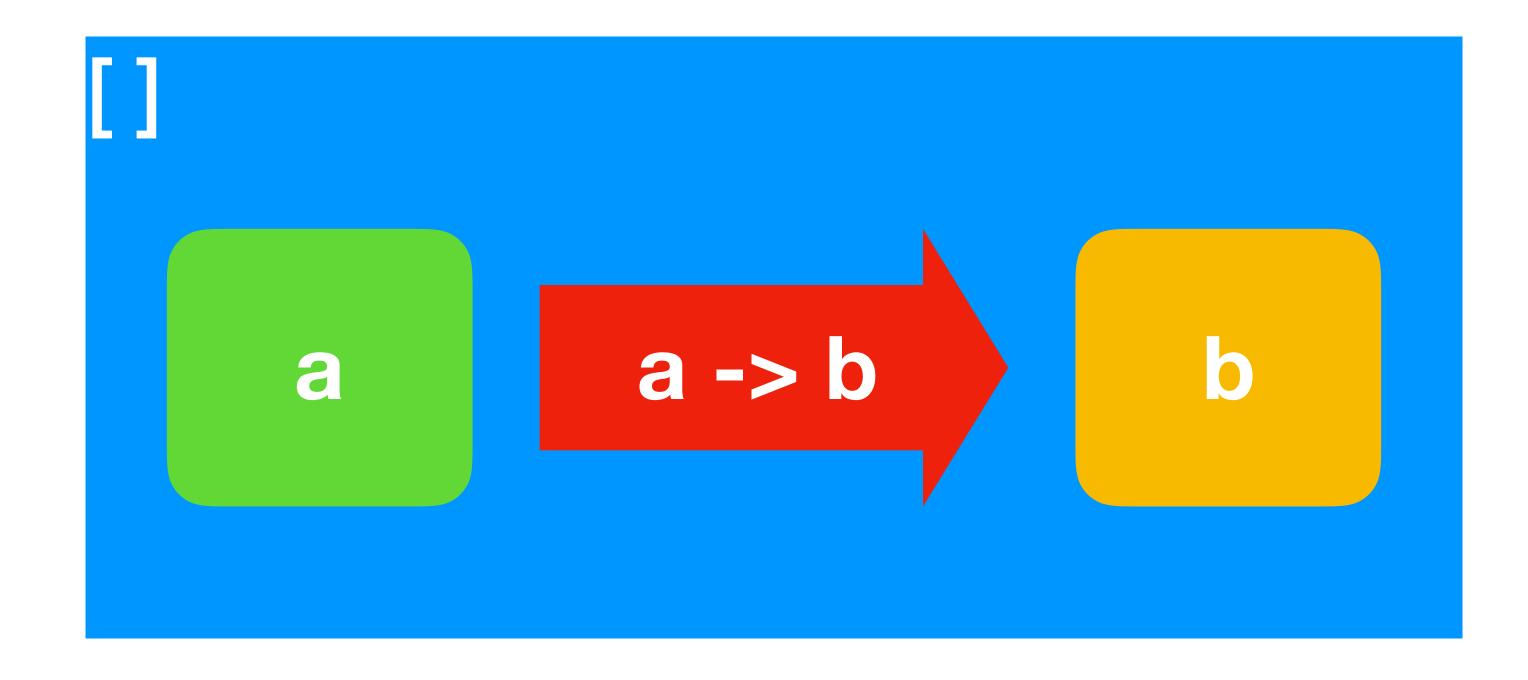
```
public static void Iterate<T>(
        this IEnumerator<T> source, Action<T> f)
{
        while(source.MoveNext())
        {
            f(source.Current);
        }
}
```

```
public static void Iterate<T>(
        this IEnumerator<T> source, Action<T> f)
{
        while(HasNext)
        {
            f(source.Current);
        }
}
```

```
public static void Iterate<T>(
        this IEnumerator<T> source, Action<T> f)
{
        while(HasNext)
        {
            f(Next);
        }
}
```

```
public static void Iterate<T>(
        this IEnumerator<T> source, Function)
{
      while(HasNext)
      {
          Function(Next);
      }
}
```

Map



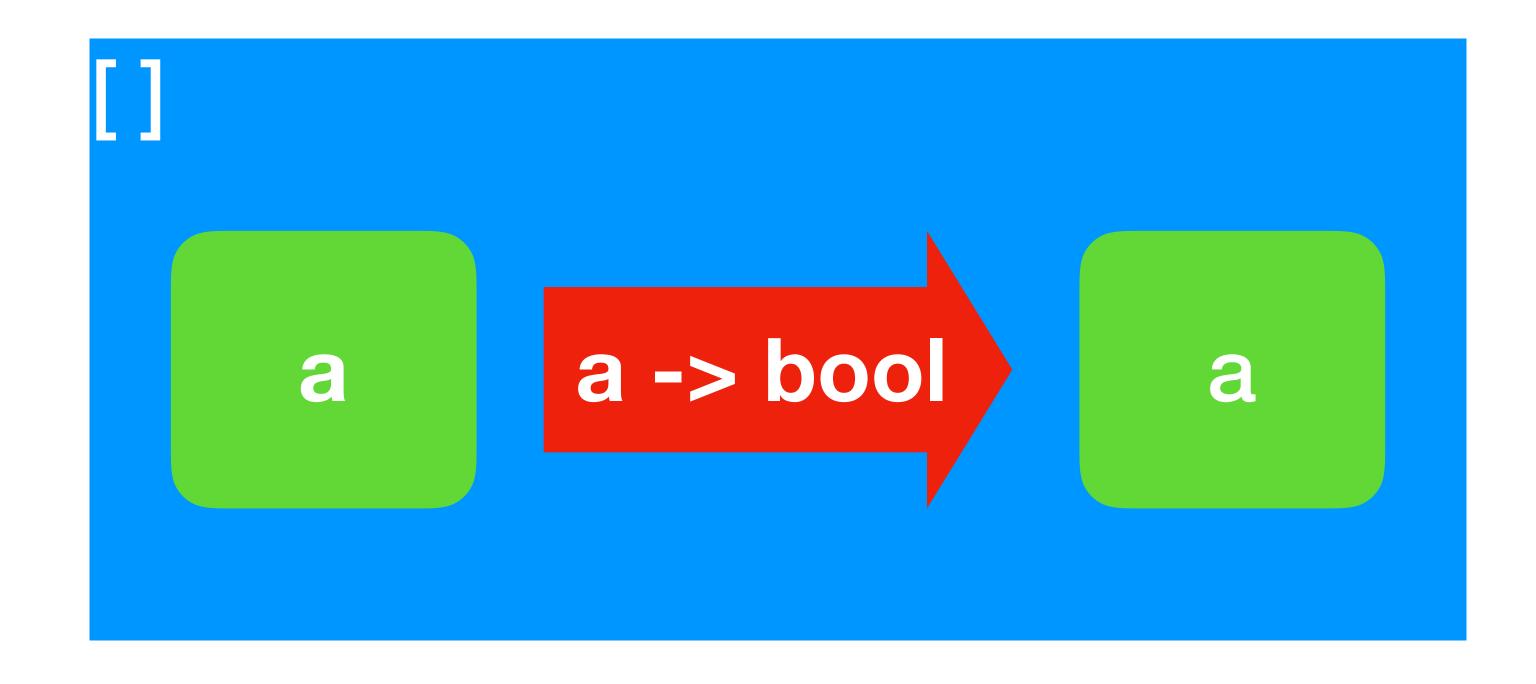
```
private sealed class SelectArrayIterator<TSource, TResult> : Iterator<TResult>, IPartition<TResult>
 private readonly TSource[] _source;
 private readonly Func<TSource, TResult> _selector;
 public override bool MoveNext()
      if (_state < 1 | _state == _source.Length + 1)</pre>
          Dispose();
          return false;
      int index = _state++ - 1;
      _current = _selector(_source[index]);
      return true;
```

```
private sealed class SelectArrayIterator<TSource, TResult> : Iterator<TResult>, IPartition<TResult>
 private readonly TSource[] _source;
 private readonly Func<TSource, TResult> _selector;
 public override bool HasNext()
      if (_state < 1 | _state == _source.Length + 1)</pre>
          Dispose();
          return false;
      int index = _state++ - 1;
      _current = _selector(_source[index]);
      return true;
```

```
private sealed class SelectArrayIterator<TSource, TResult> : Iterator<TResult>, IPartition<TResult>
 private readonly TSource[] _source;
 private readonly Func<TSource, TResult> _selector;
 public override bool HasNext()
      if (_state < 1 | _state == _source.Length + 1)</pre>
          Dispose();
          return false;
      int index = _{state++} - 1;
      Next = _selector(_source[index]);
      return true;
```

```
private sealed class SelectArrayIterator<TSource, TResult> : Iterator<TResult>, IPartition<TResult>
 private readonly TSource[] _source;
 Function
 public override bool HasNext()
      if (_state < 1 | _state == _source.Length + 1)</pre>
          Dispose();
          return false;
      int index = _{state++} - 1;
      Next = Function(_source[index]);
      return true;
```

```
public override bool HasNext()
    if (_state < 1 | _state == _source.Length + 1)</pre>
        Dispose();
        return false;
    int index = _state++ - 1;
    Next = Function(_source[index]);
    return true;
```



[a] ->
$$(a -> bool) -> [a]$$

```
internal sealed class WhereArrayIterator<TSource> : Iterator<TSource>, IIListProvider<TSource>
   private readonly TSource[] _source;
    private readonly Func<TSource, bool> _predicate;
    public override bool MoveNext()
        int index = _state - 1;
        TSource[] source = _source;
       while (unchecked((uint)index < (uint)source.Length))</pre>
            TSource item = source[index];
            index = _state++;
            if (_predicate(item))
                _current = item;
                return true;
       Dispose();
        return false;
```

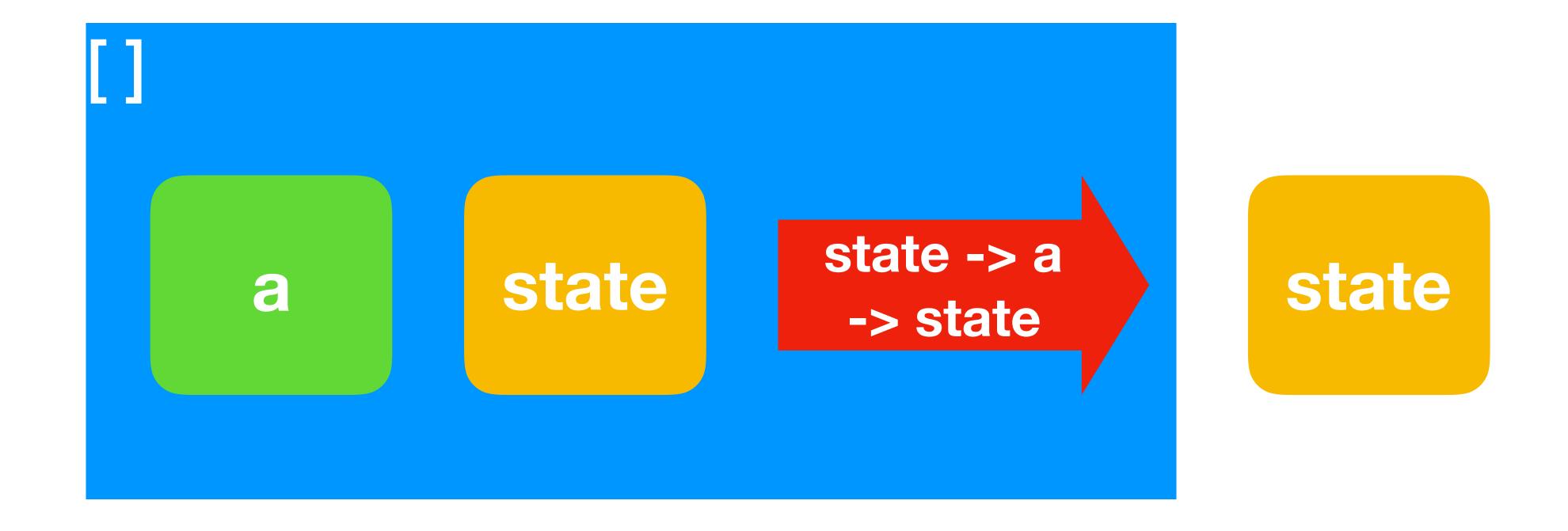
```
internal sealed class WhereArrayIterator<TSource> : Iterator<TSource>, IIListProvider<TSource>
   private readonly TSource[] _source;
    private readonly Func<TSource, bool> _predicate;
    public override bool HasNext()
        int index = _state - 1;
        TSource[] source = _source;
       while (unchecked((uint)index < (uint)source.Length))</pre>
            TSource item = source[index];
            index = _state++;
            if (_predicate(item))
                _current = item;
                return true;
       Dispose();
        return false;
```

```
internal sealed class WhereArrayIterator<TSource> : Iterator<TSource>, IIListProvider<TSource>
   private readonly TSource[] _source;
    private readonly Func<TSource, bool> _predicate;
    public override bool HasNext()
        int index = _state - 1;
        TSource[] source = _source;
       while (unchecked((uint)index < (uint)source.Length))</pre>
            TSource item = source[index];
            index = _state++;
            if (_predicate(item))
                Next = item;
                return true;
       Dispose();
        return false;
```

```
internal sealed class WhereArrayIterator<TSource> : Iterator<TSource>, IIListProvider<TSource>
    private readonly TSource[] _source;
    Function
    public override bool HasNext()
        int index = _state - 1;
        TSource[] source = _source;
       while (unchecked((uint)index < (uint)source.Length))
            TSource item = source[index];
            index = _state++;
            if (Function(item))
                Next = item;
                return true;
       Dispose();
        return false;
```

```
public override bool HasNext()
    while (index < source.Length))</pre>
        TSource item = source[index];
        index = _state++;
        if (Function(item))
                 = item;
             return true;
    Dispose();
    return false;
```

Fold



[a] -> state -> (state -> a -> state) -> state

```
public static TAccumulate Aggregate<TSource, TAccumulate>(this IEnumerable<TSource> source,
TAccumulate seed, Func<TAccumulate, TSource, TAccumulate> func)
    if (source == null)
        throw Error.ArgumentNull(nameof(source));
    if (func == null)
        throw Error.ArgumentNull(nameof(func));
    TAccumulate result = seed;
    foreach (TSource element in source)
        result = func(result, element);
    return result;
```

```
public static TAccumulate Aggregate<TSource, TAccumulate>(this IEnumerable<TSource> source,
TAccumulate seed, Func<TAccumulate, TSource, TAccumulate> func)
    if (source == null)
        throw Error.ArgumentNull(nameof(source));
    if (func == null)
        throw Error.ArgumentNull(nameof(func));
    TAccumulate result = seed;
    HasNext (TSource element in source)
        result = func(result, element);
    return result;
```

```
public static TAccumulate Aggregate<TSource, TAccumulate>(this IEnumerable<TSource> source,
TAccumulate seed, Func<TAccumulate, TSource, TAccumulate> func)
    if (source == null)
        throw Error.ArgumentNull(nameof(source));
    if (func == null)
        throw Error.ArgumentNull(nameof(func));
    TAccumulate result = seed;
    HasNext (TSource Next in source)
        result = func(result, Next);
    return result;
```

```
public static TAccumulate Aggregate<TSource, TAccumulate>(this IEnumerable<TSource> source,
TAccumulate seed, Function)
    if (source == null)
        throw Error.ArgumentNull(nameof(source));
    if (func == null)
        throw Error.ArgumentNull(nameof(func));
    TAccumulate result = seed;
    HasNext (TSource Next in source)
        result = Function(result, Next);
    return result;
```

```
TAccumulate result = seed;
HasNext (TSource Next in source)
{
    result = Function(result, Next);
}
```

LINQ Execution

Code

```
var total = orders
.Where(order => order.Zip == 53202)
.Select(order => order.Price * order.Quantity)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

Data

```
IList<(int Zip, double Price, int Quantity)> orders =
  new List<(int Zip, double Price, int Quantity)> {
          (53202, 1.89, 3),
          (60191, 1.99, 2),
          (60060, 0.99, 7),
          (53202, 1.29, 8),
          (60191, 1.89, 2),
          (53202, 0.99, 3)
    };
```

In what order does this execute?

```
var total = orders
.Where(order => order.Zip == 53202)
.Select(order => order.Price * order.Quantity)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

In what order does this execute?

```
var spy = new List<string>();
orders
    .Where(order =>
       { spy.Add("filter"); return order.Zip == 53202; })
    .Select(order =>
       { spy.Add("map");
         return order.Price * order.Quantity; })
    -Aggregate(0.0, (sub, amount) =>
       { spy.Add("fold"); return sub + amount; });
```

Answer

```
new List<string> {
    "filter", "map", "fold",
    "filter",
    "filter", "map", "fold",
    "filter",
    "filter", "map", "fold"
},
```

Does exactly what we want

```
var total = orders
.Where(order => order.Zip == 53202)
.Select(order => order.Price * order.Quantity)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

Fusion Property of Iterators

Fusion Property of Iterators

iterator $f \circ \text{iterator } g = \text{iterator } (f \circ g)$

```
var total = 0.0;
foreach (var order in orders)
{
    if (order.Zip == 53202)
        total += order.Price * order.Quantity;
}
```

```
var total = 0.0;
Iterate (var order in orders)
{
    Filter(order.Zip == 53202)
    Fold(+, Map(order.Price * order.Quantity));
}
```

iterator *filter* |> iterator *map* |> iterator *fold*

```
iterator filter |> iterator map |> iterator fold =
  (iterator fold
   (iterator map
      (iterator filter)))
```

```
iterator filter |> iterator map |> iterator fold = ( iterator fold ( iterator map ( iterator filter ) ) ) = iterator fold ∘ iterator map ∘ iterator filter
```

```
iterator filter |> iterator map |> iterator fold = ( iterator fold ( iterator map ( iterator filter ) ) ) = iterator fold ∘ iterator map ∘ iterator filter = iterator (fold ∘ map ∘ filter)
```

iterator $fold \circ iterator map \circ iterator filter = iterator (fold \circ map \circ filter)$

LINQ

```
var total = orders
.Where(order => order.Zip == 53202)
.Select(order => order.Price * order.Quantity)
.Aggregate(0.0, (sub, amount) => sub + amount);
```

LINQ

```
var total = orders
.Filter(order => order.Zip == 53202)
.Map(order => order.Price * order.Quantity)
.Fold(0.0, (sub, amount) => sub + amount);
```

LINQ

iterator *filter* ∘ iterator *map* ∘ iterator *fold* = iterator (*filter* ∘ *map* ∘ *fold*)

Universal Way to Solve Problems

C# List Comprehension

```
(from order in orders
where order.Zip == 53202
select new {Amount = order.Price * order.Quantity})
.Sum(order => order.Amount);
```

JavaScript

```
orders
.filter(order => order.zip === 53202)
.map(order => order.price * order.quantity)
.reduce((sub, amount) => sub + amount, 0.0);
```



PowerShell

```
($orders |
Where-Object { $_.Zip -eq 53202 } |
Select-Object @{
  Name = "Amount";
  Expression = {$_.Price * $_.Quantity} } |
Measure-Object Amount -Sum).Sum
```



F#

```
orders
|> List.filter (fun x -> x.Zip = 53202)
|> List.map (fun x -> x.Price * (double x.Quantity))
|> List.sum
```

T-SQL

```
select distinct
  sum(price * quantity) over (partition by zip)
  from (
    values
      (53202, 1.89, 3),
      (60191, 1.99, 2),
      (60060, 0.99, 7),
      (53202, 1.29, 8),
      (60191, 1.89, 2),
      (53202, 0.99, 3)
  ) as orders(zip, price, quantity)
  where zip = 53202
```



Thank you

Mike Harris

Say Goodbye to the For Loop with High Order Functions https://bit.ly/2uUmllM

@MikeMKH



Next Steps

- Enrico Buonanno, Functional Programming in C# [book] https://www.manning.com/books/functional-programming-in-c-sharp
- Scott Wlaschin, F# for Fun and Profit [blog] https://fsharpforfunandprofit.com/
- Mark Seemann, From Design Patterns to Category Theory [blog]
 http://blog.ploeh.dk/2017/10/04/from-design-patterns-to-category-theory/

Example Code

- C#, https://github.com/MikeMKH/talks/tree/master/say-goodbye-to-the-for-loop-with-higher-order-functions/csharp
- JavaScript, https://github.com/MikeMKH/talks/tree/master/say-goodbye-to-the-for-loop-with-higher-order-functions/javascript
- PowerShell, https://github.com/MikeMKH/talks/tree/master/say-goodbye-to-the-for-loop-with-higher-order-functions/powershell
- F#, https://github.com/MikeMKH/talks/tree/master/say-goodbye-to-the-for-loop-with-higher-order-functions/fsharp
- T-SQL, https://github.com/MikeMKH/talks/tree/master/say-goodbye-to-the-for-loop-with-higher-order-functions/sql

Images

- Annie Moore Statue by Jeanne Rynhart, Cobh, Ireland, image by DeFacto Own work, CC BY-SA 4.0, https://commons.wikimedia.org/w/index.php?curid=63434212
- Cobh county Cork, Ireland, image by Ralph Rawlinson, CC BY-SA 2.0, https://curid=336268
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- PowerShell Logo, Public Domain, https://upload.wikimedia.org/wikipedia/commons/2/2f/
 PowerShell 5.0 icon.png
- Self photo by Kelsey Harris taken at StrangeLoop

gcc Source Code

- example 1, https://github.com/gcc-mirror/gcc/blob/ e11be3ea01eaf8acd8cd86d3f9c427621b64e6b4/gcc/testsuite/gcc.c-torture/execute/930614-2.c#L1-L20
- example 2, https://github.com/gcc-mirror/gcc/blob/
 e11be3ea01eaf8acd8cd86d3f9c427621b64e6b4/gcc/testsuite/gcc.c-torture/compile/pr25513.c#L1-L9
- example 3, https://github.com/gcc-mirror/gcc/blob/
 e11be3ea01eaf8acd8cd86d3f9c427621b64e6b4/gcc/testsuite/gcc.c-torture/compile/pr43186.c#L1-L15

LINQ Source Code

- Select, https://github.com/dotnet/corefx/blob/
 a673a117846205fc1a5c648c29451ff3da83554d/src/System.Linq/src/
 System/Linq/Select.cs#L199-L226
- Where, https://github.com/dotnet/corefx/blob/
 a673a117846205fc1a5c648c29451ff3da83554d/src/System.Linq/src/
 System/Linq/Where.cs#L198-L255
- Aggregate, https://github.com/dotnet/corefx/blob/
 a673a117846205fc1a5c648c29451ff3da83554d/src/System.Linq/src/
 System/Linq/Aggregate.cs#L40-L59