

$$w_i(t+1) = w_i(t) + \Delta w_i$$

$$w_i(t+1) = w_i(t) + \alpha \left(-\frac{\partial L}{\partial w_i} \right)$$

$$L = \text{MSE} = \frac{1}{2} \sum_{p=1}^P \sum_{k=1}^M (d_k^p - y_k^p)^2$$

$$L = (d - y)^2$$

$$\frac{\partial L}{\partial w_i} = \frac{\partial L}{\partial e} \cdot \frac{\partial e}{\partial y} \cdot \frac{\partial y}{\partial w_i}$$

$$\frac{\partial L}{\partial w_i} = \frac{\partial L}{\partial e} \cdot \frac{\partial e}{\partial y} \cdot \frac{\partial y}{\partial w_i}$$

$$L = (d - y)^2 = e^2$$

$$\frac{\partial L}{\partial e} = 2 \cdot e$$

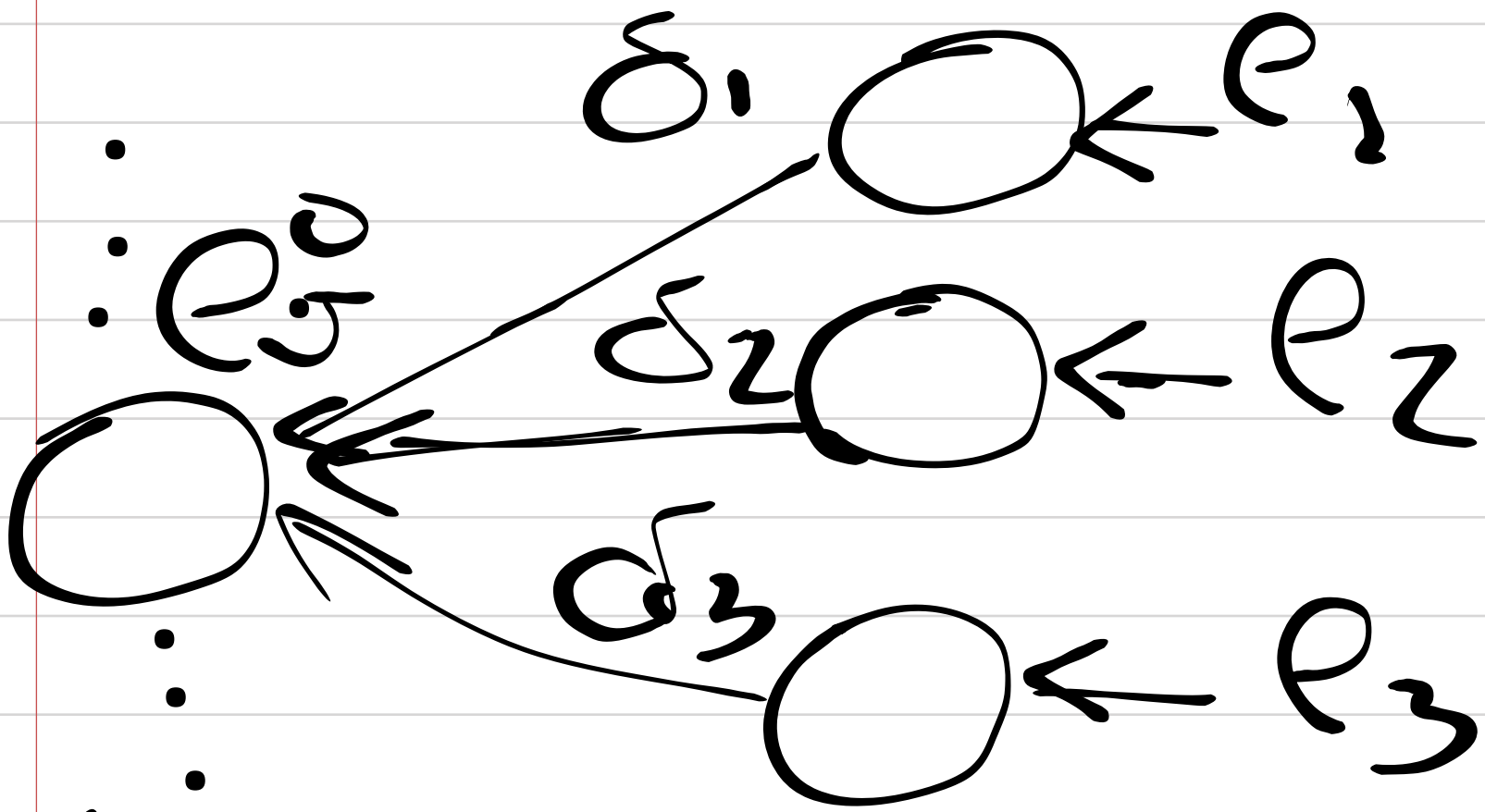
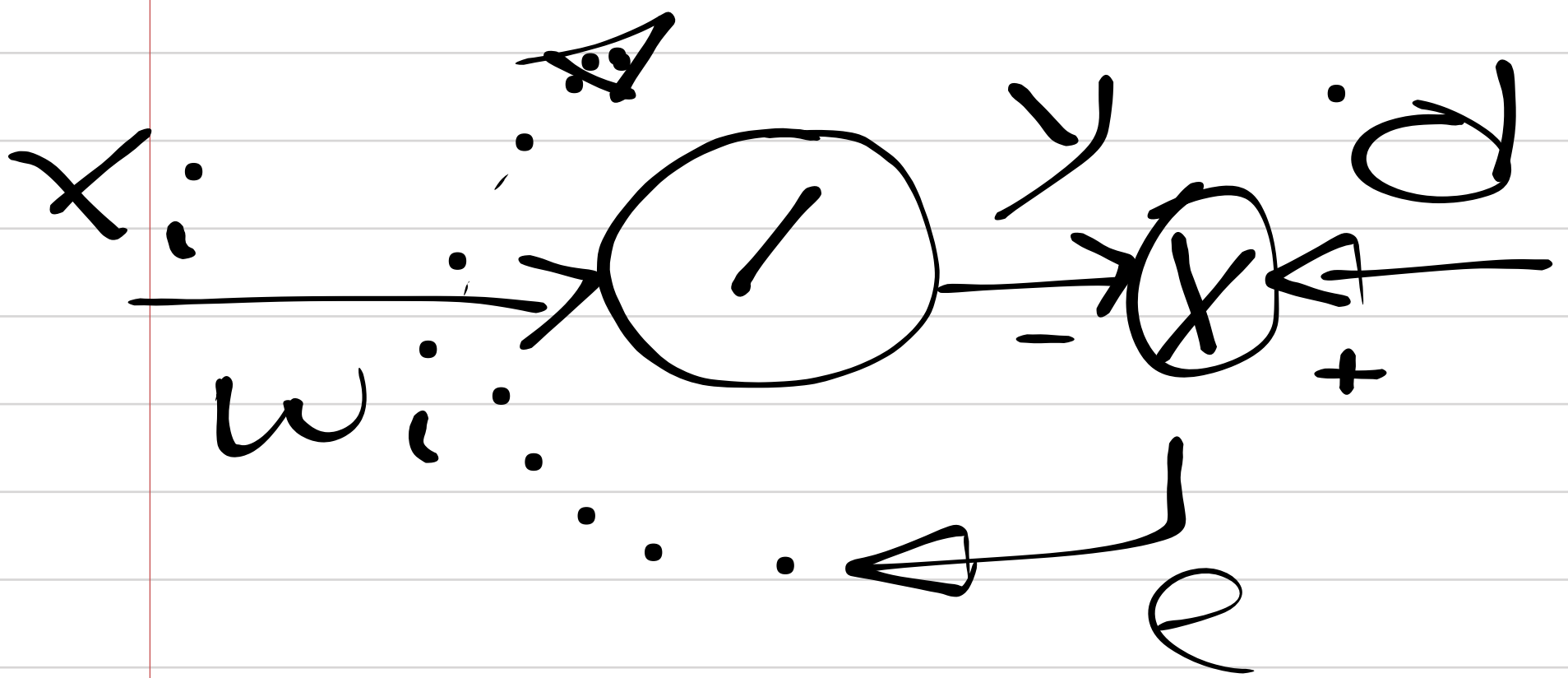
$$\frac{\partial e}{\partial y} = -1$$

$$\frac{\partial y}{\partial w_i} = x_i$$

$$\frac{\partial L}{\partial w_i} = 2(d - y)(-1)x_i$$

$$-\frac{\partial L}{\partial w_i} = 2(d - y)x_i$$

$$w_i(t+1) = w_i(t) + 2\alpha(d - y)x_i$$



$$e_j = \delta_1 w_{1j} + \delta_2 w_{2j} +$$

$$\delta_3 w_{3j}$$

$$= \sum_{k=1}^n \delta_k w_{kj}$$

Backpropagation

x_1	x_2	$x_1 \wedge x_2$
1	1	1
1	0	0
0	1	0
0	0	0

