

A high-speed photograph of a water droplet falling into a pool of water, creating a series of concentric ripples. The background is a deep blue, and the water surface is dark, with the ripples catching the light.

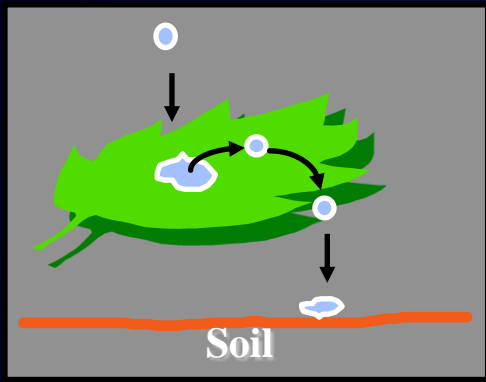
Controlling drop impact by polymer additives

Michael Smith¹, Volfango Bertola²

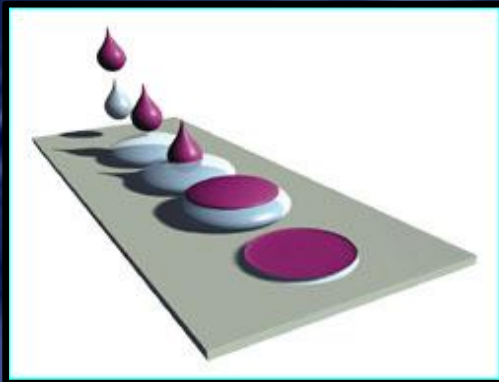
¹School of Physics, University of Nottingham

²School of Engineering, University of Liverpool

Why study droplet Impact?



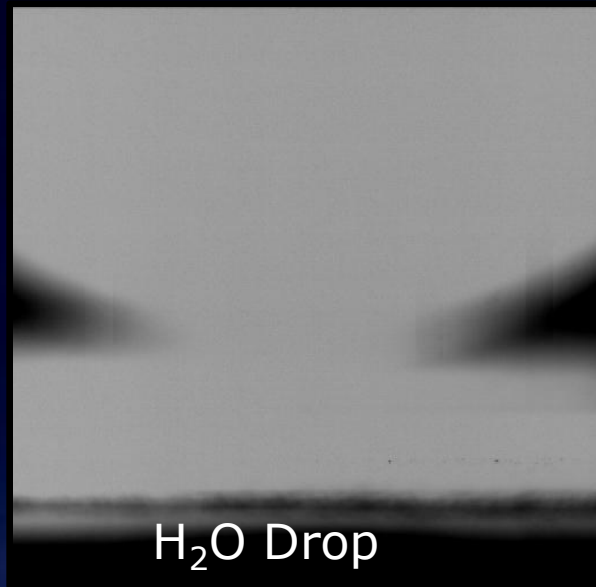
Agrochemicals



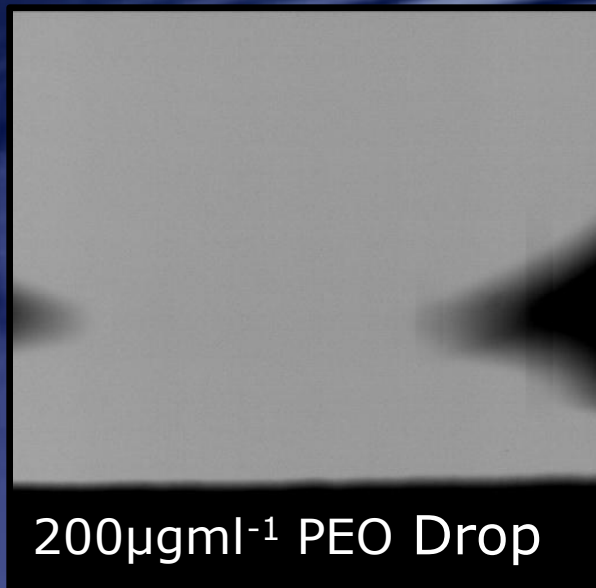
Inkjet printing

- Wetting /dewetting
- Controlling droplet deposition is important in a number of commercial applications:
 - Inkjet printing
 - Agrochemical industry
 - Spray cooling
 - Soldering of microelectronics
- Suppressing droplet rebound is advantageous

Dynamics of drop impact



H₂O Drop



200µgml⁻¹ PEO Drop

- Droplets spread on impact forming a “lamella” (~5ms)

- On hydrophobic surfaces, retraction leads to drop rebound

- Addition of tiny amounts of a flexible homopolymer completely suppresses rebound

Impact / expansion:

$$\text{Weber \#, } We = \frac{\text{inertia}}{\text{capillarity}} = \frac{\rho V_i^2 D_o}{\sigma}$$

$$\text{Reynolds \#, } Re = \frac{\text{inertia}}{\text{viscosity}} = \frac{\rho V_i D_o}{\eta}$$

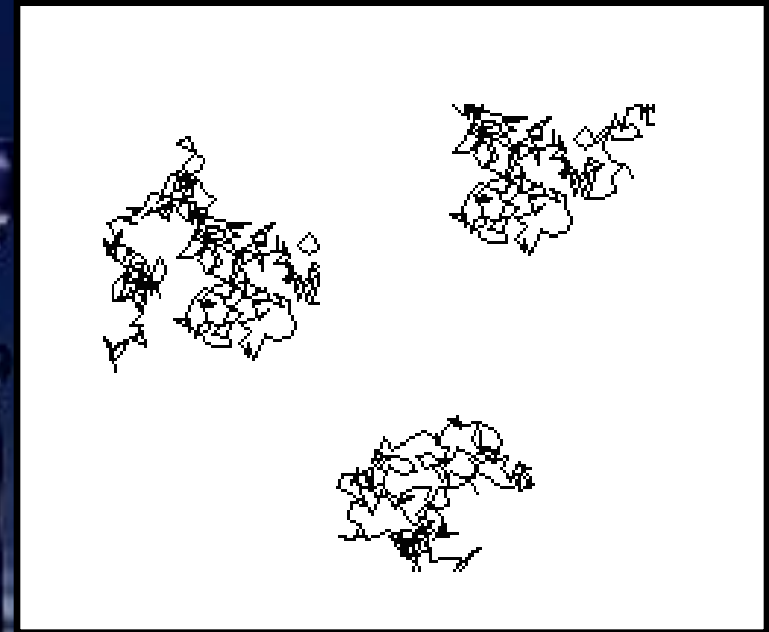
Retraction:

$$\text{Capillary \#, } Ca = \frac{\text{viscosity}}{\text{capillarity}} = \frac{We}{Re} = \frac{V_{\text{ret}} \eta}{\sigma}$$

Flexible polymers

- In solution polymer molecules adopt random coil
- Dilute regime: polymer molecules do not overlap
- No significant differences in shear viscosity or surface tension

Typical concentration:
10-200 p.p.m. (0.001-0.02%)

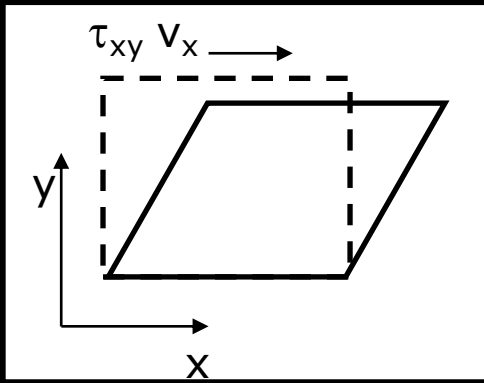


$\text{H}_2\text{O} \rightarrow \sigma \approx 72 \text{ mN/m}, \eta \approx 1 \text{ mPa s}$
 $\text{PEO}_{200\text{ppm}} \rightarrow \sigma \approx 70 \text{ mN/m}, \eta \approx 1.23 \text{ mPa s}$

→ Same parameters, different behaviour!

Elongational viscosity

Shear flow:

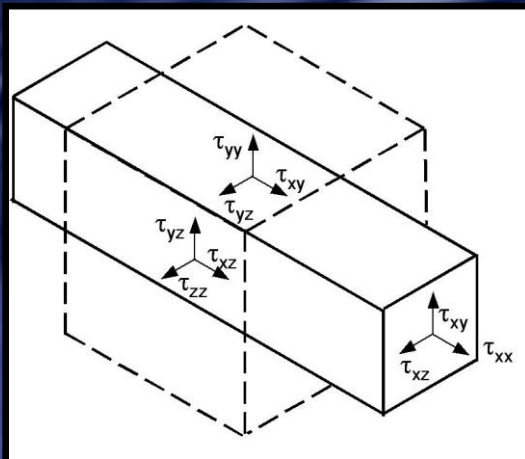


Shear Viscosity

$$\eta = \frac{\tau_{xy}}{\dot{\gamma}_{xy}}$$

$$\dot{\gamma}_{xy} = \frac{dv_x}{dy}$$

Elongational flow:



Elongational Viscosity

$$\eta_e = \frac{\tau_{xx} - \tau_{yy}}{\dot{\epsilon}_{xx}}$$

$$\dot{\epsilon}_{xx} = \frac{dv_x}{dx}$$

$$\eta_e = T\eta$$

$$T = 3 \text{ (Newtonian)}$$

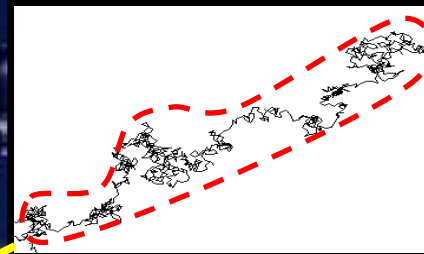
$$\text{(Trouton, 1906)} \quad T \approx 10^3 \text{ (non-Newtonian)}$$

Coil-stretch transition (De Gennes, 1974)



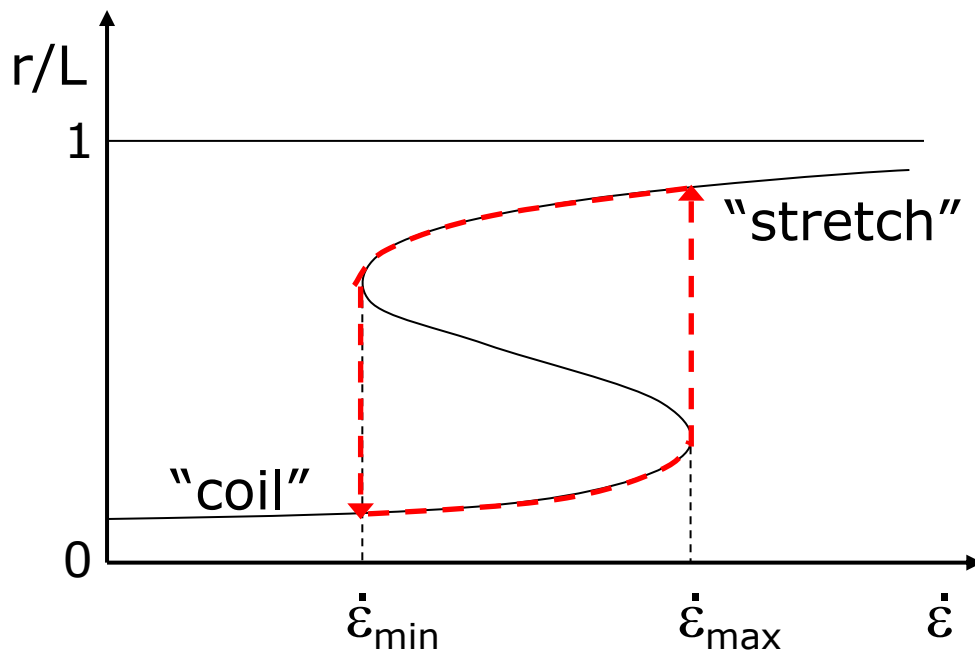
Hydrodynamic interaction with external monomers only

Coil



Hydrodynamic interaction with all monomers

Stretch

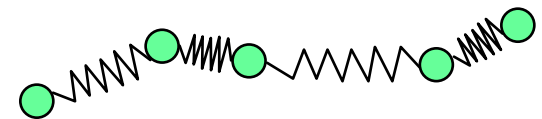


$$\dot{\epsilon}_{\max} \approx \frac{1}{\tau_{\text{Zimm}}} \approx \frac{k_B T}{\eta_s R^3}$$

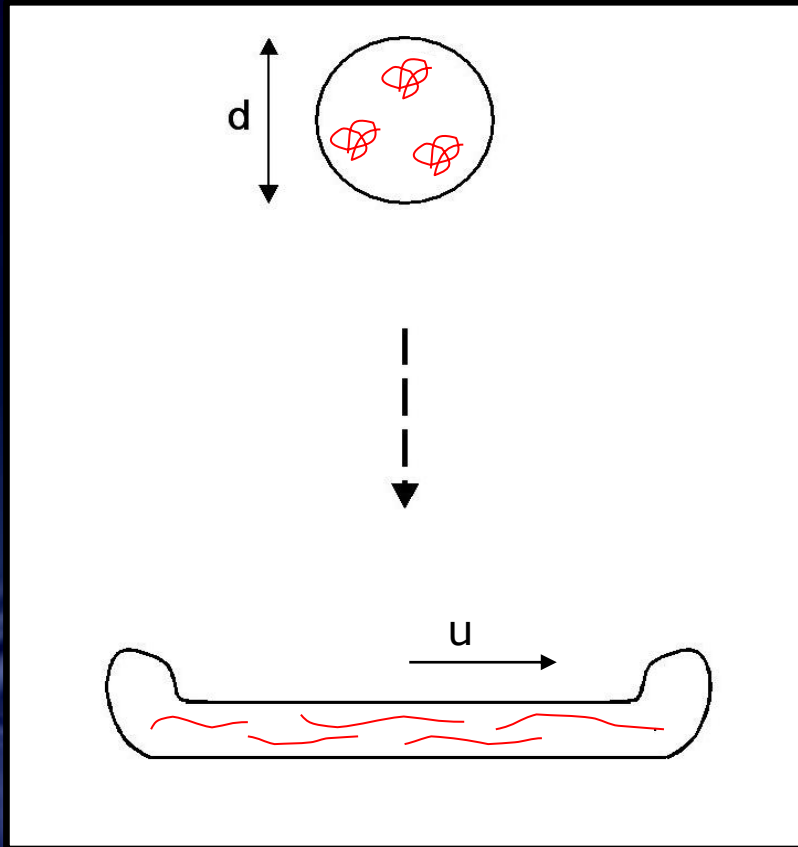
(hard sphere)

$$\dot{\epsilon}_{\min} \approx \frac{1}{\tau_{\text{Rouse}}} \approx \frac{k_B T}{\xi R^2}$$

(spring-bead)



Anti-rebound phenomenon

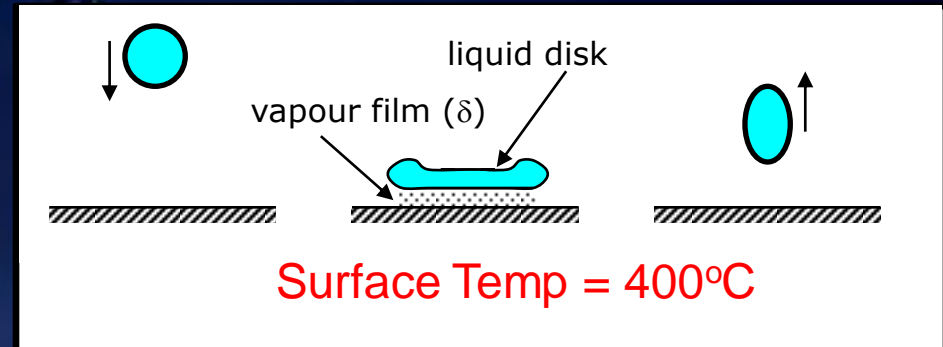
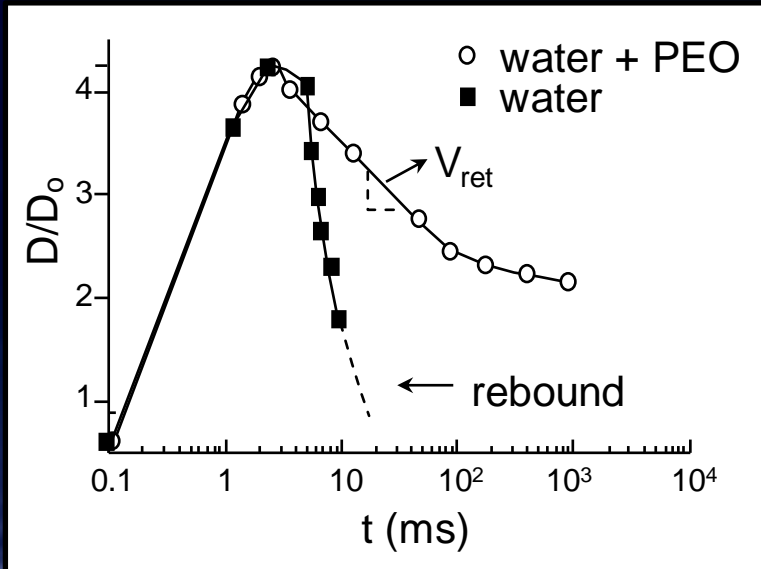


Proposed mechanism:

- Inertia causes drop to spread
- Polymers stretch in the fluid's velocity gradient
- Leads to increased extensional Viscosity
- Sufficient energy dissipated to prevent rebound

Dissipation of mechanical energy during expansion and retraction
(Bergeron, 2003)

Problems with proposed mechanism



- The polymer does NOT change the maximum spreading diameter
- Only retraction of drop is affected

Interfacial effects are important

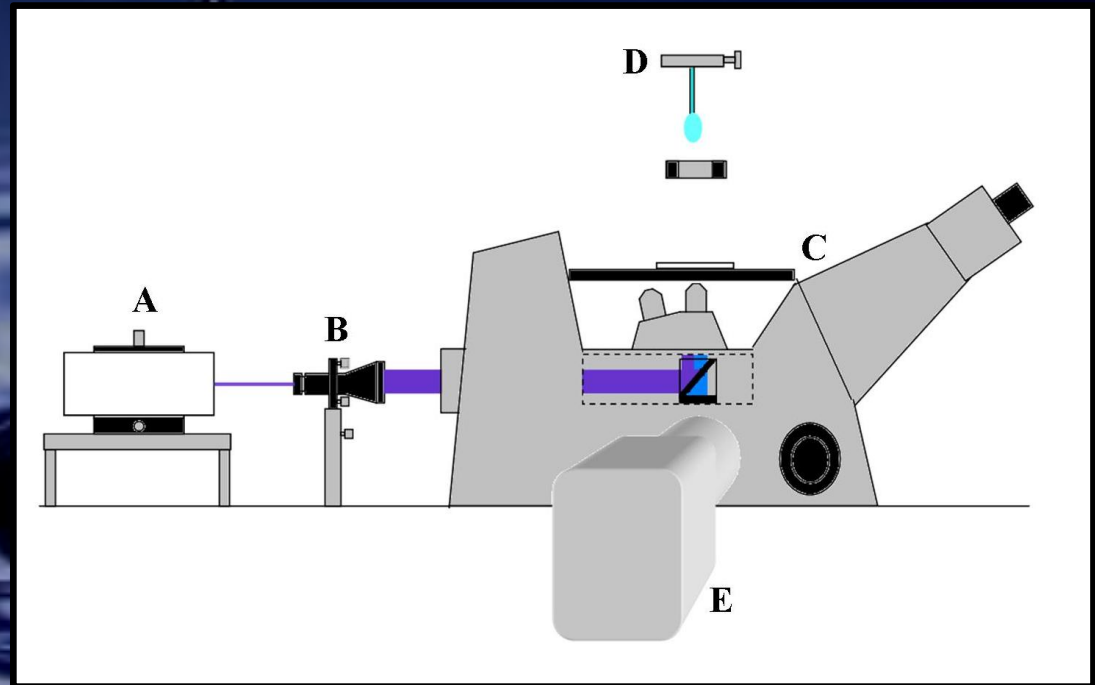
A high-speed photograph of a water droplet falling into a pool of water. The droplet is captured mid-fall, just above the point of impact. Below it, a series of concentric ripples spread outwards from the center. The water is a deep blue color, and the background is a solid, slightly darker blue. The lighting is soft, highlighting the droplet and the ripples.

***Is elongational viscosity responsible for
the anti-rebound phenomenon?***

Particle Imaging Velocimetry

Map fluid velocity profile in the impacting drop

- Fluid contains $2\mu\text{m}$ fluorescent particles ($<0.001\text{wt}\%$)
- Drop illuminated with pulsed UV laser (A), frequency $\sim 8\text{kHz}$
- High speed camera (E) with image intensifier views flow inside drop through a $\times 40$ microscope objective (2000fps)
- Movies captured at different radial positions in the spreading drop

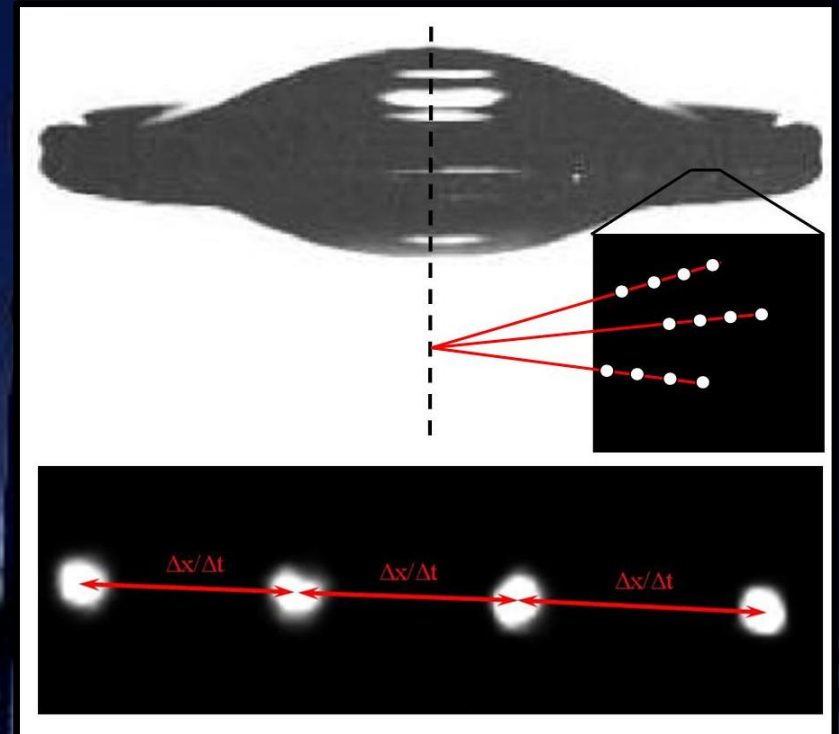


Smith, M.I. Bertola, V., Expts Fluids, (2010)

"Particle Velocimetry inside Newtonian and non-Newtonian droplets impacting a hydrophobic surface"

Measuring fluid velocity with fluorescent colloids

- Particles travel radially during spreading
- Each colloid exposed 4x in each frame



Intersection of particle paths enables radial distance to be measured.

$$\text{Fluid Velocity} = \Delta x \cdot f_{\text{Laser}}$$

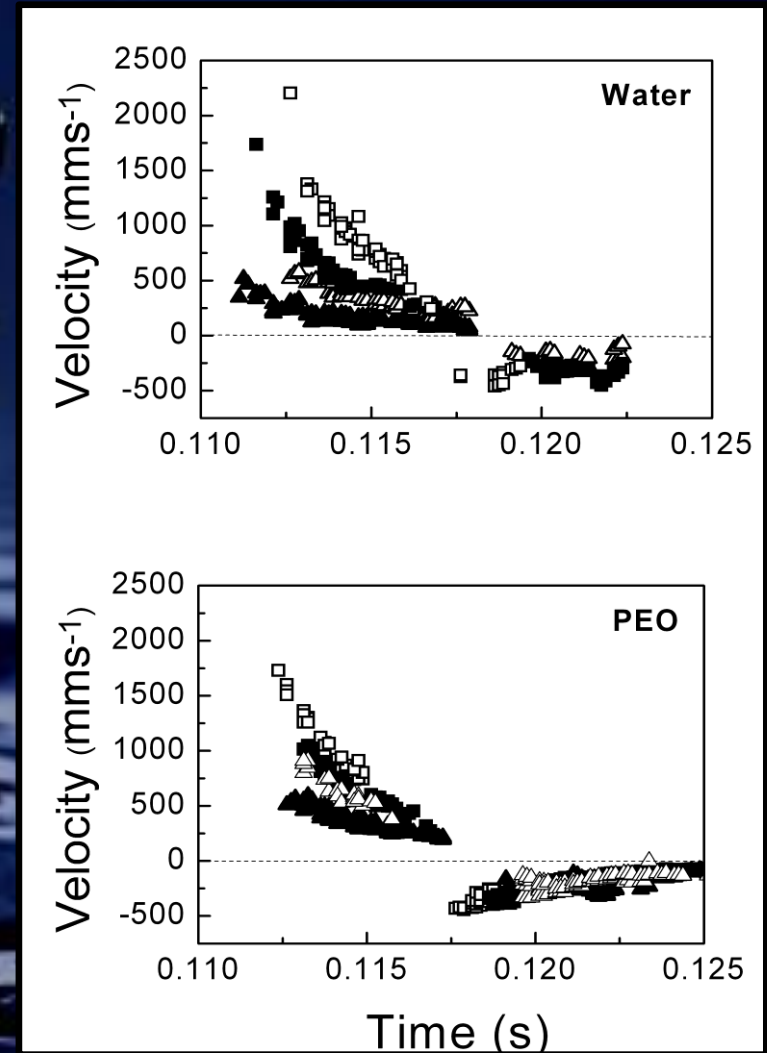
Particle Image Velocimetry

Fluid velocity as a function of time
at different radial positions

Drop spreads faster at the edge

Spreading slows as interfacial
energy increases

**Estimate initial retraction
velocity of the fluid in the drop
at different radial positions**



Smith, M.I., Bertola, V., Phys Rev Letts, 104 (2010) 154502
“Effect of Polymer Additives on the Wetting of Impacting Drops”

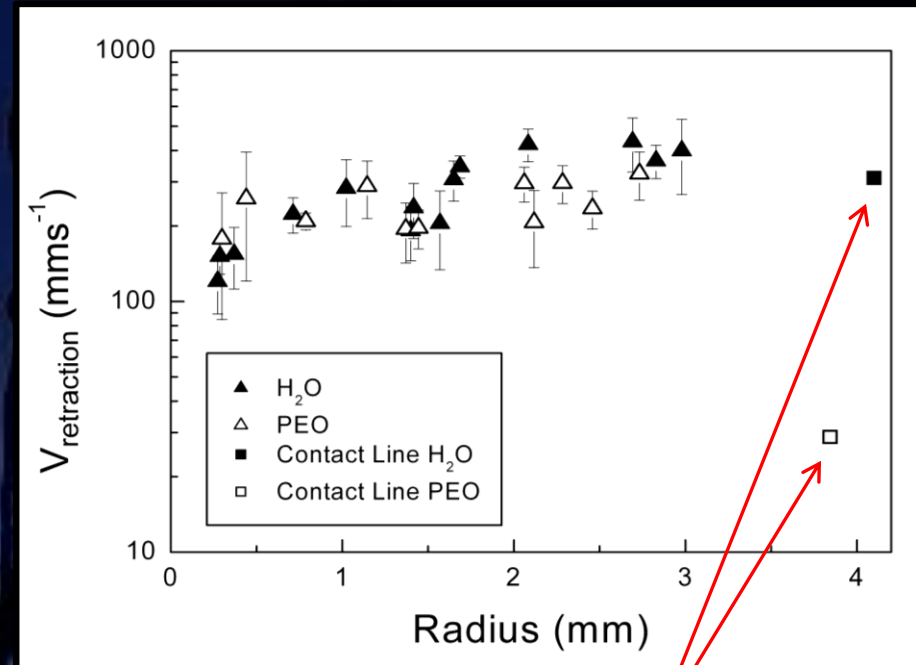
Retraction Velocity

- Retraction velocities are similar in the bulk of the drop

- Retraction Velocity is controlled by surface tension and viscosity

- Both drops have similar elongational viscosity

- Elongational viscosity is not responsible for anti-rebound effect



Comparison with drop edge suggests anti-rebound phenomenon is a contact line effect

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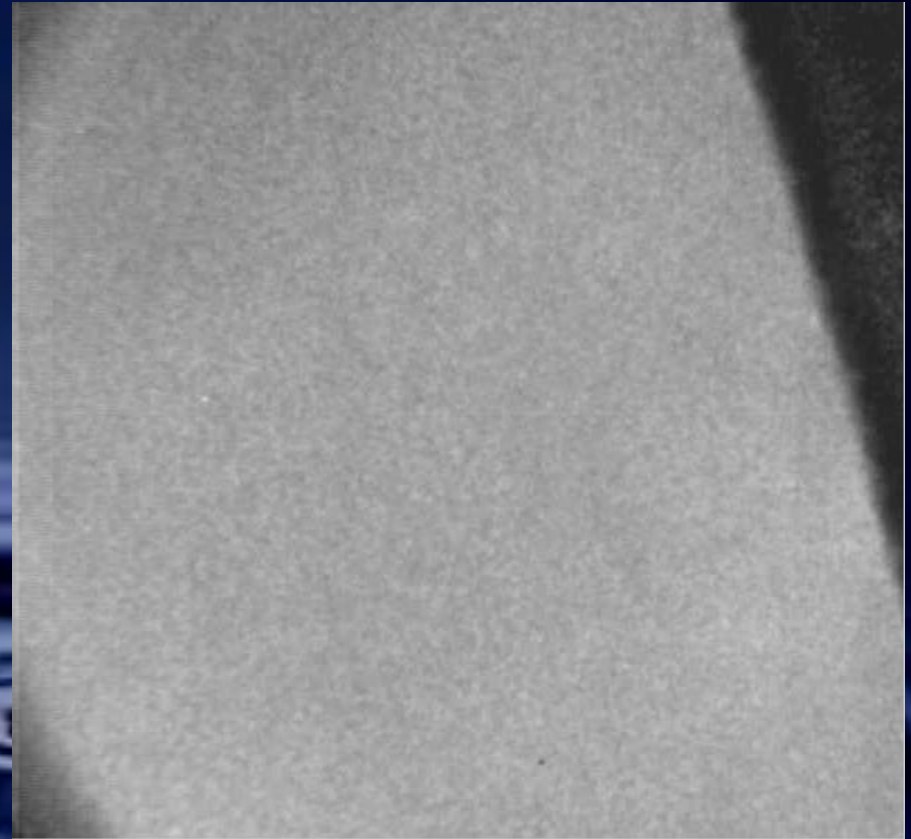
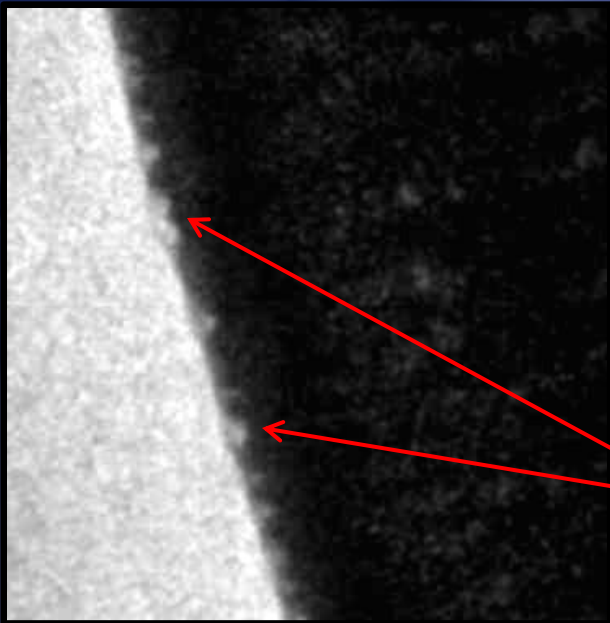
“Particle Velocimetry inside Newtonian and non-Newtonian droplets impacting a surface”

A high-speed photograph of a water droplet falling into a pool of water. The droplet is captured mid-fall, just above the point of impact. Below it, a vertical column of water rises from the point of contact. Concentric ripples spread outwards from the center. The background is a deep, uniform blue.

Visualising the contact line with DNA

Direct Visualisation of contact line with DNA

- Prepare 200ppm PEO solution
- Add 0.2ppm fluorescently stained λ -DNA
- Using a continuous wave laser and 20mm drop height



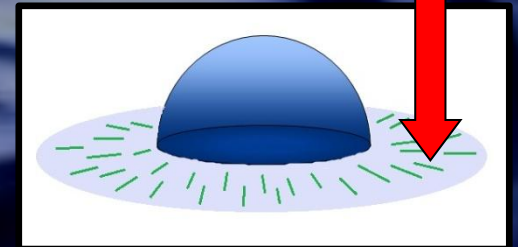
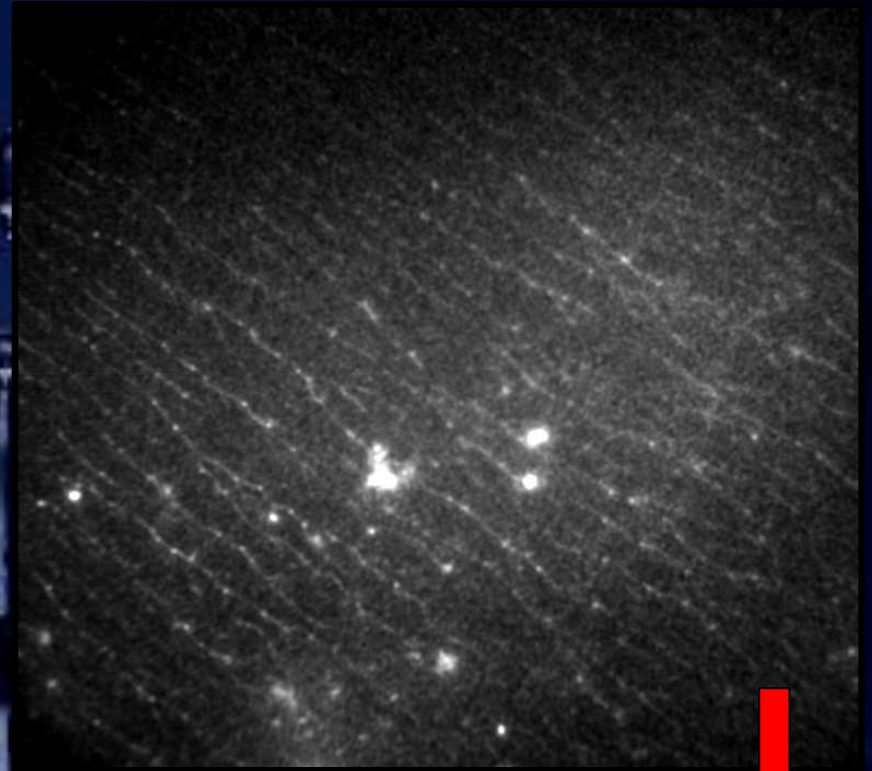
DNA stretching at contact line as drop edge recedes

"Molecular Combing"

- Retracting drop leaves molecules stretched out on substrate
- Molecules are aligned radially, lying end to end

What causes the anti-rebound effect?

→ Molecules Interact with the substrate, dissipating energy at the contact line



Smith, M.I., Bertola, V., Phys Rev Letts, 104 (2010) 154502
"Effect of Polymer Additives on the Wetting of Impacting Drops"

Conclusions

- Extensional viscosity cannot be responsible for suppressing droplet rebound
- Anti-rebound phenomenon is a contact line effect
- Stretching of polymers at the contact line by the receding drop edge prevents rebound

Acknowledgements

- Dr Volfango Bertola
- Dr Cristina Flors

- Smith, M.I., Bertola, V., Phys Rev Letts, 104 (2010) 154502
“Effect of Polymer Additives on the Wetting of Impacting Drops”
- Smith, M.I. Bertola, V., Expts Fluids, 50 (2010) 1385
“Particle Velocimetry inside Newtonian and non-Newtonian droplets impacting a hydrophobic surface”

