

# Assignment\_1

August 28, 2023

## 1 Answer 1

(a) 1 refers to model under hypothesis  $H_0 : \mu_j = \mu$

A refers to the model under alternative hypothesis against  $H_0$

$$\begin{aligned} & P(\theta_A)P(\theta_B) \\ &= P_{\theta}(\theta_A) \int_0^{\infty} \frac{1}{\theta} P_{\gamma}\left(\frac{\theta_B}{\theta}\right) P_{\theta}(\theta) d\theta \end{aligned}$$

(b) The mean residual sum of squares

$$\mathbf{MS}(res|A) = \int [SS_{tot} - SS(A|1)] / (n - g) \neq \quad (1)$$

$$(2)$$

$$\alpha = (41.7 - 23.9) / (17 + 1 - 3) = 1.1867 \quad (3)$$

[ ]: (41.7-23.9)/15

1.186666666666667

(c) the interactionn freedom terms between A and B is  $5 \cdot 14 - 14 - 5 + 1 = 52$

(d) No, we can't get an unbiased estimate. Under  $H_0$  or  $H_1$  we may not get an unbiased estimate of  $\sigma^2$ , because the  $SS_{tot}$  and its freedom are unknown which help us get  $MS(res|A)$ .

(e)

$$\mu = \sum_{i=0}^{\infty} y(y+1)(1-p^2)p^y = (1-p)^2 \left[ \frac{1}{(1-p)^2} - 1 \right]' = \frac{2}{1-p}$$

$$E(Y^2) = \sum_{i=0}^{\infty} y^2(y+1)(1-p^2)p^y = \sum_{i=0}^{\infty} (y-1)y(y+1)(1-p^2)p^y + \mu = (1-p)^2 \left[ \frac{1}{(1-p)^2} - 1 - 2p \right]'' = \frac{6}{(1-p)^2} = \frac{3}{2}\mu$$

$$V(\mu) = E(Y - \mu)^2 = E(Y^2) - \mu^2 = \frac{1}{2}\mu^2$$

the variance function  $V(\mu) = \frac{1}{2}\mu^2$

$$f(y|p) = \exp\{y \ln p + 2 \ln(1-p) + \ln(y+1)\}$$

canonical link function :  $\ln p$

inverse function:  $e^p$

## 2 Answer 2

(a) Apply a T test on co-efficient on V63

$$|t| = \frac{1508.4 - 0}{988.6} = 1.526 < t_{396, \frac{\alpha}{2}}$$

or

$$Pr(|t| > 1.526) = 0.128 < 0.05 = \alpha$$

Conclusion: do not reject  $H_0 : \alpha_{southwest} = 0$

(b)

$$F = \frac{MS(A|1)}{MS(res|A)} = \frac{\frac{3.156 \cdot 10^{10}}{1}}{\frac{2.044 \cdot 10^{10}}{398}} = 614.52 > F_{(1,398), \frac{\alpha}{2}} = 3.8649$$

$$Pr(> F) = 0$$

Conclusion: The V5 is a significant variable which affect value of V7.

```
[ ]: F<-3.156/2.044*398
print(c(F,qf(0.95,1,398),1-pf(F,1,398)))
```

```
[1] 614.524462 3.864929 0.000000
```

(c)  $H_0$  refers to that Co-efficients of V5\*V6 which refers to Co-efficients of V5 ,V6(V61,V62,V63) and V5:V6((V61,V62,V63) are 0 .

p<0.05 means to reject  $H_0$  and accept the alternativ model which is an oringial one with V5\*V6.

(d)  $H_0$ :the co-efficient of V2:V3 is 0

p>0.05 accept  $H_0$  means that V2:V3 may not have obvious effect the V7

(e) The RMS predictions errors are 17040.241,9827.318,6262.788 . The results show that (d) perform best.

```
[ ]: B<-matrix(c(1,1,1,1,52,28,56,52,1,2,2,1,30.9,25.9,31.8,31.
  ↪2,0,1,2,0,0,0,1,0,1,2,3,4),nrow=4,ncol=7)
V7<-c(23046,4134,43814,9626)
Model1<-matrix(c(12641,0,0,0,0,0,0),nrow=7)
Model2<-matrix(c(8444.314,0,0,0,0,22995.509,0),nrow=7)
Model5<-matrix(c(-10078.41,244.15,0,305.34,0,19279.05,0,5808.30,6040.71,5192.
  ↪95),nrow=10)
B5int<-t(B[,6]*matrix(c(0,1,0,0,0,0,1,0,0,0,0,1),nrow=3,ncol=4))
B5<-cbind(B[,c(1,2,3,4,5,6,7)],B5int)
RMS_1<-sqrt(sum((V7-B%*%Model1)^2)/4)
RMS_2<-sqrt(sum((V7-B%*%Model2)^2)/4)
RMS_5<-sqrt(sum((V7-B5%*%Model5)^2)/4)
print(c(RMS_1,RMS_2,RMS_5))
```

```
[1] 17040.241 9827.318 6262.788
```

```
[ ]: B[1,]  
B5
```

```
1. 1 2. 52 3. 1 4. 30.9 5. 0 6. 0 7. 1
```

```
1 52 1 30.9 0 0 1 0 0 0  
A matrix: 4 x 10 of type dbl 1 28 2 25.9 1 0 2 0 0 0  
1 56 2 31.8 2 1 3 1 0 0  
1 52 1 31.2 0 0 4 0 0 0
```