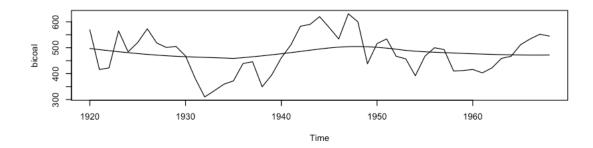
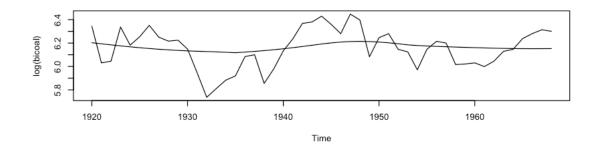
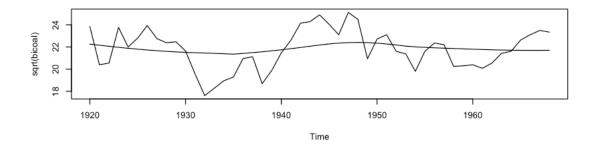
my_notebook

October 22, 2023

Let's first take a look at the time series. The series are annual production in millions of net tons of bitumous coal between 1920 and 1968. The annual data may suggest no seasonal effect. Then we take a look at the scatterplot of the time series. After applying some log or square root transformation, we may see almost the same pattern. Besides, after adding a scatterplot lowess to each graphics, we may see little linear trend from the 3 graphics below. It seems that the data shows a periodic effect. However, the period seems to be so long which might be around 30 years and it was really flat compared to the raw data. So we may view it as no trend is shown in this data.



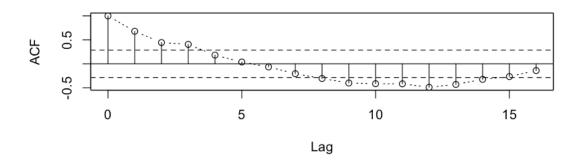




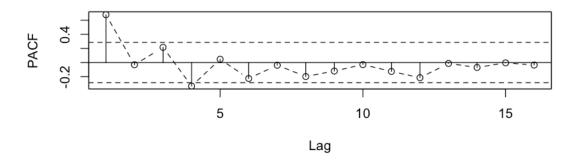
We may also want to know if the data show some dependence between each other and apply an ARMA model to the time series. Firstly, we need to check the acf and pacf of the data. From the plot below ,it strongly suggest the process are not stationary . Then we may consider applying a differenceing on the data to get stationary process.

Box-Jenkins ARMA Model Identification

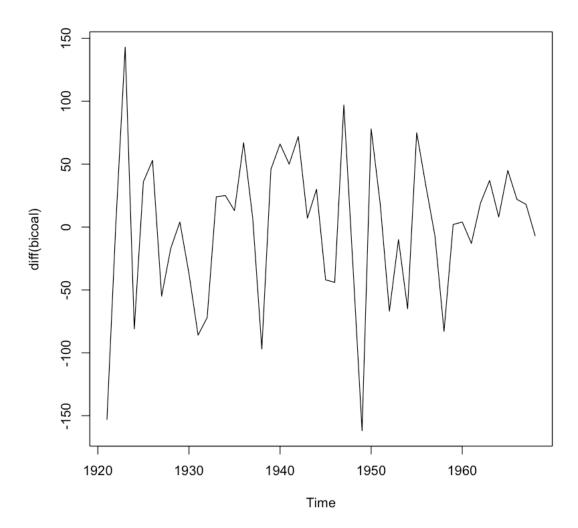
Autocorrelation Function



Partial Autocorrelation Function

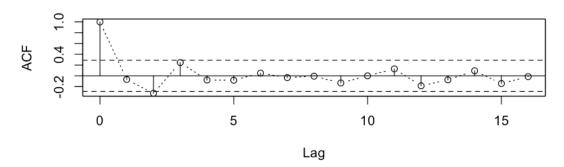


After differencing the data, we do see that acf and pacf shows a stationary process and also suggest us apply an AR(2) model to the differencing data.

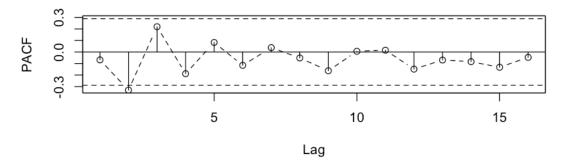


Box-Jenkins ARMA Model Identification

Autocorrelation Function



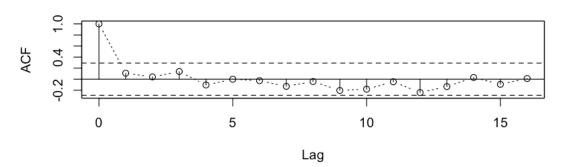
Partial Autocorrelation Function



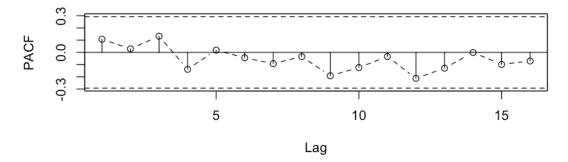
Considering an AR(2) model , the residuals of the model shows the model perform well.

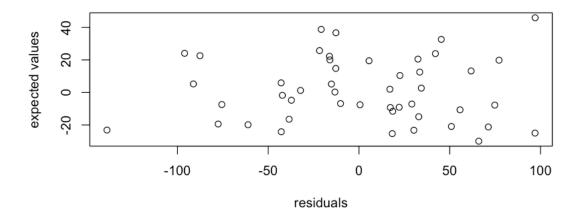
Box-Jenkins ARMA Model Identification

Autocorrelation Function



Partial Autocorrelation Function





Normal Q-Q Plot

