THE UNIVERSITY OF MELBOURNE ENGR30002 Fluid Mechanics

Workshop 04 – Fanning friction factor

Part A

Question 01

What is the value of x at the end of execution of the following MATLAB scripts? Trace through each script by hand before checking your result in MATLAB.

- (1) x=1;for i=1:5 x = x*i;end
- (2) n=17; x=0;while (n > 1) n = n/2; x = x + 1;end

Question 02

Leibniz discovered that π can be approximated using the formula

$$\frac{\pi}{4} = \sum_{k=0}^{\infty} \frac{(-1)^k}{(2k+1)^k}$$

This is called a sum of a series. For example, the first six terms of the series are

$$\pi = \frac{4}{1} - \frac{4}{3} + \frac{4}{5} - \frac{4}{7} + \frac{4}{9} - \frac{4}{11} + \cdots$$

Write a MATLAB function $Pi_Approx1(n)$ that returns the approximation of π using the first n terms of the Leibniz series above.

Part B

Question 01

First, write a function that takes three inputs (Re, ϵ , D) using the following numerical expressions for estimating fanning fraction factors and return one output, f_F .

$$f_F = \begin{cases} \frac{\frac{16}{Re} & \text{for } Re < 2100}{Re} \\ \{-1.737 \ln[0.0269 \frac{\epsilon}{D} - \frac{2.185}{Re} \ln(0.269 \frac{\epsilon}{D} + \frac{14.5}{Re})]\}^{-2} & \text{for } Re > 2100 \end{cases}$$

Next, call that function into a new m-script and plot the Fanning fraction factors using for three values of roughness ratio ($\frac{\epsilon}{D} = 0.000001, 0.001, and 0.05$). Set a range of Re, $100 \sim 2000$ for laminar flow and $2300 \sim 10^7$ for turbulent flow.

Question 02

Water at 15°C is flowing in a 30-m-long horizontal pipe made of stainless steel. If it flows at a rate of 9 litre/s, what is an effect of the pipe diameter on the pressure drop? Vary the pipe diameter from 1 to 10 cm in increments of 1 cm. Plot a graph of ΔP (kPa) vs diameter (m).

END OF WORKSHOP