

Assessment_4_STA5001_Michael_Le_21689299

2024-04-30

#Question 1. #Simulate a realization of the inhomogeneous Poisson process at $[0,5] \times [0,5]$ that exhibits all of the following properties:

#(a).points form one group;

#(b).the center of the group has a random location;

#(c).all the points of this group have an x coordinate that is within a distance of 1 from the x coordinate of the group's center;

#y-coordinates of the points in this group uniformly take on all possible values within the range of $[0,5]$.

#Repeat simulations twice and produce two plots of simulated points.

```
library(spatstat)
## Warning: package 'spatstat' was built under R version 4.3.3
## Loading required package: spatstat.data
## Warning: package 'spatstat.data' was built under R version 4.3.3
## Loading required package: spatstat.geom
## Warning: package 'spatstat.geom' was built under R version 4.3.3
## spatstat.geom 3.2-9
## Loading required package: spatstat.random
## Warning: package 'spatstat.random' was built under R version 4.3.3
## spatstat.random 3.2-3
## Loading required package: spatstat.explore
## Warning: package 'spatstat.explore' was built under R version 4.3.3
## Loading required package: nlme
## spatstat.explore 3.2-6
## Loading required package: spatstat.model
## Warning: package 'spatstat.model' was built under R version 4.3.3
## Loading required package: rpart
```

```

## spatstat.model 3.2-10
## Loading required package: spatstat.linnet
## Warning: package 'spatstat.linnet' was built under R version 4.3.3
## spatstat.linnet 3.1-4
##
## spatstat 3.0-7
## For an introduction to spatstat, type 'beginner'

par(mfrow=c(1,2))

#First simulation

a<-runif(4,min = 0, max = 5)

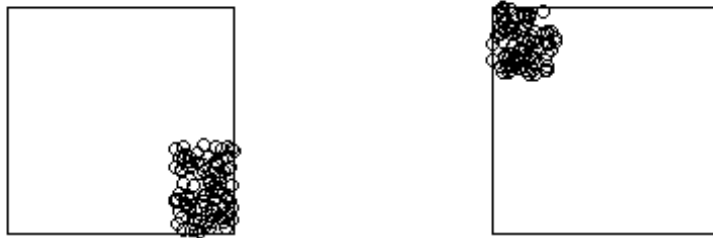
lambda1 <- function(x, y) {50*as.numeric((abs(x -a[1])<1) & (abs(y -
a[2])<1))}
plot(rpoispp(lambda1, win=owin(c(0,5),c(0,5))))

#Second simulation with two plots of simulated points
a<-runif(4,min = 0, max = 5)

lambda1 <- function(x, y) {50*as.numeric((abs(x -a[1])<1) & (abs(y -
a[2])<1))}
plot(rpoispp(lambda1, win=owin(c(0,5),c(0,5))))

```

`p(lambda1, win = owin(c(0,p(lambda1, win = owin(c(0,`

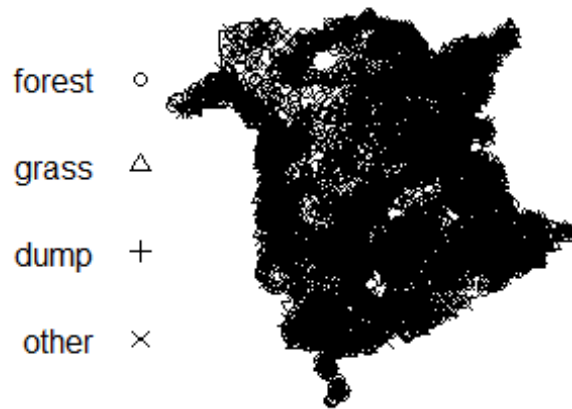


#Question 2.

```
mydata <- unmark(nbfires)
marks(mydata) <- nbfires$marks$fire.type

#Plot the data
plot(mydata)
```

mydata



#Assume stationary. What is the value of the estimated constant intensity?

```
summary(mydata)$intensity
```

```
## [1] 0.01572195
```

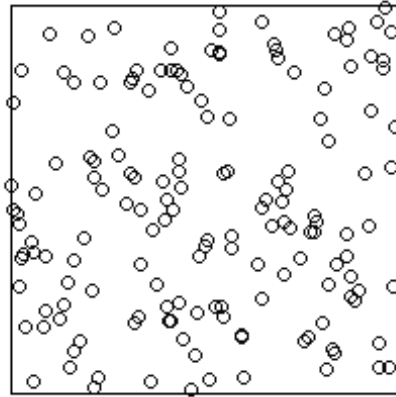
```
#0.01572195
```

#Simulate and plot a Poisson process with the estimated constant intensity multiplied by 10000.

```
lambda<-rpoispp(10000*summary(mydata)$intensity)
```

```
plot(lambda)
```

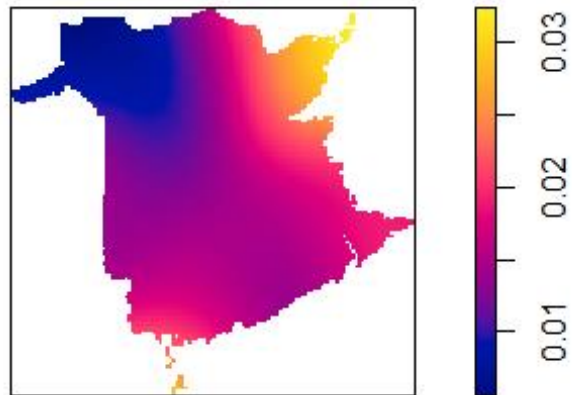
lambda



#Estimate and plot non-constant intensity.

```
den<-density(mydata)  
plot(den)
```

den

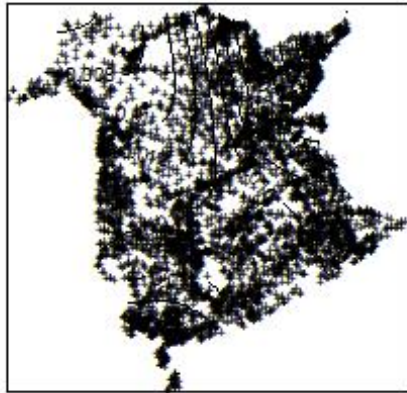


#Plot the data points and a contour plot for the estimated non-constant intensity in the same figure

```
contour(den)
```

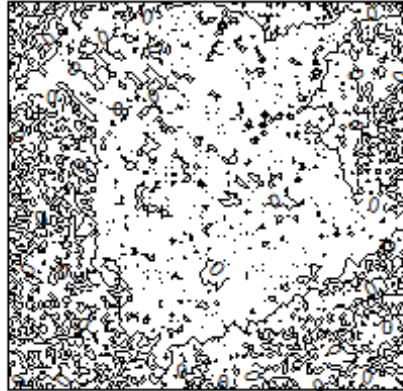
```
points(mydata, cex = 0.5, pch = "+")
```

den



```
#Alternative solution,  
x<-mydata$x  
y<-mydata$y  
myppp<- ppp(mydata$x,mydata$y,c(13.19402,988.46830),c(5.489932,956.133395))  
  
## Warning: 2 points were rejected as lying outside the specified window  
## Warning: data contain duplicated points  
  
den <- density(myppp, sigma = 1)  
contour(den)
```

den



#Use quadrat counts to investigate the intensity. Plot the data points and quadrat counts in the same figure.

```
quadratcount(myppp, nx = 6, ny = 3)
```

```
##           x
## y      [13.2,176) [176,338) [338,501) [501,663) [663,826) [826,988]
## [639,956]         90      341      300      1142      825      31
## [322,639)         0      568      711      740      856      286
## [5.49,322)         0      159      647      336      73       1
```

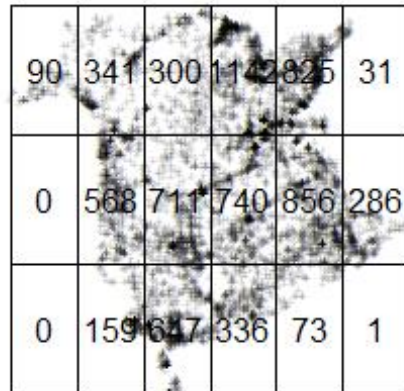
```
Q <- quadratcount(myppp, nx = 6, ny = 3)
```

```
plot(myppp, cex = 0.5, pch = "+")
```

```
## Warning in plot.ppp(myppp, cex = 0.5, pch = "+"): 2 illegal points also plotted
```

```
plot(Q, add = TRUE, cex = 1)
```


myppp



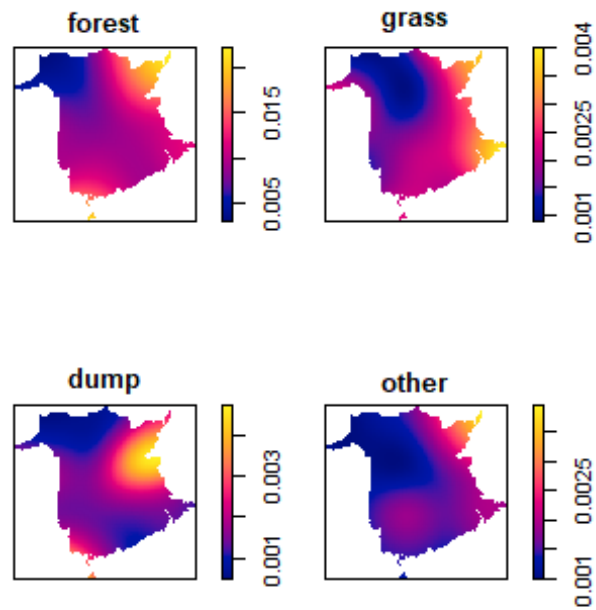
90	341	300	114	2825	31
0	568	711	740	856	286
0	159	647	336	73	1

#Elaborate on the conclusions drawn from the previous questions:

#Explanation: #After computing all the results from above, #we find out the intensity of the estimated constant density is 0.01572195. After plotting ipp, where the intensity can vary over space as a function of the position. Conclude that the intensity may be non-stationary. Which corresponds intensity measure values in each subregion.

```
#Separate the data into the sub-patterns of points by types  
#and plot their intensities.  
mydata <- unmark(nbfires)  
marks(mydata) <- nbfires$marks$fire.type  
plot(density(split(mydata),cex = 0.05))
```

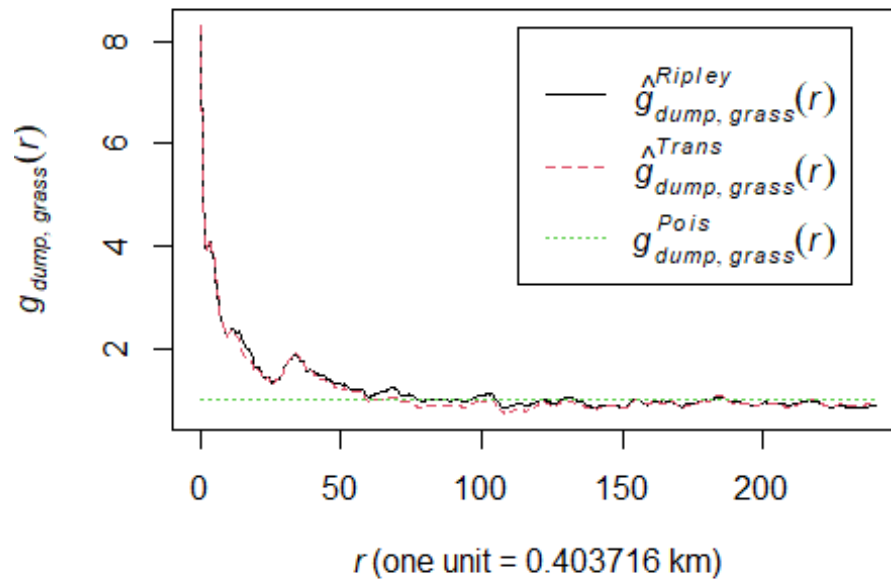
```
ensity(split(mydata), cex = 0.0
```



*#Plot the cross-type pair correlation function for "dump" and "grass" marks.
Interpret the plot.*

```
p <- pcfcross(mydata, "dump", "grass")  
plot(p)
```

p

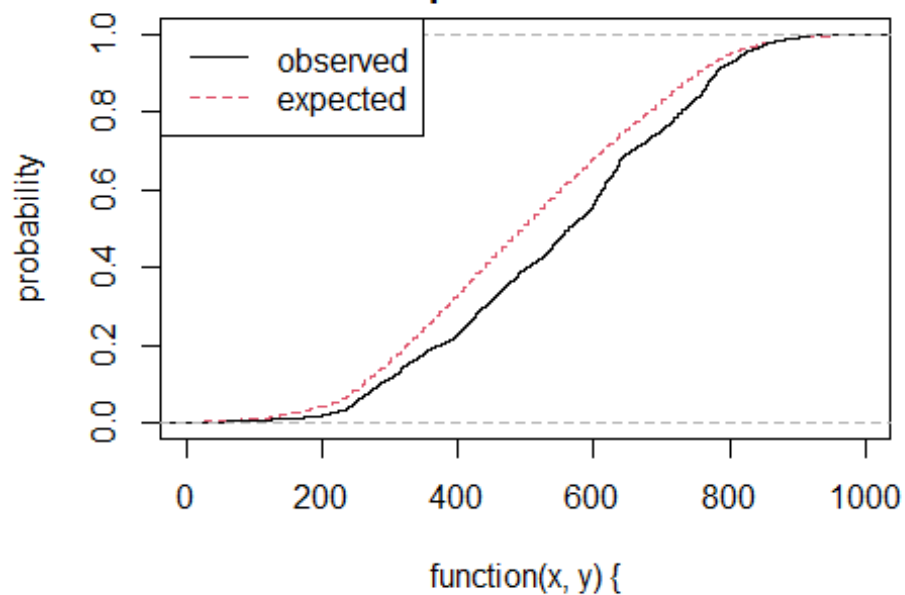


#The plot suggest that there is a inhibition between dump and grass at all scales except very small distances.

#Remove the marks from the point pattern and perform the spatial Kolmogorov-Smirnov test for the uniform distribution of the x coordinate.

```
KS <- cdf.test(mydata, function(x, y) {x})  
plot(KS)
```

patial Kolmogorov-Smirnov test of CSR in two dimen
 based on distribution of covariate "function(x, y) {
 p-value= 0



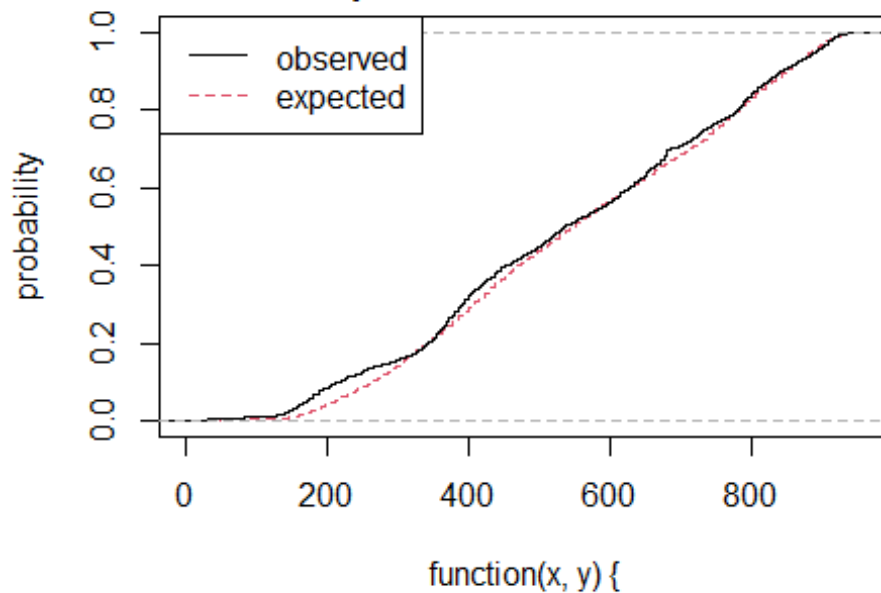
```
pval <- KS$p.value
pval

## [1] 0

#Perform the spatial Kolmogorov-Smirnov test for the uniform distribution of
the y coordinate.

KS <- cdf.test(mydata, function(x, y) {y})
plot(KS)
```

patial Kolmogorov-Smirnov test of CSR in two dimen
based on distribution of covariate "function(x, y) {"
p-value= 2.487e-14



```
pval <- KS$p.value
pval
## [1] 2.4869e-14
```

#Explanation: For the homogenous Poisson process assuming the intensity is constant,
#The p-value for the x-value is 0. Thus, the test does reject the #hypothesis of CSR. The plot
demonstrates functions for the observation and expected distribution functions that
confirms it. Similarly for the y-value, the p-value is 3.22e-14. We reject the hypothesis of
CSR as well, we can conclude that this pattern is completely spatially random.

#Question 3a.

```
library(spatstat)
library(lubridate)

## Warning: package 'lubridate' was built under R version 4.3.3

##
## Attaching package: 'lubridate'

## The following objects are masked from 'package:base':
##
##     date, intersect, setdiff, union

library(stpp)

## Warning: package 'stpp' was built under R version 4.3.3
```

```

## Loading required package: rpanel
## Warning: package 'rpanel' was built under R version 4.3.3
## Loading required package: tcltk
## Package `rpanel', version 1.1-5: type help(rpanel) for summary information
## Loading required package: splancs
## Warning: package 'splancs' was built under R version 4.3.3
## Loading required package: sp
## Warning: package 'sp' was built under R version 4.3.3

##
## Spatial Point Pattern Analysis Code in S-Plus
##
## Version 2 - Spatial and Space-Time analysis

data(nbfires)
str(nbfires)

## List of 6
## $ window :List of 5
## ..$ type : chr "polygonal"
## ..$ xrange: num [1:2] 0 1000
## ..$ yrange: num [1:2] 0 959
## ..$ bdry :List of 6
## .. ..$ :List of 2
## .. .. ..$ x: num [1:500] 412 415 415 416 419 ...
## .. .. ..$ y: num [1:500] 123 124 124 123 122 ...
## .. ..$ :List of 2
## .. .. ..$ x: num [1:54] 835 834 836 837 838 ...
## .. .. ..$ y: num [1:54] 910 912 913 914 916 ...
## .. ..$ :List of 2
## .. .. ..$ x: num [1:92] 823 826 828 828 833 ...
## .. .. ..$ y: num [1:92] 865 867 869 869 874 ...
## .. ..$ :List of 2
## .. .. ..$ x: num [1:79] 385 384 384 385 387 ...
## .. .. ..$ y: num [1:79] 90.4 91.7 91.8 93.7 95.9 ...
## .. ..$ :List of 2
## .. .. ..$ x: num [1:66] 395 395 396 397 395 ...
## .. .. ..$ y: num [1:66] 64.8 64.8 65.9 67.9 70.3 ...
## .. ..$ :List of 2
## .. .. ..$ x: num [1:80] 403 404 407 409 411 ...
## .. .. ..$ y: num [1:80] 0.417 3.753 6.103 9.212 13.578 ...
## ..$ units :List of 3
## .. ..$ singular : chr "km"
## .. ..$ plural : chr "km"
## .. ..$ multiplier: num 0.404

```

```

## .. - attr(*, "class")= chr "unitname"
## .. - attr(*, "class")= chr "owin"
## $ n      : int 7108
## $ x      : num [1:7108] 762 654 633 598 639 ...
## $ y      : num [1:7108] 778 671 625 648 611 ...
## $ markformat: chr "dataframe"
## $ marks   : 'data.frame': 7108 obs. of 9 variables:
## ..$ year      : Factor w/ 16 levels "1987","1989",...: 13 13 13 13 13 13
13 13 13 13 ...
## ..$ fire.type : Factor w/ 4 levels "forest","grass",...: 1 1 2 1 2 1 1 1
2 1 ...
## ..$ dis.date  : POSIXct[1:7108], format: "2000-05-04 19:15:00" "2000-04-
18 14:00:00" ...
## ..$ dis.julian: num [1:7108] 125 109 124 124 110 ...
## ..$ out.date  : POSIXct[1:7108], format: "2000-05-05 12:00:00" "2000-04-
18 19:00:00" ...
## ..$ out.julian: num [1:7108] 125 109 124 124 110 ...
## ..$ cause     : Factor w/ 9 levels "unknown","rrds",...: 8 3 8 1 1 8 6 6
6 8 ...
## ..$ ign.src   : Factor w/ 16 levels "unknown","cigs",...: 4 2 3 1 1 5 1 1
1 6 ...
## ..$ fnl.size  : num [1:7108] 1.6 7 1 0.1 0.5 2 0.5 1.5 0.5 1.2 ...
## - attr(*, "class")= chr "ppp"

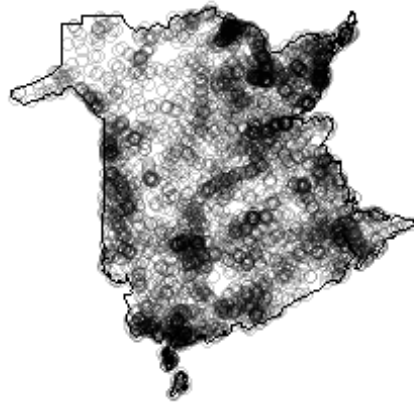
mydata <- nbfires$marks$fire.type == "forest"
mydata <- unmark(mydata)

#mydata <- unmark(nbfires)
#marks(mydata) <- nbfires$marks$fire.type

#Plot the data
plot(mydata)

```

mydata

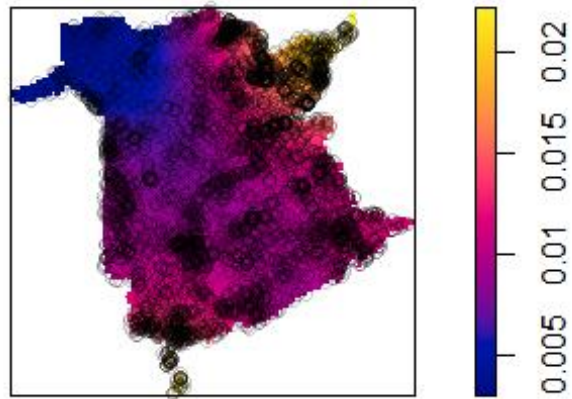


#Explanation: The dataset gives 4627 positions containing forest type fire #in a 1000 by 958.9142 meter rectangular sampling region in the Brunswick forest #fires that is occurring for the years between 1987 and 2003. Where many occurred from while there is a less on the top-left corner.

#Produce density plots.

```
plot(density(mydata))  
plot(mydata, add=TRUE, cex=1)
```

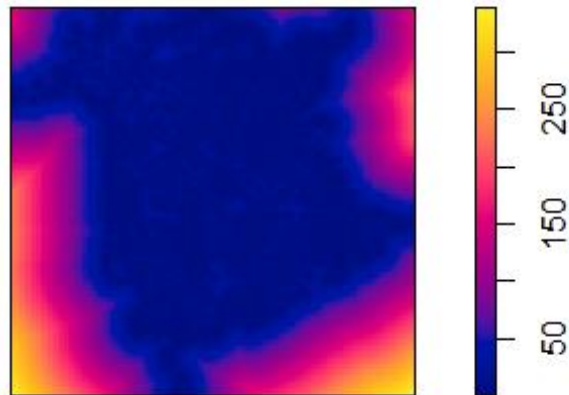

density(mydata)



#Plot the image of empty space distances for the locations of fires.

```
emp <- distmap(mydata)
plot(emp, main = "Empty space distances")
```

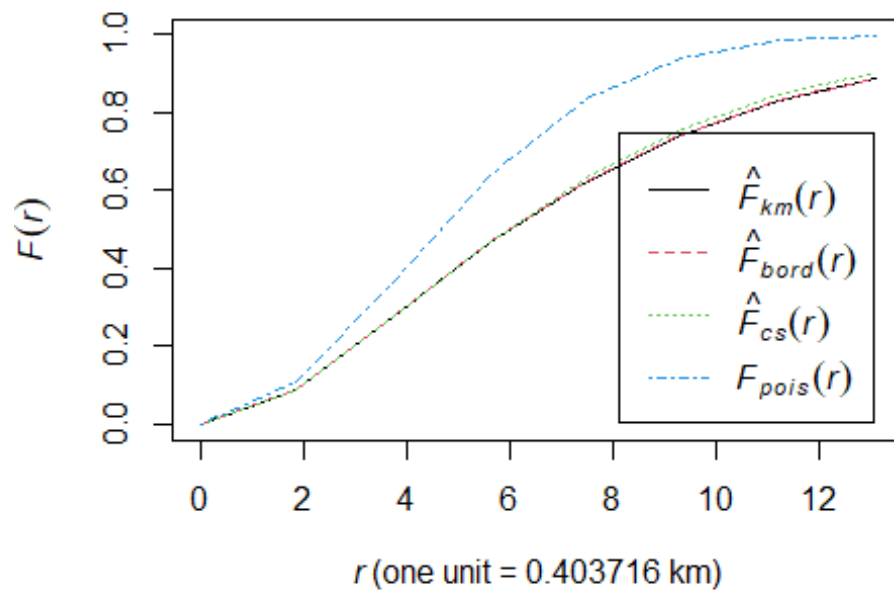
Empty space distances



#Compute and plot the F function for the locations of forest fires. Explain what kind of pattern for this data the function suggests.

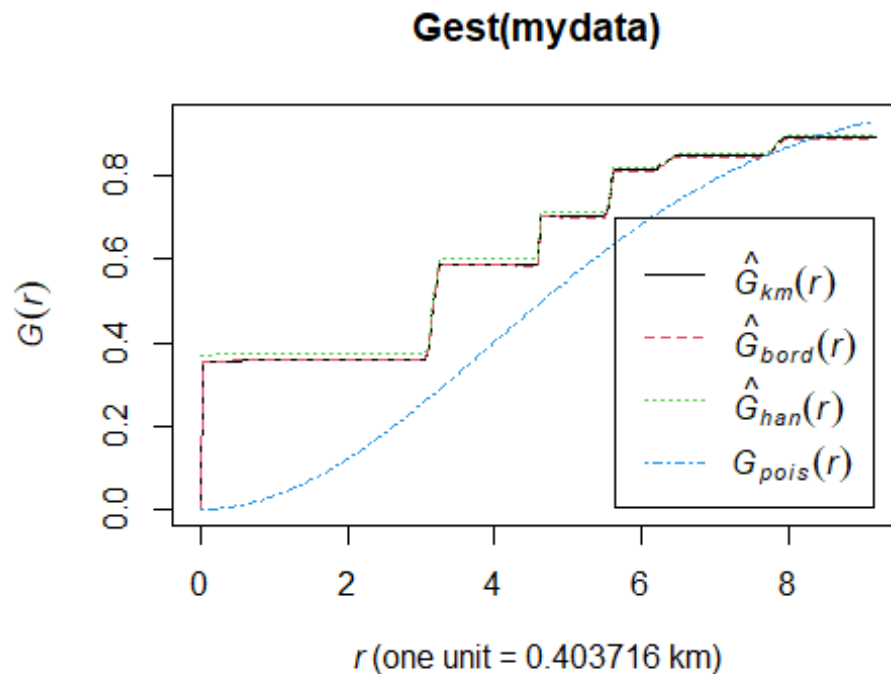
```
plot(Fest(mydata))
```

Fest(mydata)



#Compute and plot the G function for the locations of forest fires. Explain what kind of pattern for this data the function suggests.

```
plot(Gest(mydata))
```



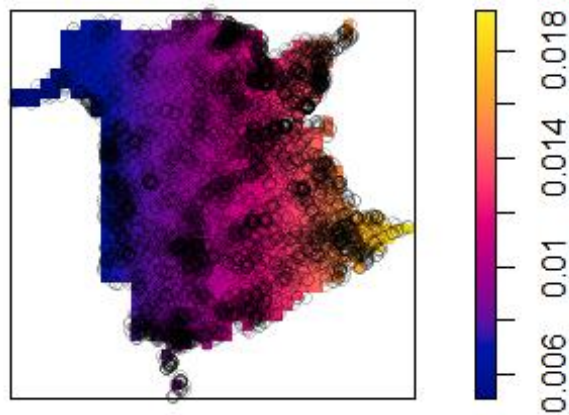
#Both functions suggest clustering behaviour as the theoretical curve G is under empirical estimators, similarly for F .

#Fit an in-homogeneous Poisson model with an intensity that is a linear function of x and y coordinates. Plot the corresponding trend and data locations in the same image.

```
fit1<-ppm(mydata,~x)
```

```
plot(fit1, how = "image", se = FALSE)
```

Fitted trend



#Question 3b.

```
mytime <- nbfires[nbfires$marks$fire.type == "forest"]$marks$dis.date
time1 <- round_date(ymd_hms("1987-01-01 00:00:00"), unit = "hour")
Date_h <- round_date(ymd_hms(mytime), unit = "hour")

## Warning: 1 failed to parse.

#Calculate a vector that represents the differences between the incident
times and the initial time moment. Display the first few values of this
vector.
hours_diff <- as.numeric(difftime(Date_h, time1, units = "hours"))
head(hours_diff)

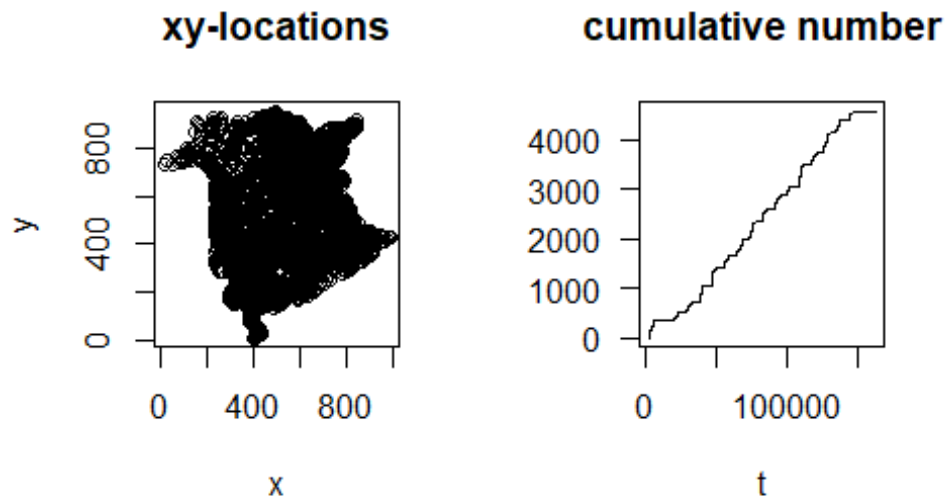
## [1] 116947 116558 116920 116292 116342 116342

#Create a data frame, using the vector of time differences and the x and y
coordinates extracted from mydata. Remove incomplete cases from it.
df1 <- data.frame( x = mydata$x, y = mydata$y, t = hours_diff )
df1 <- df1[complete.cases(df1), ]

#Create an 'stpp' object using this data frame and generate a static image
that shows the spatial locations and a plot with a cumulative number of cases
over time.
X1 <- as.3dpoints(df1)
str(X1)
```

```
## 'stpp' num [1:4558, 1:3] 274 239 678 269 324 ...
## - attr(*, "dimnames")=List of 2
## ..$ : NULL
## ..$ : chr [1:3] "x" "y" "t"
```

```
plot(X1)
```



```
#Run animation and show the obtained final plot
#NOTE: break the runtime, if case the loop is not finite.
dev.new()
animation(X1, runtime = 20)
dev.off()
```

```
## png
## 2
```

#Explanation: This patterns shows stationary behavior. Less points occurred at the top-left sub-regions and the appears most frequently in central and lower sub-regions. Overall time rate of events looks constant, but at smaller time resolution it seems exhibit some periodic behaviour