Lecture 18 - tensor flow - math

What is A "tensor" and how will it "flow"?

In the general definition "tensors" are arrays of numbers organized into an n-dimensional grid.

A scalar is a 1-ish number. This is the simplest kind of tensor:

```
import tensorflow as tf

x = tf.constant(-2.0, name="x", dtype=tf.float32)
a = tf.constant(5.0, name="a", dtype=tf.float32)
b = tf.constant(13.0, name="b", dtype=tf.float32)

y = tf.Variable(tf.add(tf.multiply(a, x), b))

print ( "result is:" )
tf.print ( y )
```

Elements are positionally identifiable. So A at i,i,k is Ai, j,k.

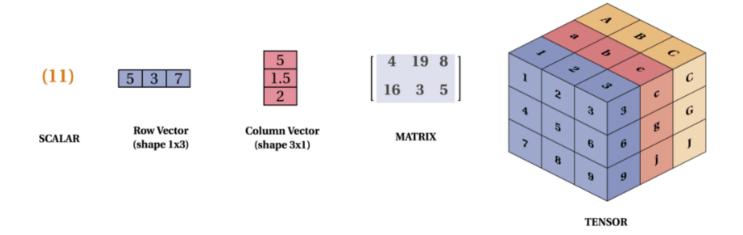
A vector is a 1x array of numbers. [1,2,4] that is the x,y,z distance from the origin.

The tensor is the 3d vector of each of these.

You are not limited to 3d data.

So...

Tensor:



Ranking:

rank 0 - scalar

rank 1 - vector [1,2,3]

rank 2 - matrix [[1,2] , [2, 3]]

rank 3 - 3 tensor

rank 4 - 4 tensor

Add of 2 matrix tensors

add1.py:

```
# let's create a ones 3x3 rank 2 tensor
rank_2_tensor_A = tf.ones([3, 3], name='MatrixA')
print("3x3 Rank 2 Tensor A: \n{}\n".format(rank_2_tensor_A))

# let's manually create a 3x3 rank two tensor and specify the data type as float
rank_2_tensor_B = tf.constant([[1, 2, 3], [4, 5, 6], [7, 8, 9]], name='MatrixB', dtype=
print("3x3 Rank 2 Tensor B: \n{}\n".format(rank_2_tensor_B))

# addition of the two tensors
rank_2_tensor_C = tf.add(rank_2_tensor_A, rank_2_tensor_B, name='MatrixC')
print("Rank 2 Tensor C with shape={} and elements: \n{}\".format(rank 2 tensor C.shape,
```

$$[A]_{m \times n} [B]_{n \times p} = [C]_{m \times p}$$

Some matrix multiplication:

Definition of multiply

$$\mathrm{c}_{ij} = \sum_{k=1}^n a_{ik} b_{kj}$$

Let's multiply using TF:

matmul1.py:

```
1: import tensorflow as tf
 3: # Matrix A and B with shapes (2, 3) and (3, 4)
 4: mmv_matrix_A = tf.ones([2, 3], name="matrix_A")
5: mmv_matrix_B = tf.constant([[1, 2, 3, 4], [1, 2, 3, 4], [1, 2, 3, 4]], \
        name="matrix_B", dtype=tf.float32)
6:
7:
8: # Matrix Multiplication: C = AB with C shape (2, 4)
9: matrix_multiply_C = tf.matmul(mmv_matrix_A, mmv_matrix_B, \
10:
        name="matrix_multiply_C")
11:
12: print("""Matrix A: shape {0} \nelements: \n{1} \n\n
13: Matrix B: shape {2} \nelements: \n{3}\n
14: Matrix C: shape {4} \nelements: \n{5}""". \
15:
        format(mmv_matrix_A.shape, mmv_matrix_A, mmv_matrix_B.shape, \
        mmv_matrix_B, matrix_multiply_C.shape, matrix_multiply_C))
16:
```

output matmul1.out:

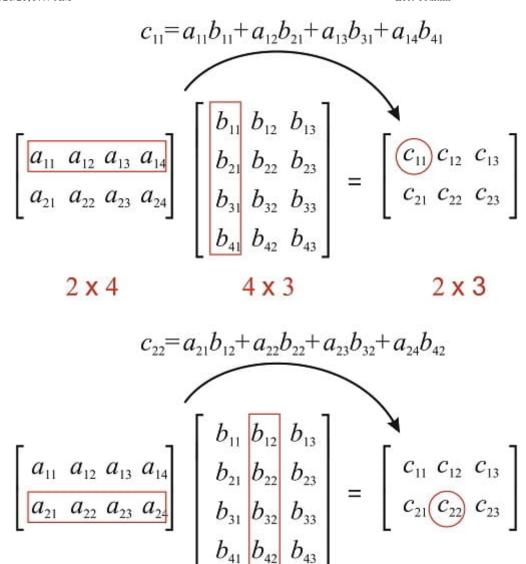
```
Matrix A: shape (2, 3)
elements:
[[1. 1. 1.]
[1. 1. 1.]]

Matrix B: shape (3, 4)
elements:
[[1. 2. 3. 4.]
[1. 2. 3. 4.]
[1. 2. 3. 4.]]

Matrix C: shape (2, 4)
elements:
[[ 3. 6. 9. 12.]
[ 3. 6. 9. 12.]]
```

Inner Dimentions must be the same.

A by hand example:



With Some Data

First a 1x example:

$$\begin{bmatrix} 5 \\ 3 \\ 7 \\ 1 \end{bmatrix} \begin{bmatrix} 6 & 2 & 3 & 4 \end{bmatrix} = \begin{bmatrix} 30 & 10 & 15 & 20 \\ 18 & 6 & 9 & 12 \\ 42 & 14 & 21 & 28 \\ 6 & 2 & 3 & 4 \end{bmatrix}$$

Matrices are useful

Calculate Inverse of a Matrix:

inv.py:

```
1: import tensorflow as tf
 2:
 3: iim_matrix_A = tf.constant([[2, 3], [2, 2]], name='MatrixA', dtype=tf.float32)
 4:
 5: try:
 6:
        # Tensorflow function to take the inverse
 7:
        inverse_matrix_A = tf.linalg.inv(iim_matrix_A)
 9:
        # Creating a identity matrix using tf.eye
        identity_matrix = tf.eye(2, 2, dtype=tf.float32, name="identity")
10:
11:
12:
        iim RHS = identity matrix
        iim_LHS = tf.matmul(inverse_matrix_A, iim_matrix_A, name="LHS")
13:
14:
15:
        predictor = tf.reduce_all(tf.equal(iim_RHS, iim_LHS))
16:
        def true_print(): print("""A^-1 times A equals the Identity Matrix
17: Matrix A: \n{0} \n\operatorname{Inverse} of Matrix A: \n{1} \n\operatorname{RHS}: I: \n{2} \n
18: LHS: A^(-1) A: \n{3}""".format(iim_matrix_A, inverse_matrix_A,
        iim_RHS, iim_LHS))
19:
20:
        def false_print(): print("Condition Failed")
21:
        tf.cond(predictor, true_print, false_print)
22:
23: except:
24:
        print("""A^-1 doesnt exist
25:
        Matrix A: \n{} \n\n \n\nInverse of Matrix A: \n{} \n\n \n\nRHS: I: \n{}
        \nLHS: (A^{(-1)} A): \n{}'''''.format(iim_matrix_A, inverse_matrix_A, iim_RHS, iim_matrix_A)
26:
```

And the output:

```
A^-1 times A equals the Identity Matrix
Matrix A:
[[2. 3.]
[2. 2.]]

Inverse of Matrix A:
[[-1.  1.5]
[ 1. -1. ]]

RHS: I:
[[1. 0.]
[0. 1.]]

LHS: A^(-1) A:
[[1. 0.]
```

[0. 1.]]